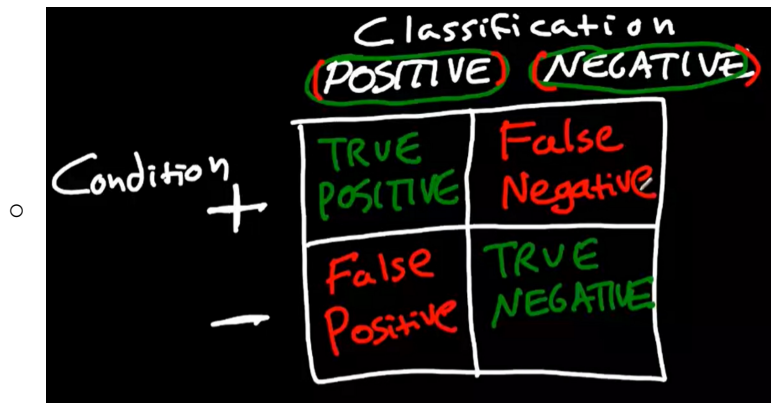


Week 2 Binary classification and confusion matrix

29 June 2020 18:02

Binary classification and confusion matrix

- binary outcomes and a binary classification -> confusion matrix



Confusion Matrix			Test Classification Y	
Condition X	"	a	"Positive"	"Negative"
			c	d
			e	f
"	b		g	h

Individual Probabilities	Name	
P("+")	a	Incidence of Condition "+"
p("-")	b	Incidence of "Condition "-"
p(Test POS)	c	Classification Incidence "POS"
p(Test NEG)	d	Classification Incidence "NEG"
p(Test POS, "+")	e	True Positives
p(Test NEG, "+")	f	False Negatives
p(Test "POS, "-")	g	False Positives
p(Test "NEG", "-")	h	True Negatives

Probability Distributions		Name
$P(X)$	$p(a,b)$	Marginal Probability of the Condition
$P(Y)$	$p(c,d)$	Marginal Probability of the Classification
$p(X,Y)$	$p(e,f,g,h)$	Joint Distribution of X and Y
$P(X)p(Y)$	$p(ac,ad,bc,bd)$	Product Distribution of X and Y
Conditional Probabilities		Name
$p(\text{Test POS} \mid "+")$	e/a	True Positive Rate
$p(\text{Test NEG} \mid "+")$	f/a	False Negative Rate
$p(\text{Test POS} \mid "-")$	g/b	False Positive Rate
$p(\text{Test NEG} \mid "-")$	h/b	True Negative Rate
$p("+ \mid \text{Test POS})$	e/c	Positive Predictive Value (PPV)
$p("- \mid \text{Test POS})$	g/c	1- PPV
$p("+ \mid \text{Test NEG})$	f/d	1- NPV
$p("- \mid \text{Test NEG})$	h/d	Negative Predictive Value (NPV)
Other implied rules		
$a+b = 1$	$e+f = a$	
$c+d = 1$	$g+h = b$	
$e+f+g+h=1$	$e+g = c$	
	$f+h = d$	

- ROC curve
 - x = false positive rate; y = true positive rate
 - FP rate: probability of FP conditional upon actually not sick
 - TP rate: probability of TP conditional upon actually sick
 - scatter plot with different threshold determined by cost of FN and FP
- Performance metrics for binary classification models: AUC(area under ROC curve)
 - between $1/2$ - 1
 - $1/2$: same as random
 - 1 : perfect model