

APS APRIL MEETING 2024

IMPACT OF NOISE TRANSIENTS ON GRAVITATIONAL-WAVE BURST DETECTION EFFICIENCY OF THE BAYESWAVE PIPELINE WITH MULTI-DETECTOR NETWORKS

3RD OF APRIL 2024

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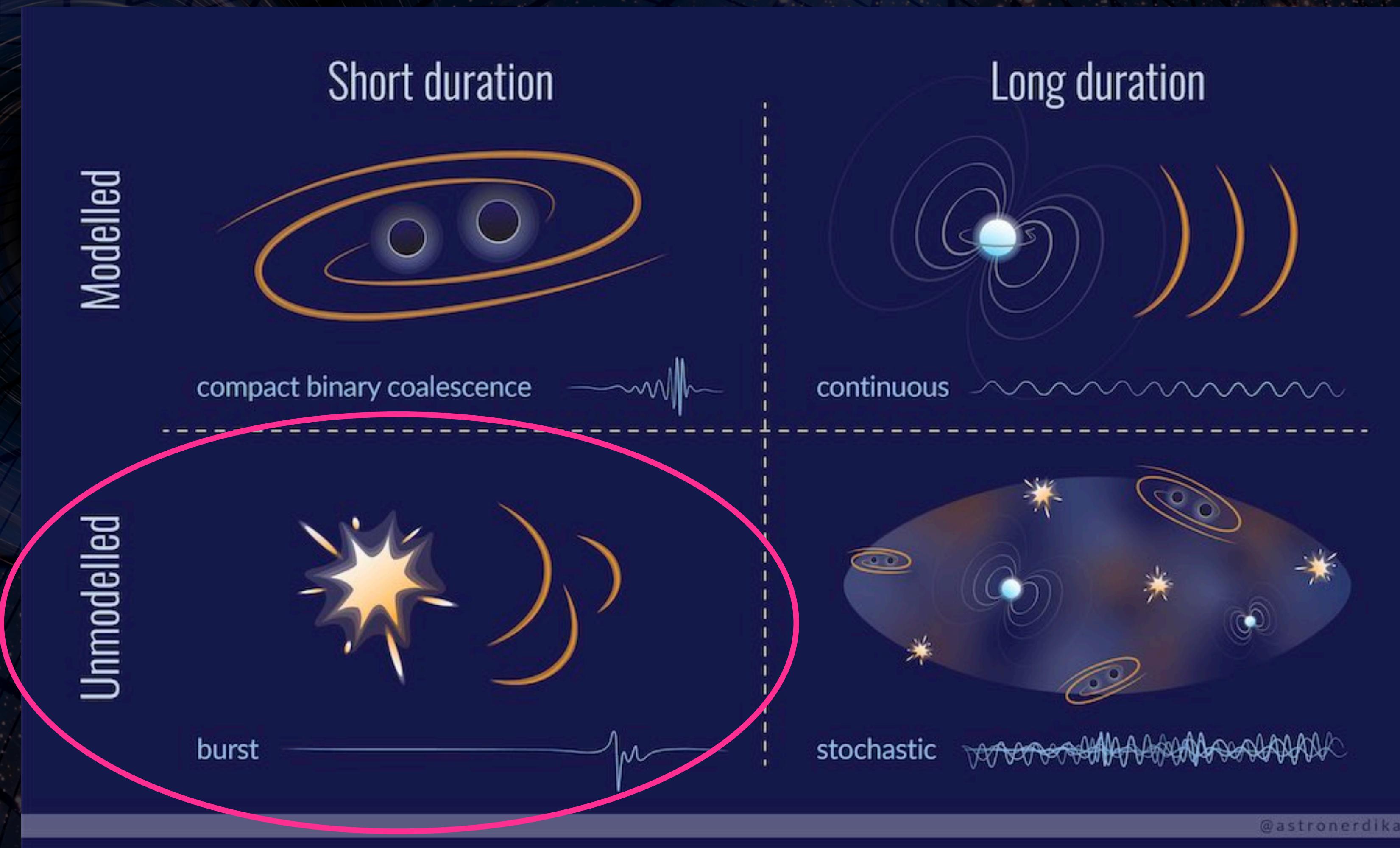
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TYPES OF GW SOURCES



WHAT IS IN THE DETECTOR DATA?

Data

=

Signal
(maybe)

+

Noise



\vec{s}

$h(\vec{\theta})$

\vec{n}

Noise components:

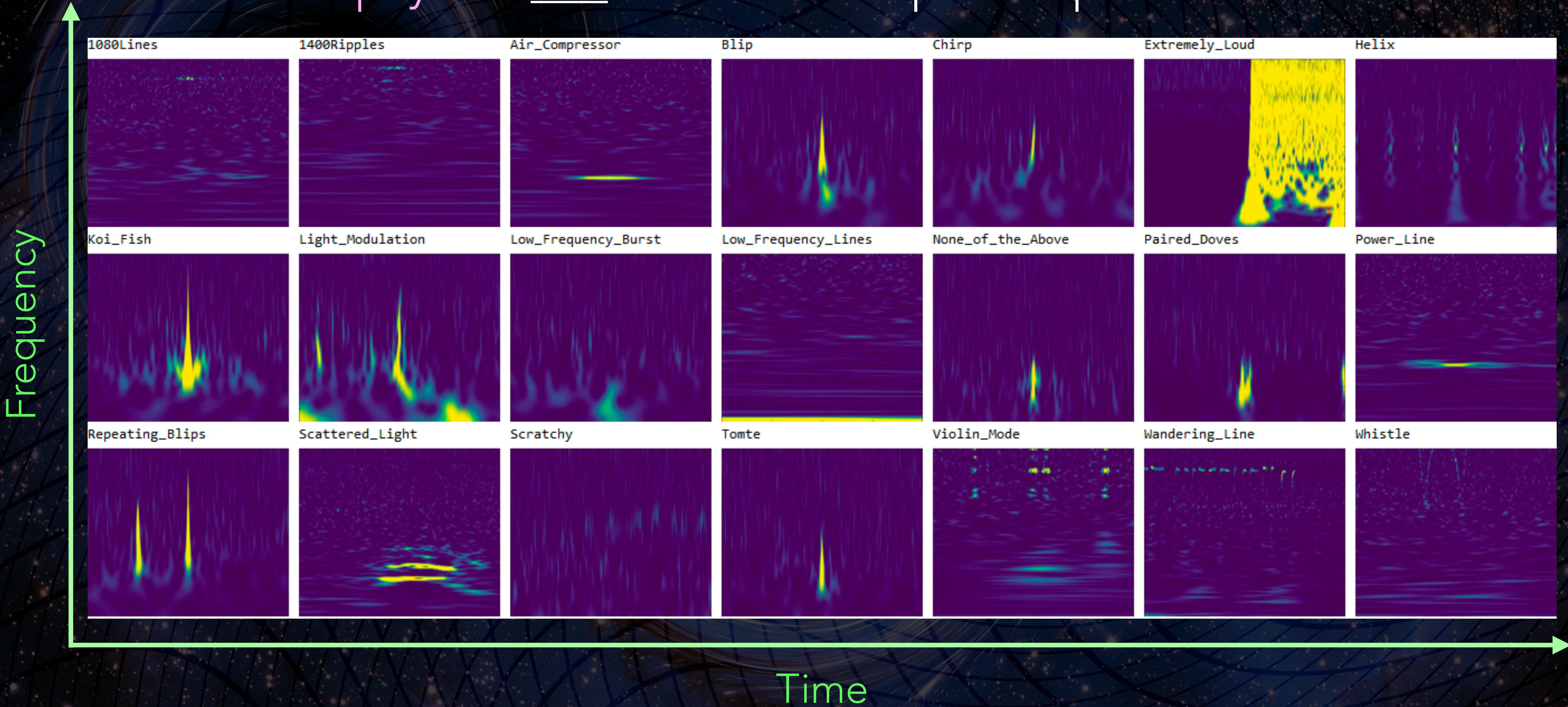
$$\vec{n} = \overrightarrow{n_G} + \vec{g}$$

