# University of Colorado - Boulder

ASEN 3128: Lab 4

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# **Lab 4: Quadrotor Control**

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# **Table of Contents**

			Page				
ı	Problem	1	2				
II	Problem 2 and 3 Plots and Discussion						
	II.A De	viation by +5 deg in roll	3				
	II.B De	viation by +5 deg in pitch	4				
	II.C De	viation by +0.1 rad/sec in roll rate	5				
	II.D De	viation by +0.1 rad/sec in pitch rate	6				
III	Problem •	4	8				
IV	Problem	5	10				
	IV.A Late	eral Model	10				
	IV.B Lon	gitudinal Model	11				
٧	Problem	6	12				
Pa	articipation	1	14				
Ą	pendices		14				
	Code		14				

#### I. Problem 1

Using the following equations the maximum eigenvalue for a given A state matrix can be solved for.

$$\tau = \frac{-1}{\lambda_i} \tag{1}$$

$$(\mathbf{A} - \lambda_i)\mathbf{v_i} = 0 \tag{2}$$

For questions 2 and 3 a time constant of 0.5 seconds is required which corresponds to a dominating eigenvalue term of -2. The matrix A can then be solved as it is only a function of k1 given an initial guess of k2 and using this process the following control laws were derived to stabilize roll and pitch attitude.

$$\Delta L_c = -0.004 \Delta p - 0.0021 \Delta \phi \tag{3}$$

$$\Delta M_c = -0.004 \Delta q - 0.0021 \Delta \theta \tag{4}$$

## II. Problem 2 and 3 Plots and Discussion

## A. Deviation by +5 deg in roll

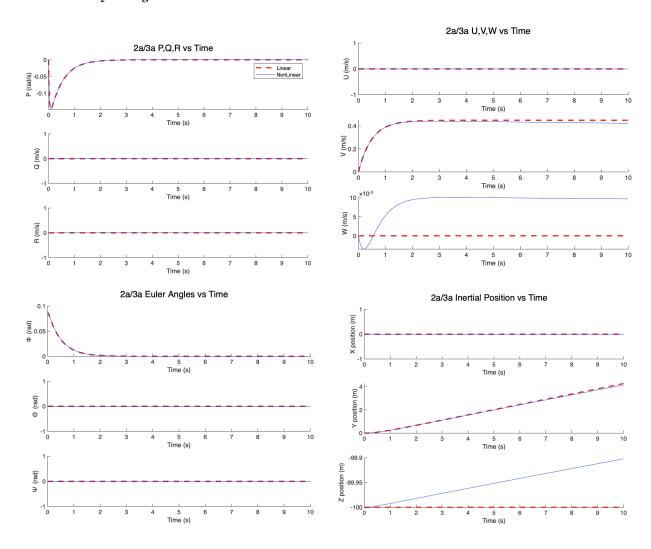


Fig. 1 Linearized vs. Nonlinearized Behaviour 2a/3a

## B. Deviation by +5 deg in pitch

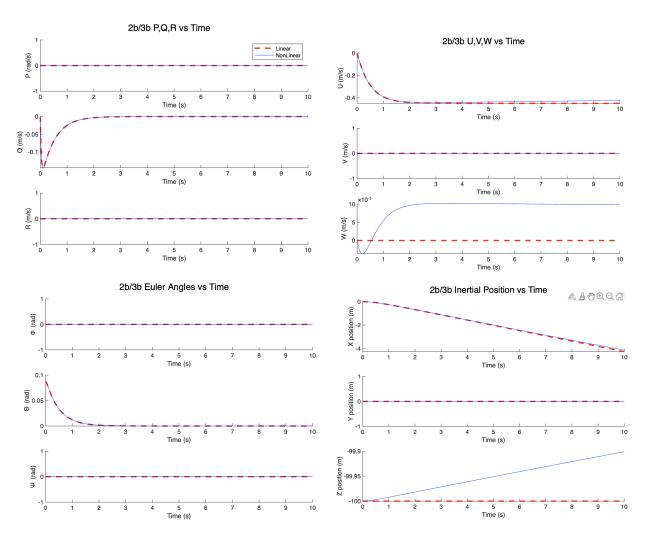


Fig. 2 Linearized vs. Nonlinearized Behaviour 2b/3b

## C. Deviation by +0.1 rad/sec in roll rate

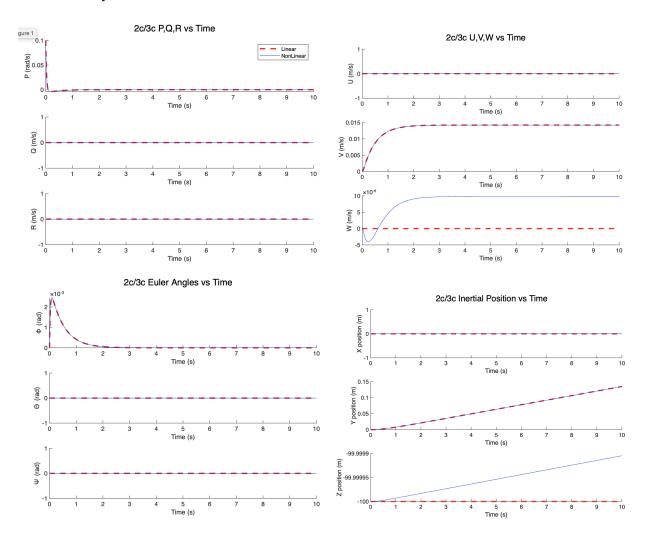


Fig. 3 Linearized vs. Nonlinearized Behaviour 2c/3c

#### D. Deviation by +0.1 rad/sec in pitch rate

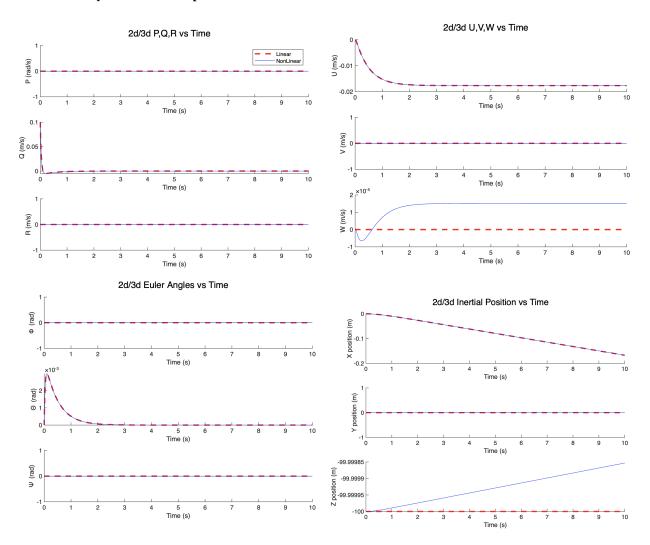


Fig. 4 Linearized vs. Nonlinearized Behaviour 2d/3d

For this particular model, the lateral variables are accounted for in the feedback control loop. The main purpose of feedback control is to keep the controlled variables close to their set point. So this means moving the system from some initial rate to zero.

