

# Notes

November 24, 2014

## example 5.6.E

let  $T(x)$  be the temperature at point  $x$  on surface of planet where we assume that the planet is a sphere.  $T$  is a continuous function

Then  $\exists x$  on the surface of the planet such that  $T(x) = T(-x)$ .

### proof

$f(x) = T(x) - T(-x)$  and  $f(-x) = -f(x)$  for all  $x$  on surface. either  $f(x) = 0 \forall$  or  $\exists x_0$  such that  $f(x_0) \neq 0$  assume  $f(x_0) > 0$  then  $f(-x_0) < 0$  and there is a point in between where  $f$  is 0.

## example 5.6.f

map from  $[0, 2\pi) \rightarrow$  unit circle  $\rightarrow \mathbb{R}$