CISS240: Introduction to Programming Assignment 9

Name:	

OBJECTIVES

- Write nested for-loops
- Write nested for-loops containing if/if-else statements.
- Write nested for-loops contained inside if/if-else statements.

Q1. Write a program that prompts the user for 4 integers values for a, b, c, d and prints a table of c-powers to d-powers for integers from a to b. In the output below, the column widths are all set to 15.

Test 1.

3 10 4 7				
	4	5	6	7
3	81	243	 729	2187
4	256	1024	4096	16384
5	625	3125	15625	78125
61	1296	7776	46656	279936
7	2401	16807	117649	823543
81	4096	32768	262144	2097152
91	6561	59049	531441	4782969
10	10000	100000	1000000	10000000

Test 2.

-5 5 4 8					
	4	5	6	7	8
-5	625	-3125	15625	-78125	390625
-4	256	-1024	4096	-16384	65536
-3	81	-243	729	-2187	6561
-2	16	-32	64	-128	256
-1	1	-1	1	-1	1
0	0	0	0	0	0
1	1	1	1	1	1
2	16	32	64	128	256
3	81	243	729	2187	6561
4	256	1024	4096	16384	65536
51	625	3125	15625	78125	390625

Test 3.

1 10 2 2	
	2
1	1
2	4
3	9
4	16
5	25
6	36
7	49
81	64
91	81
10	100

20 20 2 5	2	3	4	5
20	400	8000	160000	3200000

Q2. Write the following program that prints a calendar month. The program prompts the user for three integers: the month, the year, and the day—of—week for the first day of the month (with 0 representing Sunday, 1 representing Monday, etc.) For instance, if the user entered

```
<u>3 2008 6</u>
```

It means that he/she wants the calendar for March 2008 and the first day of the month is a Saturday. The output is

See the "Hints" section for hints and suggestions.

Test 1.

Test 2.

Test 3.

Test 4.

Of course your program should be smart enough to compute the number of days in the month (including leap year cases for the month of February.)

Spoiler Warning ... Incoming Hints ...

Analyze the problem carefully and try to break it down to smaller sub-problems. Look at **Test 1**:

STEP 1. Try to get your program just to do this:

This should be easy. Make sure you try different test cases.

STEP 2. When that's done, you can try to get your program to do this:

```
3 2008 6
March 2008
------
Su Mo Tu We Th Fr Sa
1
```

In other words try to print the first day of the month at the right spot. Again, try as many test cases as possible, making sure that the first day of the month is always printed at the right place.

STEP 3. Next print all the days in the month without wrap—around.

STEP 4. Next get your program to print newline at the right places.

	2008 ril)8			
Su	Мо				Fr 4	
	7 14	8	9	10	11	12
20	21 28	22	23			

Q3. Brute-force search for integer solutions in mod n

Find all solutions to this problem:

$$x * x \% n = a \% n$$

 x is an integer between 0 and $n - 1$

Note that this means that we are only interested in remainders mod n (that's why we are only interested in $0, 1, 2, \ldots, n-1$.) Using the correct mathematical notation in Computer Science (especially in the area of Cryptography) one would say that we're solving this equation:

$$x * x \equiv a \pmod{n}$$

or

$$x^2 \equiv a \pmod{n}$$

The program prompts the user for n and a, prints all the solutions, and prints the number of solutions.

Let's do one by hand. Let's try n=5 and a=1. Then, the equation we are looking at is this:

$$(x*x)\%5 = 1\%5$$

x is an integer between 0 and 4

i.e.,

$$(x*x)\%5 = 1$$

x is an integer between 0 and 4

Next, we try all the integers from 0 to 4 and see which one is a solution:

x	(x*x)%5
0	(0*0)%5 = 0%5 = 0
1	(1*1)%5 = 1%5 = 1
2	(2*2)%5 = 4%5 = 4
3	(3*3)%5 = 9%5 = 4
4	(4*4)%5 = 16%5 = 1

The solutions are x = 1, x = 4. (See Test 1.)