As seen in the plots, the linear and non linear lines are almost identical with the exception of a few plots. This all corresponds to the expected behavior from the linearized modal response theory. The linearized equations are based on small angle approximations and due to the actual small angles used in this lab, the linearized model captures true behavior.

As depicted in the plots, the models for linear velocity and non linear produce very similar outputs. Roll and angle roll rate are controlled and driven back to zero, however neither lateral nor vertical speeds are zero. This is because the

feedback control is not implemented on speed or position.

For example, for scenarios a and b, uvw don't all go back to zero, which is why the y and z positions for a then x and z positions for b vary. As shown in Figures 1 and 2, the uvw terms converge on a value but do not converge back to zero because there is no feedback control implemented.

The quadrotor was also expected to fall for a deviation in pitch, because the sum of the four motor forces is set to equal the weight of the aircraft. So when it is tiled, the forces equal less than the total weight and the aircraft falls. So because the quadrotor was falling after it was tilted, it created speed downwards and sideways, and this is all expected motion.

When roll and pitch are deviated, the quadrotor drifts sideways as seen in v and y position plots in Figure 1 and u and x position plots in Figure 2. This drift is due to drag. We do account for drag in the nonlinear system, and this drag is so small that it takes a long time to the aircraft. These linear equations do not account for drag, which describes the small discrepancy between these V vs. Time, Y Position vs. Time, U vs. Time, and X Position vs. Time plots.

As seen in the plots, the only time when there is a large discrepancy between the linear and nonlinear models are w and z position. This is consistent for all cases a-d. The linearized model is based off the small disturbance theory. Due to this, when the aircraft is disrupted and has to use control to make adjustments, these adjustments will be so minimal, they will fall under small disturbances, and will be taken to be zero. Also, this particular lab only focuses on longitudinal and lateral variables, so w and the z position are not controlled in this model.

Steady hover is now a stable flight condition due to the control feedback loop. For example, if the drone experiences a deviation in pitch angle instead of falling out of equilibrium the control law adjusts the angle and stabilizes the drone.

#### III. Problem 4

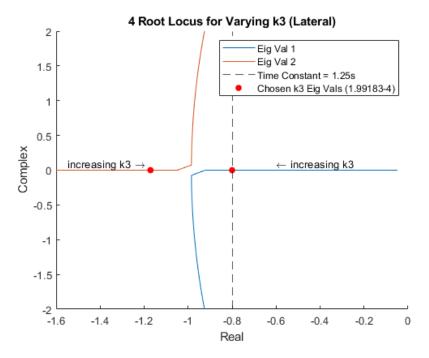


Fig. 5 Lateral

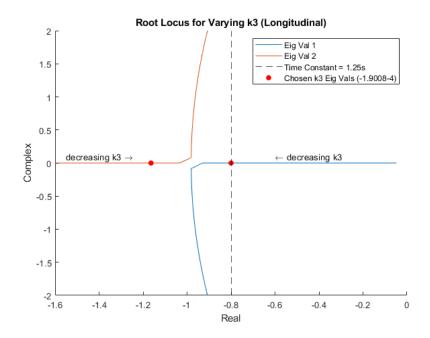


Fig. 6 Longitudinal

Following the same procedure as Problem 1, the maximum eigenvalue for our a given state matrix A can be determined,

$$\tau = \frac{-1}{\lambda_i} \tag{5}$$

$$(\mathbf{A} - \lambda_i)\mathbf{v_i} = 0 \tag{6}$$

a time constant less than 1.25 [sec] was required, corresponding to a dominating eigenvalue of -0.8. Using the feedback control gains  $K_1 = 0.004$  and  $K_2 = 0.0021$  designed in problem 1 the tracking control gain  $K_3$  was determined by solving the state matrix A. For the closed loop three-state longitudinal system  $K_3$  was computed to be  $-1.9008 \times 10^{-4}$  and for the lateral system  $K_3$  was determined to be  $1.99183 \times 10^{-4}$ . Following, the builtin MATLAB function eig() was used to plot the locus of the eigenvalues for the lateral and longitudinal systems for a range of  $K_3$  values. For the longitudinal system,  $K_3$  ranged from  $-1.9008 \times 10^{-4}$  to  $-1.9008 \times 10^{-2}$  and for the lateral system  $K_3$  ranged from  $1.99183 \times 10^{-4}$  to  $1.99183 \times 10^{-2}$ . Using the root locus for both systems the determined gain values satisfied the design objectives. Using the determind gain values the following control laws were derived

#### **Longitudinal System:**

$$\Delta L_c = -0.004\Delta p - 0.0021\Delta \phi - (1.9008 \times 10^{-4})(\Delta v_r - \Delta v)$$
(7)

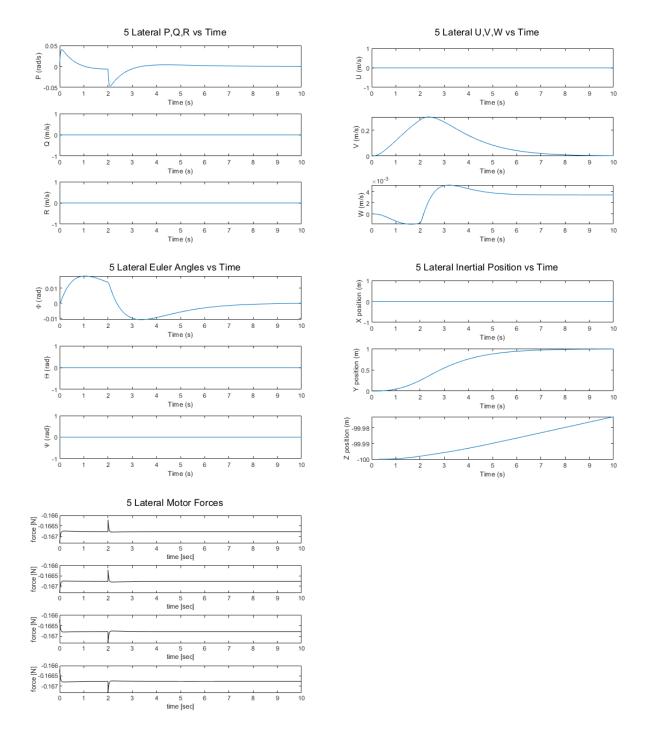
#### **Lateral System:**

$$\Delta M_c = -0.004\Delta q - 0.0021\Delta\theta + (1.99183 \times 10^{-4})(\Delta u_r - \Delta u)$$
(8)

