

## CISS350: Data Structures and Advanced Algorithms Assignment 1

Name: \_\_\_\_\_

### Q1. [Introduction to Lexing]

If you're given a string such as

"10 + 21 \* (33 - 47)"

which corresponds to a mathematical expression and you want to evaluate it, you want to convert this into a sequence of meaningful items:

"10", "+", "21", "\*", "(", "33", "-", "47", ")"

where each string in this sequence has meaning. For instance "10" corresponds to the meaning of “ten”, etc. The strings above (such as "10") are called lexemes.

It is convenient to attach types to these lexemes. For instance we want to think of "10" as a lexeme that is different from the lexeme "+". Using object-oriented programming, we will convert these lexemes into different token types. For instance "10" will be converted into an integer token object and "+" will be converted into a plus token object.

Here are the classes:

```
class Token
{};

class IntTok: public Token
{
public:
    int value;
};

class PlusTok: public Token
{};

class MinusTok: public Token
{};

class MultTok: public Tok
{};
```

```
class DivTok: public Token
{};

class LParenTok: public Token // Left parenthesis
{};

class RParenTok: public Token // Right parenthesis
{};
```

(You don't have to worry about the mod % operator.)

The goal is to write a program that gets a string such as

"10 + 21 \* (33 - 47)"

from the user and then produce a `std::vector` of tokens.

You must provide code to print all the above tokens. For instance

```
std::cout << IntTok(5) << '\n'; // Prints IntTok(5)
std::cout << PlusTok() << '\n'; // Prints PlusTok
```

You must also provide code to print a `std::vector` of tokens.

```
std::vector< Token > toks;
toks.push_back(IntTok(5));
toks.push_back(PlusTok());
std::cout << toks << '\n'; // Prints [IntTok(5), PlusTok]
```

The above of course does not work. You want `toks` to be a vector of *different types of tokens*. But as it stands you can only put `Token` objects into `toks`. See hints later. (Look for the section A `std::vector` CONTAINING DIFFERENT TYPES OF OBJECTS).

Here's an execution of the program. (Note that you will need to get a string input from the user that includes spaces. Check my CISS245 notes on strings. See chapter 18 on characters and C-strings.)

#### TEST 1

```
10 + 21 * (33 - 47)
[IntTok(10), PlusTok, IntTok(21), MultTok, LParenTok, IntTok(33), MinusTok, IntTok(47), RParenTok]
```

Ignore "negative of" (the unary `-`). In other words, when your program sees a `-`, generate a `MinusTok`.

#### TEST 2

```
10 + 21 * (33 - -47)
[IntTok(10), PlusTok, IntTok(21), MultTok, LParenTok, IntTok(33), MinusTok, MinusTok, IntTok(47), RParenTok]
```

NOTE. In a compiler, the process of analysing a source file is not broken up into lexing as a complete first step:

```
get string s from program source file
get toks, a vector of tokens, from s (lexing)
analyze tokens (parsing)
```

The process actually extracts enough characters from a source file to form a token and then pass the token to the part of the compiler that analyzes the structure of the program. In other words, the compiler alternates between lexing and analysis:

```
get string s from program source file
loop as long as there are characters in s:
    extract enough characters from s to get the next token t
    continue analyzing structure of program with new token t
```

So the process is more like lex-parse-lex-parse-lex-parse-... The reason is because it's too costly to lex the whole string – what if there's a very early program error in an extremely huge source file?

A `std::vector` CONTAINING DIFFERENT TYPES OF OBJECTS

WARNING: INCOMING SPOILERS ...

If `tok` is a `std::vector< Token >`, then you can only put `Token` objects into `tok`.

You might want to read and review my CISS245 notes on inheritance and polymorphism.

More spoilers on the next page ...

continue ... WARNING: MORE INCOMING SPOILERS ...

If `tok` is a `std::vector< Token >`, then you can only put `Token` objects into `tok`.

If you try to put a `IntTok` object `x` into a `std::vector< Token >` object `v`, say at index 0, then you are doing

```
v[0] = x;
```

(Review CISS245 notes – it’s possible to assign a child object to a parent object.)

