Parallelizing Programs

• Goal: speed up programs using multiple processors/cores

(Sequential) Matrix Multiplication

```
double A[n][n], B[n][n], C[n][n] // assume n x n for i = 0 to n-1 for j = 0 to n-1 double sum = 0.0 for k = 0 to n-1 sum += A[i][k] * B[k][j] C[i][j] = sum
```

Question: how can this program be parallelized?

- First: find parallelism
 - Concerned about what can *legally* execute in parallel
 - At this stage, expose as much parallelism as possible
 - Partitioning can be based on data structures or by function

Note: other steps are architecture dependent

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- Can we parallelize the outer loops?
 - Yes, because the read and write sets are independent for each iteration (i,j)
 - Read set for process (i,j) is sum, A[i][k=0:n-1], B[k=0:n-1][j]
 - Write set for process (i,j) is sum, C[i][j]
 - Note: we have the option to parallelize just one of these loops

Terminology

• co statement: creates parallelism
co i := 0 to n-1
Body
oc

- Meaning: *n* instances of body are created and executed concurrently until the end of the *co* (i.e., at the *oc*)
- Implementation: fork *n* threads, join them at the *oc*

Need to understand what processes/threads are!

Processes

- History: OS had to coordinate many activities
 - Example: deal with multiple users (each running multiple programs), incoming network data, I/O interrupts
- Solution: Define a model that makes complexity easier to manage
 - Process (thread) model

What's a process?

- Informally: program in execution
- Process encapsulates a physical processor
 - everything needed to run a program
 - code ("text")
 - registers (PC, SP, general purpose)
 - stack
 - data (global variables or dynamically allocated)
 - files
- NOTE: a process is sequential

Examples of Processes

• Shell: creates a process to execute command

```
lectura:> ls foo
(shell creates process that executes "ls")
lectura:> ls foo & cat bar & more
(shell creates three processes, one per command)
```

- OS: creates a process to manage printer
 - process executes code such as:
 wait for data to come into system buffer
 move data to printer buffer

Creating a Process

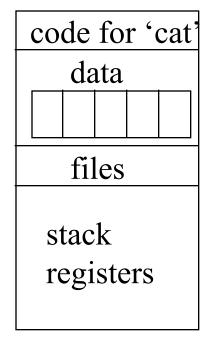
- Must somehow specify code, data, files, stack, registers
- Ex: UNIX
 - Use the fork() system call to create a process
 - Makes an exact duplicate of the current process
 - (returns 0 to indicate child process)
 - Typically exec() is run on the child

We will not be doing this (systems programming)

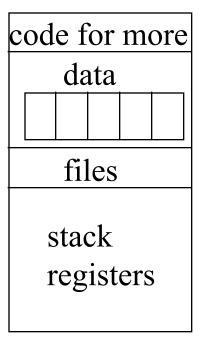
Example of Three Processes

code for 'ls'
data
files
stack
registers

Process 0



Process 1



Process 2

OS switches between the three processes ("multiprogramming")

Review: Run-time Stack

```
A(int x) {
  int y = x;
  if (x == 0) return;
  else return A(y-1) + 1;
B() {
  int z;
  A(1);
```

Decomposing a Process

- Process: everything needed to run a program
- Consists of:
 - Thread(s)
 - Address space

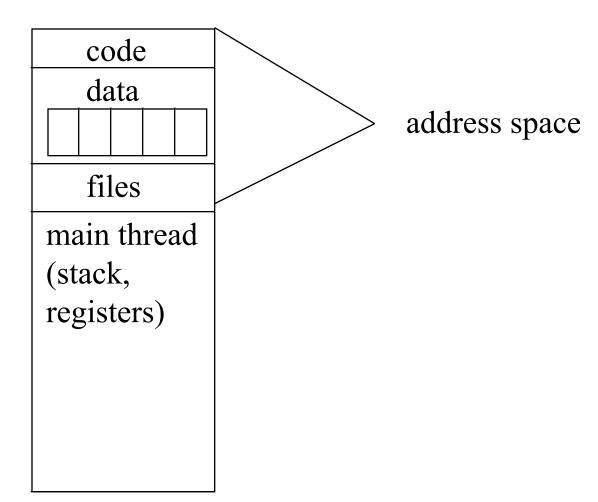
Thread

- Sequential stream of execution
- More concretely:
 - program counter (PC)
 - register set
 - stack
- Sometimes called lightweight process