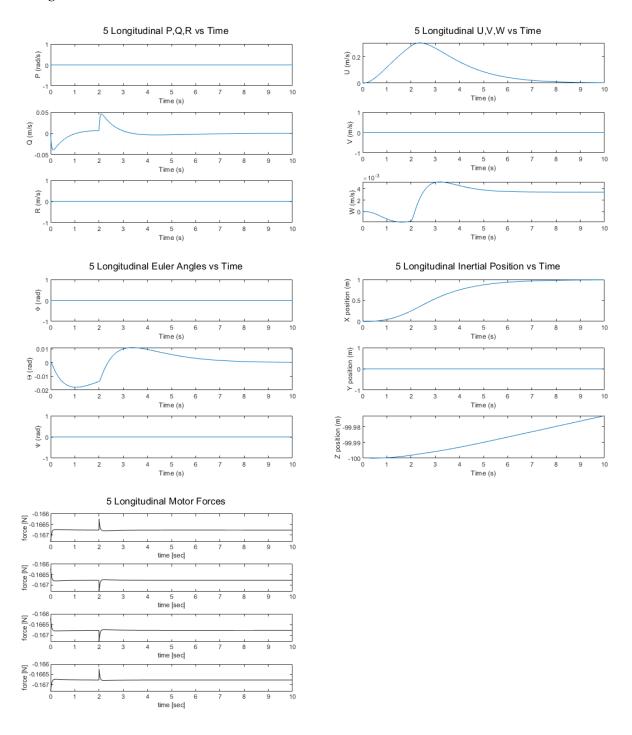
## IV. Problem 5

Using the lateral and longitudinal control laws designed in problem 4 the models are simulated and shown in the following plots.

#### A. Lateral Model



#### **B.** Longitudinal Model



The simulated models behave as predicted because the u and v components of velocity approach the desired value of 0.5m/s for t<2s and then they go back to 0m/s as the control law no longer acts.

# V. Problem 6

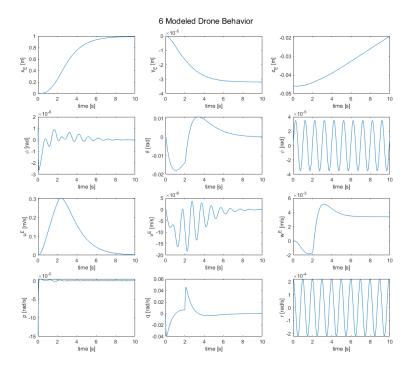


Fig. 7 Modeled Drone Behavior

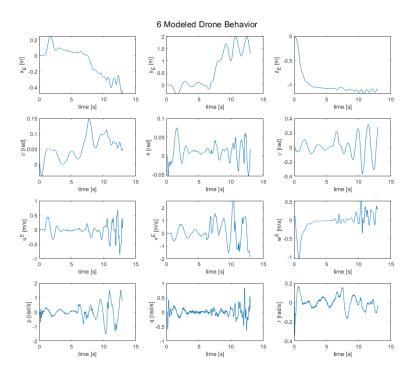


Fig. 8 Experimental Drone Behavior

The experimental data is quite different from the data simulated with the non-linear control model and this is due to the imperfect control forces applied by the motors. Drone motors can experience voltage spikes which could increase the error in the modeled drone behavior which then propagates through the simulation and results in more inaccuracy. Another error could stem from level of accuracy of the accelerometer and gyroscope readings. Without proper filtering these sensors could experience large amounts of error which again could propagate through the model and result in more error.

## **Participation Table**

	Plan	Model	Experiment	Results	Report	Code	ACK
Emerson Beinhauer	2	1	N/A	1	1	1	ЕВ
Luke Engelken	1	2	N/A	2	1	2	LE
Connor O'Rilly	2	1	N/A	1	1	1	СТО
Thyme Zuschlag	1	1	N/A	1	2	1	TZ

2 = Lead, 1 = Participate, 0 = Not involved, for each element. X = acknowledged by each team member.

