

It's a Type of Magic

#CTD2019

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TypeScript

Just JavaScript with type annotations?

TypeScript

- Generics
- Intersection types
- Union Types
- Literal Types
- Mapped Types
- Conditional Types

Typescript Config

- Minimum config for type safety:
 - Variables are non-nullable unless explicitly stated
 - Expressions and declarations cannot be any unless explicitly stated

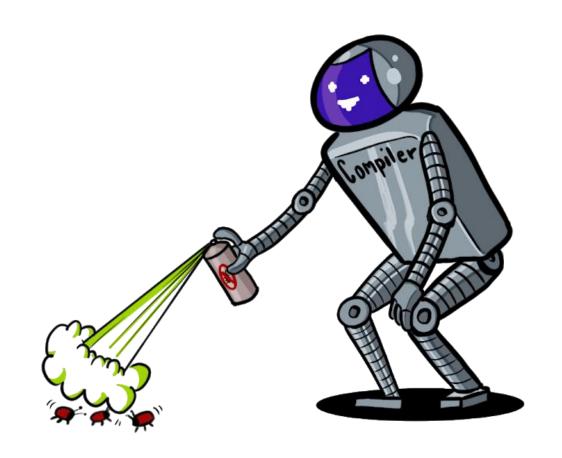
```
{
  "compilerOptions": {
    "strictNullChecks": true,
    "noImplicitAny": true,
    // ...
}
```

• Enable all strict type checking options with "strict": true

Why Type-Safety?

- Let the compiler help you!
- Prevents several classes of bugs
- Less testing effort
- Self-documentation

Can be fun too!