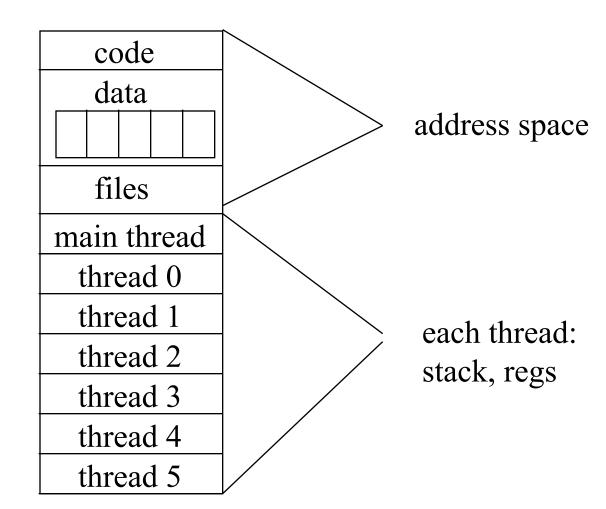
Address Space

- Consists of:
 - code
 - data
 - open files
- Address space can have > 1 thread
 - threads share code, data, files
 - threads have separate stacks, register set

One Thread, One Address Space



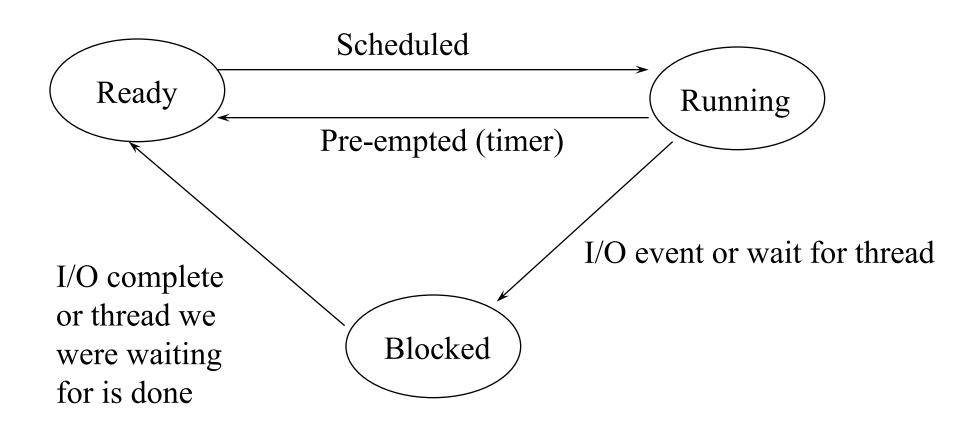
Many Threads, One Address Space



Thread States

- Ready
 - eligible to run, but another thread is running
- Running
 - using CPU
- Blocked
 - waiting for something to happen

Thread State Graph



Scheduler

- Decides which thread to run
 - (from ready list only)
- Chooses from some algorithm
- From our point of view, the scheduler is something we cannot control
 - We have no idea which thread will be run, and our programs must not depend on execution order of two ready threads

Context Switching

- Switching between 2 threads
 - change PC to current instruction of new thread
 - might need to restart old thread in the future
 - must save exact state of first thread
- What must be saved?
 - registers (including PC and SP)
 - what about stack itself?

Multiple Threads, One Machine (Single Core)

PC **Initial State** SP (nothing running) **R**1 Machine R2 Stack Stack Code Files Data PC, SP, R1, R2 PC, SP, R1, R2 Thread 1 Thread 2 Address Space

Multiple Threads, One Machine (Single Core)

PC Start Thread 1 SP **R**1 R2 Stack Stack Code Files Data (PC, SP, R1, R2) PC, SP, R1, R2 Thread 1 Thread 2 Address Space

Machine

Multiple Threads, One Machine (Single Core)

PC Context Switch to SP Thread 2, Step 1 **R**1 Machine R2 Stack Stack Code Files Data PC, SP, R1, R2 PC, SP, R1, R2 Thread 2 Thread 1 Address Space

Multiple Threads, One Machine (Single Core)

PC Context Switch to SP Thread 2, Step 2 **R**1 Machine R2 Stack Stack Code Files Data PC, SP, R1, R2 PC, SP, R1, R2 Thread 2 Thread 1 Address Space

Why Save Registers?

