# A Comprehensive Study of Characterizing Program Execution Time

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#### Abstract

(Tentative) Measuring execution time is a useful tool in evaluating the performance of a program. But it is challenging to obtain precise, accurate program execution time due to the presence of various system daemons and their unpredictable activities. Such activities significantly contribute to varying program execution time. It will be very useful to predict the concrete performance of a program with different input sizes in a real situation, if a (probabilistic) distribution of the execution times of that program is found, considering the daemon activities. In this work, we discuss several interesting phenomenon observed to characterize program execution times. We find that such a distribution of the execution times cannot be uniquely identified, and it will be more likely to be mixture of two or more models formed by different periodicity of different daemon processes. Finally, we discuss some remaining issues that should be resolved to successfully identify a distribution of program execution times.

### 1 Experiment Notes

Task Length	Description	Time Length
	Regular PUT experiment. Refer to Sections 2, 3, and 4	
PUT1~PUT64	Runs of 1000 samples (on sodb12).	$2013-10-14 \sim 2013-10-15$
PUT128~PUT2048	Runs of 300 samples (on sodb12).	$2013-12-12 \sim 2013-12-21$
PUT4096	A run of 300 samples (on sodb12).	$2014-06-23 \sim 2014-07-10$
PUT8192	Runs of $40/260$ samples (on sodb12).	$2015-04-23 \sim 2015-04-27$ /
		$2015-10-31 \sim 2015-11-24$
PUT16384	Runs of $40/260$ samples (on sodb12).	$2015-04-23 \sim 2015-04-23$ /
		$2015-11-25 \sim 2016-01-14$

Table 1: Notes on the regular PUT data used for the histograms

Task Length	Description	Time Length
	Regular PUT experiment. Refer to Section 5.	
PUT1/2	Runs of 20k samples on sodb9/sodb10.	$2015-12-15 \sim 2015-12-15$
PUT4/8	Runs of 20k samples on sodb10.	$2016-01-20 \sim 2016-01-20$
PUT16	Runs of 2k, 4k, 8k, 16k, and 32k samples (on sodb12).	$2016-01-25 \sim 2016-02-09$
Dual PUT experiment. Refer to Section 6.		
PUT4096	A run of 500 samples on sodb8.	$2015-11-08 \sim 2015-12-25$
PUT2	A run of 1k samples on sodb9.	$2015-12-27 \sim 2015-12-27$
PUT4~PUT32	Runs of 1k samples on sodb9.	$2016-01-27 \sim 2016-01-31$
PUT64~PUT4096	Runs of 1k samples on sodb9.	$2016-02-17 \sim ?$

Table 2: Notes on the new PUT experiments

### 2 Summary of the EMPv4 data

EMPv4: Running PUT with a specific task length under a controlled environment, with i) daemon processes disabled, ii) the NTP daemon process activated, iii) major CPU features (turbo and speedstep) disabled, and iv) an up-to-date Linux version (RHEL 6.0) installed.

	Num. of Samples	Minimum	Maximum	Average	Std. Dev.
		(msec)	(msec)	(msec)	(msec)
PUT1	1,000	999.0	1,005.0	1,002.4	0.73
PUT2	1,000	1,996.0	2,007.0	2,004.5	1.38
PUT4	1,000	4,004.0	4,012.0	4,008.6	1.64
PUT8	1,000	8,014.0	8,023.0	8,018.1	1.72
PUT16	1,000	16,029.0	16,041.0	16,034.3	1.86
PUT32	1,000	32,064.0	32,084.0	32,068.2	2.05
PUT64	1,000	64,129.0	64,145.0	64,135.0	2.27
PUT128	300	128,244.0	128,260.0	128,251.2	2.32
PUT256	300	256,494.0	256,523.0	256,502.3	3.29
PUT512	300	512,995.0	513,152.0	513,005.1	9.41
PUT1024	300	1,025,997.0	1,026,141.0	1,026,012.4	11.43
PUT2048	300	2,051,981.0	2,052,156.0	2,052,012.0	11.19
PUT4096	300	4,105,451.0	4,105,629.0	4,105,526.0	25.98
PUT8192	40 (last Apr)	8,207,870.0	8,207,967.0	8,207,918.0	21.03
PUT8192	260 (Nov)	8,210,940.0	8,211,196.0	8,211,049.0	36.60
PUT16384	40 (last Apr)	16,415,757.0	16,415,964.0	16,415,810.3	40.43
PUT16384	260 (Nov)	16,422,028	16,422,389	16,422,153.0	52.54

Table 3: PT statistics by EMPv4 (See Table 1.)

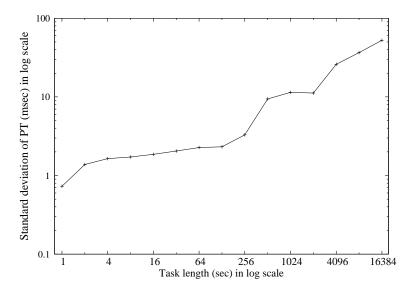


Figure 1: Std. dev. of PT over increasing task length (See Table 1.)

## 3 Histograms on the EMPv4 Data

The base data of the following histograms are from Table 1.

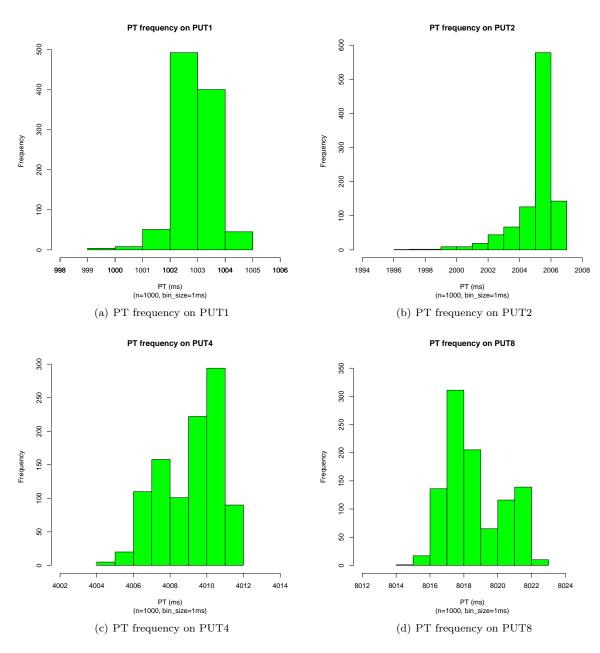
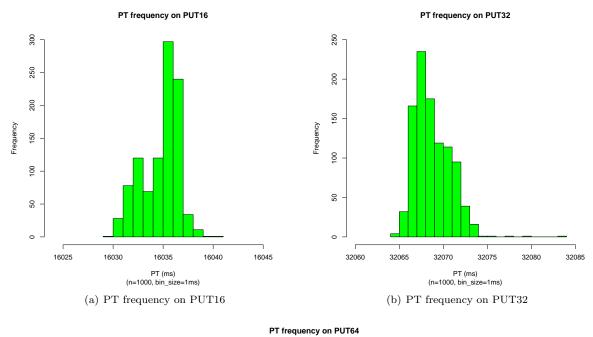