Stationary, Gaussian noise

Instrumental glitches
(non-stationary, non-Gaussian)

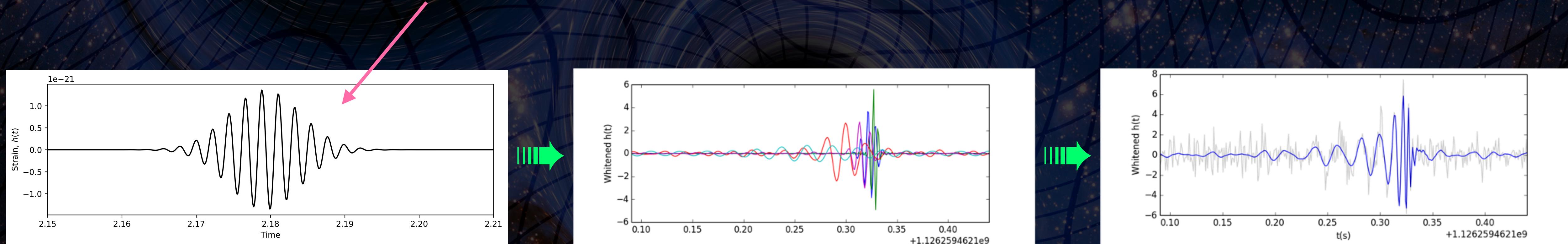
THE PROBLEM: INSTRUMENTAL GLITCHES

Non-astrophysical and non-Gaussian power spikes in the detector



BAYESWAVE: ALGORITHM OVERVIEW

- Unmodelled transient gravitational wave (burst) analysis algorithm
- Enables joint detection of instrumental glitches and GW bursts
- Reconstructs transient, non-Gaussian features in the data by summing a set of sine-Gaussian wavelets, with no *a priori* assumptions



Images courtesy of Meg Millhouse

BayesWave publications:

Cornish + Littenberg, *Class. Quant. Grav.* 32, 130512 (2015)

Cornish et al., *Phys. Rev. D* 103, 044006 (2021)

BAYESWAVE: MODEL SELECTION

- Three independent models:
 - Signal plus Gaussian-noise model, \mathcal{S}
 - Glitch plus Gaussian-noise model, \mathcal{G}
 - Gaussian-noise only model, \mathcal{N}
- Compare models using the **Bayes Factor**

Bayesian evidence ratio between two models

$$\text{e.g. } \mathcal{B}_{\mathcal{S},\mathcal{G}} = \frac{p(\vec{s} | \mathcal{S})}{p(\vec{s} | \mathcal{G})}$$

If $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}} > 0 \Rightarrow \mathcal{S}$ is more strongly supported by data than \mathcal{G}

BAYESWAVE: ROLE IN GW BURST SEARCHES

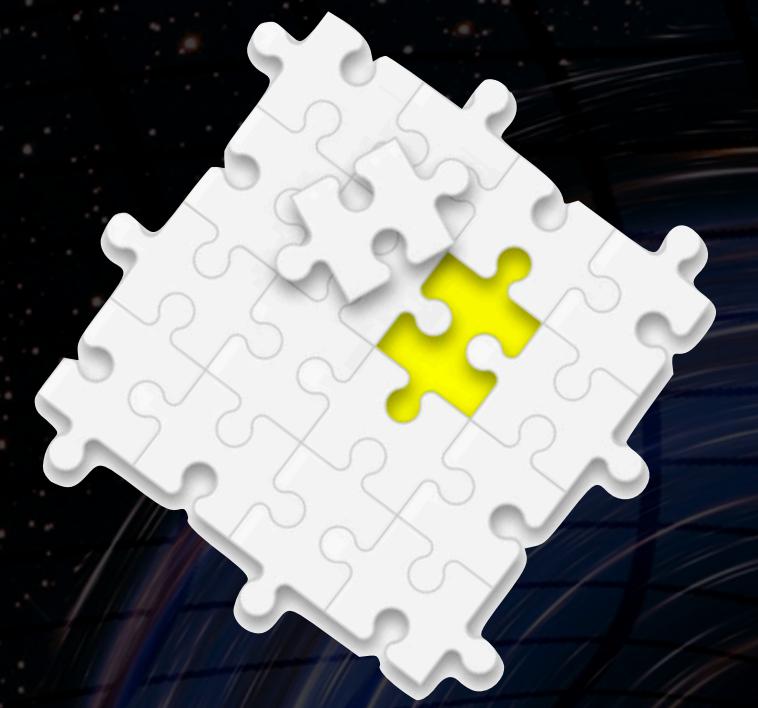
- GWTC-1, -2 and -3:
Assess consistency with matched-filter (model-based) searches
- O1, O2 and O3 all-sky burst searches:
Follow-up trigger events found by coherent WaveBurst (cWB)
- Glitch subtraction
- PSD estimation

GWTC-1: Phys. Rev. X 9, 031040 (2019),
GWTC-2: Phys. Rev. X 11, 021053 (2021),
GWTC-3: arXiv:2111.03606 (2021).

All-sky search O1: Phys. Rev. D 95, 042003 (2017),
All-sky search O2: Phys. Rev. D 100, 024017 (2019),
All-sky search O3: Phys. Rev. D. 104, 122004 (2021).

PREVIOUS WORK - PHYS. REV. D 103, 062002

- BayesWave's detection statistics: $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$
- Global detector network is expanding
- How does the size of the detector network affects $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$?
- Analytically and empirically showed that $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ scales as
 - $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}} \sim \mathcal{I}N \ln \text{SNR}_{\text{net}}$
 - (i) \mathcal{I} : number of detectors
 - (ii) N : number of wavelets (i.e. model complexity)
 - (iii) SNR_{net} : signal-to-noise ratio



THE MISSING PUZZLE PIECE

- This work studies the improvement in $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ of astrophysical triggers with expanded detector networks
- BUT...
Larger detector networks are more susceptible to instrumental glitches i.e. noisier detector backgrounds!



AIM OF THIS WORK

- To study the overall performance of *BayesWave* by accounting for the noise background
- Compare performance between:
 - Hanford-Livingston (HL), 2-detector network
 - Hanford-Livingston-Virgo (HLV), 3-detector network

FALSE ALARM PROBABILITY, P_{FA}

/measure of detection significance/
a function of detection statistics ($\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$)

Probability that a trigger with a given $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ is a
false alarm

Lower P_{FA} = Higher astrophysical significance

DETECTION EFFICIENCY P_{det}

/figure of merit for *BayesWave*'s overall performance/

Probability of detecting an astrophysical event
with a given significance (P_{FA})

EFFICIENCY CURVES

To characterise

DETECTION EFFICIENCY P_{det}

as a function of

FALSE ALARM PROBABILITY P_{FA}

EFFICIENCY CURVE "RECIPE"

2 COMPONENTS:

(1) NOISE BACKGROUND MEASUREMENTS $\rightarrow P_{\text{FA}}$

- Distribution of BayesWave's detection statistics $\ln \mathcal{B}_{\mathcal{S}, \mathcal{G}}$ for **non-astrophysical triggers**

(2) ASTROPHYSICAL MEASUREMENTS $\rightarrow P_{\text{det}}$

- As above, but for **astrophysical triggers**



EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

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STEP 1: Obtaining detection statistics for background triggers

- Down-select triggers from the Coherent WaveBurst (cWB) trigger lists of O3a time-slide data
- Selected triggers satisfy the cWB nominal significance threshold: $\rho \geq 7$
- Analyse triggers using BayesWave to get $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

STEP 1: Down-selecting background triggers

- From Coherent WaveBurst (cWB) trigger lists of O3a time-slide data

Stage 1 down-selection:

Triggers satisfying $\rho \geq 7$

- $\sim 2 \times 10^3$ triggers for HL
- $\sim 7 \times 10^3$ triggers for HLV

Stage 2 down-selection:

Keep only a fraction of $\rho \geq 7$ triggers
(randomly selected)

- 45% of HL $\rightarrow 1008$ triggers
- 15% of HLV $\rightarrow 1134$ triggers

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

STEP 2: Identifying Gaussian-noise-like background triggers

- Events more consistent with the Gaussian-noise model, \mathcal{N} than the Gaussian-noise plus signal model, \mathcal{S} :

$$\ln \mathcal{B}_{\mathcal{S},\mathcal{N}} - \Delta \ln \mathcal{B}_{\mathcal{S},\mathcal{N}} \leq 0$$

- Meaningless to compare odds between signal and glitch models via $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$
- Cannot remove from dataset as they still satisfy $\rho \geq 7$
- Assign arbitrarily low detection statistics: $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}} = -500$
- **THIS APPLIES TO ALL EVENTS IN THIS STUDY!**

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

STEP 3: Calculate P_{FA} as a function of $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$

P_{FA}
/probability of false alarm/

Fraction of non-astrophysical triggers detected above a
given $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ threshold

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

STEP 3: Calculate P_{FA} as a function of $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$

P_{FA}
/probability of false alarm/

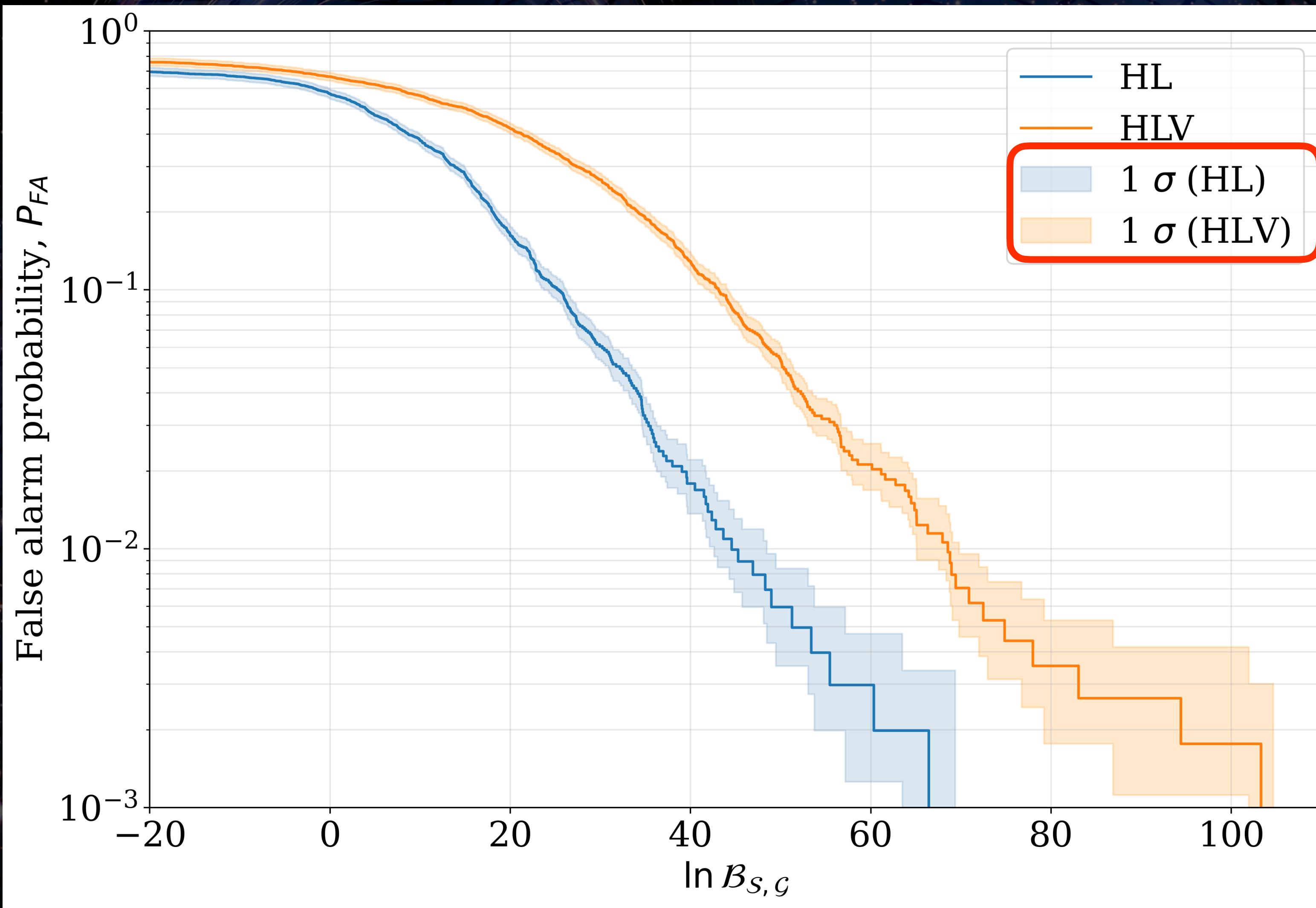
Per-trigger probability (i.e. fraction) of non-astrophysical triggers detected above a given $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ threshold

Why not False alarm RATE (FAR)?

- FAR is a time-averaged quantity
- The timescales of HL and HLV time-slide background data are different

- P_{FA} is time-independent and marginalises over the number of triggers analysed is more suitable for comparison between the two networks

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT



STEP 3: Error bars

Assume Poisson process

s.t.

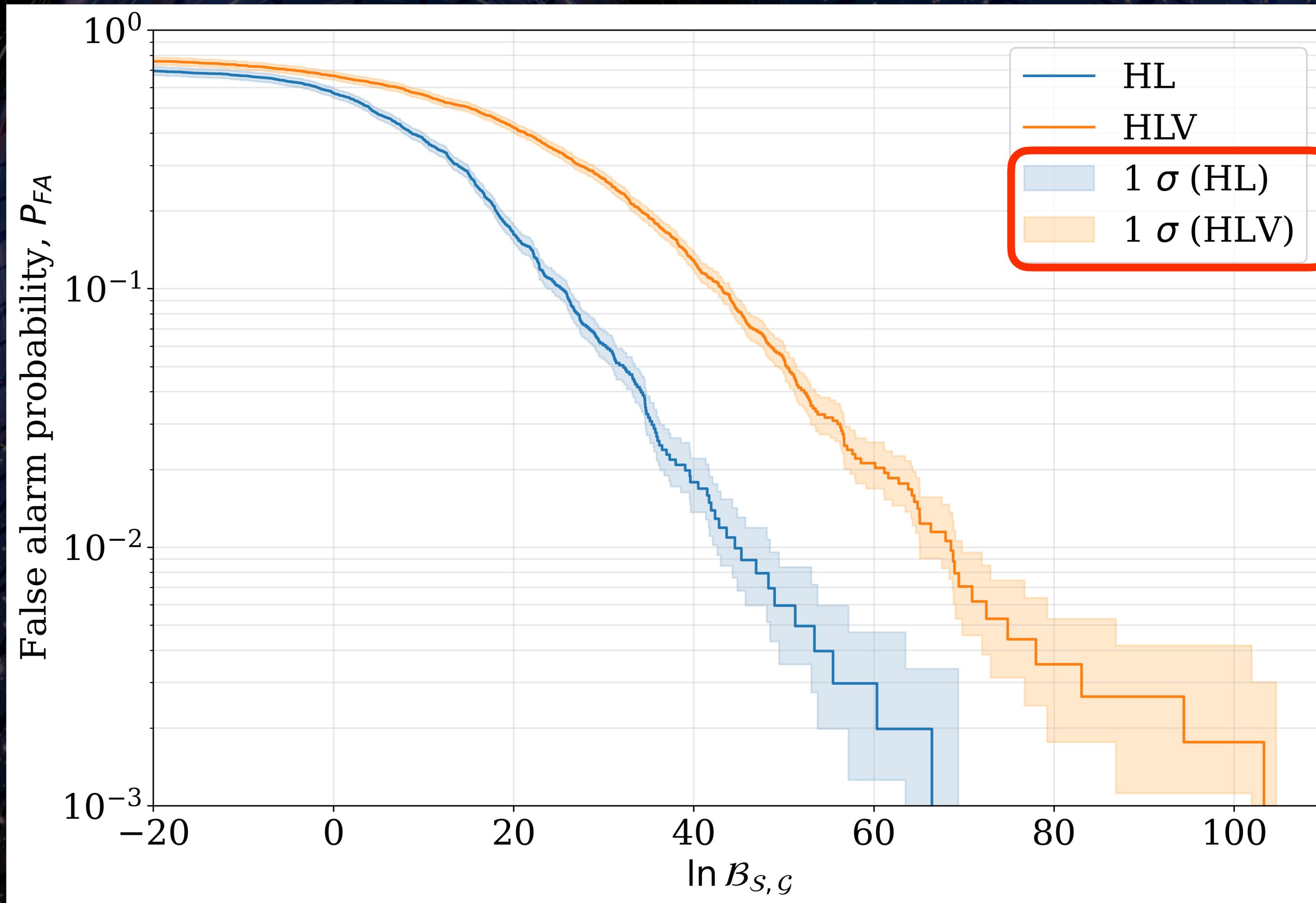
$1-\sigma$ in background event
counts, $n = \sqrt{n}$