• code for Thread 0

$$x := x+1$$

$$x := x*2$$

Assembly code:

$$R1 := R1 + 1 /* !! */$$

$$R1 := R1 * 2$$

code for Thread 1

$$y := y+2$$

$$y := y-3$$

Assembly code:

$$R1 := R1 + 2$$

$$R1 := R1 - 3$$

Suppose context switch occurs after line "!!"

Matrix Multiplication, n^2 threads

```
double A[n][n], B[n][n], C[n][n] // assume n x n
co i = 0 to n-1 {
                             We already argued the two outer
                            "for" loops were parallelizable
 co i = 0 to n-1 {
    double sum = 0.0
   for k = 0 to n-1
     sum += A[i][k] * B[k][i]
   C[i][j] = sum
```

- Second: control granularity
 - Must trade off advantages/disadvantages of fine-granularity
 - Advantages: better load balancing, better scalability
 - Disadvantages: process/thread overhead and communication
 - Combine small processes into larger ones to coarsen granularity
 - Try to keep the load balanced

Matrix Multiplication, *n* threads

```
double A[n][n], B[n][n], C[n][n] // assume n x n
co i = 0 to n-1 {
                             This is plenty of parallelization
 for j = 0 to n-1 {
                             if the number of cores is <= n
    double sum = 0.0
    for k = 0 to n-1
      sum += A[i][k] * B[k][i]
    C[i][i] = sum
```

Matrix Multiplication, p threads

```
double A[n][n], B[n][n], C[n][n] // assume n x n
co t = 0 to p-1  {
  startrow = t * n / p; endrow = (t+1) * n/p - 1
  for i = startrow to endrow
   for j = 0 to n-1 {
     double sum = 0.0
     for k = 0 to n-1
      sum += A[i][k] * B[k][j]
     C[i][j] = sum
```

- Third: distribute computation and data
 - Assign which processor does which computation
 - The co statement does *not* do this
 - If memory is distributed, decide which processor stores which data (why is this?)
 - Data can be replicated also
 - Goals: minimize communication and balance the computational workload
 - Often conflicting goals

- Fourth: synchronize and/or communicate
 - If shared-memory machine, synchronize
 - Both mutual exclusion and sequence control
 - Locks, semaphores, condition variables, barriers, reductions
 - If distributed-memory machine, communicate
 - Message passing
 - Usually communication involves implicit synchronization

Parallel Matrix Multiplication--Distributed-Memory Version

```
process worker [i = 0 \text{ to p-1}] {
 double A[n][n], B[n][n], C[n][n] // wasting space!
 startrow = i * n / p; endrow = (i+1) * n/p - 1
 if (i == 0)
   for j = 1 to p-1 {
      sr = j * n / p; er = (j+1) * n/p - 1
      send A[sr:er][0:n-1], B[0:n-1][0:n-1] to process j
 else
    receive A[startrow:endrow][0:n-1], B[0:n-1][0:n-1] from 0
```

Parallel Matrix Multiplication--Distributed-Memory Version

```
for i = startrow to endrow
   for j = 0 to n-1 {
     double sum = 0.0
     for k = 0 to n-1
      sum += A[i][k] * B[k][j]
    C[i][j] = sum
 // here, need to send my piece back to master
 // how do we do this?
} // end of process statement
```

Adaptive Quadrature: Sequential Program

```
double f() {
double area(a, b)
 c := (a+b)/2
 compute area of each half and area of whole
 if (close)
  return area of whole
 else
  return area(a,c) + area (c,b)
```

Adaptive Quadrature: Recursive Program

```
double f() {
double area(a, b)
 c := (a+b)/2
 compute area of each half and area of whole
 if (close)
  return area of whole
 else
   co leftArea = area(a,c) // rightArea = area (c,b) oc
   return leftArea + rightArea
```

Challenge with Adaptive Quadrature

- For efficiency, must control granularity (step 2)
 - Without such control, granularity will be too fine
 - Can stop thread creation after "enough" threads created
 - Hard in general, as do not want cores idle either
 - Thread implementation can perform work stealing
 - Idle cores take a thread and execute that thread, but care must be taken to avoid synchronization problems and/or efficiency problems

- Fifth: assign processors to tasks (only if using task and data parallelism)
 - Must also know dependencies between tasks
 - Usually task parallelism used if limits of data parallelism are reached

- Sixth: parallelism-specific optimizations
 - Examples: message aggregation, overlapping communication with computation

- Seventh: acceleration
 - Find parts of code that can run on GPU/Xeon
 Phi/etc., and optimize those parts
 - Difficult and time consuming
 - But may be quite worth it