## Appendix A: MATLAB Code

```
function [motor_forces] = ComputeMotorForces(Zc, Lc, Mc, Nc, R, km)
   %Function explanation stuff
  A = [-1 \ -1 \ -1 \ -1; \ -R/sqrt(2) \ -R/sqrt(2) \ R/sqrt(2) \ R/sqrt(2); ...
     R/sqrt(2) -R/sqrt(2) -R/sqrt(2); km -km km -km];
  motor_forces = inv(A) * [Zc; Lc; Mc; Nc];
  % motor_forces = motor_forces';
  end
   % Luke Engelken
   % ASEN 3128
  % prob1.m
  % Created: 9/11/20
  %To run, in command window type "prob(<insert quetsion number)" and you
  %will see plots
  %ex: prob('1a')
  function [] = drone(prob)
     %% Declare Constants
     m = 0.068; %mass of drone (kg)
     r = 0.06; %radial distance from cg to motor (m)
     km = 0.0024; %control moment coefficient (N*m/N)
14
      Ix = 5.8e-5; %x-axis moment of inertia (kg*m^2)
```

```
Iy = 7.2e-5; %y-axis moment of inertia (kg*m^2)
      Iz = 1e-4; %z-axis moment of inertia (kg*m^2)
      v = 1e-3; %aerodynamic force coefficient (N/(m/s^2))
18
      mu = 2e-6; %N*m/(rad/s^2)
19
      g = 9.81; %m/s^2
      %xstate vector: [x; y; z; phi; theta; psi; xdot; ydot; zdot; phidot;
      %thetadot; psidot] (integral of eom state vector)
22
      tspan = [0 10];
23
      switch prob
24
         case 'la'
25
            %Prob 1a - steady state hover, no drag
26
            f1 = q*m/4; %Assume -force up
            f2 = f1;
2.8
            f3 = f1;
29
            f4 = f1;
30
            pinit = [0; 0; 100; 0; 0; 0; 0; 0; 0; 0; 0; 0];
            [tx, x1] = ode45(@(t, x)
32
                objectEOMnodrag(t,x,m,r,km,Ix,Iy,Iz,v,mu,f1,f2,f3,f4),tspan,pinit);
         case '2a'
33
            %Prob 2a - steady state hover, with drag
34
            f1 = 2; %g*m/4; %Assume -force up
35
            f2 = f1;
36
            f3 = f1;
            f4 = f1;
38
            pinit = [0; 0; -10; 0; 0; 0; 0; 0; 0; 0; 0; 0];
            [tx, x1] = ode45(@(t, x)
40
                objectEOM(t,x,m,r,km,Ix,Iy,Iz,v,mu,f1,f2,f3,f4),tspan,pinit);
         case '2b'
41
            %Prob 2b - constant y velocity = 5m/s, psi = 0
42
            syms phi
43
            eqn = 5*v*5*cos(phi)+m*g*sin(phi)^3+m*g*sin(phi)*cos(phi)^2 == 0;
            eqn = atan(phi) == v*25/(m*g);
45
            phi = solve(eqn);
            phi = eval(phi(1,1)); %3.1041
47
            phi = 2.12;
```

```
pinit = [0; 0; 0; phi; 0; 0; 0; 5*cos(phi); -5*sin(phi); 0; 0; 0];
            Zc = m*q*(cos(pinit(4))+sin(pinit(4))^2/cos(pinit(4))); %-0.667080298221064
            %Zc = 25*v/sin(phi); %-.6681
51
            %Zc = .6665;
52
            f1 = Zc/4;
            f2 = f1;
            f3 = f2;
55
            f4 = f3;
            [tx, x1] = ode45(@(t, x)
57
                objectEOM(t,x,m,r,km,Ix,Iy,Iz,v,mu,f1,f2,f3,f4),tspan,pinit);
         case '2c'
58
            %Prob 2c - constant y velocity = -5m/s, psi = 90deg
59
            syms phi
60
            eqn = 5*v*5*cos(phi)+m*g*sin(phi)^3+m*g*sin(phi)*cos(phi)^2 == 0;
61
            eqn = atan(phi) == v*25/(m*q);
62
            phi = solve(eqn);
63
            phi = eval(phi(1,1)); %3.1041
64
            phi = 2.12;
            pinit = [0; 0; 0; 0; -phi; pi/2; 5*cos(phi); 0; -5*sin(phi); 0; 0; 0];
            Zc = m*g*(cos(pinit(5))+sin(pinit(5))^2/cos(pinit(5))); %-0.667080298221064
            %Zc = 25*v/sin(phi); %-.6681
68
            %Zc = .6665;
69
            f1 = Zc/4;
            f2 = f1;
71
            f3 = f2;
72
            f4 = f3;
            [tx, x1] = ode45(@(t, x)
74
                objectEOM(t,x,m,r,km,Ix,Iy,Iz,v,mu,f1,f2,f3,f4),tspan,pinit);
         case '3'
75
            %Prob 2a - steady state hover, with drag
            f1 = g*m/4; %Assume -force up
            f2 = f1;
            f3 = f1;
            f4 = f1;
            pinit = [0; 0; -10; 0; 0; 0; 0; 0; 0; 0; 0; 0];
81
```

```
82
             [tx, x1] = ode45(@(t, x)
                 objectEOM_disturb(t,x,m,r,km,Ix,Iy,Iz,v,mu,f1,f2,f3,f4),tspan,pinit);
          case '5'
83
               f1 = -m * g/4; %Assume -force up
84
               f2 = f1;
              f3 = f1;
              f4 = f1;
87
             pinit = [0; 0; -100; 5*pi/180; 0; 0; 0; 0; 0; 0; 0; 0];
88
             [tx, x1] = ode45(@(t, x)
89
                 LinearQuadControlQ2(t,x,m,r,km,Ix,Iy,Iz,v,mu),tspan,pinit);
      end
90
91
      xval = x1(:,1);
92
      yval = x1(:,2);
93
      zval = x1(:,3);
94
      phival = x1(:,4);
      thetaval = x1(:,5);
      psival = x1(:,6);
      uval = x1(:,7);
      vval = x1(:,8);
      wval = x1(:, 9);
100
      pval = x1(:,10);
101
      qval = x1(:,11);
102
      rval = x1(:,12);
103
104
      figure(1)
105
      drone_plot(x1,tx,'pqr',prob);
106
107
       figure(2)
108
      drone_plot(x1,tx,'uvw',prob);
109
      figure(3)
111
      drone_plot(x1,tx,'euler',prob);
112
113
       figure(4)
114
```

```
115
      drone_plot(x1,tx,'xyz',prob);
      figure (5)
      plot3(xval, yval, zval);
118
      grid on
119
   end
   function [] = drone_plot(x1,tx,type,prob)
   %DRONE_PLOT: Plots the 4 subplots of inertial position, Euler angles,
   %body acceleration, and Euler rates
   xval = x1(:,1);
      yval = x1(:,2);
      zval = x1(:,3);
      phival = x1(:,4);
      thetaval = x1(:,5);
      psival = x1(:,6);
      uval = x1(:,7);
10
      vval = x1(:,8);
      wval = x1(:, 9);
12
      pval = x1(:,10);
13
      qval = x1(:,11);
14
      rval = x1(:,12);
15
   switch type
      case 'pqr'
         subplot (3,1,1)
19
         plot(tx,pval,'LineWidth',5);
20
         xlabel('Time (s)');
21
         ylabel('P (rad/s)');
22
         subplot(3,1,2)
         plot(tx,qval,'LineWidth',5);
24
         xlabel('Time (s)');
25
         ylabel('Q (m/s)');
26
         subplot (3, 1, 3)
27
```

plot(tx,rval,'LineWidth',5);

28

```
xlabel('Time (s)');
29
         ylabel('R (m/s)');
31
         sgtitle(sprintf('%s P,Q,R vs Time',prob));
      case 'uvw'
32
         subplot (3, 1, 1)
33
         plot(tx,uval,'LineWidth',5);
34
         xlabel('Time (s)');
35
         ylabel('U (m/s)');
         if prob == '2c'
37
            axis([0 10 4.5 5.5]);
38
         end
39
         subplot (3,1,2)
40
         plot(tx, vval, 'LineWidth', 5);
41
         xlabel('Time (s)');
42
         ylabel('V (m/s)');
43
         if prob == '2b'
44
             axis([0 10 4.9 5.1]);
45
         end
         subplot (3,1,3)
47
         plot(tx,wval,'LineWidth',5);
48
         xlabel('Time (s)');
49
         ylabel('W (m/s)');
50
         if prob == '2b' | prob == '2c'
51
            axis([0 10 -1 0]);
52
53
         sgtitle(sprintf('%s U, V, W vs Time', prob));
54
      case 'euler'
55
         subplot (3, 1, 1)
56
         plot(tx,phival,'LineWidth',5);
57
         xlabel('Time (s)');
58
         ylabel('\Phi (rad)');
         subplot(3,1,2)
         plot(tx,thetaval,'LineWidth',5);
61
         xlabel('Time (s)');
62
         ylabel('\Theta (rad)');
63
```

```
plot(tx,psival,'LineWidth',5);
         xlabel('Time (s)');
66
         ylabel('\Psi (rad)');
         sgtitle(sprintf('%s Euler Angles vs Time',prob));
      case 'xyz'
         subplot(3,1,1)
70
         plot(tx,xval,'LineWidth',5);
         xlabel('Time (s)');
         ylabel('X position (m)');
73
         subplot (3,1,2)
74
         plot(tx,yval,'LineWidth',5);
         xlabel('Time (s)');
76
         ylabel('Y position (m)');
77
         subplot(3,1,3)
78
         plot(tx, zval, 'LineWidth', 5);
         if prob == '2b' | prob == '2c'
80
            axis([0 10 -1 1]);
         end
82
         xlabel('Time (s)');
83
         ylabel('Z position (m)');
84
         sgtitle(sprintf('%s Inertial Position vs Time',prob));
85
86
87
  end
   %Author: Thyme Zuschlag
  %Class: 3128 Lab 4
  %Date: 10/21
  %Purpose: Plot nicely on subplots with appropriate titles
  function [] = drone_plot2(x1,tx,x2, tx2, type,prob)
  %DRONE_PLOT: Plots the 4 subplots of inertial position, Euler angles,
```

%body acceleration, and Euler rates

xval = x1(:,1);

subplot(3,1,3)