∴

$1-\sigma$ in P_{FA} is $\frac{\sqrt{n}}{N}$

N : Total number of triggers
(1008 in HL, 1134 in HLV)

EFFICIENCY CURVE: (1) NOISE BACKGROUND MEASUREMENT

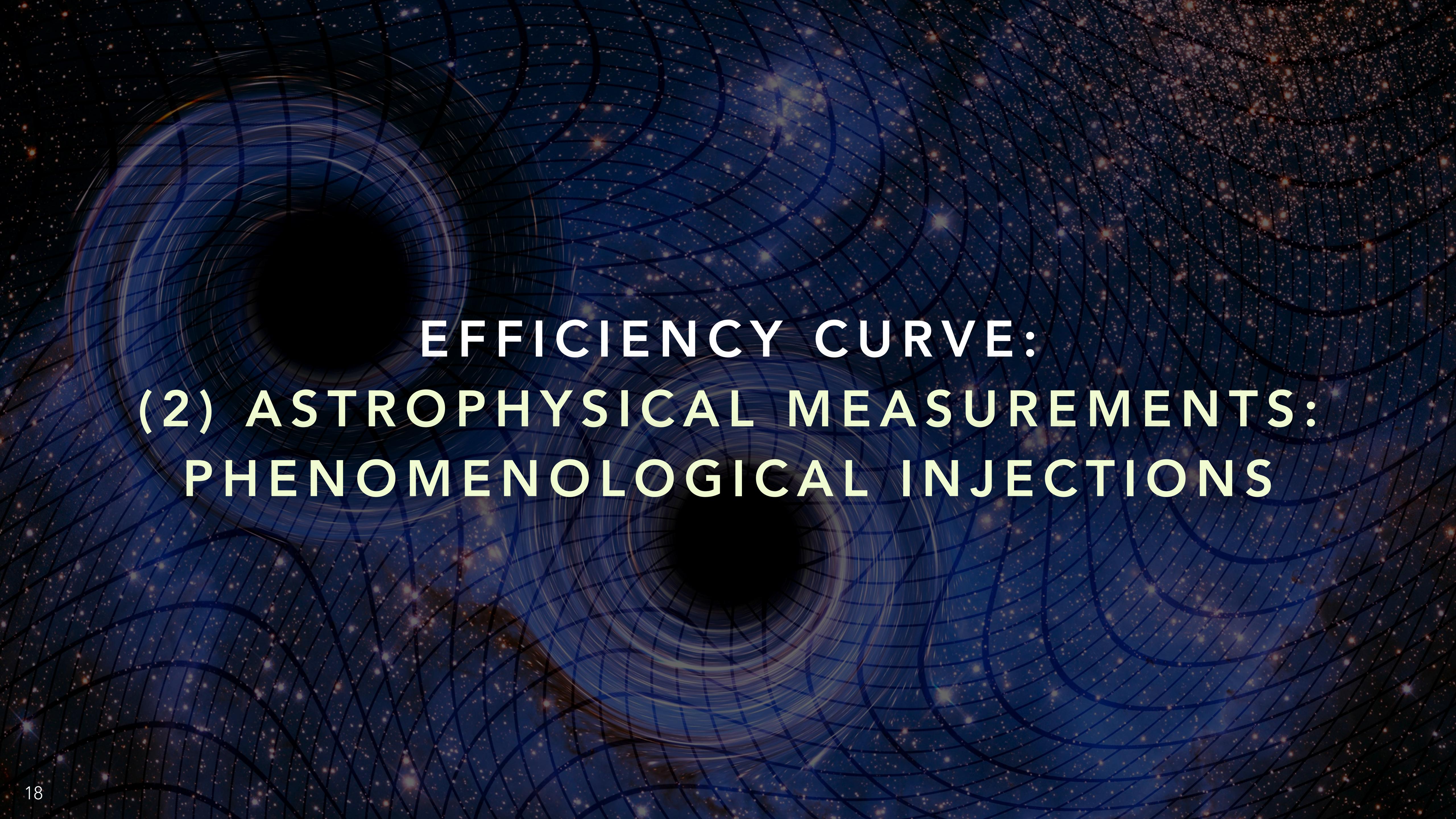


Poisson uncertainty region

Assuming background noise is
a Poisson process

P_{FA} in HLV is higher than HL
for all $\ln \mathcal{B}_{S,G}$

i.e. HLV background is
NOISIER than HL



EFFICIENCY CURVE: (2) ASTROPHYSICAL MEASUREMENTS: PHENOMENOLOGICAL INJECTIONS

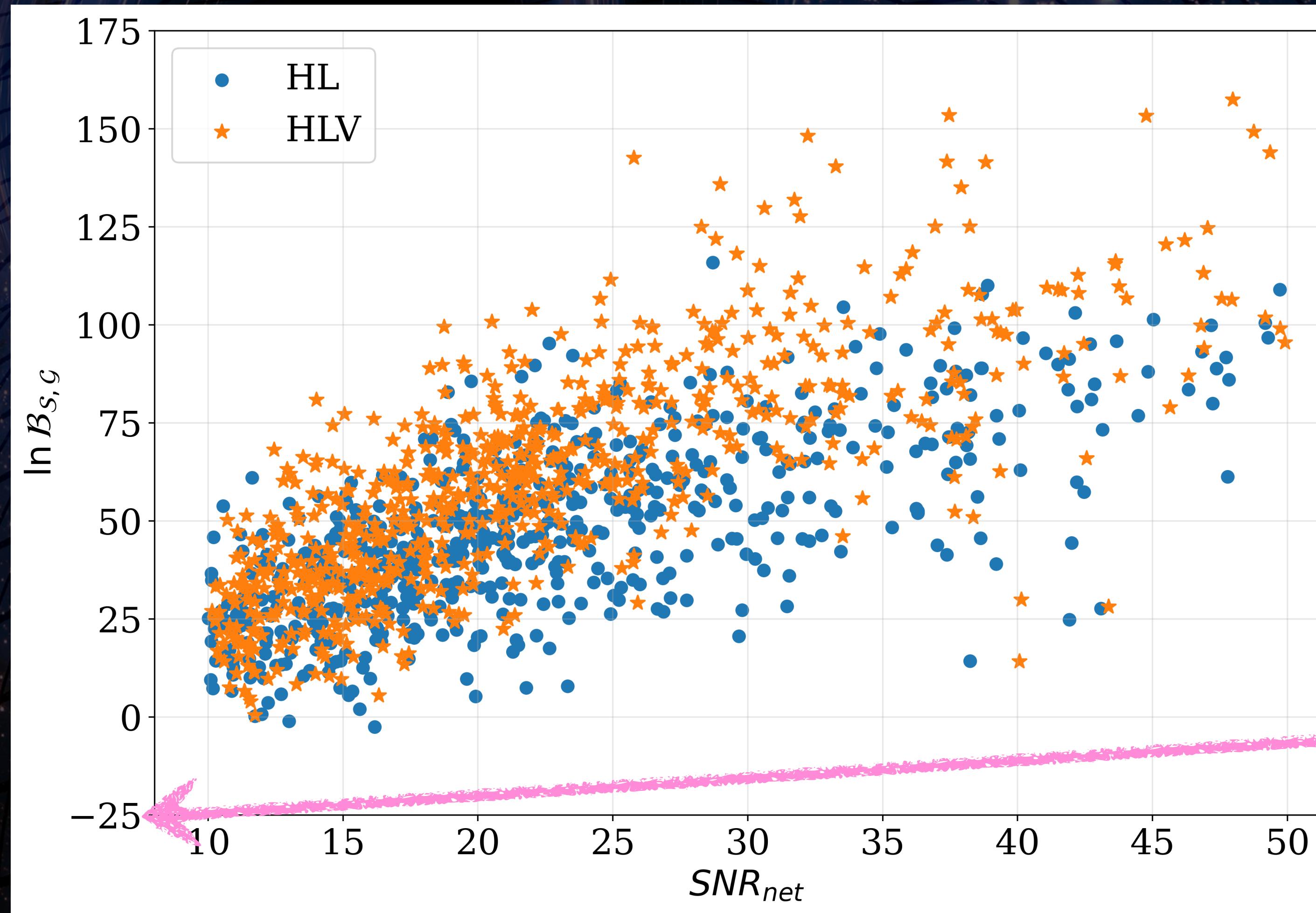