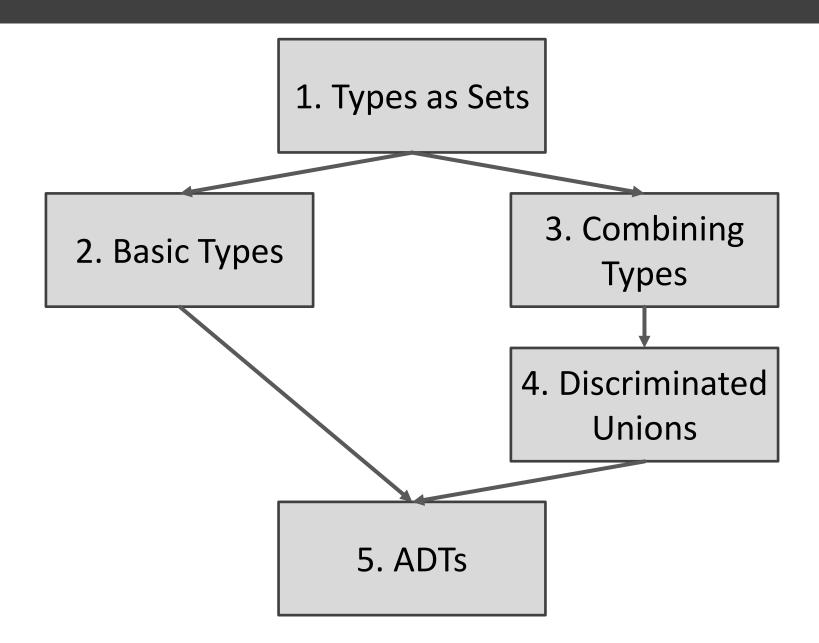
Goals

Get an intuition for types as a concept

See some examples how to use type features of TS effectively

Learn about ADTs

Structure



Types as Sets

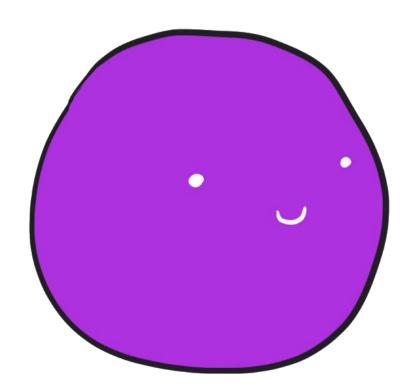
Types as Sets

Looking at types as sets helps to understand the underlying concepts

What is a Set? A collection of Objects

 What is a Type? A class of Objects confining to a set of constraints

 Types can be described with simple algebra



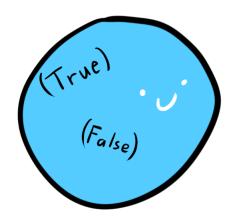


Intuition: Counting inhabitants

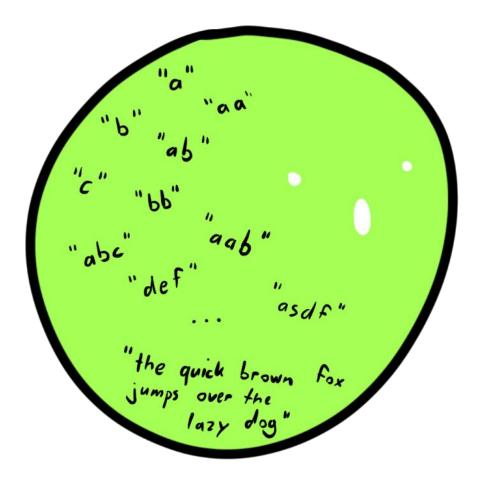
• Boolean?

• Integer?

• String?







Structural Type Equality

- C#, Java, etc: Nominal type systems
- TypeScript, Haskell, Elm: types are defined by their shape, not their names

```
declare function call(c: Contact): boolean;
var personWithContact = {
name: "JoJo",
phone: "079 123 45 67"
call(personWithContact);
```

Basic Types

Singleton Types

Types with only one inhabitant

In Typescript:

```
let u; // undefined

let a = null; // null

const x = "foo"; // "foo"

const y = 5; // 5
```



Type Literals

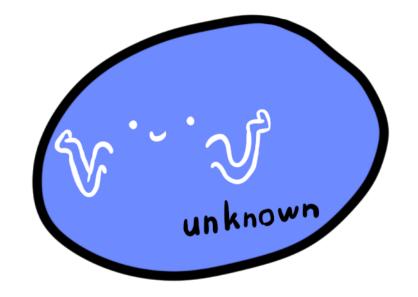
Top Types

- Also universal supertype, contains every possible value, equals the universal set U
- In typescript: any and unkown

```
let c: any = "foo";
let d: number = c;
```



```
let e: unknown = 42;
let f: string = e; // type error
```



Example of using unknown

```
type Duck = { walkSpeed: number, quack: () => string };
function tryQuack(x: unknown) {
 return x.quack();
                                      Operations on an
```

Operations on an object of type unknown are not allowed

Example of using unknown

Type guard

```
type Duck = { walkSpeed: number, quack: () => string }
function isDuck(thing: unknown): thing is Duck {
 return typeof (thing as Duck).walkSpeed === "number"
     && typeof (thing as Duck).quack === "function";
function tryQuack(x: unknown) {
  if (isDuck(x)) {
    return x.quack();
  console.log("Wasn't a duck, sorry.")
```

The compiler knows that x must be of type Duck

Bottom Type

A type that contains no values, equals the empty set Ø

```
let g: never = ({} as any); // Error
```

- Has several interesting applications, similar to 0 in algebra
- If the typescript ever reaches a never, it will not compile



Basic Types as Sets: Summary

```
never = \{\} = \emptyset

any = unknown = U

null = \{null\}

"foo" = \{"foo"\}

number = \{1, 2, ...\} = \mathbb{R}
```

