

# Study Notes

October 6, 2014

## definitions

### bounds

#### bounded above

a set  $S \subset \mathbb{R}$  is **bounded above** if there is a real number  $M$  such that  $s \leq M$  for all  $s \in S$ .

#### upper bound

If  $M \geq s, \forall s \in S \subset \mathbb{R}$  then  $M$  is an **upper bound**

#### supremum

if  $L$  is the lowest upper bound such that  $M \geq L \geq s \forall s \in S \subset \mathbb{R}$  where  $M$  is any upper bound of  $S$ , then  $L$  is the supremum.

## least upper bound principle

### proof

### squeeze theorem

### proof

### define limit

### thm

If  $(a_n)$  is a convergent sequence of real numbers, then the set  $\{a_n : n \in \mathbb{N}\}$  is bounded

## 2.5.2 arithmetic operations of limits, addition, multiplication, constant multiplication and inversion