EFFICIENCY CURVE: (2) ASTROPHYSICAL MEASUREMENTS

Properties of Injection Set 1 (IS1)

- Phenomenological binary black hole (BBH) waveforms
- Injected into randomly selected segments throughout all of O3a
- 790 injections, all satisfying $\text{SNR}_{\text{net}} \geq 10$
c.f. Only followed-up cWB (background) events with $\rho \geq 7$

EFFICIENCY CURVE: (2) ASTROPHYSICAL MEASUREMENTS

Distribution of IS1 injections

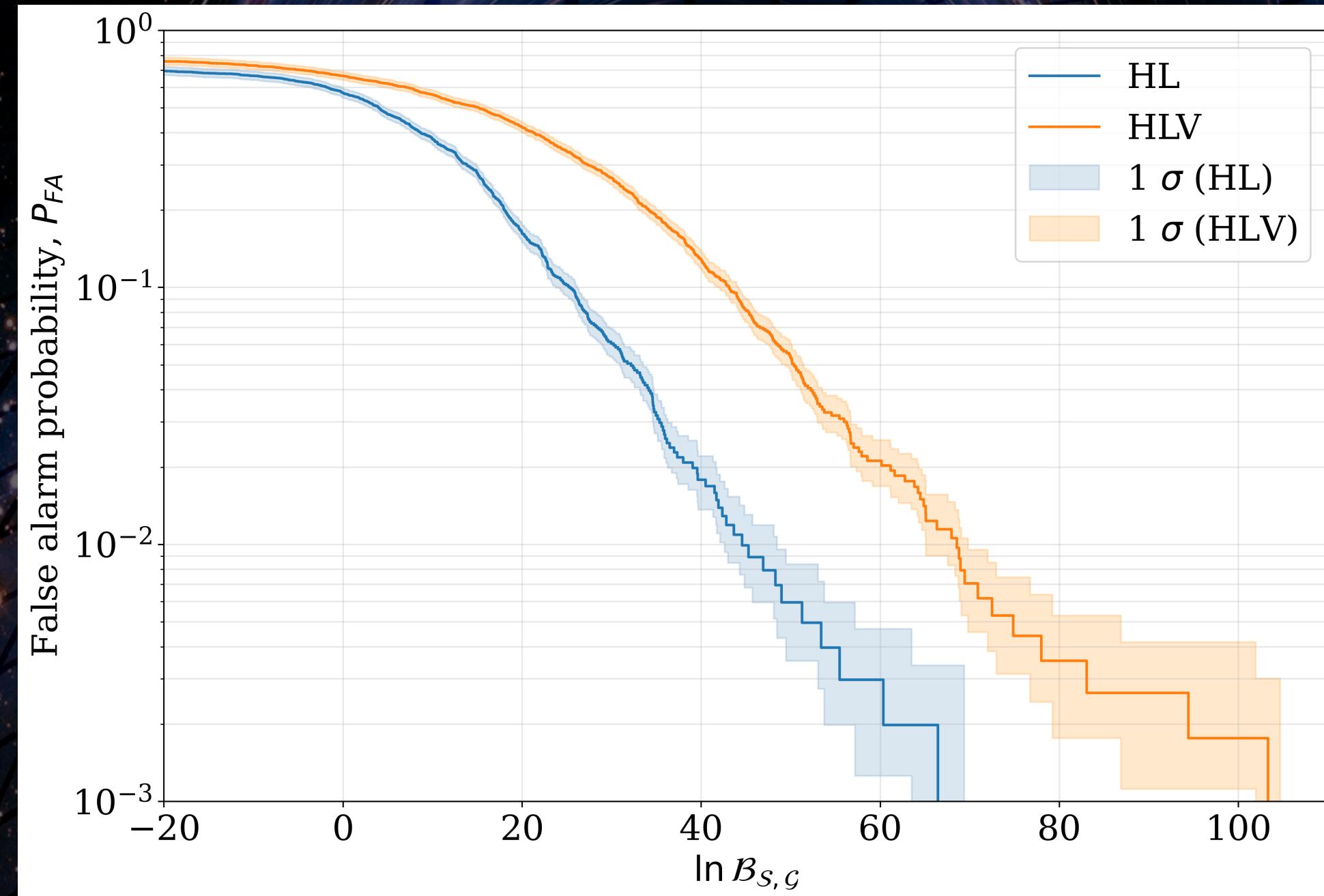


Consistent with previous work:

$$\ln \mathcal{B}_{S,G} \sim \mathcal{I}N \ln \text{SNR}_{\text{net}}$$

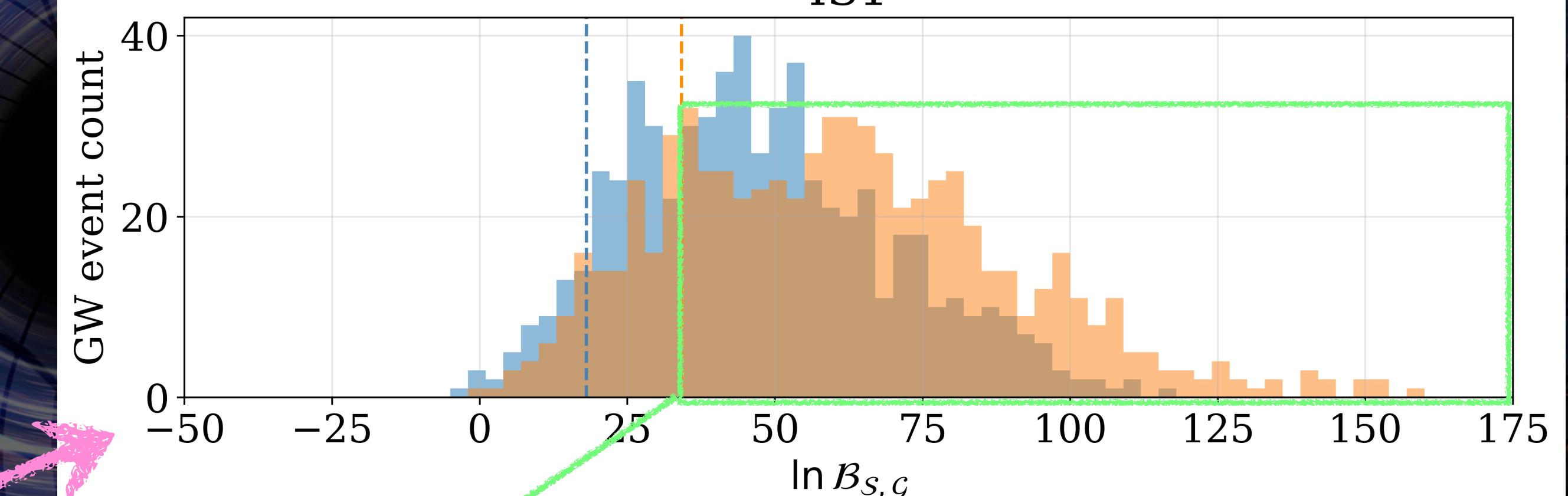
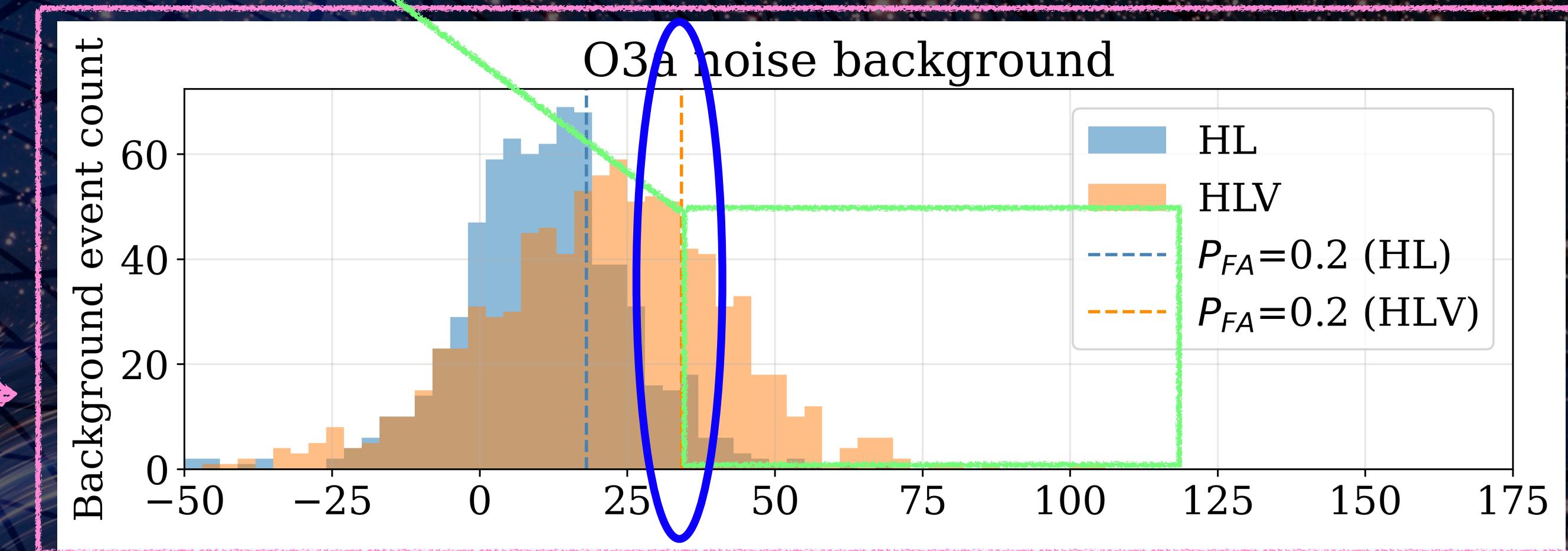
$\ln \mathcal{B}_{S,G} = -500$ events
not shown

CONSTRUCTING EFFICIENCY CURVE



$P_{FA} = 0.2$
/probability of false alarm/

Fraction of non-astrophysical triggers detected above a given $\ln \mathcal{B}_{S,G}$ threshold

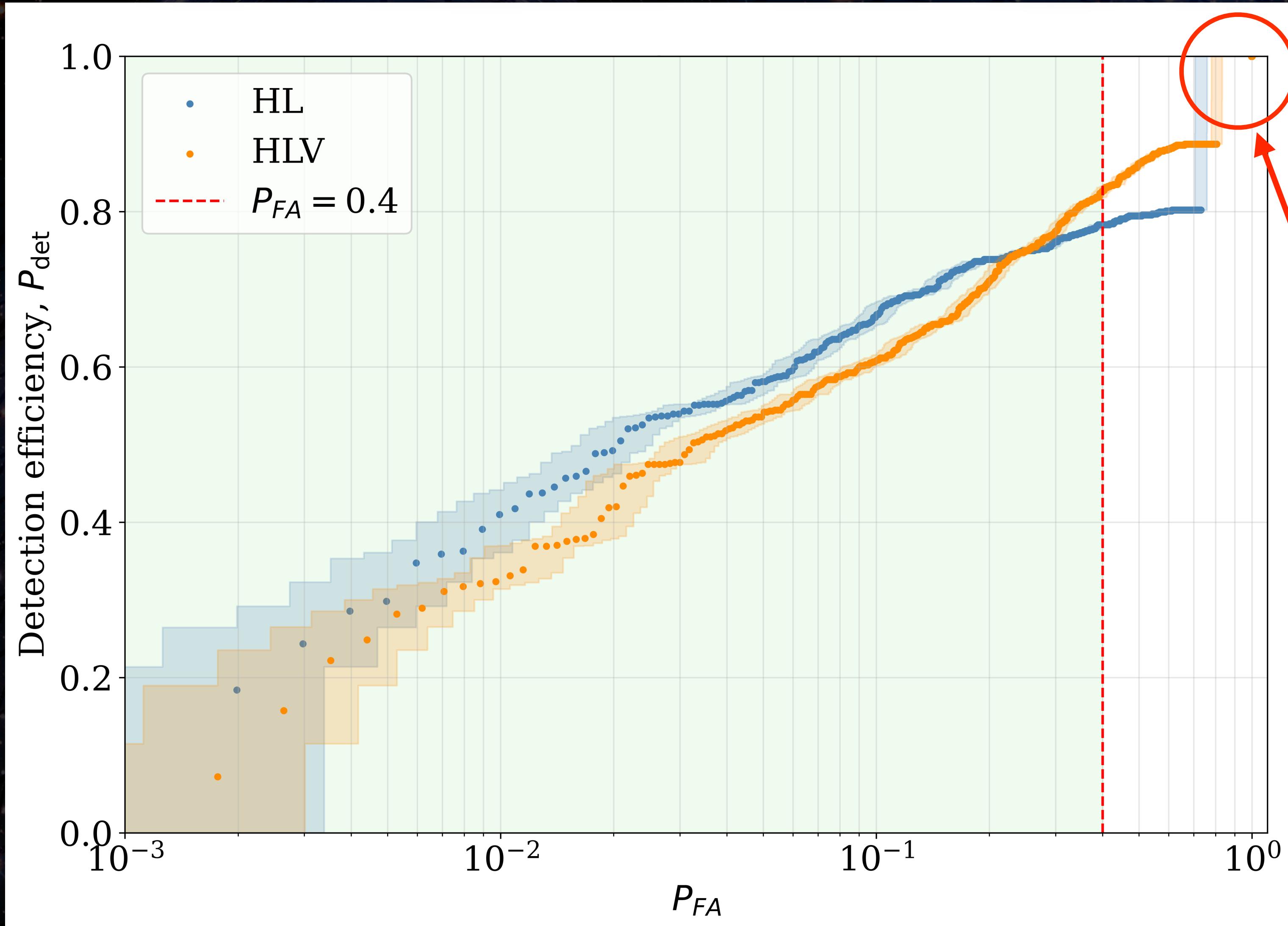


Again, $\ln \mathcal{B}_{S,G} = -500$
events not shown

P_{det}
/Detection efficiency/

Fraction of astrophysical events detected with significance i.e. $P_{FA} \geq 0.2$