64

```
yval = x1(:,2);
      zval = x1(:,3);
      phival = x1(:,4);
12
      thetaval = x1(:,5);
13
      psival = x1(:,6);
14
      uval = x1(:,7);
15
      vval = x1(:,8);
16
      wval = x1(:,9);
17
      pval = x1(:,10);
18
      qval = x1(:,11);
19
      rval = x1(:,12);
20
21
      xval2 = x2(:,1);
22
      yval2 = x2(:,2);
23
      zval2 = x2(:,3);
24
      phival2 = x2(:,4);
25
      thetaval2 = x2(:,5);
26
      psival2 = x2(:,6);
27
      uval2 = x2(:,7);
28
      vval2 = x2(:,8);
29
      wval2 = x2(:,9);
30
      pval2 = x2(:,10);
31
      qval2 = x2(:,11);
32
      rval2 = x2(:,12);
33
34
   switch type
35
      case 'pqr'
36
         subplot (3, 1, 1)
37
         hold on
38
         plot(tx,pval,'--r', "LineWidth", 2);
39
         plot(tx2,pval2, 'b');
         xlabel('Time (s)');
41
         ylabel('P (rad/s)');
42
         legend('Linear', 'NonLinear');
43
         subplot (3,1,2)
```

```
45
         hold on
         plot(tx,qval,'--r', "LineWidth", 2);
47
         plot(tx2,qval2, 'b');
         xlabel('Time (s)');
48
         ylabel('Q (m/s)');
         subplot(3,1,3)
         hold on
51
         plot(tx,rval,'--r', "LineWidth", 2);
52
         plot(tx2,rval2, 'b');
53
         xlabel('Time (s)');
54
         ylabel('R (m/s)');
55
         sgtitle(sprintf('%s 2d/3d P,Q,R vs Time',prob));
56
57
      case 'uvw'
58
         subplot (3, 1, 1)
59
         hold on
60
         plot(tx,uval,'--r', "LineWidth", 2);
61
         plot(tx2,uval2, 'b');
62
         xlabel('Time (s)');
         ylabel('U (m/s)');
         if prob == '2c'
65
            axis([0 10 4.5 5.5]);
66
         end
67
         subplot (3,1,2)
68
         hold on
69
         plot(tx,vval,'--r', "LineWidth", 2);
70
         plot(tx2, vval2, 'b');
71
         xlabel('Time (s)');
72
         ylabel('V (m/s)');
73
         if prob == '2b'
74
            axis([0 10 4.9 5.1]);
75
         end
76
         subplot (3,1,3)
77
         hold on
78
         plot(tx,wval,'--r', "LineWidth", 2);
```

```
plot(tx2, wval2, 'b');
          xlabel('Time (s)');
81
82
          ylabel('W (m/s)');
          if prob == '2b' | prob == '2c'
83
             axis([0 10 -1 0]);
          end
          sgtitle(sprintf('%s 2d/3d U,V,W vs Time',prob));
86
       case 'euler'
          subplot (3,1,1)
88
          hold on
89
          plot(tx,phival,'--r', "LineWidth", 2);
90
          plot(tx2,phival2, 'b');
91
          xlabel('Time (s)');
92
          ylabel('\Phi (rad)');
93
          subplot (3, 1, 2)
94
          hold on
95
          plot(tx,thetaval,'--r', "LineWidth", 2);
96
          plot(tx2,thetaval2, 'b');
          xlabel('Time (s)');
          ylabel('\Theta (rad)');
          subplot(3,1,3)
100
          hold on
101
          plot(tx,psival,'--r', "LineWidth", 2);
102
          plot(tx2,psival2, 'b');
103
          xlabel('Time (s)');
104
          ylabel('\Psi (rad)');
105
          sqtitle(sprintf('%s 2d/3d Euler Angles vs Time',prob));
106
      case 'xyz'
107
          subplot(3,1,1)
108
          hold on
109
          plot(tx,xval,'--r', "LineWidth", 2);
          plot(tx2,xval2, 'b');
          xlabel('Time (s)');
          ylabel('X position (m)');
113
          subplot (3,1,2)
114
```

```
hold on
         plot(tx,yval,'--r', "LineWidth", 2);
         plot(tx2, yval2, 'b');
         xlabel('Time (s)');
118
         ylabel('Y position (m)');
119
         subplot (3, 1, 3)
         hold on
121
         plot(tx,zval,'--r', "LineWidth", 2);
122
         plot(tx2, zval2, 'b');
         if prob == '2b' | prob == '2c'
124
            axis([0 10 -1 1]);
125
         end
126
         xlabel('Time (s)');
         ylabel('Z position (m)');
128
         sgtitle(sprintf('%s 2d/3d Inertial Position vs Time',prob));
130
131
   end
   function [xstate] = LinearQuadControlQ2(t,x,m,r,km,Ix,Iy,Iz,v,mu)
   %Inputs:
   % t = time
   % \ x = 12-dimension state vector includes the inertial velocity in
   % inertial coordinates and the inertial position in inertial coordinates
   % [x; y; z; phi; theta; psi; u; v; w; p; q; r]
   % m = mass of drone (kg)
   % r = radius of frame from motor to cg
   % km = control moment coefficient
   % Ix, Iy, Iz = moments about axis
   % v = drag coefficient
12
   % mu = moment coefficient
   % f1, f2, f3, f4 = forces from motors
14
15
   %Outputs:
```

```
% xdot = 12-dimension state vector includes inertial velocity in inertial
      coordinates and the inertial acceleration in inertial coordinates
19
      [xdot; ydot; zdot; phidot; thetadot; psidot; udot; vdot; wdot;
      pdot; qdot; rdot]
21
  %Methodology: Use Newton's second law F=ma to calculate the acceleration
22
  % and velocity at each point in time for ode45 to integrate to find
23
   % position. Drag, gravity and motor thrust are only forces acting on drone.
25
26
  g = 9.81;
27
28
  %Get IV's
  x1 = x(1);
  y1 = x(2);
  z1 = x(3);
32
  phi1 = x(4);
  theta1 = x(5);
  psi1 = x(6);
  u1 = x(7);
  v1 = x(8);
  w1 = x(9);
  p1 = x(10);
  q1 = x(11);
  r1 = x(12);
  Zc = -m*g;
42
43
  %Calculate moments
  k1Lat = 0.0021;
  k2Lat = 0.004;
  k3Lat = 1.9118e-4;