Figure 2: PT Histograms of PUT1  $\dots$  PUT8



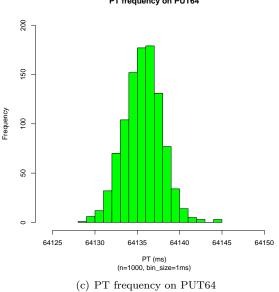


Figure 3: PT Histograms of PUT16  $\dots$  PUT64

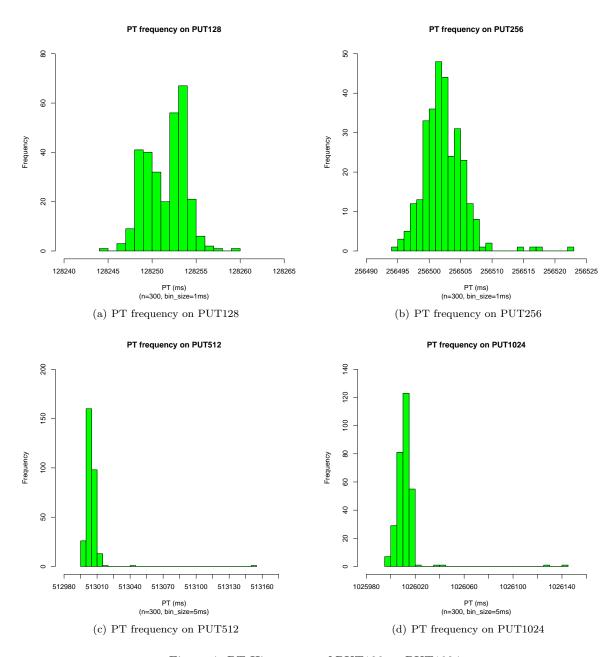


Figure 4: PT Histograms of PUT128 ... PUT1024

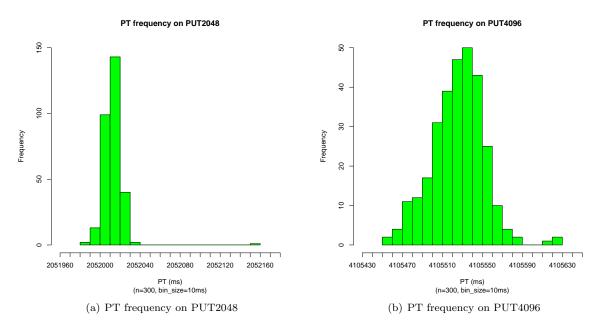
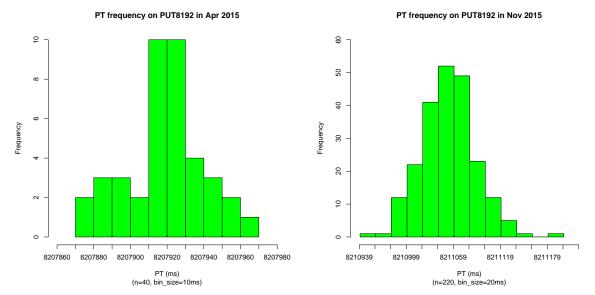


Figure 5: PT Histograms of PUT2048 and PUT4096



(a) PT frequency on PUT8192 with 40 samples (See Table 1.) (b) PT frequency on PUT8192 with 260 samples (See Table 1.)

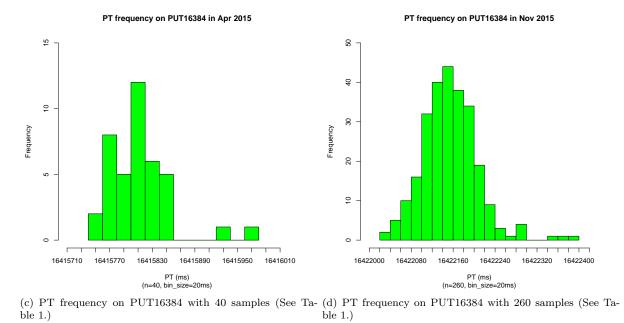


Figure 6: PT Histograms of PUT8192 and PUT16384

### 4 Histograms on the EMPv5 Data

The base data of the following histograms are from Table 1. EMPv5(-relaxed) trims outliers from the data of each PUT by EMPv4. To be more specific, for each run of PUT an outlier is determined as the one above and below the average  $\pm$  \*five<sup>1\*</sup> standard deviations computed from the EMPv4 data.

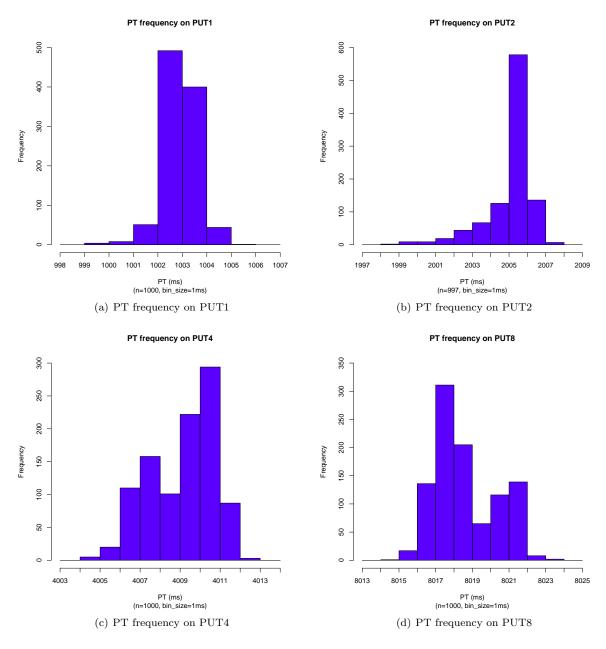
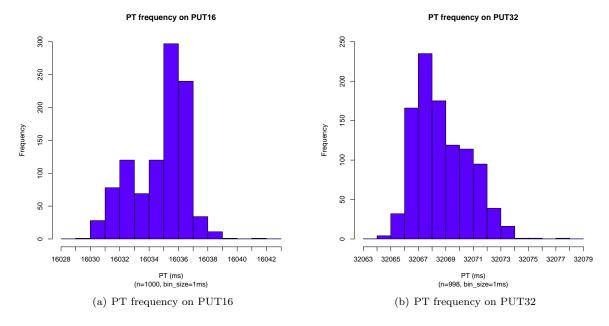


Figure 7: PT Histograms of PUT1 ... PUT8

<sup>&</sup>lt;sup>1</sup>In the stricter version, we use \*two\*.



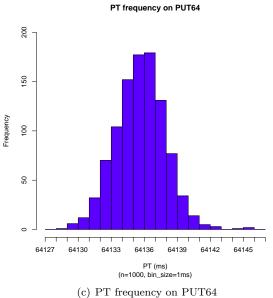


Figure 8: PT Histograms of PUT16 ... PUT64

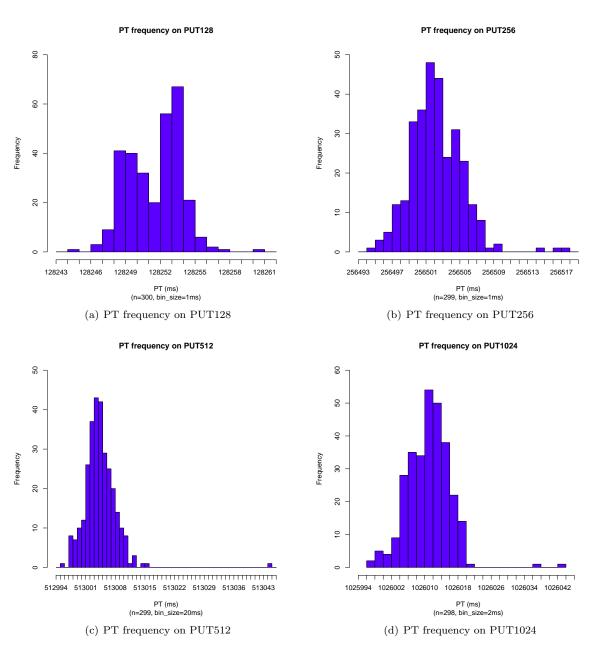


Figure 9: PT Histograms of PUT128 ... PUT1024

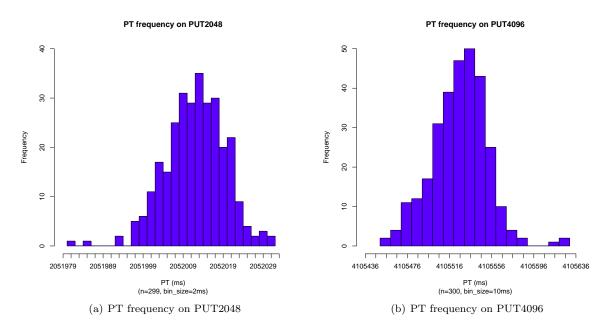
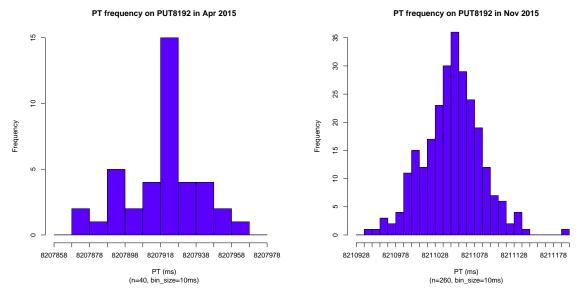


Figure 10: PT Histograms of PUT2048 and PUT4096



(a) PT frequency on PUT8192 with 40 samples (See Table 1.) (b) PT frequency on PUT8192 with 260 samples (See Table 1.)