EFFICIENCY CURVES OF HL AND HLV



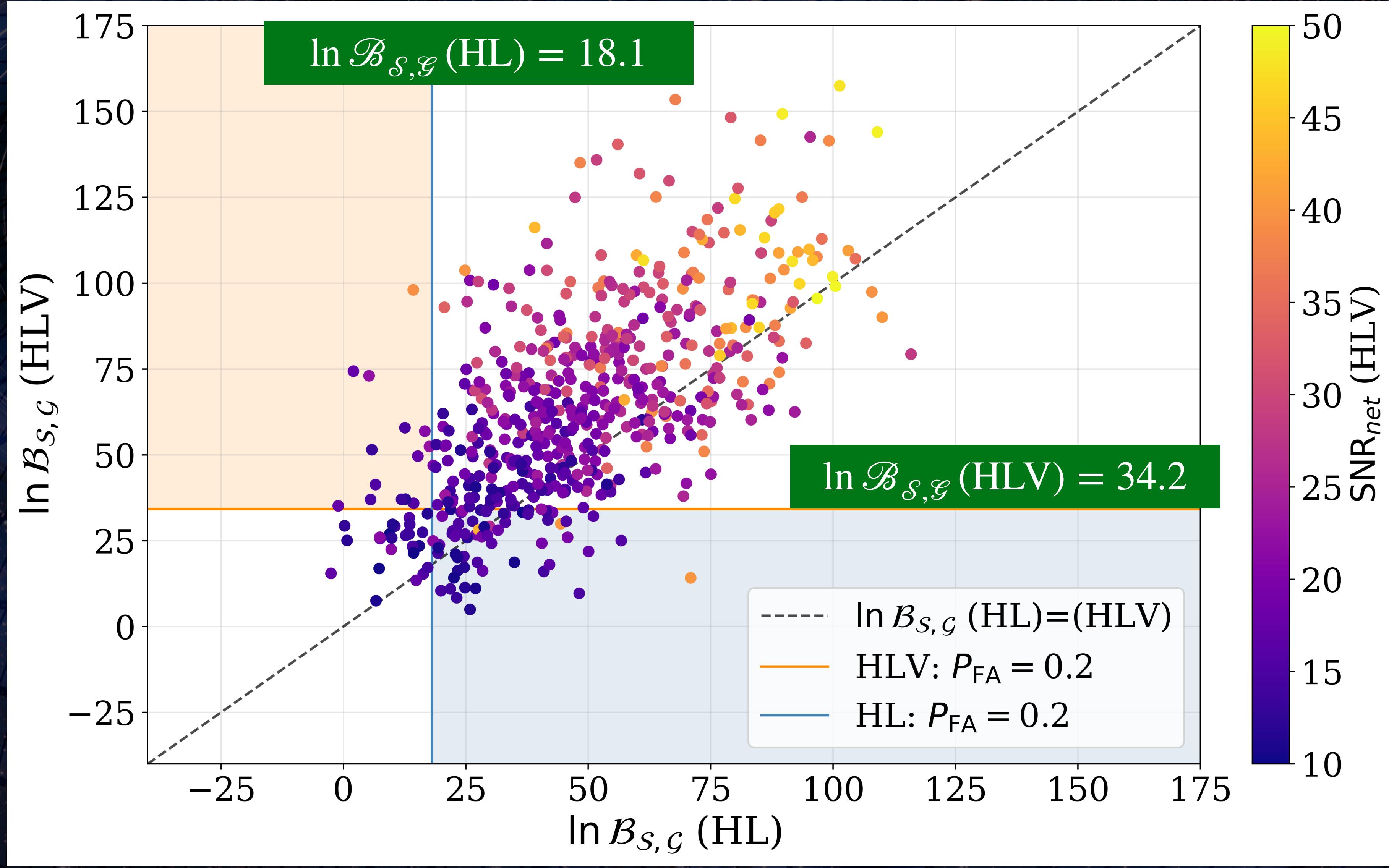
1- σ P_{FA} POISSON UNCERTAINTY REGION
same as background measurement

Cluster of Gaussian-noise-like events with
 $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}} = -500$ and $P_{FA} = 1$
(i.e. minimal detection significance)

Practically meaningful regime $P_{FA} \leq 0.4$

No significant difference between P_{det} of
HL and HLV

P_{FA} AND $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ COMPARISON



INJECTION SET 2 (IS2) O3-LIKE CBC INJECTIONS

- (1) A consistency check
- (2) To measure *BayesWave's* detection significance of O3 GW candidates
Using the HL and HLV backgrounds measured in this study

O3-LIKE CBC INJECTIONS

Properties of Injection Set 2 (IS2)

- **Off-source waveforms:**
 - Waveform parameters sampled from matched-filter posteriors of O3 GW events
 - Injected in the proximity of the actual event
- **18 GW events, each with 50 off-source waveforms**
 - Only follow-up injections with $\text{SNR}_{\text{net}} \geq 10$

O3-LIKE CBC INJECTIONS

Properties of Injection Set 2 (IS2)

- **Off-source waveforms:**
 - Waveform parameters sampled from matched-filter posteriors of O3a/O3b candidate GW events, injected in the proximity of the actual event
 - Consistency test candidates in GWTC-2/GWTC-3
 - 17 candidates from O3a, 5 candidates from O3b
** O3b waveforms are injected into random segments of O3a data
 - 50 off-source waveforms per GW candidate
i.e. $(17+5) \times 50 = 1100$ injections in IS2