If `Token` is a concrete class (i.e., no pure virtual method), sure you can do the above. But `v[0]` is a `Token` object, not a `IntTok` object. For instance since `x` is an `IntTok` object `x` will hold an integer value. But `v[0]` is a `Token` object and does not hold an integer value. So `v[0]` will lose some critical information in `x`. In fact, you cannot even tell if `v[0]` came from an `IntTok` or a `PlusTok`.

However from CISS245, you know that this is possible:

```
P * p = new C;
```

where `P` is a parent class of class `C`. Therefore you can put `p` into a `std::vector< P * >`. This `p` can point to any subclass of `P`.

Suppose `P` is a parent class of classes `C0` and `C1`. Suppose pointer `p` is declared as

```
P * p;
```

and `p` is assigned an address from a `std::vector< P * >` object. Furthermore `*p` is either a `C0` object or `C1` object.

The above should be enough hints. (It pretty much gives away everything.) So you probably want to review inheritance, polymorphism, virtual methods, pure virtual methods, etc.

Also, if you like you can have a class for `std::vector< Token * >`, say call it `Tokens`. Note that if `toks` is a `Tokens` object, you insert token pointers into `toks` to be processed “at the back” and you remove token pointers “from the front”. So you might want to more or less think of your `Tokens` objects as queues (or double-ended queue).

C++ `std::stack`, `std::queue`, `std::deque`, `std::forward_list`, AND `std::list` CLASSES

You can find information on the above C++ STL classes in my CISS350 notes. You can also use the web to read up more on these classes. Also, you have already seen the `std::vector` class from CISS245.

In the questions of this assignment, you can use these class. (You can also write your own dynamic array, singly-linked list, doubly-linked list, stack, queue, and deque classes.)

Here's an example of some basic methods in the `std::stack` class template:

```
#include <iostream>
#include <stack>

int main()
{
    std::stack< int > s;
    std::cout << s.empty() << ' ' << s.size() << '\n';

    std::cout << "pushing 42, 23, 6 ... \n";
    s.push(42);
    std::cout << s.empty() << ' ' << s.size() << ' ' << s.top() << '\n';

    s.push(23);
    std::cout << s.empty() << ' ' << s.size() << ' ' << s.top() << '\n';

    s.push(6);
    std::cout << s.empty() << ' ' << s.size() << ' ' << s.top() << '\n';

    std::cout << "changing top to 1000 ... \n";
    s.top() = 1000;
    std::cout << s.empty() << ' ' << s.size() << ' ' << s.top() << '\n';

    std::cout << "pop until empty ... \n";
    while (!s.empty())
    {
        std::cout << s.empty() << ' ' << s.size() << ' ' << s.top() << '\n';
        s.pop();
    }

    std::cout << s.empty() << ' ' << s.size() << '\n';

    std::cout << "copy constructor, operator=, operator== ... \n";
    s.push(5); s.push(3); s.push(7);
    std::stack< int > t = s;
    std::cout << (s == t) << '\n';
}
```

```
while (!t.empty()) t.pop();
t = s;
std::cout << (s == t) << '\n';

return 0;
}
```

Run the program and look at the output. Check the web for more methods for this class.

Here's an example of some basic methods in the `std::queue` class template:

```
#include <iostream>
#include <queue>

int main()
{
    std::queue< int > q;
    std::cout << q.empty() << ' ' << q.size() << '\n';

    std::cout << "Putting 42, 23, 6 into the queue ... \n";
    q.push(42);
    std::cout << q.empty() << ' ' << q.size() << ' '
              << q.front() << ' ' << q.back() << '\n';
    q.push(23);
    std::cout << q.empty() << ' ' << q.size() << ' '
              << q.front() << ' ' << q.back() << '\n';
    q.push(6);
    std::cout << q.empty() << ' ' << q.size() << ' '
              << q.front() << ' ' << q.back() << '\n';

    std::cout << "changing front to 1000 ... \n";
    q.front() = 1000;
    std::cout << q.empty() << ' ' << q.size() << ' '
              << q.front() << ' ' << q.back() << '\n';

    std::cout << "changing back to -1000 ... \n";
    q.back() = -1000;
    std::cout << q.empty() << ' ' << q.size() << ' '
              << q.front() << ' ' << q.back() << '\n';

    std::cout << "dequeue until empty ... \n";
    while (!q.empty())
    {
        std::cout << q.empty() << ' ' << q.size() << ' '
                  << q.front() << ' ' << q.back() << '\n';
        q.pop();
    }
}
```

```
std::cout << "copy constructor, operator=, operator== ...\n";
q.push(5); q.push(3); q.push(7);
std::queue< int > r = q;
std::cout << (r == q) << '\n';

while (!r.empty()) r.pop();
r = q;
std::cout << (r == q) << '\n';
return 0;
}
```

Run the program and look at the output. Check the web for more methods for this class.