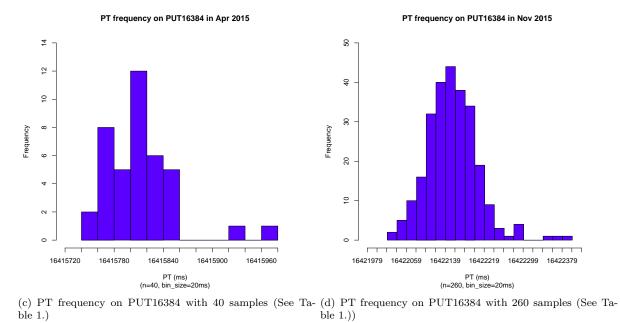


Figure 11: PT Histograms of PUT8192 and PUT16384

## 5 Sample Size vs. Standard Deviation of PT

The base data of the following histograms are from Table 2.

#### 5.1 PUT1 and PUT2

Table 4 exhibits varying standard deviations over increasing sample size on PUT1 and PUT2. EMPv4 is applied to the table's data.

Num. of Samples	Std. Dev. (msec)	
Num. of Samples	PUT1	PUT2
1,000	1.07	1.40
2,000	1.06	1.39
3,000	1.07	1.38
4,000	1.07	1.37
5,000	1.07	1.40
6,000	1.06	1.70
7,000	1.06	1.65
8,000	1.07	1.62
9,000	1.07	1.60
10,000	1.07	1.58
11,000	1.08	1.57
12,000	1.08	1.56
13,000	1.08	1.54
14,000	1.08	1.53
15,000	1.08	1.52
16,000	1.08	1.51
17,000	1.08	1.50
18,000	1.08	1.50
19,000	1.08	1.50
20,000	1.08	1.49

Table 4: Std. Dev. of PUT1 and PUT2 over increasing sample size

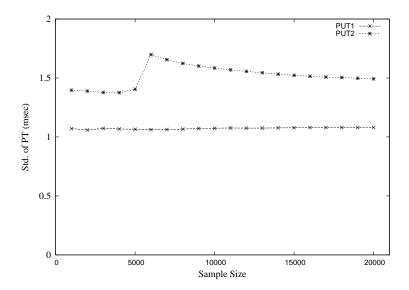


Figure 12: Std. dev. of PT on PUT1 and PUT2 over increasing sample size

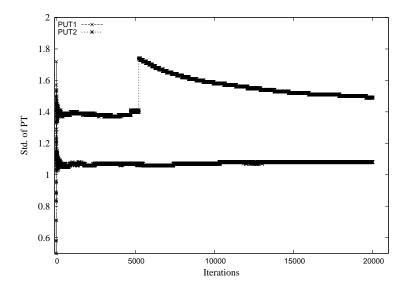


Figure 13: Std. dev. of PT on PUT1 and PUT2 over increasing sample size

PUT2	Program Time
incr_work	2078 msecs (at the 5276th iteration)
Daemon Processes	Program Time
md0_raid1	1 msec
proc_monitor	198 msecs
rhn_check	460 msecs
Total	659 msecs

Table 5: The daemon processes captured at the hike of PUT2

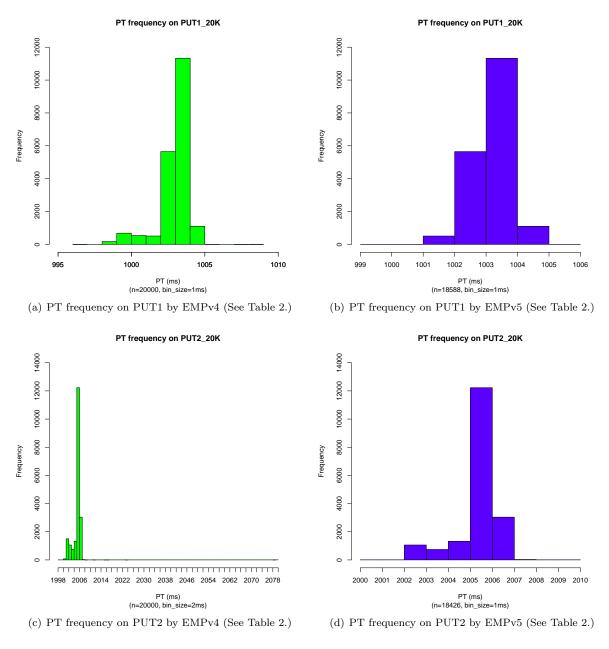


Figure 14: PT Histograms of PUT1 and PUT2 by 20,000 trials

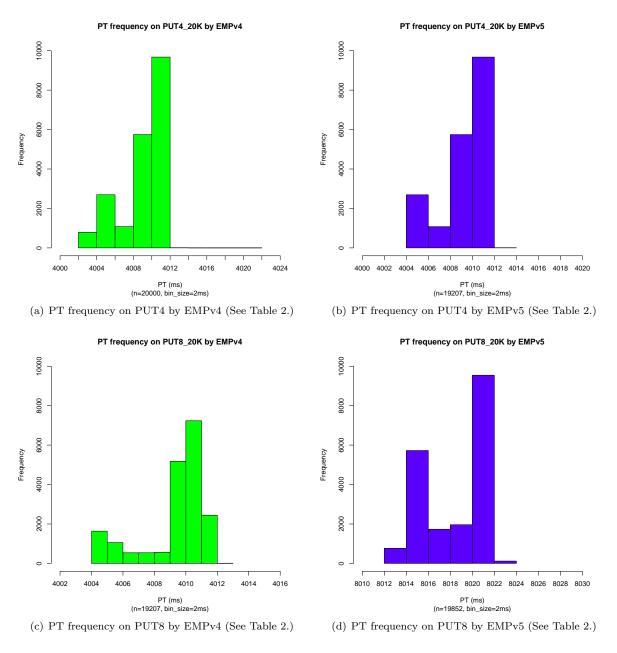


Figure 15: PT Histograms of PUT4 and PUT8 by 20,000 trials

#### 5.2 PUT16

In this experiment we ran PUT16 up to 32,000 from 1,000 times by a factor of two. The relaxed version of EMPv5 (called *EMPv5-relaxed*) uses \*five\* standard deviations whereas its strict version (called *EMPv5-strict*) does \*two\* standard deviations for a vertical gap below and above the average. (Young: 2k samples seem most appropriate to represent the whole population of PUT16, in that the standard deviations by EMPv5 on the 2k sample size are almost at peak compared to those of the other sample sizes.)

Num of Complex	Std. Dev. (msec)			
Num. of Samples	EMPv4	EMPv5-relaxed	EMPv5-strict	
1,000	1.86	1.86	1.68	
2,000	2.20	2.12	1.81	
4,000	2.21	1.89	1.65	
8,000	2.23	1.97	1.71	
16,000	2.07	2.00	1.61	
32,000	1.81	1.75	1.53	

Table 6: Standard deviations of PUT16 over increasing sample size

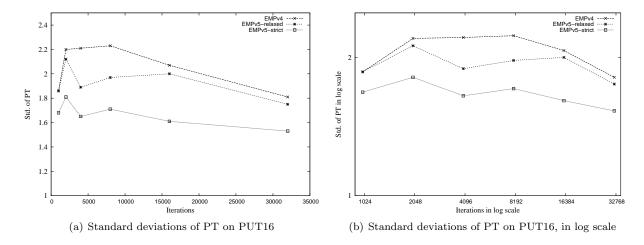


Figure 16: Standard deviations of PT on PUT16 over increasing sample size

#### 5.3 Histograms by EMPv4

We apply EMPv4 to the runs of PUT16 as mentioned above. The following histograms are the results of EMPv4.