  k1Lon = 0.0021;
  k2Lon = 0.004;
  k3Lon = -1.9008e-4;
51 | m_ctl(1) = -k1Lat*p1-k2Lat*phi1;
```

```
m_{ctl}(2) = -k1Lon*q1-k2Lon*theta1;
  m_{ctl}(3) = -0.004*psil;
  Lc = m_ctl(1);
55
  Mc = m_ctl(2);
  Nc = m_ctl(3);
58
  %Put back into ode45
  xstate(1) = u1; %xdot
  xstate(2) = v1; %ydot
  xstate(3) = w1; %zdot
  xstate(4) = p1; %phidot
63
  xstate(5) = q1; %thetadot
  xstate(6) = r1; %psidot
  xstate(7) = -g*theta1; %udot
  xstate(8) = g*phi1; %vdot
  xstate(9) = 0; %wdot
  xstate(10) = 1/Ix*(Lc); %pdot
  xstate(11) = 1/Iy*(Mc); %qdot
71 \mid xstate(12) = 1/Ix*(Nc); %rdot
72 | xstate = xstate';
73 end
   function [xstate] = LinearQuadControlQ4(t,x,m,r,km,Ix,Iy,Iz,v,mu,vref)
  %Inputs:
  % t = time
  % x = 12-dimension state vector includes the inertial velocity in
  % inertial coordinates and the inertial position in inertial coordinates
  % [x; y; z; phi; theta; psi; u; v; w; p; q; r]
  % m = mass of drone (kg)
  % r = radius of frame from motor to cg
  % km = control moment coefficient
  % Ix, Iy, Iz = moments about axis
  % v = drag coefficient
```

```
% mu = moment coefficient
   % f1, f2, f3, f4 = forces from motors
15
  %Outputs:
16
  % xdot = 12-dimension state vector includes inertial velocity in inertial
     coordinates and the inertial acceleration in inertial coordinates
     [xdot; ydot; zdot; phidot; thetadot; psidot; udot; vdot; wdot;
19
     pdot; qdot; rdot]
21
  %Methodology: Use Newton's second law F=ma to calculate the acceleration
22
  % and velocity at each point in time for ode45 to integrate to find
23
  % position. Drag, gravity and motor thrust are only forces acting on drone.
24
25
26
  g = 9.81;
27
28
  %Get IV's
  x1 = x(1);
  y1 = x(2);
  z1 = x(3);
  phi1 = x(4);
33
  theta1 = x(5);
  psi1 = x(6);
  u1 = x(7);
  v1 = x(8);
37
  w1 = x(9);
38
  p1 = x(10);
  q1 = x(11);
  r1 = x(12);
  Zc = -m*q;
42
  ur = vref(1);
  vr = vref(2);
44
  %K vals from q1
  k1Lat = 0.0021;
```

```
k2Lat = 0.004;
   k3Lat = 1.9118e-4;
  k1Lon = 0.0021;
  k2Lon = 0.004;
  k3Lon = -1.9008e-4;
  m_{ctl}(1) = -k1Lat*p1-k2Lat*phi1+k3Lat*(vr-v1);
  m_{ctl}(2) = -k1Lon*q1-k2Lon*theta1+k3Lon*(ur-u1);
  m_{ctl}(3) = -0.004*psi1;
56
  Lc = m_ctl(1);
  Mc = m_ctl(2);
  Nc = m_ctl(3);
60
  %Put back into ode45
  xstate(1) = u1; %xdot
62
  xstate(2) = v1; %ydot
  xstate(3) = w1; %zdot
  xstate(4) = p1; %phidot
  xstate(5) = q1; %thetadot
  xstate(6) = r1; %psidot
  xstate(7) = -g*theta1; %udot
  xstate(8) = g*phi1; %vdot
  xstate(9) = 0; %wdot
  xstate(10) = 1/Ix*(Lc); %pdot
72 | xstate(11) = 1/Iy*(Mc); %qdot
  xstate(12) = 1/Ix*(Nc); %rdot
74 | xstate = xstate';
  clc
  clear all
  close all
  %% Q2 and 3: Find k vals using the A matrix
  %time constant of 0.5s \rightarrow eig = -2
```

```
Ix = 5.8e-5;
  Iy = 7.2e-5;
  k2Latreal = 0.004;
  k1Latreal = (-k2Latreal/Ix - 4) *-Ix/2;
  % k2Lat = linspace(k2Latreal/100,k2Latreal,100);
  k2Lonreal = 0.004;
  k1Lonreal = (-k2Lonreal/Iy - 4) *-Iy/2;
  g = 9.81;
  %%Lat k vals
15
  % for i = 1:100
     k1Lat = (-k2(i)/Ix - 4)*-Ix/2;
     A = [0 1; -k2(i)/Ix -k1Lat/Ix];
18
     eigval(i,:) = eig(A)';
19
  % end
20
  % A1 = [0 1; -k2Latreal/Ix -k1Latreal/Ix];
21
  % eigreal = eig(A1)
  %Lin k vals
  % A1 = [0 1; -k2Lonreal/Iy -k1Lonreal/Iy];
  % eigreal = eig(A1)
26
  % %% Q4
  bLat = -k2Latreal/Ix;
  cLat = -k1Latreal/Ix;
  bLon = -k2Lonreal/Iy;
  cLon = -k1Lonreal/Iy;
31
  k3Latreal = -Ix*(0.8*bLat-0.64*cLat-0.512)/9.81;
32
  k3Lonreal = Iy*(0.8*bLon-0.64*cLon-0.512)/9.81;
33
  aLatreal = -k3Latreal/Ix;
  aLonreal = -k3Lonreal/Iy;
  ALatreal = [0 g 0; 0 0 1; aLatreal bLat cLat];
  ALonreal = [0 -g 0; 0 0 1; aLonreal bLon cLon];
  eigsLat = eig(ALatreal);
  eigsLon = eig(ALonreal)
  k3Lat = linspace(k3Latreal/10,k3Latreal*10,1000);
  aLat = -k3Lat/Ix;
```

```
for i = 1:1000
      A = [0 \ g \ 0; \ 0 \ 0 \ 1; \ aLat(i) \ bLat \ cLat];
44
      eigs = eig(A);
      eigvalLat(i,:) = eigs';
  end
  figure(1)
  hold on
  axis([-1.6 0 -2 2]);
  % plot(eigvalLat(:,1),0);
  plot(eigvalLat(:,2));
  plot(eigvalLat(:,3));
  xline(-0.8,'--k');
53
  plot (eigsLat(1), 0, 'r.', 'MarkerSize', 20);
  plot(eigsLat(2),0,'r.','MarkerSize',20);
  plot(eigsLat(3),0,'r.','MarkerSize',20);
  text(-1.55,.1,'increasing k3 \rightarrow');
  text(-.6,.1,'\leftarrow increasing k3 ');
  xlabel('Real');
  ylabel('Complex');
  title('4 Root Locus for Varying k3 (Lateral)');
  legend('Eig Val 1','Eig Val 2','Time Constant = 1.25s',...
62
      'Chosen k3 Eig Vals (1.99183-4)');
63
64
  % k3Lon = linspace(k3Lonreal/10,k3Lonreal*10,1000);
  % aLon = -k3Lon/Iy;
  % for i = 1:1000
67
     A = [0 - q 0; 0 0 1; aLon(i) bLon cLon];
68
69
     eigs = eig(A);
     eigvalLon(i,:) = eigs';
  % end
  % figure(2)
  % hold on
73
  % axis([-1.6 0 -2 2]);
  % % plot(eigvalLat(:,1),0);
  % plot(eigvalLon(:,2));
```

```
% plot(eigvalLon(:,3));
   % xline(-0.8,'--k');
   % plot(eigsLon(1),0,'r.','MarkerSize',20);
   % plot(eigsLon(2),0,'r.','MarkerSize',20);
   % plot(eigsLon(3),0,'r.','MarkerSize',20);
   % text(-1.55,.1,'decreasing k3 \rightarrow');
   % text(-.6,.1,'\leftarrow decreasing k3 ');