Test 1.

<u>5 1</u>			
1 4			
2			

Test 2.

```
1<u>9 2</u>
0
```

Test 3.

```
19 4
2 17
2
```

Test 4.

```
19 5
9 10
2
```

(Note: Is it true that there are always either none or exactly two solutions when n is prime?)

Q4. Brute force search for integer solutions

Here's something from Wikipedia:

1729 is known as the Hardy-Ramanujan number, after a famous anecdote of the British mathematician G. H. Hardy regarding a hospital visit to the Indian mathematician Srinivasa Ramanujan. In Hardy's words:

"I remember once going to see him when he was ill at Putney. I had ridden in taxi cab number 1729 and remarked that the number seemed to me rather a dull one, and that I hoped it was not an unfavorable omen. "No,"he replied, "it is a very interesting number; it is the smallest number expressible as the sum of two cubes in two different ways.""

Numbers such as

$$1729 = 1^3 + 12^3 = 9^3 + 10^3$$

that are the smallest number that can be expressed as the sum of two cubes in n distinct ways have been dubbed taxicab numbers. 1729 is the second taxicab number (the first is $2 = 1^3 + 1^3$). The number was also found in one of Ramanujan's notebooks dated years before the incident.

Write a program that prompts the user for an integer z and finds all positive (i.e., at least 1) integer solutions to the equation

$$x^3 + y^3 = z$$

Do not list repeats. For instance when z is 1729

$$1^3 + 12^3 = 1729$$
$$12^3 + 1^3 = 1729$$

But only 1, 12 should be listed (i.e., do not list 12, 1.)

[Hint: Write a double for-loop.]

Test 1.

1

Test 2.

 $\frac{2}{1,1}$

Test 3.

1729	
1,12 9,10	

2000	
10,10	

Q5. The above exercise verified that there are exactly two integer solutions. It does not verify that 1729 is the "smallest number expressible as the sum of two cubes in two different ways". To do that you need to solve this:

$$x^3 + y^3 = z$$

where z runs from 1 to 1729.

Write a program that prompts the user for an integer variable n and prints solutions to

$$x^3 + y^3 = z$$

for positive integers x, y, z where z runs from 1 to n. (Here, positive integers means integers which are at least 1.) You should print out x, y, and z only when there is at least one solution. See the output for the format.

Test 1.

```
1729
2: 1,1
9: 1,2
16: 2,2
28: 1,3
35: 2,3
54: 3,3
65: 1,4
72: 2,4
91: 3,4
126: 1,5
128: 4,4
133: 2,5
152: 3,5
189: 4,5
217: 1,6
224: 2,6
243: 3,6
250: 5,5
280: 4,6
341: 5,6
344: 1,7
351: 2,7
370: 3,7
407: 4,7
432: 6,6
```

```
468: 5,7
513: 1,8
520: 2,8
539: 3,8
559: 6,7
576: 4,8
637: 5,8
686: 7,7
728: 6,8
730: 1,9
737: 2,9
756: 3,9
793: 4,9
854: 5,9
855: 7,8
945: 6,9
1001: 1,10
1008: 2,10
1024: 8,8
1027: 3,10
1064: 4,10
1072: 7,9
1125: 5,10
1216: 6,10
1241: 8,9
1332: 1,11
1339: 2,11
1343: 7,10
1358: 3,11
1395: 4,11
1456: 5,11
1458: 9,9
1512: 8,10
1547: 6,11
1674: 7,11
1729: 1,12 9,10
```

Test 2.