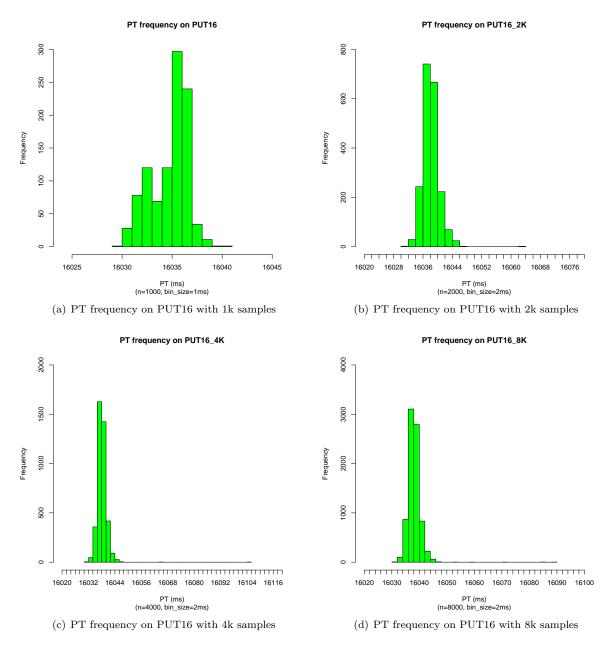


Figure 17: PT histogram of PUT16 by EMPv4, with the sample size increasing from 1k to 8k

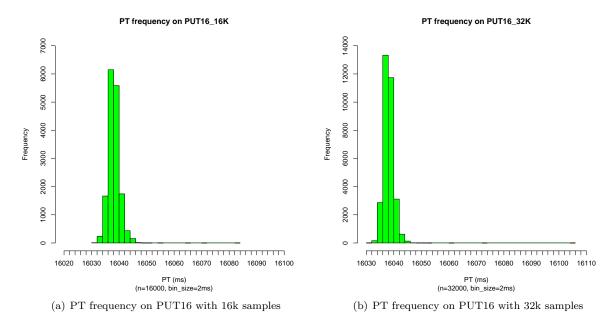


Figure 18: PT histogram of PUT16 by EMPv4, with the sample size increasing from 16k to 32k

#### 5.4 Histograms by EMPv5

We now apply EMPv5 to the same data of PUT16. To be more specific, we use EMPv5-strict, by which the following histograms are obtained.

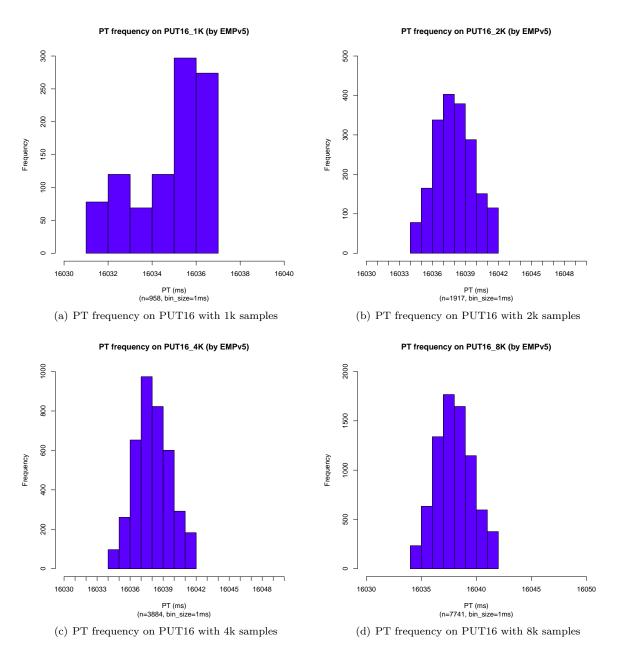


Figure 19: PT histogram of PUT16 by EMPv5, with the sample size increasing from 1k to 8k

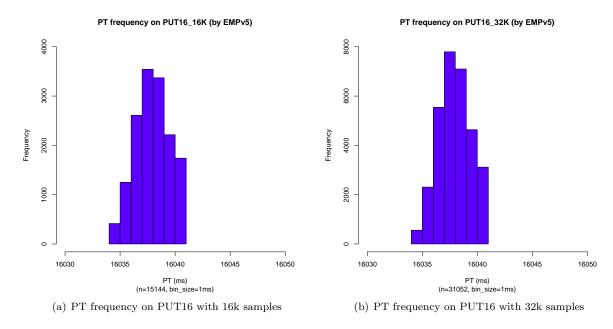


Figure 20: PT histogram of PUT16 by EMPv5, with the sample size increasing from 16k to 32k

### 6 Dual PUT Experiment

In this section we study the characteristics of program times measured in dual PUT experiment, in which the for-loop of PUT is broken up into two equal-sized for-loops  $(for_1 \text{ and } for_2)$  of which elapsed times are individually measured using gettimeofday(). The experiment is designed to see whether there exists "internal dependency" of measured times of the two for-loops when PUT is timed. To be more specific, we compute correlation coefficients between corresponding measured times of  $for_1$  and  $for_2$ , within the same run of each PUT. In this experiment we expect that little dependency will be observed within the same run for any PUT.

The base data of the following table and histograms are from Table 2.

	Corr. Coeff.	Corr. Coeff.	Sample Size (# of regulars)
		with outliers	
		removed	
PUT2	0.3	0.5	1,000
PUT4	-0.07	-0.2	1,000
PUT8	0.8	-0.2	1,000
PUT16	0.3	-0.6	1,000
PUT32	0.01	-0.4	1,000
PUT64	0.003	-0.5	1,000
PUT128	0.04	-0.5	1,000
PUT256	0.004	-0.1	1,000
PUT512	-0.03	-0.1	1,000
PUT1024	0.14	-0.04	1,000
PUT2048	?	?	1,000
PUT4096	-0.01	-0.2	500

Table 7: Overall statistics of dual PUT experiment

#### 6.1 Scatter Plots

In this section we plot measured times of dual PUT experiments. We provide not only scatter plots of raw data but also those of focused clouds to further look inside. The focused clouds were obtained by cutting off outliers chosen by eye.

