Notes

January 16, 2015

error fixup

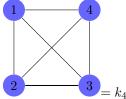
neighborhood is $N_G(V_i) = \{V_j | (v_i, v_j) \in E(G)\}$

degree sequences

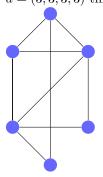
these will be ascending, book is descending

definitionn

if G is finite with $V(G) = \{v_1, \dots, v_n\}$ such that $d_i = \deg(v_i) \le \deg(v_j)$ for $i \le j$ then (d_1, \dots, d_n) is the degree sequence of G.



d = (3, 3, 3, 3) three regular graph



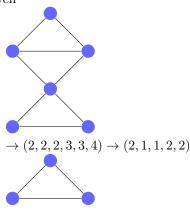
d = (2, 3, 3, 3, 3, 4)

Havel, Hakimi thm

if (d_1, \ldots, d_n) is a non decreasing sequence with $d_n \ge 1$ (avoid the empty graph) it is a degree sequence iff $(d_1, \ldots, d_{n-d_n-1}, d_{n-d_n}-1, \ldots, d_{n-1}-1)$ is a degree sequence

example







proof

 \Rightarrow careful vertex deletion

claim

havel-hakimi can be used to verify, refute the degree sequenceness of any nondecreasing sequence of integers i.e. we can say rather quickly that (polynomial time) if (2,3,3,5,5,5,5,5,5,6) is graphical $n=10,10-6-1=3, d_3=3, n-d_n=4, d_4-1=4, d_9-1=5$ $(2,3,3,4,4,4,4,4,4) \cdots \rightarrow \ldots (1,1,2,2,2,2)$ question, if two degree sequences are the same, are the graphs isomorphic? no!

homework 1.2

6a,b,7,10,15