   % xlabel('Real');
   % ylabel('Complex');
   % title('4 Root Locus for Varying k3 (Longitudinal)');
   % legend('Eig Val 1','Eig Val 2','Time Constant = 1.25s',...
     'Chosen k3 Eig Vals (-1.9008-4)');
88
89
   %% Q5
   % k2Latreal = 0.004;
   % k1Latreal = (-k2Latreal/Ix - 4) *-Ix/2;
   % k2Lonreal = 0.004;
   % k1Lonreal = (-k2Lonreal/Iy - 4) *-Iy/2;
   % bLat4 = -k2Latreal/Ix;
   % cLat4 = -k1Latreal/Ix;
   % bLon4 = -k2Lonreal/Iy;
   % cLon4 = -k1Lonreal/Iy;
   % k3Latreal = -Ix*(0.8*bLat4-0.64*cLat4-0.512)/9.81;
   % k3Lonreal = Iv*(0.8*bLon4-0.64*cLon4-0.512)/9.81;
100
101
   % ALatreal = [0 1 0 0; 0 0 g 0; 0 0 0 1; aLatreal bLat cLat dLat];
102
   % ALonreal = [0 1 0 0; 0 0 -g 0; 0 0 0 1; aLonreal bLon cLon dLon];
   function [REB] = R_eb(phi,theta,psi,units)
   %switch if input is either rad or deg
   switch units
      case 'deg'
         REB(1,1) = cosd(theta)*cosd(psi);
         REB(1,2) = cosd(theta) * sind(psi);
         REB(1,3) = -sind(theta);
```

```
REB(2,1) = sind(phi)*sind(theta)*cosd(psi)-cosd(phi)*sind(psi);
         REB(2,2) = sind(phi)*sind(theta)*sind(psi)+cosd(phi)*cosd(psi);
         REB(2,3) = sind(phi)*cosd(theta);
10
         REB(3,1) = cosd(phi) *sind(theta) *cosd(psi) +sind(phi) *sind(psi);
11
         REB(3,2) = cosd(phi) *sind(theta) *sind(psi) -sind(phi) *cosd(psi);
         REB(3,3) = cosd(phi)*cosd(theta);
      case 'rad'
14
         phi = phi * (180/pi);
15
         theta = theta * (180/pi);
16
         psi = psi * (180/pi);
         REB(1,1) = cosd(theta)*cosd(psi);
18
         REB(1,2) = cosd(theta)*sind(psi);
19
         REB(1,3) = -sind(theta);
2.0
         REB(2,1) = sind(phi)*sind(theta)*cosd(psi)-cosd(phi)*sind(psi);
         REB(2,2) = sind(phi)*sind(theta)*sind(psi)+cosd(phi)*cosd(psi);
         REB(2,3) = sind(phi)*cosd(theta);
         REB(3,1) = cosd(phi) *sind(theta) *cosd(psi) +sind(phi) *sind(psi);
24
         REB(3,2) = cosd(phi) *sind(theta) *sind(psi) -sind(phi) *cosd(psi);
         REB(3,3) = cosd(phi)*cosd(theta);
27
  end
  REB = inv(REB);
28
29
  end
   function [Tmat] = T(phi, theta, psi, units)
  %T Summary of this function goes here
  % Detailed explanation goes here
  switch units
      case 'deg'
         Tmat(1,1) = 1;
         Tmat(1,2) = sind(phi)*tand(theta);
         Tmat(1,3) = cosd(phi) *tand(theta);
         Tmat(2,1) = 0;
         Tmat(2,2) = cosd(phi);
10
         Tmat(2,3) = -sind(phi);
```

```
12
         Tmat(3,1) = 0;
         Tmat(3,2) = sind(phi) *secd(theta);
13
         Tmat(3,3) = cosd(phi) *secd(theta);
14
15
      case 'rad'
16
         phi = phi * (180/pi);
17
         theta = theta * (180/pi);
18
         psi = psi * (180/pi);
19
         Tmat(1,1) = 1;
20
         Tmat(1,2) = sind(phi)*tand(theta);
21
         Tmat(1,3) = cosd(phi)*tand(theta);
         Tmat(2,1) = 0;
         Tmat(2,2) = cosd(phi);
24
         Tmat(2,3) = -sind(phi);
25
         Tmat(3,1) = 0;
26
         Tmat(3,2) = sind(phi)*secd(theta);
27
         Tmat(3,3) = cosd(phi) *secd(theta);
28
  end
   % Luke Engelken
  % ASEN 3128
  % prob1.m
  % Created: 9/11/20
  %To run, in command window type "prob(<insert quetsion number)" and you
  %will see plots
  %ex: prob('1a')
  function [] = updated_drone()
10
      %% Declare Constants
     m = 0.068; %mass of drone (kg)
      r = 0.06; %radial distance from cg to motor (m)
     km = 0.0024; %control moment coefficient (N*m/N)
14
      Ix = 5.8e-5; %x-axis moment of inertia (kg*m^2)
15
      Iy = 7.2e-5; %y-axis moment of inertia (kg*m^2)
16
```

```
Iz = 1e-4; %z-axis moment of inertia (kg*m^2)
      v = 1e-3; %aerodynamic force coefficient (N/(m/s^2))
18
19
     mu = 2e-6; %N*m/(rad/s^2)
      g = 9.81; %m/s^2
20
      %xstate vector: [x; y; z; phi; theta; psi; xdot; ydot; zdot; phidot;
21
      %thetadot; psidot] (integral of eom state vector)
22
      tspan = [0 10];
23
      pinit = [0; 0; -100; 0; 0; 0; 0; 0; 0; 0; 0.1; 0];
24
      [tx,x1] = ode45(@(t,x) LinearQuadControlQ2(t,x,m,r,km,Ix,Iy,Iz,v,mu),tspan,pinit);
25
      [tx2, x2] = ode45(@(t, x))
26
          QuadrotorEOM_controlQ3(t,x,m,r,km,Ix,Iy,Iz,v,mu),tspan,pinit);
28
      xval = x1(:,1);
29
      yval = x1(:,2);
30
      zval = x1(:,3);
      phival = x1(:,4);
32
33
      thetaval = x1(:,5);
      psival = x1(:,6);
     uval = x1(:,7);
35
     vval = x1(:,8);
36
     wval = x1(:,9);
37
      pval = x1(:,10);
38
      qval = x1(:,11);
39
     rval = x1(:,12);
40
41
     xval2 = x2(:,1);
42
43
      yval2 = x2(:,2);
      zval2 = x2(:,3);
      phival2 = x2(:,4);
45
      thetaval2 = x2(:,5);
      psival2 = x2(:,6);
47
     uval2 = x2(:,7);
48
      vval2 = x2(:,8);
      wval2 = x2(:,9);
```

```
pval2 = x2(:,10);
51
      qval2 = x2(:,11);
52
      rval2 = x2(:,12);
53
54
      prob = 0;
55
57
      figure(1)
58
      hold on
59
      %drone_plot(x1,tx,'pqr', prob);
60
      drone_plot2(x1,tx, x2,tx2, 'pqr', prob);
61
      hold off
62
63
      hold on
64
      figure(2)
65
      %drone_plot(x1,tx,'uvw',prob);
66
67
      drone_plot2(x1, tx, x2, tx2, 'uvw', prob);
      hold off
      hold on
70
      figure(3)
71
      %drone_plot(x1,tx,'euler',prob);