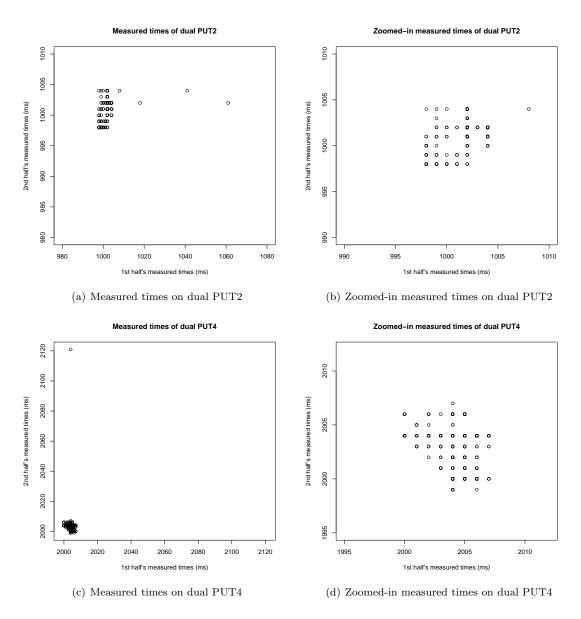


Figure 21: Scatter plots on dual PUT2 $\sim$ PUT8

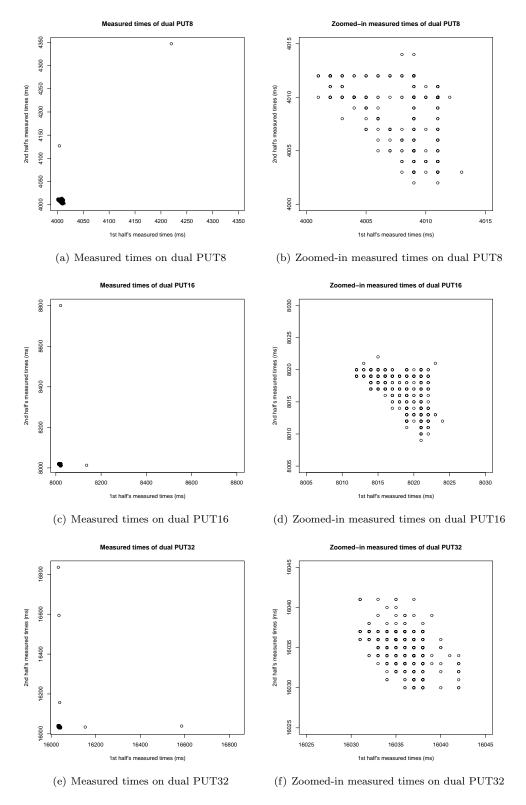


Figure 22: Scatter plots on dual PUT8 $\sim$ PUT32

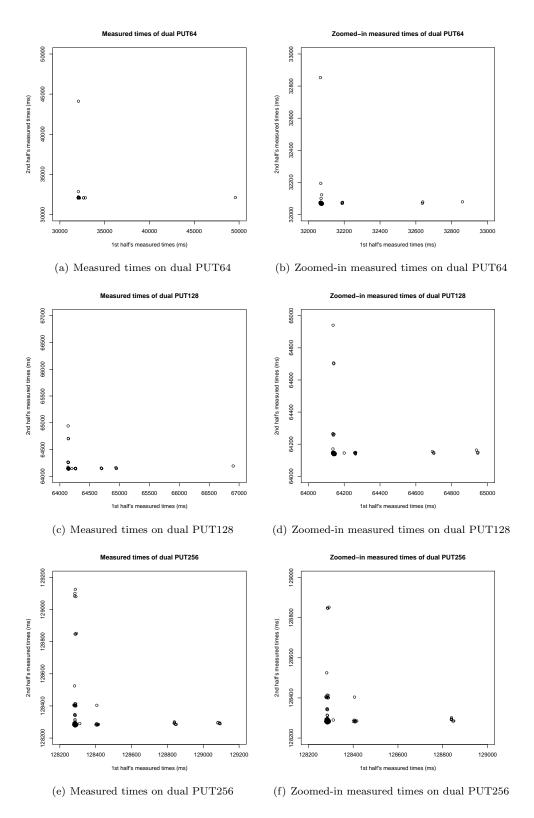


Figure 23: Scatter plots on dual PUT64 $\sim$ PUT256

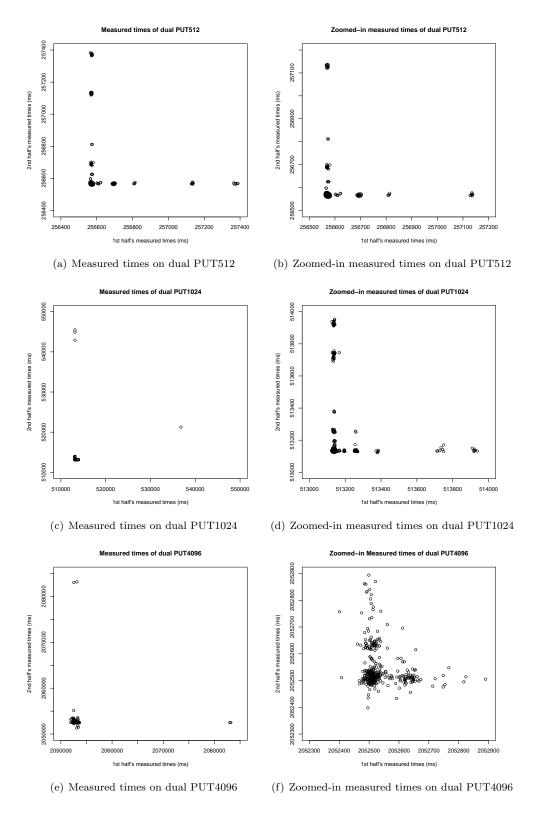


Figure 24: Scatter plots on dual PUT512, PUT1024, and PUT4096

#### 6.1.1 Supplementary Scatter Plots

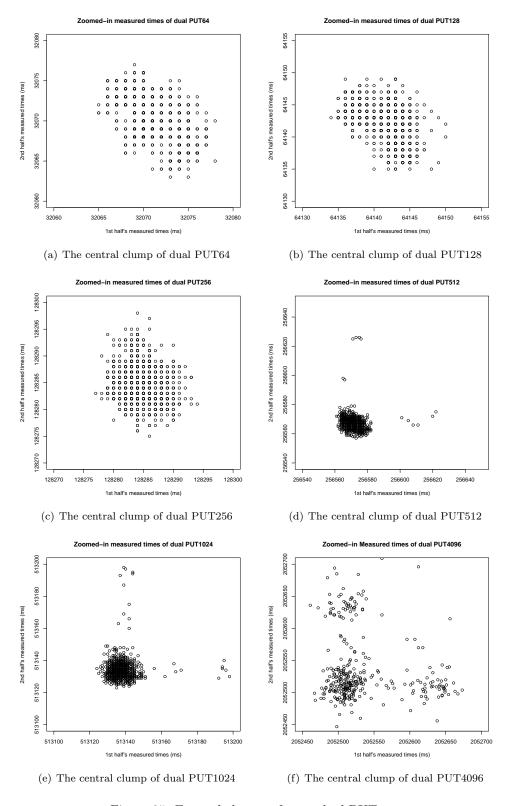


Figure 25: Focused clumps of some dual PUT runs

#### 6.1.2 Captured Processes on Dual PUT4096

In this study we examine a list of processes captured in a specific region of measured times on dual PUT4096. The base data is from Figure 24(e). We divide the data into four subregions by the pivot point of "2,052,575" msec on the x and y axes. This pivot is chosen by eye, based on Figure 25(f).

Table 8 represents a list of daemon processes captured in each of the four subregions while Table 9 shows a list of regions in which a specific daemon process(es) appeared. The last column in Table 8 indicates the average time executed by the captured daemon processes in each region. Table 9 also shows how long each daemon process was on average run whenever it appeared in a specific region.

Subregion	Daemon Processes	Avg. Daemon (Running) Time (msecs)
Region 1 ( $x < \text{pivot}, y < \text{pivot}$ )	bash, id, java, rhn_check,	3,494
	rhsmcertd-worke, sshd, uname	
Region 2 ( $x < \text{pivot}, y \ge \text{pivot}$ )	id, java, rhn_check,	6,954
	rhsmcertd-worke, sshd	
Region 3 $(x \ge \text{pivot}, y < \text{pivot})$	java, rhn_check,	16,350
	rhsmcertd-worke, sshd	
Region 4 $(x \ge \text{pivot}, y \ge \text{pivot})$	java, rhn_check,	2,130
	rhsmcertd-worke, sshd	

Table 8: Captured Daemon Processes and Their Times in Each Region

Daemon Processes	Captured Region List
bash	1 (370 msecs)
id	1 (10 msecs), 2 (10 msecs)
java	1 (11 msecs), 2 (11 msecs), 3 (12 msecs), 4 (12 msecs)
rhn_check	1 (6,415 msecs), 2 (25,855 msecs), 3 (21,923 msecs), 4 (7,585 msecs)
rhsmcertd-worke	1 (1,157 msecs), 2 (1,156 msecs), 3 (1,158 msecs), 4 (1,152 msecs)
sshd	1 (183 msecs), 2 (64 msecs), 3 (80 msecs), 4 (75 msecs)
uname	1 (10 msecs)

Table 9: Per-Daemon Appearance Region and Its Averge Running Time

### 6.2 Program Time Comparison

In this section we perform one-to-one comparison on measured times of parts I and II for the same iteration of each PUT.

