

Notes

September 17, 2014

assignment

Section 1.4: # 17, 19, 20, 23, 24, 27.

2.3 5.

6. $(1), (12), (13), (14), (23), (24), (34), (123), (124), (134), (234), (132), (243), (142), (143), (1234)$

2.3.5 theorem

sketch of a proof

$$\tau = \begin{pmatrix} 1 & 2 & 3 & \dots & n \\ \sigma(1) & \sigma(2) & \sigma(3) & \dots & \sigma(n) \end{pmatrix}$$

example

$$\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 7 & 2 & 6 & 3 & 1 & 5 & 4 \end{pmatrix} = (1, 7, 4, 3, 6, 5)$$

definition: let $\sigma \in S$ the least positive integer m such that $\sigma^m = (1)$ is called the order of σ

example

$$\sigma = (123)(45) \rightarrow (123)^3(45)^2 = \sigma^6$$

observation for 2.3.8 proof

$(a_1 a_2 a_3 \dots a_k)^i = (1)$ and $(b_1 b_2 b_3 \dots b_k)^i = 1$ because they are disjoint and applying the a permutations don't change the b elements and vice versa