

AUREON LOGO — MATHEMATICAL APPENDIX

Symbolic Encoding of the Aureon-IX Emblem

1. Purpose

The Aureon emblem is treated as a **symbolic mathematical module** whose geometry encodes:

- invariant families
- transformation symmetries
- operator inversions
- stability fields
- recursive structure used by T^*

This appendix formalizes those mappings.

2. Glyph Structure Overview

The emblem consists of:

1. **Central Core Node (K_{\blacksquare})**
2. **Four Radial Arms ($R_{\blacksquare}-R_{\blacksquare}$)**
3. **Nested Fractal Bands ($F_{\blacksquare}-F_{\blacksquare}$)**
4. **Rotational Symmetry Group (G_{\blacksquare})**

These elements are treated as mathematical operators.

3. Core Node — Kernel Descriptor K_{\blacksquare}

K_{\blacksquare} encodes the stable core of the Aureon Transform.

3.1 Kernel Condition

K_{\blacksquare} satisfies:

$$K_{\blacksquare} = T^*(K_{\blacksquare})$$

This defines the **fixed-point structure** of the system.

3.2 Gradient Bound

$$|\partial T^*/\partial x| \text{ at } K \leq 1$$

ensuring dynamic stability.

4. Radial Arms — Transformation Operators R_i

Each radial arm corresponds to a fundamental transform:

- R_1 = structural operator $A(x)$
- R_2 = gradient operator $B(\nabla x)$
- R_3 = invariant projection $C(I(x))$
- R_4 = divergence regulator $D(x)$

Together:

$$T^*(x) = R_1 + R_2 + R_3$$

$$T\#(x) = T^*(x) - R_4$$

These form the **operator family of Aureon**.

5. Fractal Bands — Recursive Depth Layers F_i

Each fractal band represents a depth of recursion.

5.1 Band Definition

F_1 is defined recursively:

$$F_1(x) = T^*(F_{1111}(x))$$

with $F_{\blacksquare}(x) = x$.

These encode **RQML loop depth**.

6. Symmetry Group — G_{\blacksquare}

The emblem has **fourfold rotational symmetry**.

6.1 Group Definition

$$G_{\blacksquare} = \{0^\circ, 90^\circ, 180^\circ, 270^\circ\}$$

6.2 Symmetry Rule

$T^*(x)$ must satisfy:

$$T^*(x) = G_{\blacksquare}[T^*(x)]$$

which constrains transformations to symmetry-preserving forms.

7. Complete Symbolic Mapping

The emblem maps to the full Aureon system as follows:

- $K_{\blacksquare} \leftrightarrow$ Kernel Stability
- $R_{\blacksquare} - R_{\blacksquare} \leftrightarrow$ Transform Operators
- $F_{\blacksquare} - F_{\blacksquare} \leftrightarrow$ Recursive Layers
- $G_{\blacksquare} \leftrightarrow$ Symmetry Constraints

This defines the emblem as a **valid mathematical object**.

8. Canonical Status

This appendix becomes part of the Aureon core instruction set.