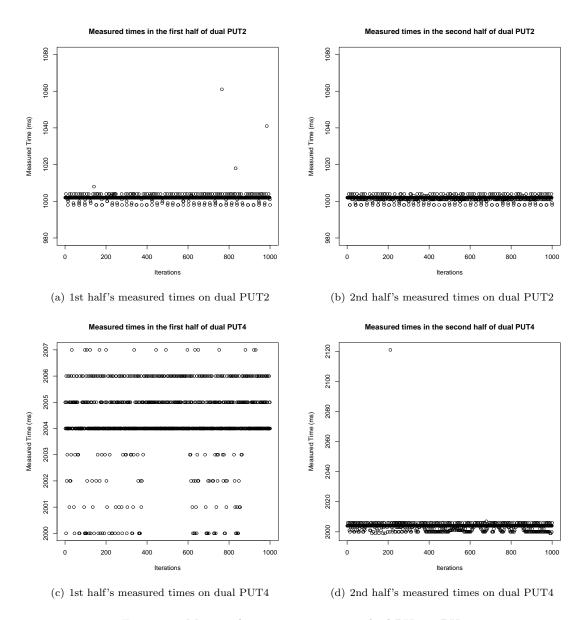


Figure 26: Measured time comparison on dual PUT2~PUT8

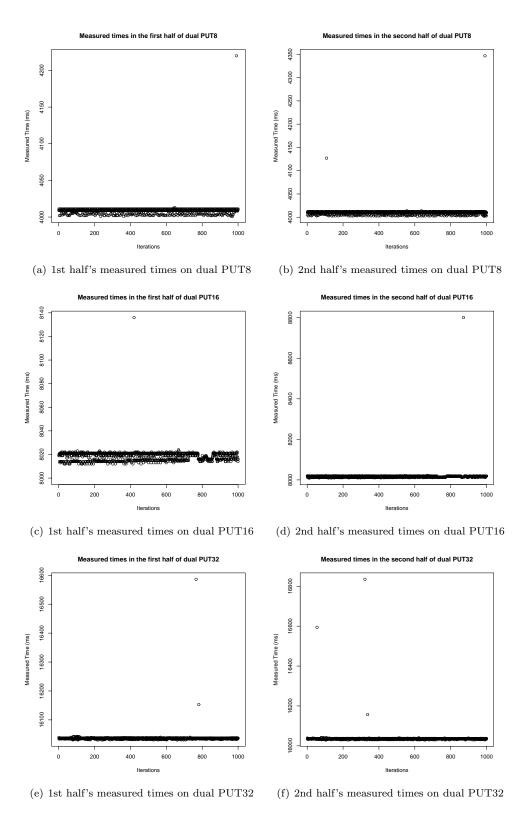


Figure 27: Measured time comparison on dual PUT8~PUT16

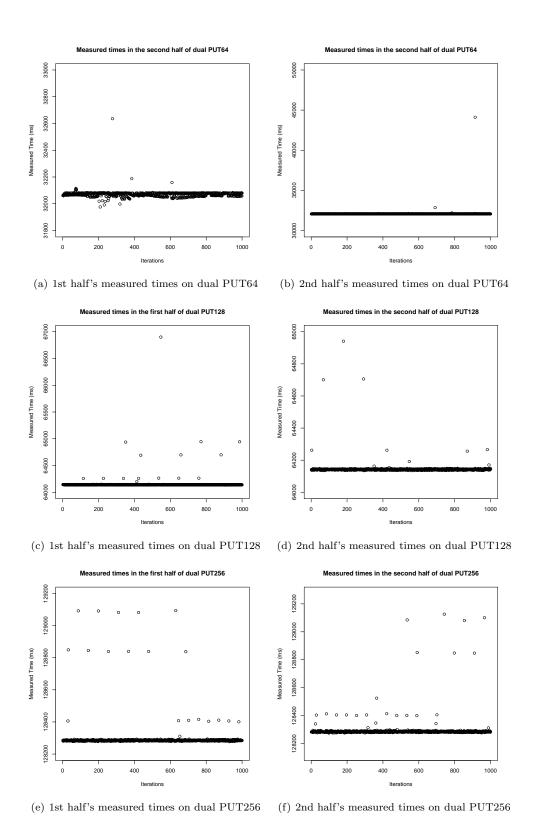


Figure 28: Measured time comparison on dual PUT64  $\sim$  PUT256

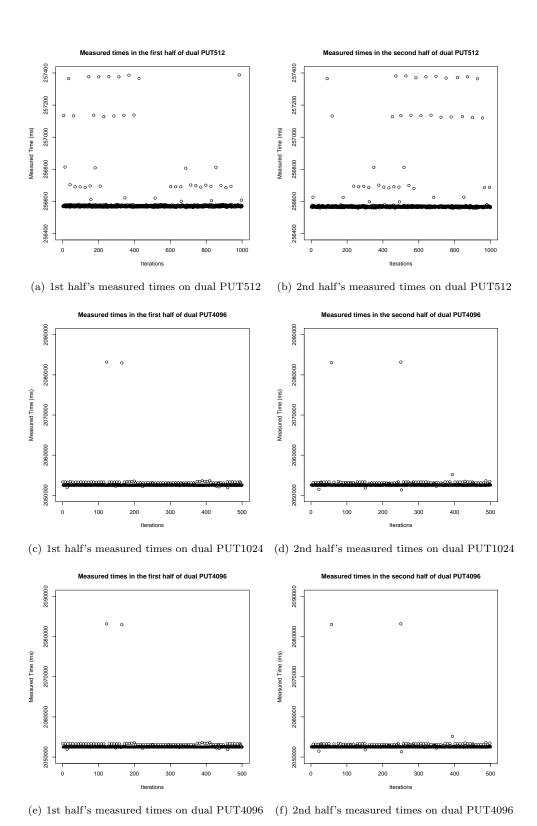


Figure 29: Measured time comparison on dual PUT512, PUT1024, and dual PUT4096

### 7 Successive Iterations' Dependency

In this section we plot measured times of each iteration pair consisting of odd and even iterations. Specifically, the measured times at adjacent, odd and even iterations consist of x and y coordinates and plotted. The data are described in Table 1. The data in Figure 32 exclude outliers chosen by eye.