72
      drone_plot2(x1,tx,x2,tx2,'euler',prob);
      hold off
74
75
      hold on
76
      figure (4)
77
      %drone_plot(x1,tx,'xyz',prob);
78
      drone_plot2(x1, tx,x2,tx2,'xyz',prob);
      hold off
80
      figure(5)
82
      plot3(xval, yval, zval);
83
      grid on
84
  end
85
```

```
function [Output_Plot] = Plot12(Time, State)
  t=Time;%time
  x=State(:,1);%populate variables
  y=State(:,2);%populate variables
  z=State(:,3);%populate variables
  phi=State(:,4);%populate variables
  theta=State(:,5);%populate variables
  psi=State(:,6);%populate variables
  u=State(:,7);%populate variables
  v=State(:,8);%populate variables
12
  w=State(:,9);%populate variables
  p=State(:,10);%populate variables
  q=State(:,11);%populate variables
15
  r=State(:,12);%populate variables
17
18
19
  sgtitle('6 Experimental Drone Behavior')%main title
  subplot(4,3,1)%sub plot call
  plot(t,x)
  ylabel('x_E [m]')
  xlabel('time [s]')
25
  subplot(4,3,2)%sub plot call
  plot(t,y)
  ylabel('y_E [m]')
  xlabel('time [s]')
30
  subplot(4,3,3)%sub plot call
  plot(t,z)
  ylabel('z_E [m]')
  xlabel('time [s]')
```

```
subplot(4,3,4)%sub plot call
  plot(t,phi)
  ylabel('\phi [rad]')
  xlabel('time [s]')
42
43
  subplot(4,3,5)%sub plot call
  plot(t,theta)
  ylabel('\theta [rad]')
  xlabel('time [s]')
48
49
  subplot(4,3,6)%sub plot call
  plot(t,psi)
  ylabel('\psi [rad]')
  xlabel('time [s]')
55
  subplot(4,3,7)%sub plot call
  plot(t,u)
  ylabel('u^E [m/s]')
  xlabel('time [s]')
60
61
  subplot(4,3,8)%sub plot call
  plot(t, v)
  ylabel('v^E [m/s]')
  xlabel('time [s]')
  subplot(4,3,9)%sub plot call
  plot(t,w)
70 | ylabel('w^E [m/s]')
```

```
xlabel('time [s]')
72
73
  subplot(4,3,10)%sub plot call
  plot(t,p)
  ylabel('p [rad/s]')
  xlabel('time [s]')
79
  subplot(4,3,11)%sub plot call
  plot(t,q)
  ylabel('q [rad/s]')
  xlabel('time [s]')
84
85
  subplot(4,3,12)%sub plot call
  plot(t,r)
  ylabel('r [rad/s]')
  xlabel('time [s]')
91
92
93
  Output_Plot=1;%lazy
94
  end
  %Part 6 Data read in and plot
  \mbox{\ensuremath{\mbox{\$Emerson}}} and group
  %10/22/2020
  clear; close; clc
  data=load('RSdata_10_21_1451');% load file
```

```
응____
  A=data.rt_sensor; %get data
  B=data.rt_optical; %get data
  C=data.rt_calib; %get data
12
  D=data.rt_cmd; %get data
  G1=data.rt_estim; %get data
  %G2=data.rt_estimatedStates; %obsolete
  MotorForce=data.rt_motor; %motor forces get data
  MotorForceTime=MotorForce.time; %motor forces get data
  MotorForceStrut=MotorForce.signals; %motor forces get data
  MotorForcesValues=MotorForceStrut.values; %motor forces get data
22
  time=G1.time(:);%time call
  xval_data=G1.signals.values(:,1); %get x data
  yval_data=G1.signals.values(:,2); % get y data
  zval_data=G1.signals.values(:,3);%get z data
  phival_data=G1.signals.values(:,4);%get angle data
  thetaval_data=G1.signals.values(:,5); %get angle data
  psival_data=G1.signals.values(:,6);%get angle data
  uval_data=G1.signals.values(:,7); % get u data
  vval_data=G1.signals.values(:,8);%get v data
32
  wval_data=G1.signals.values(:,9); %get w data
33
  pval_data=G1.signals.values(:,10);%get p data
34
  qval_data=G1.signals.values(:,11);%get q data
  rval_data=G1.signals.values(:,12);%get r data
  %---
38
  %___
  LLL=length(xval_data);%get length
  x1_data=zeros(LLL, 12); %make blank matrix
  x1_data(:,1)=xval_data;%populate matrix
  x1_data(:,2)=yval_data;%populate matrix
```

```
x1_data(:,3)=zval_data;%populate matrix
  x1_data(:,4)=phival_data;%populate matrix
  x1_data(:,5)=thetaval_data;%populate matrix
  x1_data(:,6)=psival_data;%populate matrix
  x1_data(:,7) = uval_data; % populate matrix
  x1_data(:,8) = vval_data; % populate matrix
  x1_data(:,9)=wval_data;%populate matrix
  x1_data(:,10) = pval_data; % populate matrix
  x1_data(:,11) =qval_data;%populate matrix
  x1_data(:,12)=rval_data;%populate matrix
53
54
55
  plot=Plot12(time,x1_data)%plot call
57
58
60
62
63
64
65
66
67
68
69
71
72
73
75
77
```

```
79 % t=2600;
   % State=x1_data;
81
82
   % x=State(:,1);
   % y=State(2);
   % z=State(3);
   % phi=State(4);
   % theta=State(5);
   % psi=State(6);
88
   % u=State(7);
   % v=State(8);
   % w=State(9);
91
   % p=State(10);
92
   % q=State(11);
93
   % r=State(12);
   % subplot (4,3,1)
   % plot(t,x)
99
   % subplot(4,3,2)
   % plot(t,y)
101
102
   % subplot (4,3,3)
103
   % plot(t,z)
104
105
   % subplot(4,3,4)
   % plot(t,phi)
108
   % subplot (4,3,5)
   % plot(t,theta)
111
% subplot (4,3,6)
113 % plot(t,psi)
```

```
% subplot (4,3,7)
   % plot(t,u)
   % subplot(4,3,8)
   % plot(t,v)
120
   % subplot(4,3,9)
   % plot(t,w)
123
   % subplot(4,3,10)
124
   % plot(t,p)
126
   % subplot(4,3,11)
   % plot(t,q)
128
129
   % subplot(4,3,12)
   % plot(t,r)
132
133
134
   % % plot=Plot12(time,x1_data)
135
136
   % % subplot(4,3,1)
   % % plot(time, xval_data)
138
139
   % % subplot(4,3,2)
140
   % % plot(time,xval_data)
   응 응
   % % subplot (4,3,3)
   % % plot(time, xval_data)
   응 응
145
   % % subplot (4,3,4)
   % % plot(time,xval_data)
   응
148
```

```
% %Plot Function(time, matrix12)
```