If **s** is a stack and **q** is a queue, then:

```
s.empty() -- true if s is empty; otherwise false
q.empty() -- true if q is empty; otherwise false

s.size() -- size of s
q.size() -- size of q

s.push(x) -- push x onto top of s
q.push(x) -- enqueue x into back of q

s.pop() -- remove top of s
q.pop() -- remove front of q

s.top() -- reference to the top of stack s
q.front() -- reference to the front of queue q
q.back() -- reference to the end of queue q
```

C++ `std::list` class is a doubly-linked list class. Here's an example of some basic methods in the `std::list` class template:

```
#include <iostream>
#include <list>

int main()
{
    std::list< int > list;
    std::cout << list.empty() << ' ' << list.size() << '\n';

    list.push_front(1);
    list.push_back(5);
    list.push_front(0);
    std::cout << list.front() << ' ' << list.back() << '\n';
    std::cout << list.empty() << ' ' << list.size() << '\n';
}
```



```
list.front() = 1000;
list.back() = 9000;
std::cout << list.front() << ' ' << list.back() << '\n';
std::cout << list.empty() << ' ' << list.size() << '\n';

std::cout << "iterator ...\n";
std::list< int >::iterator p = list.begin();
std::cout << *p << '\n';
++p;
std::cout << *p << '\n';
++p;
std::cout << *p << '\n';
--p;
std::cout << *p << '\n';

std::cout << "loop using an iterator ... ";
for (typename std::list< int >::iterator p = list.begin();
     p != list.end();
     ++p)
{
    std::cout << (*p) << ' ';
}
std::cout << '\n';

std::cout << "loop using a constant iterator (if list is a constant) ... ";
for (typename std::list< int >::const_iterator p = list.begin();
     p != list.end();
     ++p)
{
    std::cout << (*p) << ' ';
}
std::cout << '\n';

std::cout << "erase() ...\n";
list.erase(p);
std::cout << list.front() << ' ' << list.back() << '\n';
std::cout << list.empty() << ' ' << list.size() << '\n';

std::cout << "copy constructor, operator=, operator== ...\n";
std::list< int > list2 = list;
std::cout << (list2 == list) << '\n';
list2 = list;
std::cout << (list2 == list) << '\n';

std::cout << "clear() ...\n";
list.clear();
std::cout << list.front() << ' ' << list.back() << '\n';
std::cout << list.empty() << ' ' << list.size() << '\n';

return 0;
```

```
}

```

Run the program and look at the output. Check on the web for more methods for this class. A constant iterator cannot modify the value that it points to. In other words if `p` is a constant iterator, you cannot do

```
*p = newvalue;

```

If `list` is a `std::list` object, then

```
list.empty()          -- true if list is empty; otherwise false
list.size()           -- size of list
list.push_front(x)    -- insert x at head
list.push_back(x)     -- insert x at tail
list.pop_front()      -- remove front of list
list.pop_back()       -- remove back of list
list.front()          -- reference to the front/head of list
list.back()           -- reference to the end/tail of list
list.clear()          -- delete all nodes from list
list.erase(p)         -- delete node that iterator p points to

```

Here `p` is an iterator of the list (see example code), i.e., it's an object that acts like a pointer to the list.

Q2. [Polish notation calculator]

Write a program that evaluates an integer expression written using the Polish notation. For simplicity, assume that the user does not enter negative numbers. Make sure you test cases where the integer value has more than one digit.

TEST 1

<pre>* 1 - + 2 - 3 5 4 -4</pre>
---------------------------------

TEST 2

<pre>* 1 ERROR</pre>
----------------------

Try out more test cases of your own.