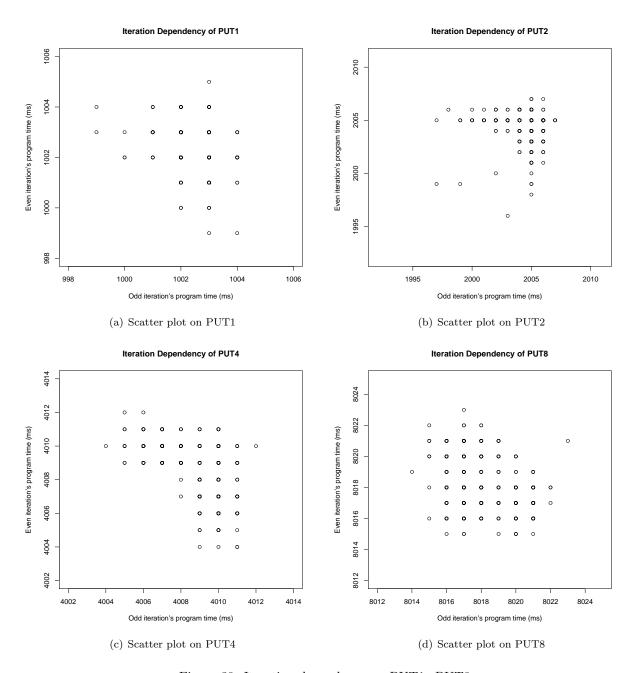


Figure 30: Iteration dependency on PUT1 $\sim$ PUT8

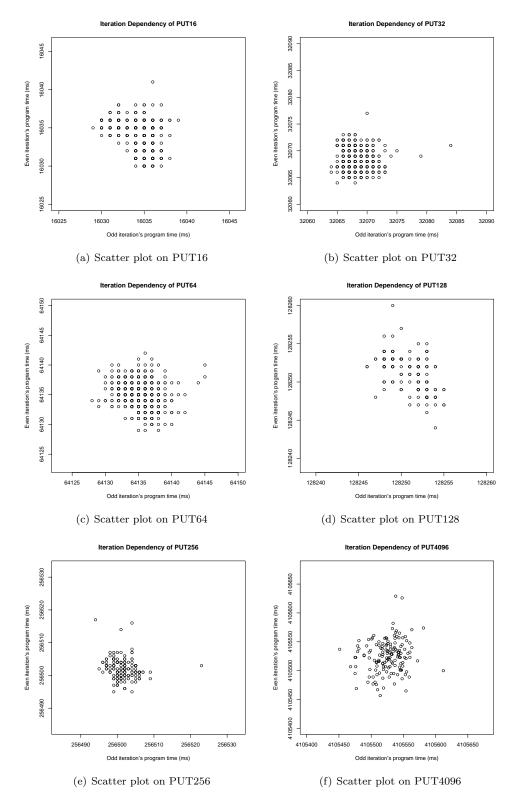


Figure 31: Iteration Dependency on PUT16 $\sim$ PUT256 and PUT4096

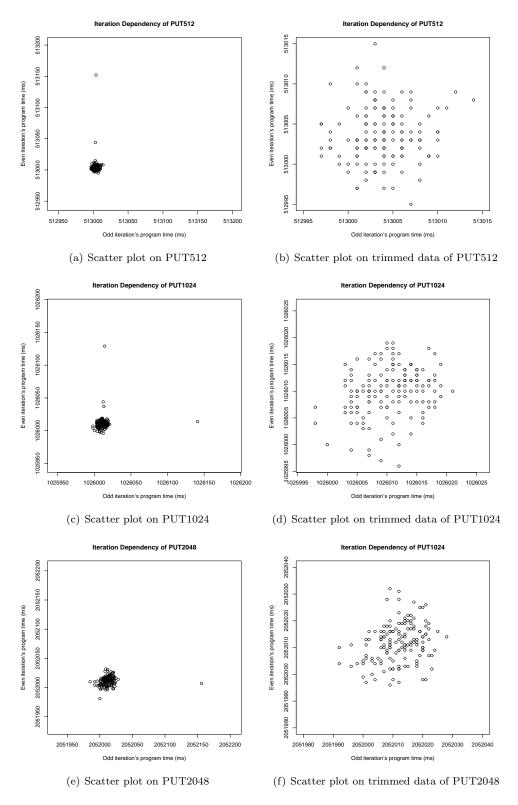


Figure 32: Iteration dependency on PUT512, PUT1024, and PUT2048

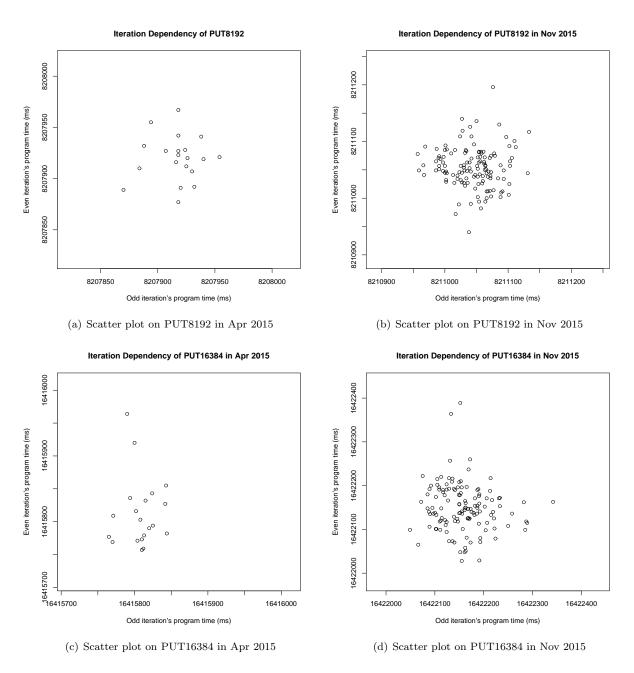


Figure 33: Iteration dependency on PUT8192~PUT16384

### 8 Influence of Daemon Process on Program Time Measurement

In this section we investigate correlations of program times between PUT and a group of daemon processes. The base data, obtained by EMPv4, are from Table 1. It seems that the longer PUT, the stronger correlation of its PT with that of daemon processes.

PUT	Correlation Coefficient by EMPv4	Correlation Coefficient by EMPv5-relaxed
PUT1	-0.2	-0.2
PUT2	-0.005	-0.009
PUT4	-0.05	-0.05
PUT8	0.1	0.1
PUT16	0.1	0.1
PUT32	0.3	0.15
PUT64	0.2	0.2
PUT128	0.2	0.2
PUT256	0.4	0.4
PUT512	0.9	0.6
PUT1024	0.9	0.2
PUT2048	0.8	0.24
PUT4096	0.4	0.4
PUT8192 in Apr	0.4	0.4
PUT8192 in Nov	0.3	0.3
PUT16384 in Apr	0.4	0.8
PUT16384 in Nov	0.5	0.5

Table 10: Correlation Coefficients between Program Times of Daemon and PUT by EMPv4 and EMPv5