E.g.
$$U \supseteq \mathbb{R} \supseteq \emptyset$$

Combining Types

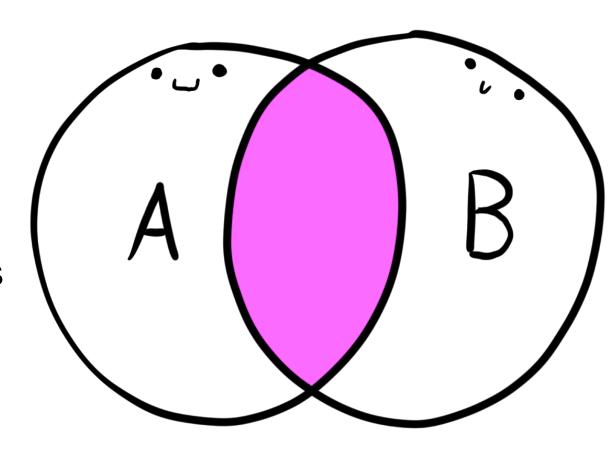
Intersection Type

• As sets: $A \cap B$

 Objects of an intersection type must contain properties of both types

```
type Person = { name: string }
type Contact = { phone: string }

let p: Person & Contact = {
  name = "JoJo",
  phone = "079 123 45 67",
};
```

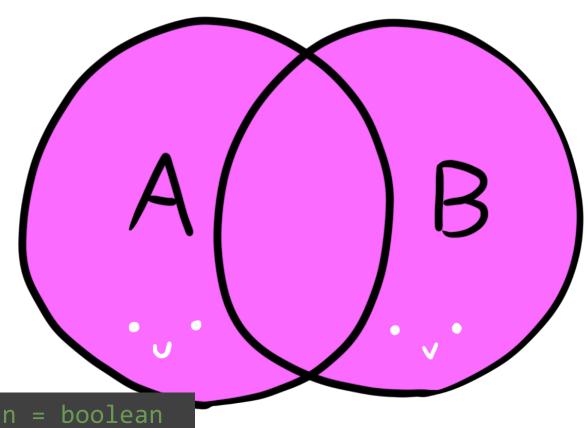


Union Type

 \cdot As Sets: $A \cup B$

 The object can be either of the two types

```
let h: string | number;
h = "hello";
h = 42;
```



```
type MyBoolean = true | false;// MyBoolean = boolean
```

```
type Workdays = "Mon" | "Tue" | "Wed" | "Thu" | "Fri";
type Weekdays = Workdays | "Sat" | "Sun";
```

Some set algebra

Identity Laws:

$$A \cup \emptyset = A$$

$$A \cap U = A$$

Commutativity:

$$A \cup B = B \cup A$$

$$A \cap B = B \cap A$$

Associativity:

$$(A \cup B) \cup C = A \cup (B \cup C)$$

$$(A \cap B) \cap C = A \cap (B \cap C)$$

And others apply as well ©

Example of using Union Types

```
function double(x: number | string) {
  return x * 2;
}
```

A string cannot be multiplied

Example of using Union Types

```
function double(x: number | string) {
  if(typeof x == "number") {
    return x * 2;
  }
  return (2 * Number(x)).toString();
}
```

The control flow analysis infers the type of x in both cases

Discriminated Unions

Opaque Types

The structural type equality can stand in our way

Sometimes we want to differentiate values with identical structure

```
type Username = string;
type Password = string;
const displayUserName = (u: Username) => `User: ${u}`;
const pw: Password = "hunter2";
displayUserName(pw); // valid, but not what we want
```

Opaque Types

- How to make your types "Opaque"?
 - Type Literals
 - Intersection Types

```
type Username = string & { type: "Username" };
type Password = string & { type: "Password" };

const displayUserName = (u: Username) => `User: ${u}`;

const pw: Password = "hunter2" as Password;

displayUserName(pw); // compiler prevents us from misusing sensitive data
```

These types are

now

(structurally)

Opaque Types

Can be made even cleaner with mapped types

The compiler prevents us to use a password value where we shouldn't

```
type Opaque<K, T> = T & {_type: K};

type Username = Opaque<"Username", string>;
type Password = Opaque<"Password", string>;

const displayUserName = (u: Username) => `User: ${u}`;

const pw: Password = "hunter2" as Password;

displayUserName(pw); // A-OK!
```