The input for the following test is 5000. I'm only showing part of the output because the full listing is too long.

```
<u>5000</u>
... OUTPUT NOT DISPLAYED HERE ...
4075: 11,14
4097: 1,16
4104: 2,16 9,15
4123: 3,16
4160: 4,16
4221: 5,16
4312: 6,16
4375: 10,15
4394: 13,13
4439: 7,16
4472: 12,14
4608: 8,16
4706: 11,15
4825: 9,16
4914: 1,17
4921: 2,17
4940: 3,17
4941: 13,14
4977: 4,17
```

Q6. Write a program that prompts the user and produces the following ASCII art.

Test 1.



Test 2.



Test 3.

```
<u>3</u>
* *
* *
* *
```

```
4
* *
* *
* *
*
```

Q7. Another crazy pesky ASCII art problem . . .

Test 1.

```
<u>1</u> *
```

Test 2.

```
2
*
***
```

Test 3.

```
<u>3</u>
*
***
****
```

Test 4.

```
4
*
***
***
****
```

Test 5.

```
<u>5</u>

*

***

***

***

***
```

Test 6.

```
6

*

***

***

***

***

****
```

Test 7.

```
7
```

Test 8.

Test 9.

```
9
```

Test 10.

```
<u>10</u>
```

Test 11.

```
<u>11</u>
```

Test 12.

```
12
```

Spoiler Warning ... Incoming Hints ...

This problem is not as difficult as you think. This is Test 10:

Test 10

Of course, you can see that there are ten lines. You would expect a for-loop where i runs from 1 to 10. Each iteration of the loop basically prints some spaces, some stars, and a newline. The question is this: how many spaces and how many stars?

Each time you go to the next line, the number of spaces and number of stars changes in a certain way.

The general structure of the code for the case when the user enters 10 is this:

```
prompt user for n
numSpaces = ???
numStars = ???

for i = 1, 2, 3, 4, ..., n:
   print numSpaces spaces
   print numStars stars
   print newline (i.e., std::endl)

   modify numSpaces
   modify numStars
```

I suggest you initialize numSpaces to 20 and try to get numStars correct first:

```
prompt user for n
numSpaces = 20 // temporary!!!
numStars = ???
```

```
for i = 1, 2, 3, 4, ..., n:
    print numSpaces spaces
    print numStars stars
    print newline (i.e. std::endl)

    update numStars
    update numSpaces
```

Complete this table and see the pattern when you run the program with n = 10.

```
i = 1    numStars = 1
i = 2    numStars = 3
i = 3    numStars = 5
i = 4    numStars = 3
```

Here's a final hint: numStars goes up by 2 when a condition is true and goes down by 2 when that condition is false. (This tells you that this is an if-else). What is that condition? (Of course the condition depends on i.)

In fact, the condition is used for the update on numSpaces as well. In other words, the code looks like this:

```
prompt user for n
numSpaces = 20 // temporary
numStars = ???
for i = 1, 2, 3, 4, ..., n:
   print numSpaces spaces
   print numStars stars
   print newline (i.e., std::endl)

if (______):
   increment numStars by 2
   decrement numSpaces by ____
else:
   decrement numStars by 2
   increment numStars by 2
   increment numStars by 2
```

Back to the initialization of numSpaces. There are many ways of doing this. Look at Test 10:

Test 10

The first line has 4 spaces. Why 4 spaces? Look at the line of output with the maximum number of stars. See the 9 stars?

Test 10:

Q8. [OPTIONAL]

ASCII art strikes again!

Test 1.

```
<u>3</u>
***
* *
***
```

Test 2.

```
<u>5</u>
****

* *

* *

* *

* *

* *
```

Test 3.

```
7
******

* *
*** *

* * *

* * *

* * *

* * *

* * *

* * *

* * *
```

```
9
*******
* * * * *
* * * *
* * * *
* * * *
* * * *
* * * *
```

Q9. [OPTIONAL]

Uh-oh ... another ASCII art program.

Test 1.

```
1
*
***
****
```

Test 2.

Test 3.

Spoiler Warning ... Incoming Hints ...

Look at the case of Test 4:

Test 4

There are two possible outermost for-loop:

Either

or