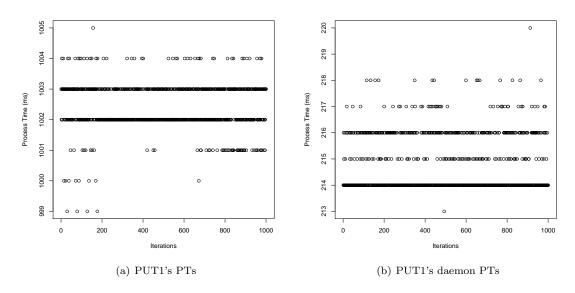


Figure 34: Program times between PUT1 vs. Daemon processes

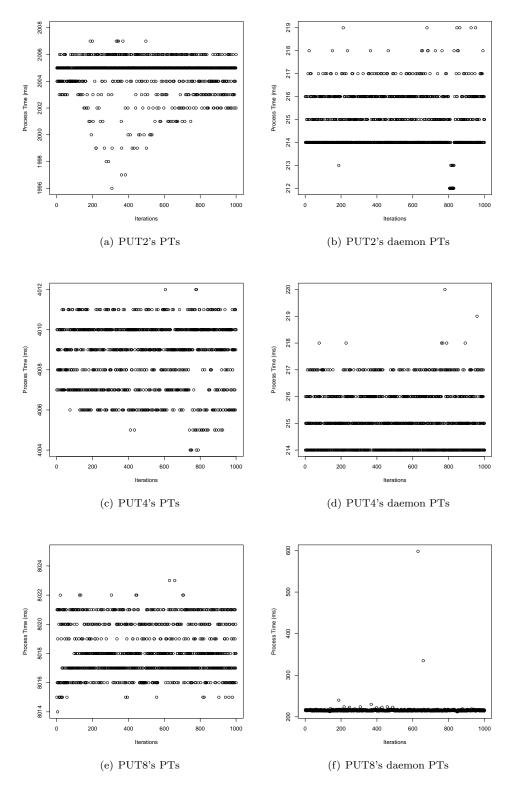


Figure 35: Program times between PUT2 $\sim$ PUT8 vs. Daemon processes

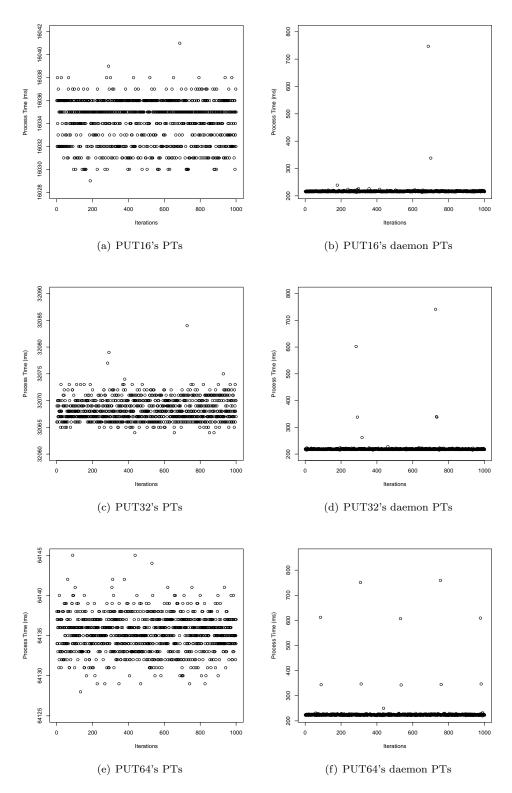


Figure 36: Program times between PUT16~PUT64 vs. Daemon processes

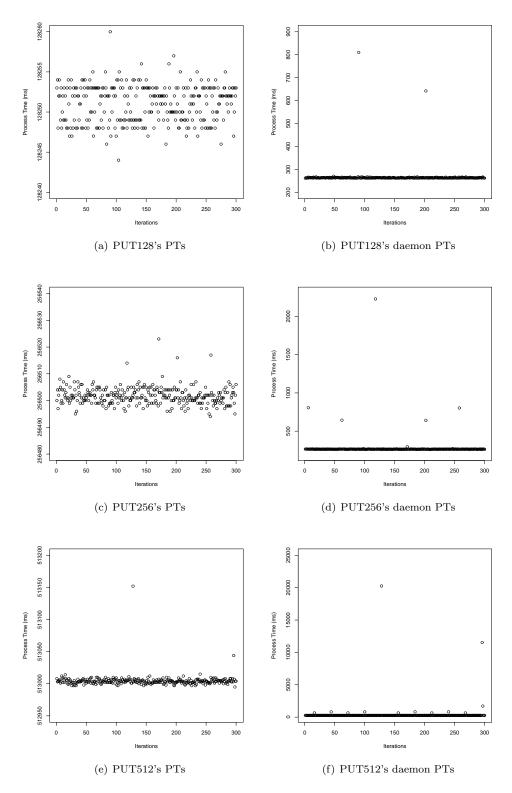


Figure 37: Program times between PUT128~PUT512 vs. Daemon processes

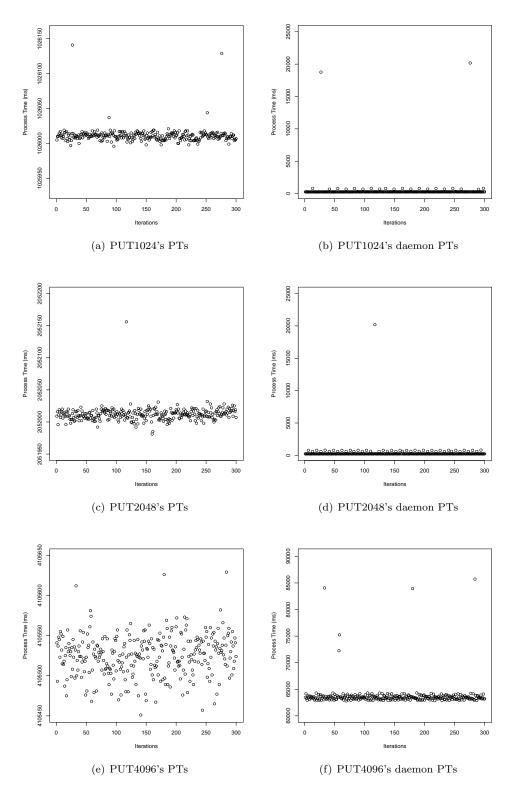


Figure 38: Program times between PUT1024 $\sim$ PUT4096 vs. Daemon processes

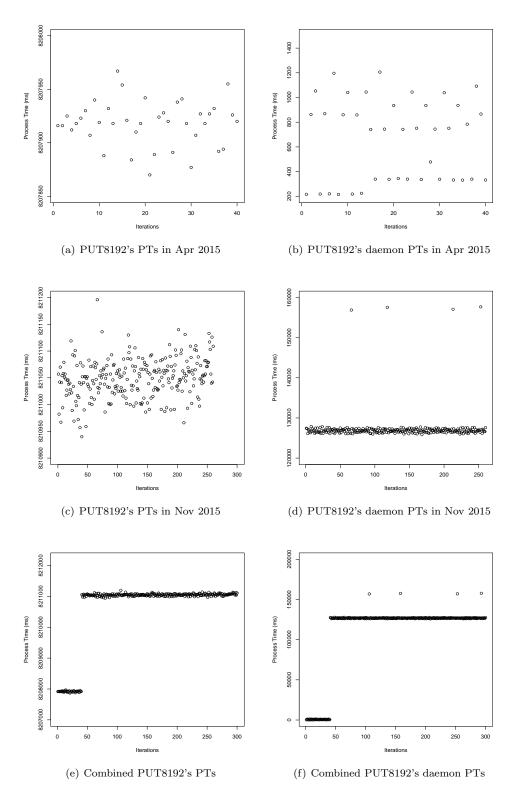


Figure 39: Program times between PUT8192 vs. Daemon processes

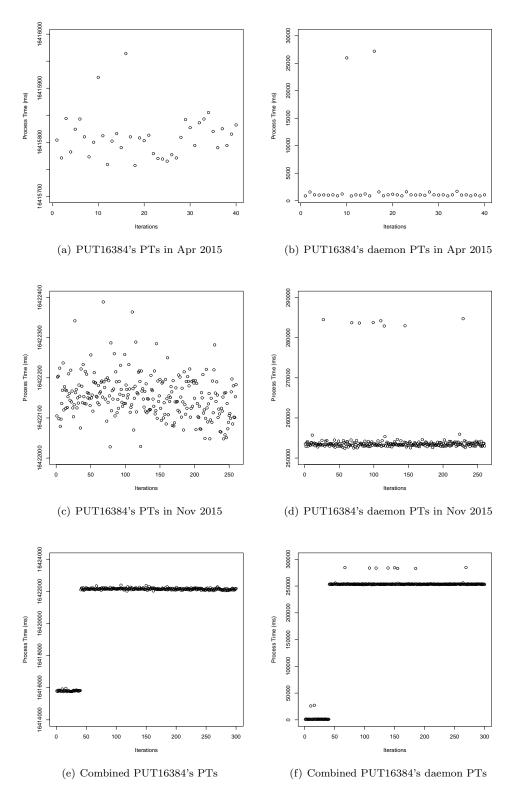


Figure 40: Program times between PUT16384 vs. Daemon processes

#### 9 Conclusion

Below are the summarized observations by this study. (Order does not matter.)

- Typically, the distribution of program times (PTs) of PUT is somewhat mixture of two (or possibly more) models. (But only when you compare fist/second half.)
- Outlier trimming does not well shape a normal distribution of PT. Outliers are higher non-normal. Still, we don't have a precise characterization of outliers, but doing so would be difficult because of very large, very infrequent outliers (cf. Figure 12).
- For a short task length of PUT, it seems there is dependency between iterations in the same run of PUT.
- Presence and activation of (infrequent) daemon processes strongly contribute to creating high variance in PT measurement, due to a few very-far outliers. This results in a very long, very thin tail with a structure we don't understand.
- The bigger task length, the stronger correlation between PTs of PUT and daemon processes, probably because the longer the PUT runs, the more likely that there will be a daemon process. **Caveat**: what if the task size is not large and the sample size is small?
- New: The bigger task length, the more clumps formed, probably caused by different periodicity of different daemon processes (cf. Figures 23 and 24). This implies that when a given task length is big, it will give more room to capture activities of various daemon processes at different times. Accordingly, it leads to observing mixture of two (or more) models, as addressed in the second item.
- When PUT is timed affects PT distribution, due to the presence of daemon processes whose running can't be controlled.
- Measurement protocol is scalable with growing sample size and increasing task length, because the protocol can do the trimming: see above. **Idea**: Run one version \*many\* times to estimate the distribution and what is a reasonable criterion for dropping outliers.

Below is a remaining issue(s) revealed through this study.

• We want a definition of "outlier" over a wide range of program times.

# 10 Appendix

This appendix provides specific details of what daemon processes was captured and how much time was taken at a specific iteration revealing the most program time of a certain PUT.

### 10.1 Breakdown on Program Times of Daemon Processes

PUT256	Program Time
incr_work	256,514 msecs (at the 118th iteration)
Daemon Processes	Program Time
java	2 msecs
md0_raid1	4 msecs
jbd2/md0-8	1 msec
flush-9:0	10 msecs
proc_monitor	262 msecs
rhnsd	6 msecs
rhn_check	1,944 msecs
Total	2,229 msecs

Table 11: The daemon processes captured at the worst PT of PUT256  $\,$ 

PUT256	Program Time
incr_work	513,152 msecs (at the 128th iteration)
Daemon Processes	Program Time
java	2 msecs
md0_raid1	51 msecs
jbd2/md0-8	27 msecs
flush-9:0	86 msecs
proc_monitor	270 msecs
rhnsd	6 msecs
rhn_check	19,820 msecs
Total	20,262 msecs

Table 12: The daemon processes captured at the worst PT of PUT512

PUT4096	Program Time
incr_work	4,105,629 msecs (at the 284th iteration)
Daemon Processes	Program Time
events/0	1 msec
kblockd/0	1 msec
kslowd000	31,710 msecs
kslowd001	31,782 msecs
md0_raid1	82 msecs
jbd2/md0-8	21 msecs
flush-9:0	79 msecs
proc_monitor	206 msecs
rhnsd	3 msecs
ntpd	1 msec
java	2 msecs
rhn_check	21,840 msecs
Total	85,728 msecs

Table 13: The daemon processes captured at the worst PT of PUT4096  $\,$ 

PUT8192	Program Time
incr_work	8,207,884 msecs (at the 244th iteration)
Daemon Processes	Program Time
kblockd/0	3 msecs
kslowd000	31,710 msecs
kslowd001	31,782 msecs
md0_raid1	12 msecs
jbd2/md0-8	2 msecs
proc_monitor	204 msecs
rhnsd	6 msecs
java	1 msec
rhsmcertd-worke	114 msecs
rhsmcertd-worke	114 msecs
rhn_check	708 msecs
Total	64,656 msecs

Table 14: The daemon processes captured at the worst PT of PUT8192  $\,$ 

Daemon Processes	Descriptions
kslowd000 (kslowd001)	A kernel threads for performing things that
	take a relatively long time. "Typically, when
	processing something, these items will spend
	a lot of time, blocking a thread on I/O,
	thus making that thread unavailable for doing
	other work." (http://www.mjmwired.net/
	kernel/Documentation/slow-work.txt)
rhn_check	An external program for check for updates,
	run by rhnsd
rhnsd	"A background daemon process that periodi-
	cally polls the Red Hat Network to see if there
	are any queued actions available. Typically
	started from the initialization (init) scripts in
	/etc/init.d/rhnsd when its time to poll the
	Red Hat Network server for available updates
	and actions. The default interval is every 240
	minutes. The minimum polling interval is 60
	minutes. Any network activity is done via the
	rhn_check utility." (http://linuxcommand.
	org/man_pages/rhnsd8.html)

Table 15: Descriptions of some daemon processes