Discriminated Unions

- The concept of «Opaque» Types can be extended to Discriminated Unions
 - In Set Theory called **disjoint union**: $A \sqcup B$
 - Also called tagged union
- Sets are explicitly split with a "Tag" or "Discriminator"

Especially useful if combined with TypeScripts control flow analysis

Example of using Discriminated Unions

```
type InitAction = { type: "INIT" }
type LoginAction = { type: "LOGIN", name: string, password: string }
type Actions = InitAction | LoginAction;
                                                             Property "name"
function handleAction(action: Actions) {
 switch (action.type) {
                                                               can be safely
   case "INIT":
                                                               accessed here
     return "Initialized";
   case "LOGIN":
     console.log(action.name + " logged in");
     return "Logged In"
   default:
     console.log("WTF");
```

Exhaustiveness Checking

We often have types that cover several cases

What if you can guarantee that you cover them all?

- Benefits:
 - Cut down bugs
 - Make extending functionality easier

Example of using Discriminated Unions

```
type InitAction = { type: "INIT" }
type LoginAction = { type: "LOGIN", name: string, password: string }
type LogOutAction = { type: "LOGOUT" }
type Actions = InitAction | LoginAction | LogOutAction;
function handleAction(action: Actions) {
                                                                   We don't
  switch (action.type) {
    case "INIT":
                                                               handle all cases
      return "Initialized";
    case "LOGIN":
                                                                  anymore!
      console.log(action.name + " logged in");
      return "Logged In"
    default:
      console.log("WTF");
```

Example of using Discriminated Unions

```
type InitAction = { type: "INIT" }
type LoginAction = { type: "LOGIN", name: string, password: string }
type LogOutAction = { type: "LOGOUT" }
type Actions = InitAction | LoginAction | LogOutAction;
function handleAction2(action: Actions): string {
 switch (action.type) {
   case "INIT":
     return "Initialized";
   case "LOGIN":
     console.log(action.name + " logged in");
     return "Logged In"
   default:
     console.log("WTF");
```

Compiler complains: Function returns string | undefined

Another Example of using Union Types

```
type InitAction = { type: "INIT" } ...
type Actions = InitAction | LoginAction | LogOutAction;
function assertNever(x: never): never {
 throw new Error("Unexpected object: " + x);
function exhaustiveHandleAction(action: Actions) {
 switch (action.type) {
   case "INIT":
     return "Initialized";
   case "LOGIN":
     console.log(action.name + " logged in");
     return "Logged In"
   default:
     return assertNever(action);
```

The compiler complains if it ever reaches this point

Algebraic Data Types

Algebraic data types

Algebraic data types (ADTs) are composite types with algebraic properties

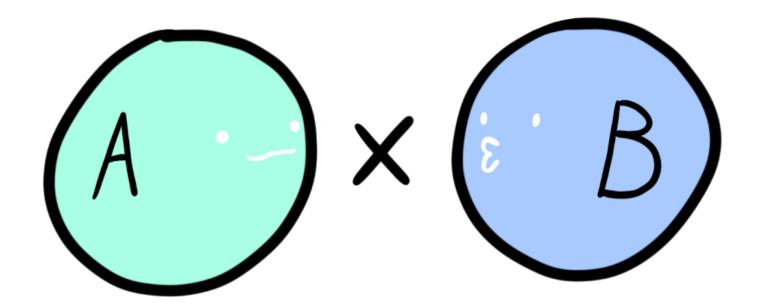
Most common classes: Products and Sums

- We want:
 - Type Checking
 - Exhaustivity

Product Types

- Is equal to the carthesian product of sets
- Can be modelled as a Tuple: let p: [number, boolean] = [5, true];
- Or, more explicit, as an object with two properties:

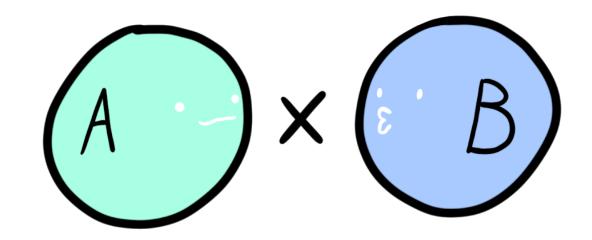
```
type Product<A, B> = { fst: A, snd: B };
let prod: Product<number, boolean> = { fst: 5, snd: true };
```



Product Types

- Why «Product»?
- Try counting the inhabitants

$$|[A,B]| = |A| \times |B|$$



Product Types

Does other algebra apply?

Commutativity: $A \times B = B \times A$

```
let p1: [A, B] = ["A", "B"];
let p2: [B, A] = ["B", "A"];
const swap = ([x, y]) => [y, x];
```

Associativity: $(A \times B) \times C = A \times (B \times C)$

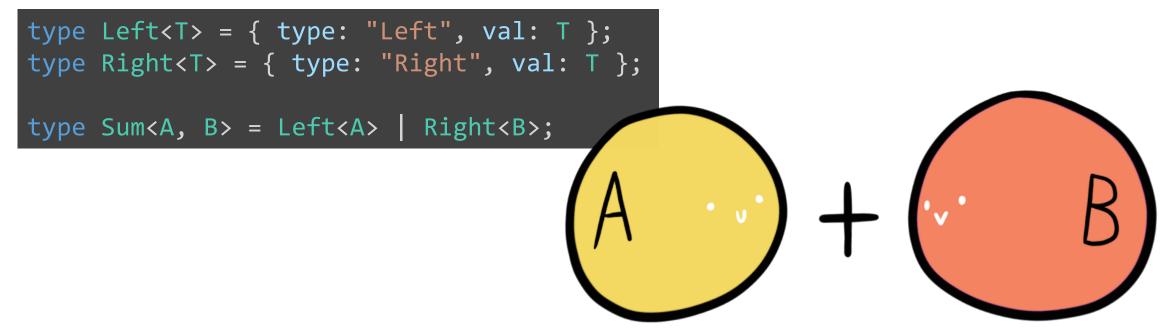
```
let p2: [A, [B, C]] = ["A", ["B", "C"]];
let p3: [[A, B], C] = [["A", "B"], "C"];
```

Neutral-Element: $A \times 1 = A$

```
let p4 = ["A", null];
const rho = ([a, _]: [any, null]) => a;
const rho_inv = (a: any) => [a, null];
```

Sum Types

- Sum types aren't a native language feature of TS
- But they can be built with discriminated unions



The sum type is also known as «Either»

```
type Either<A, B> = Sum<A, B>;
```

Type Algebra: Commutativity

```
(A \times (B + C))
= (A \times B) + (A \times C)
```

```
type X < A, B, C > = [A, Either < B, C >];
type Y<A, B, C> = Either<[A, B], [A, C]>
function prodToSumA, B, C>([x, y]: [A, EitherAB, C>]): EitherA[A, B], [A, C]> {
 if (e.type === "Left") {
   return { type: "Left", val: [x, y.val] }
 } else {
   return { type: "Right", val: [x, y.val] }
function sumToProd<A, B, C>(x: Either<[A, B], [A, C]>): [A, Either<B, C>] {
 if (x.type === "Left") {
   return [x.val[0], { type: "Left", val: y.val[1] }]
 } else {
   return [x.val[0], { type: "Right", val: y.val[1] }]
```

Type Algebra

Numbers	Types
0	Never
1	undefined, null, «foo»
a + b	Either <a, b=""> = Left<a> Right</a,>
a x b	[A, B], Product <a, b=""> = [A, B]</a,>
2 = 1 + 1	type bool = True False
1 + a	Optional <a> = «nothing» Some<a>

Logic	Types
False	never
True	undefined, null, «foo»
a b	Either <a, b=""> = Left<a> Right</a,>
a && b	[A, B], Product <a, <math="">B> = $[A, B]$</a,>