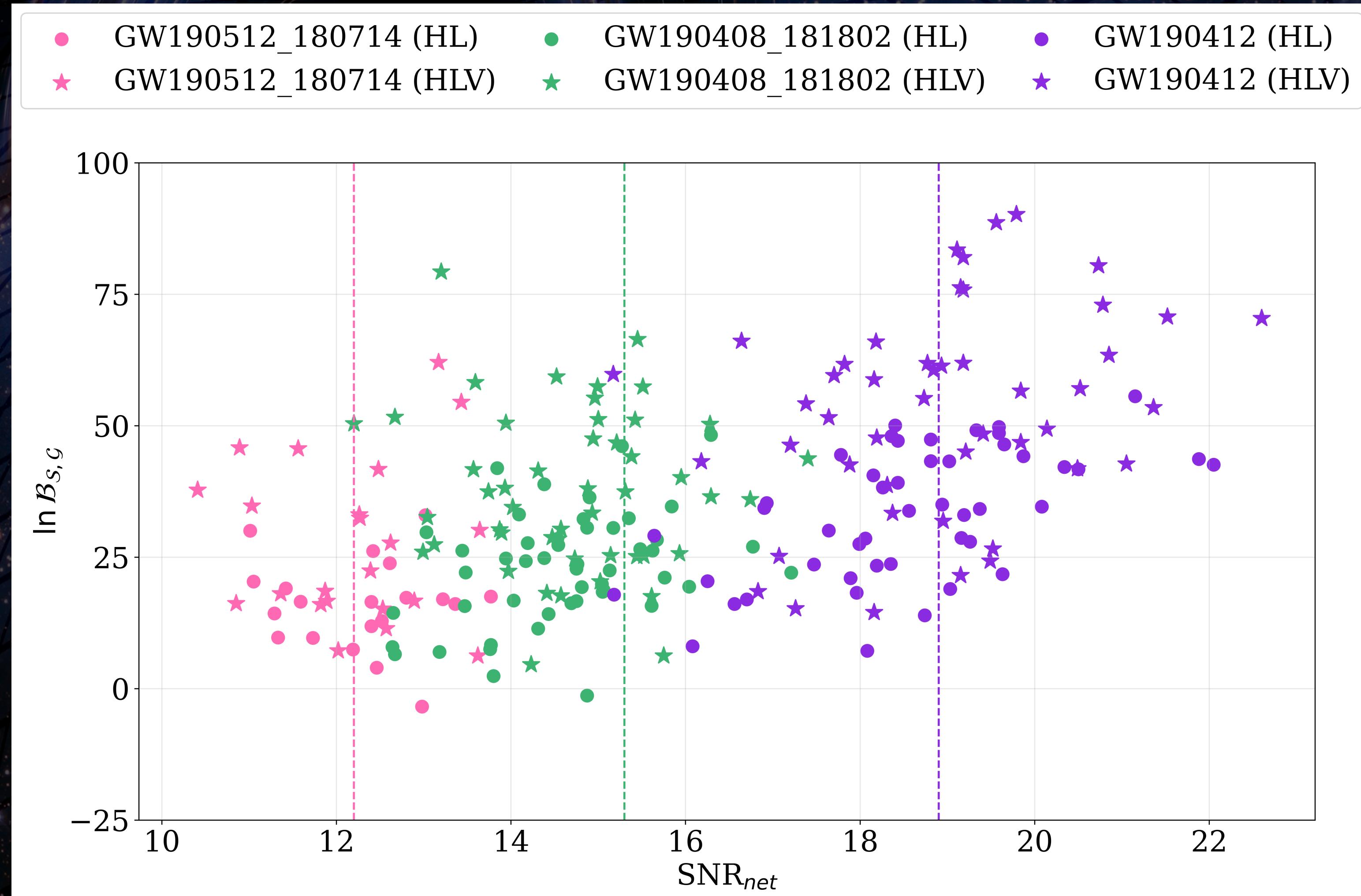
O3-LIKE CBC INJECTIONS

Filtering Injection Set 2 (IS2)

- **Non-detections:**
 - Only follow-up injections with $\text{SNR}_{\text{net}} \geq 10$
 - 4 (low match-filter SNR) GW candidates removed :: ≤ 25 (less than half of off-source waveforms satisfy BayesWave's detection criteria)
- **Gaussian-noise-like injections**
 - Assign arbitrarily low detection statistics: $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}} = -500$

O3-LIKE CBC INJECTIONS

Visualising distributions of off-source injections



Median match-filter SNR

GW190512_180714 → 12.2

GW190408_181802 → 15.3

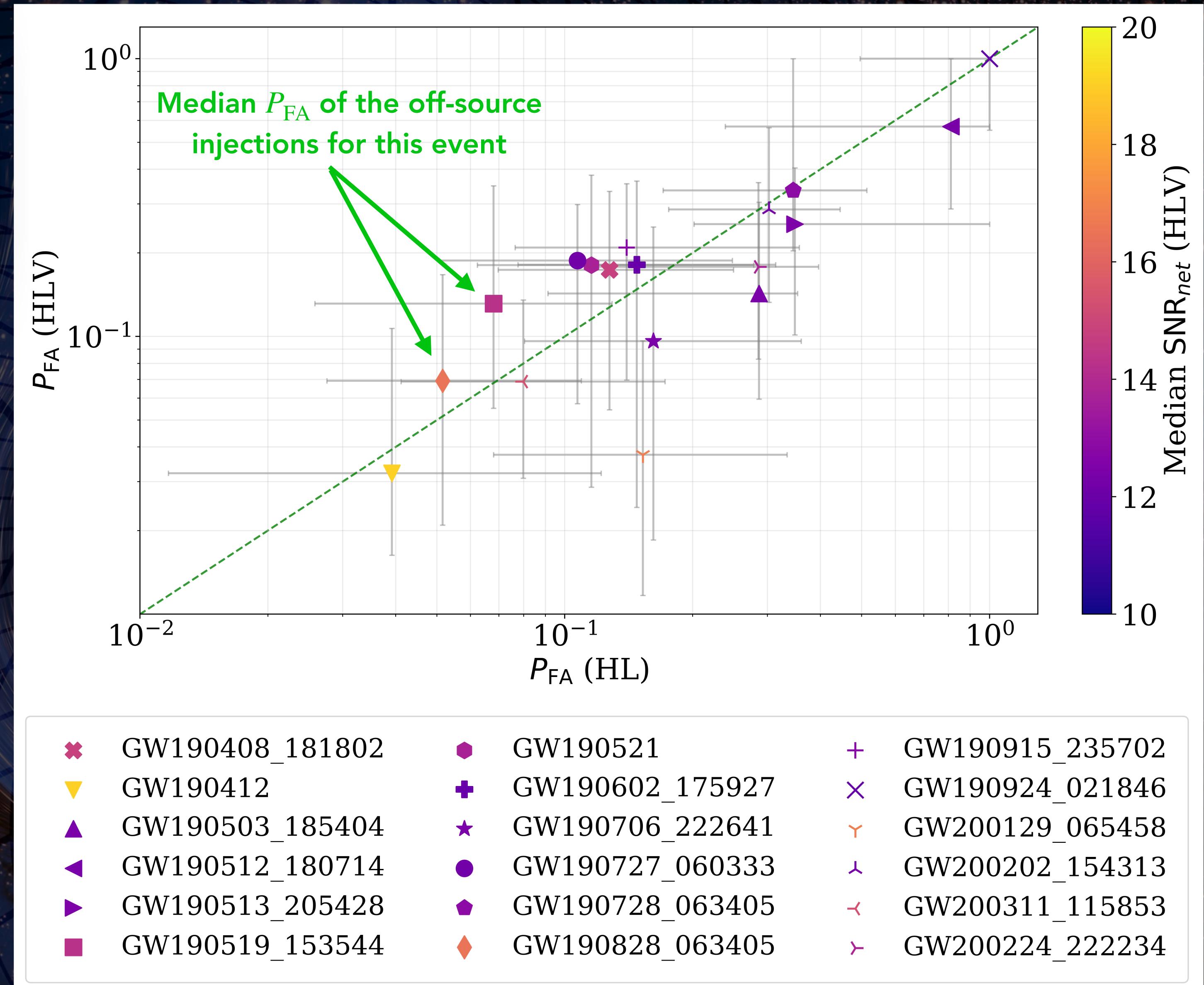
GW190412 → 18.9

P_{FA} comparison - HLV vs. HL

18
O3-LIKE
CBC INJECTIONS

Error bars
IQR of P_{FA} within each GW candidate

All events are detected with comparable significance between HL and HLV



SUMMARY OF RESULTS

- Both the phenomenological BBH injections (IS1) and O3-like events (IS2) show comparable *BayesWave* performance with HL and HLV
 - Although $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ increases with more detectors, false alarm probability P_{FA} is also higher (i.e. noisier detector backgrounds)
∴ Larger detector networks need to attain higher $\ln \mathcal{B}_{\mathcal{S},\mathcal{G}}$ to achieve the same significance (P_{FA}) as smaller networks
- Findings consistent with:
 - LVK O3 all-sky burst search (Phys. Rev. D **104**, 122004)
 - ML-enhanced cWB burst search, Szczepański et al. (2023)

KEY TAKEAWAY

BayesWave's detection efficiency is comparable for two- and three-detector networks

because

more frequent glitches in expanded detector networks offsets the advantage of higher detection statistics

$(\ln \mathcal{B}_{\mathcal{S}, \mathcal{G}})$

[Link to arXiv](#)

