

# An integrative multi-context Mendelian randomization method for identifying risk genes across human tissues

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## Introduction

This vignette provides an introduction to the `mintMR` package. The R package `mintMR` implements the `mintMR` method for integrative multi-context Mendelian randomization analysis.

To install the development version of the `mintMR` package, please load the `devtools` package first. Note that `mintMR` requires the `CCA`, `Rcpp`, and `RcppArmadillo` packages.

To install this package, run the following command in R

```
library(devtools)
install_github("ylustat/mintMR")
```

Load the package using the following command:

```
library("mintMR")
```

This vignette depends on R packages `MendelianRandomization`, `ggplot2` and `tidyverse`, you can load these packages using the following command:

```
suppressMessages(library("tidyverse"))
library("ggplot2")
library("MendelianRandomization")
```

## Fit `mintMR` for correlated SNPs using simulated data

In this section, we fit `mintMR` using simulated data (provided in the package) as an example to illustrate the basic usage of `mintMR`. `gamma_hat` and `se_g` are the estimated IV-to-exposure effect and its standard error, and `Gamma_hat` and `se_G` are the estimated IV-to-outcome effect and its standard error. `LD` is the estimated linkage disequilibrium matrix among IVs. `latent_status` is the true underlying effect status, where 1 indicates the presence of non-zero effect and 0 indicates the absence of effect.

```
data(example_data)
names(example_data)
```

```
## [1] "gamma_hat"      "Gamma_hat"      "se_g"           "se_G"
## [5] "LD"             "latent_status"
```

The example data includes 50 simulated genes, each with effects from 5 different contexts/tissues.

```
L <- length(example_data$gamma_hat)
K1 <- K2 <- 5
L
```

```
## [1] 50
```

In the input IV-to-exposure statistics, each exposure have effects from multiple contexts/tissues. The `group` variable is used to represent the indices of contexts/tissues in the input statistics that belong to each exposure. The `group` variable is a list, and each element of it is a vector of column indices for the `gamma_hat` and `se_g`.

```
group <- list(exposure1 = 1:K1, exposure2 = 1:K2+K1)
# column 1 to 5 in gamma_hat and se_g are from exposure 1
# column 6 to 10 in gamma_hat and se_g are from exposure 2
group
```

```
## $exposure1
## [1] 1 2 3 4 5
##
## $exposure2
## [1] 6 7 8 9 10
```

In addition, mintMR takes IV-to-exposure effect (a list of  $I_g \times \sum K_l$  matrices with length  $L$ ) and standard errors, IV-to-outcome effect and standard errors. The LD matrices (`corr_mat`) and sample overlap (`Lambda`) are optional.

The default prior parameters used in the algorithm is

```
opts <- get_opts(L)
names(opts)

## [1] "a_gamma" "b_gamma" "a_alpha" "b_alpha" "a_beta" "b_beta" "a"
## [8] "b" "maxIter" "thin" "burnin"
```

It can be changed by specifying the parameters you would like to use. For example:

```
opts <- get_opts(L, maxIter = 1000)
```

MintMR can be run without specifying LD or sample overlap using the following command.

```
set.seed(1)
res_no_LD <- mintMR(gammah = example_data$gamma_hat,
                    Gammah = example_data$Gamma_hat,
                    se1 = example_data$se_g,
                    se2 = example_data$se_G,
                    group = group)
```

When LD information is available and is formatted as a list of matrices, it can be accounted for:

```
set.seed(1)
res <- mintMR(gammah = example_data$gamma_hat,
              Gammah = example_data$Gamma_hat,
              se1 = example_data$se_g,
              se2 = example_data$se_G,
              corr_mat = example_data$LD,
              group = group)
```

When sample overlap information  $\hat{C}$  is available as a  $(1 + \sum_l K_l) \times (1 + \sum_l K_l)$  matrix, it can be used in the function as

```
set.seed(1)
# Example correlation matrix for sample overlap. In real data, it can be pre-estimated.
C <- 0.9 * diag(1, (1+K1+K2)) +
    0.1 * matrix(1, nrow=1+K1+K2, ncol=1+K1+K2)

Lambda <- solve(C)

res_LD_sample_overlap <- mintMR(gammah = example_data$gamma_hat,
                                Gammah = example_data$Gamma_hat,
```

```
se1 = example_data$se_g,
se2 = example_data$se_G,
corr_mat = example_data$LD,
Lambda = Lambda,
group = group)
```

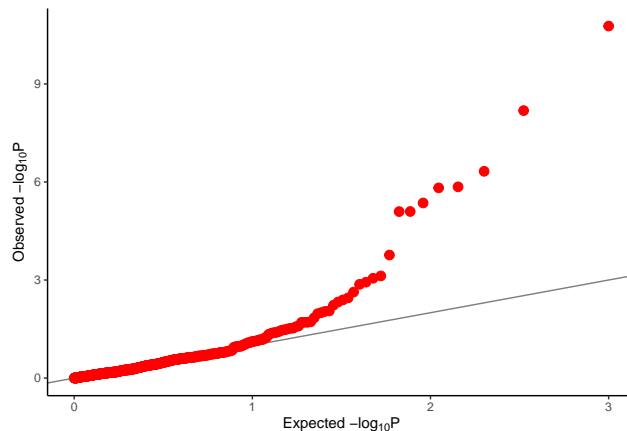
The output includes the effect estimates and p-values for each exposure in each context/tissue.

```
names(res)
```

```
## [1] "Estimate" "Pvalue"
```

