

Optimal Bidding Strategy for Auto Bidding Campaigns

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Problem Statement

- ▶ Auto bidding requires advertisers to set a campaign budget.
- ▶ Bidding strategies are automated by an algorithm.
- ▶ Objective: Design a bidding algorithm to maximize ad engagement within budget.
- ▶ Importance: Poor performance could lead to advertiser churn and revenue loss.

Solution: Notations

- ▶ B : Campaign budget
- ▶ T : Total auction opportunities
- ▶ t : t^{th} auction opportunity
- ▶ x_t : Indicator if the campaign wins the t^{th} auction
- ▶ c_t : Engagement cost of the t^{th} auction
- ▶ b_t : Bid price at t
- ▶ r_t : Conversion rate at t

Optimization Problem: CPC Campaign Example

- **Objective:** Maximize expected engagement under Second Price Auction(SPA)

$$\max_{x_t \in \{0,1\}} \sum_{t=1}^T x_t r_t$$

- **Constraint:** Stay within budget

$$\sum_{t=1}^T x_t c_t \leq B \quad \text{where } x_t = \mathbb{1}_{\{b_t > c_t\}}$$

Lagrangian Formulation

- Lagrangian:

$$L = \sum_{t=1}^T x_t r_t - \lambda \left(\sum_{t=1}^T x_t c_t - B \right)$$

- Dual Problem:

$$\min_{\lambda \geq 0} \sum_{t=1}^T (r_t - \lambda c_t)_+ + \lambda B$$

Optimality Condition and Solution

- **Optimality Condition:**

$$b_t^* = \frac{r_t}{\lambda^*} \quad \text{where } \lambda^* \text{ is the optimal dual param}$$

- **Bid Update via Dual Online Gradient Descent (DOGD):**

$$\lambda_{t+1} = \lambda_t - \epsilon_t \cdot \left(\frac{B}{T} - c_t \cdot \mathbb{1}_{\{r_t \geq \lambda c_t\}} \right)$$

Extension to Cost Cap

► Problem Formulation

$$\max_{x_t \in \{0,1\}} \sum_{t=1}^T x_t r_t$$

s.t.

$$\sum_{t=1}^T x_t c_t \leq B, \quad \sum_{t=1}^T x_t c_t \leq C \sum_{t=1}^T x_t r_t$$

► Derive Bid Update Rule via DOGD as well

Alternative Solution: Model Predictive Control (MPC)

- ▶ **Model Predictive Control**
- ▶ **Dependent on Bid Landscape Forecasting**
- ▶ **Sensitive to forecasting accuracy**

A/B Testing: Budget Split Test

- ▶ Baseline: PID controller
- ▶ Treatment: OGD
- ▶ **Result:** more than 10% improvement in ROI metrics.