## Q3. [Reverse polish notation calculator]

Write a program that evaluates an integer expression written using the reverse polish notation. For simplicity, assume that the user does not enter negative numbers. Make sure you test cases where the integer value has more than one digit.

## TEST 1

$\frac{1\ 2\ 3\ 5\ +\ -\ 4\ -\ *}{-10}$
---

## TEST 2

$\frac{1\ +}{\text{ERROR}}$
-----------------------------

Try out more test cases of your own.

## Q4. [Infix calculator]

Write a program that evaluates an integer expression written using the infix notation. For simplicity, assume that the user does not enter negative numbers. Make sure you test cases where the integer value has more than one digit.

## TEST 1

$0 - ( 1 + 2 + 3 * ( 4 - 5 ) + 6 )$ $-6$
--

## TEST 2

$0 - 6 )$ $\text{ERROR}$
--------------------------

Try out more test cases of your own.

## Q5. [Sparse polynomial]

Using `std::list`, implement an integer polynomial class where zero coefficient terms are not stored. (The case of a class template is easy once the integer version is done.)

```
// A monomial is a term in a polynomial. For instance 5 * x ^ 3 is a
// monomial. For this term, we store (3, 5), i.e., the degree and the
// coefficient.
class Monomial
{
public:
    int degree;
    int coefficient;
};

class Polynomial
{
public:
private:
    std::list< Monomial > p; // The term with smallest degree is at the head.
};
```

The following describes the expected usage of the class:

```
Polynomial p("3*x^2 + 7*x^12 - 9*x^100 + -2*x^32 + x^5 + 0*x^6 + 6*x^2 + 32 + 1*x^0");
std::cout << p << '\n'; // prints -9x^100 - 2x^32 + 7x^12 + x^5 + 9x^2 + 33

Polynomial p0(42);        // p0 = 42 as a polynomial
Polynomial p1(p);         // p1 = p as a polynomial

std::cout << (p0 == p) << '\n';
std::cout << (p1 != p) << '\n';
std::cout << (5 == p) << '\n';
std::cout << (p != 5) << '\n';

std::cout << deg(p) << '\n'; // degree of p

Polynomial q("x^2 + x + 1");

p += q;
p -= q;
p *= q;

p += 42;
p -= 42;
p *= 42;

Polynomial r; // r = 0 as a polynomial

r = p - q;
```

```
r = p * q;  
  
r = 42 + p;  
r = p + 42;  
  
r = 42 - p;  
r = p - 42;  
  
r = 42 * p;  
r = p * 42;  
  
r = 42 * p;
```

Make sure you examine the constructors and output carefully. In particular, note that in the constructors, the input string need not list monomials in any particular order by degree. Also, in the printout of the polynomials, higher degree terms are printed first.

#### OPTIONAL DIY.

- It's a good exercise to use your **Rational** class to model polynomials with fractions as coefficients. Then you can also perform long division to get quotients and remainders. In fact your polynomial class should really be a class template.
- Recall that in CISS240, there was an assignment question that attempts to factorize polynomials. With this class you can now attempt to factorize an integer polynomial of any degree into two polynomials of smaller degree. For self-study and research, you can google for algorithms for polynomial factorization.

Q6. [Infix to reverse polish notation]

Write a program that converts an integer expression written using the infix notation into RPN.

TEST 1

0 - 1 + 2 * 3 - 4 / 5 * 6
0 1 - 2 3 * + 4 5 / 6 * -

Try out more test cases of your own.

[Suppose the output of the above computation is an RPN expression. For instance from  $1 + 2$ , you want to compute  $1\ 2\ +$ . Of course as a vector of tokens, the input is `[IntTok(1), PlusTok, IntTok(2)]` and the output is `[IntTok(1), IntTok(2), PlusTok]`. The algorithm to evaluate an infix expression `[IntTok(1), PlusTok, IntTok(2)]` basically computes `IntTok(3)`. But for this problem you won't want `IntTok(3)`. You want `[IntTok(1), IntTok(2), PlusTok]`. All you need to do is to modify the algorithm to evaluation an infix expression so that instead of `IntTok(3)`, you compute `[IntTok(1), IntTok(2), PlusTok]`. ]