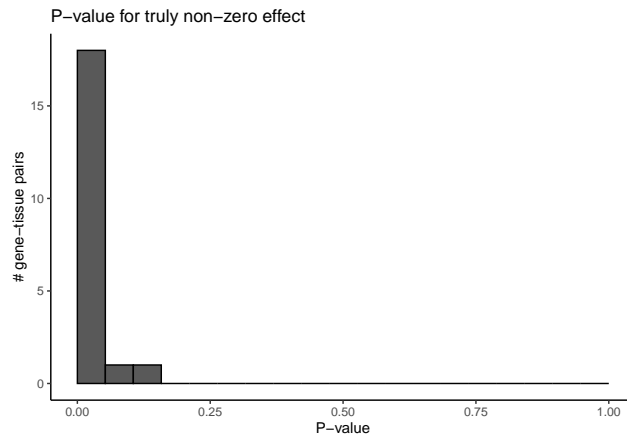
The p-value distribution for all gene-tissue pairs analyzed can be visualized as below.

```
p <- data.frame(mintMR = as.vector(res$Pvalue))
p %>%
  arrange(mintMR) %>%
  mutate(unif = ppoints(n())) %>%
  mutate(value = -log10(mintMR), unif = -log10(unif)) %>%
  ggplot(aes(y = value, x = unif))+
  geom_abline(intercept = 0, slope = 1, alpha = 0.5)+
  geom_point(size = 3, col = "red", alpha=1)+
  theme_classic()+
  labs(y = expression(paste("Observed  $-\log_{10}$ ", plain(P))),
       x = expression(paste("Expected  $-\log_{10}$ ", plain(P))))
```



The p-value distribution for truly non-zero effects:

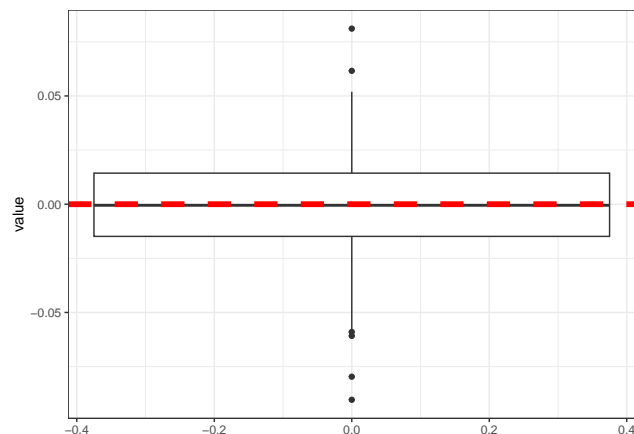
```
p <- data.frame(mintMR = res$Pvalue[example_data$latent_status == 1])
p %>%
  ggplot(aes(x = mintMR))+
  geom_histogram(col="black", boundary = 0, bins=20)+
  theme_classic()+
  scale_x_continuous(limits = c(NA,1))+
  labs(x = "P-value", y = "# gene-tissue pairs",
       title = "P-value for truly non-zero effect")
```



The effect estimates for truly zero effects:

```
estimate <- res$Estimate
estimate[example_data$latent_status == 1] <- NA

estimate %>%
  reshape2::melt() %>%
  tidyr::drop_na() %>%
  ggplot(aes(y = value))+
  theme_bw()+
  geom_boxplot()+
  geom_hline(yintercept = 0,col="red",linetype="dashed",linewidth=2)
```



In real data analysis, we recommend to first estimate the parameter `b_beta` for the prior distribution of causal effects using other MR methods. For example, we may fit MVMR-IVW and calculated the estimate as follows

```
ivw <- mapply(function(bx,by,bxse,byse,ld) {
  res <- mr_mvivw(mr_mvinput(bx = bx, by = as.numeric(by),
                             bxse = bxse, byse = as.numeric(byse),
                             correlation = ld))
  return(list(p = res$Pvalue, b = res$Estimate))
},example_data$gamma_hat,example_data$Gamma_hat,
example_data$se_g,example_data$se_G,
example_data$LD,SIMPLIFY = F)

b_ivw <- lapply(ivw, function(x) x$b) %>% do.call(rbind,.)
```

```
p_ivw <- lapply(ivw, function(x) x$p) %>% do.call(rbind,.)

b_beta <- var(b_ivw[p_ivw > 0.05]) * (K1+K2) / 2
opts <- get_opts(L, b_beta = rep(b_beta,L))
```

The estimated parameter can be used in the mintMR by setting the opts option.

```
set.seed(1)
res <- mintMR(gammah = example_data$gamma_hat,
             Gammah = example_data$Gamma_hat,
             se1 = example_data$se_g,
             se2 = example_data$se_G,
             corr_mat = example_data$LD,
             group = group,
             opts = opts)

p <- data.frame(mintMR = as.vector(res$Pvalue))
p %>%
  arrange(mintMR) %>%
  mutate(unif = ppoints(n())) %>%
  mutate(value = -log10(mintMR), unif = -log10(unif)) %>%
  ggplot(aes(y = value, x = unif))+
  geom_abline(intercept = 0, slope = 1, alpha = 0.5)+
  geom_point(size = 3, col = "red", alpha=1)+
  theme_classic()+
  labs(y = expression(paste("Observed -log"[10], plain(P))),
       x = expression(paste("Expected -log"[10], plain(P))))
```