Applications

Many common data structures can be modelled as ADTs

```
type List<T> = { head: T, tail: List<T> };
```

```
type Leaf<T> = { kind: "leaf", value: T };
type Node<T> = { kind: "node", element: T, left: Tree<T>, right: Tree<T> };
type Tree<T> = Leaf<T> | Node<T>;
```

Example: Query Service

```
type Found<T> = { status: "Found", value: T };
type NotFound = { status: "Not Found" };
type Error = { status: "Error", message: string };
type QueryResult<T> = Found<T> | NotFound | Error;

function query<T>(sql: string): QueryResult<T> {
    // ...
}
```

Example: Query Service

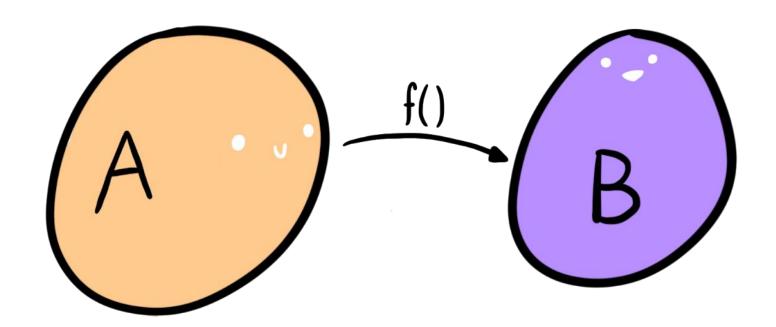
```
function handleResult<T, U>(
  result: QueryResult<T>,
  found: (r: Found<T>) => U,
  notFound: (r: NotFound) => U,
  switch (result.status) {
    case "Found":
      return found(result);
    case "Not Found":
      return notFound(result);
    case "Error":
      return printError(result.message);
    default:
      assertNever(result);
```

Example: Query Service

```
function handleResult<T, U>(
  result: QueryResult<T>,
 found: (r: Found<T>) => U,
 notFound: (r: NotFound) => U,
) { ... }
function getPetNames(personName: number): string[] | undefined {
  return handleResult(
    query<Person>(`Select * FROM Person WHERE name = ${personName}`),
    foundPersonResult => handleResult(
      query<Pet[]>(`Select * FROM Pet WHERE ownerId = ${foundPersonResult.value.id}`),
      foundPetResult => foundPetResult.value.map(pet => pet.name),
      _ => [],
      => [],
```

Bonus round: Set of Functions

- Function Types are also ADTs
- $f(A) \Rightarrow B = B^A$
- Functions are Exponentials



Bonus round: Set of Functions

Sum
$$\langle A, B \rangle \Rightarrow C$$

= C^{A+B}
= $C^A \times C^B$
= $(A \Rightarrow C, B \Rightarrow C)$

$$(A,B) \Rightarrow C$$

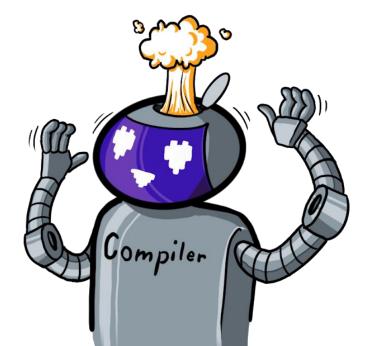
$$= C^{A \times B}$$

$$= (C^A)^B$$

$$= A \Rightarrow (B \Rightarrow C)$$

Conclusion

 We have a powerful, functional-language-level type system built into JavaScript, one of the most used, handiest languages of our time





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Reading List

https://www.typescriptlang.org/docs/handbook/advanced-types.html

 https://bartoszmilewski.com/2014/10/28/category-theory-forprogrammers-the-preface/

 Git repository of this presentation incl. code samples: https://github.com/ymekesser/a-type-of-magic-presentation