Notes

January 14, 2015

homework:

```
no scruffy edges
name: top right
state the problem
solution, grammar, words, not just notation
repeat
finally: list resources, exclude book and this instructor. include other instructors, classmates, internet,
etc.
```

course outline

```
chapter 8, 10, 11, 16, not exhaustively skipped things will be a good source for projects first couple weeks will not be in the book, we cover real life integration in the small, then start chapter 8. measure theory is how to do integrals, they are done by approximating functions then polynomial approximation. these are standard analysis last bit is fun stuff of his choice
```

review integration

 $f:[a,b]\to\mathbb{R}$ we partition etc, randomly choose a point in the partition, sum rectangles integrable if we can always find a partition and get arbitrarily close

lebesgue metaphor

take a pile of money, coins of different values. to calculate money, you add each coin up. think of each coin as one of the riemann rectangles.

now for the lebesgue integral you sort the change, add the things of the same size together first, then add these sums.

riemann to lebesgue

reimann is chopping up domain and measuring the height, lebesgue is chopping up range and, complication is that "rectangles" are a little weirder, the function goes in and out of the rectangle. or multiple riemann rectangles for each rectangle height, to make this work, we need to be able to measure the size of a set

measure theory

measure the size of a set

- 1. what properties do we want? disjoint etc?
- 2. what measures? not going here, start with the classic type of measure

Lindelf's theorem

- if $E \in \mathbb{R}$ there is a countable collection of intervals $\{(a_i,b_i)\}_{i=1}^{\infty}$ such that $E \in \bigcup_{i=1}^{\infty}(a_i,b_i)$ this is obvious because of $\mathbb{R} \subseteq \mathbb{R}$ check subcovers, etc these sets
 - 1. not unique
 - 2. may overlap

example

$$[0,1] \subseteq \bigcap_{n=1}^{\infty} (-\frac{1}{n}, 1 + \frac{1}{n})$$

$$[0,1] \subseteq \bigcap_{n=1}^{\infty} (-n, n)$$

$$[0,1] \subseteq (\frac{1}{2}, \frac{3}{2}) \cup (\frac{1}{4}, \frac{3}{4}) \cup (\frac{1}{8}, \frac{3}{8}) \cup \dots (-\frac{1}{2}, \frac{1}{2}) \cup$$
hello goodbye