

Data Analysis

We will use DAVE Mslice to visualize and analyze the data.

Steps:

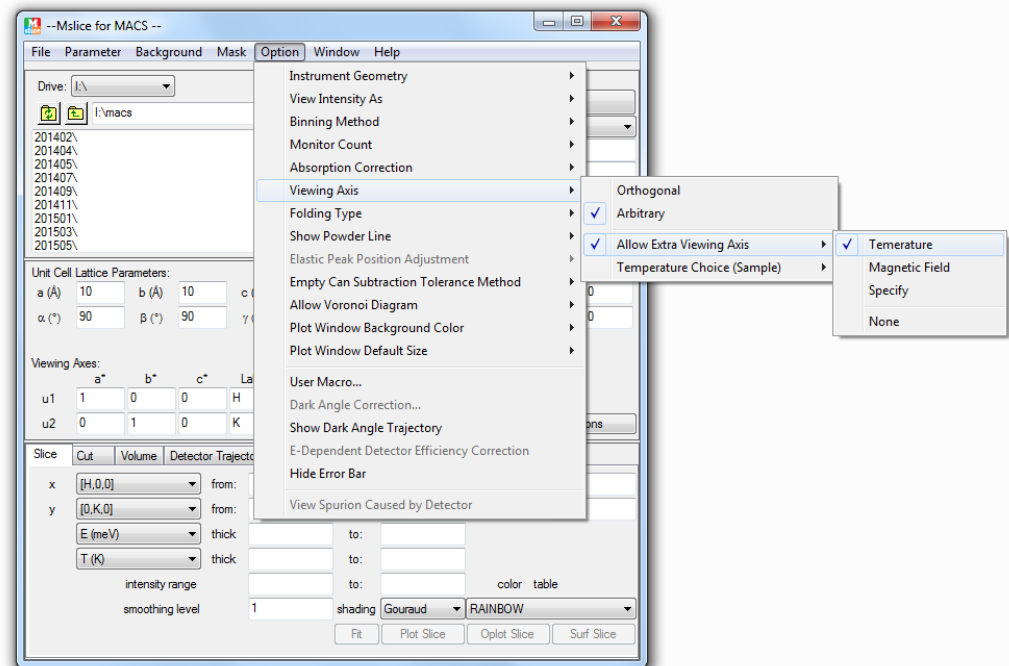
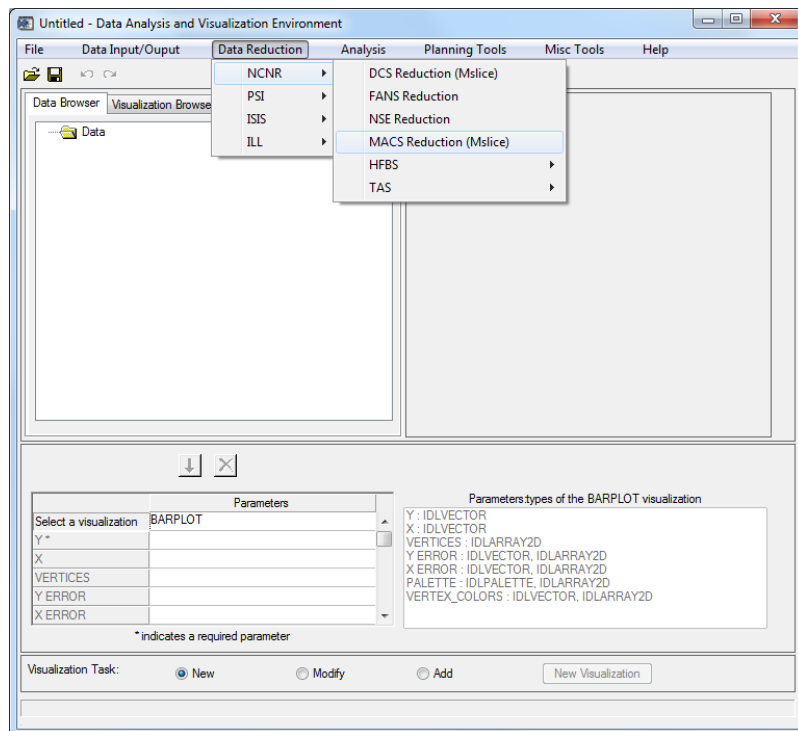
- Start DAVE Mslice.
- Load and plot constant E data.
- Load data and plot H vs E dispersion slice.
- Figure out J and overplot the dispersion curve.
- Plot $\chi''T$ vs $\hbar\omega/k_B T$ at $\tilde{q}=\pi(H=0.5)$.
- Fit to the scaling function.

$$\chi''(\tilde{q} = \pi, \omega) = \frac{\pi}{T} \text{Im} \left[\rho^2 \left(\frac{\hbar\omega}{4\pi k_B T} \right) \right]$$

$$\rho(x) = \frac{\Gamma\left(\frac{1}{4} - ix\right)}{\Gamma\left(\frac{3}{4} - ix\right)}$$

DAVE Mslice

- DAVE->Data Reduction->NCNR->MACS Reduction (Mslice)
- Mslice->Option->View Intensity As->S(Q,omega)
- Mslice->Option->Viewing Axis->Allow Extra Viewing Axis->Temperature



Data Files

- Use the NCNR ftp directory in mslice to remotely load data files. For windows computer, the ftp directory is <ftp://ncnr.nist.gov> in the drive list. For Mac computers, the ftp directory is in the **NCNR_ftp** directory in the root directory.
- Or download the files from the ftp site to you computer and view them locally. You can use the tool in the mslice menu **File->File Tools->Copy Files from NCNR FTP Server** to download the files.
- File list:

Constant-E A3 scan files:

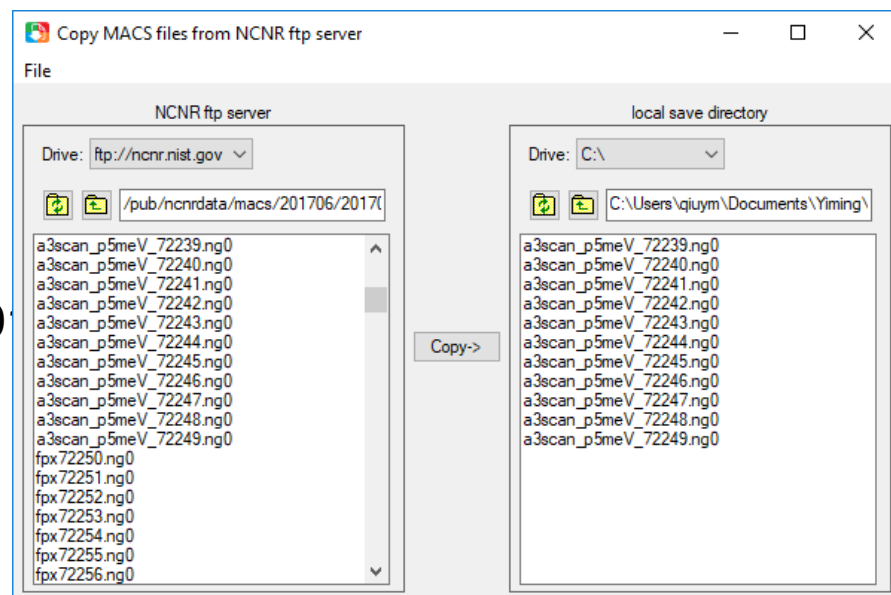
macs/201706/20170619/data
72239-72249

Dispersion data files: macs/201304/20

Low-T: fpx17722-fpx17879

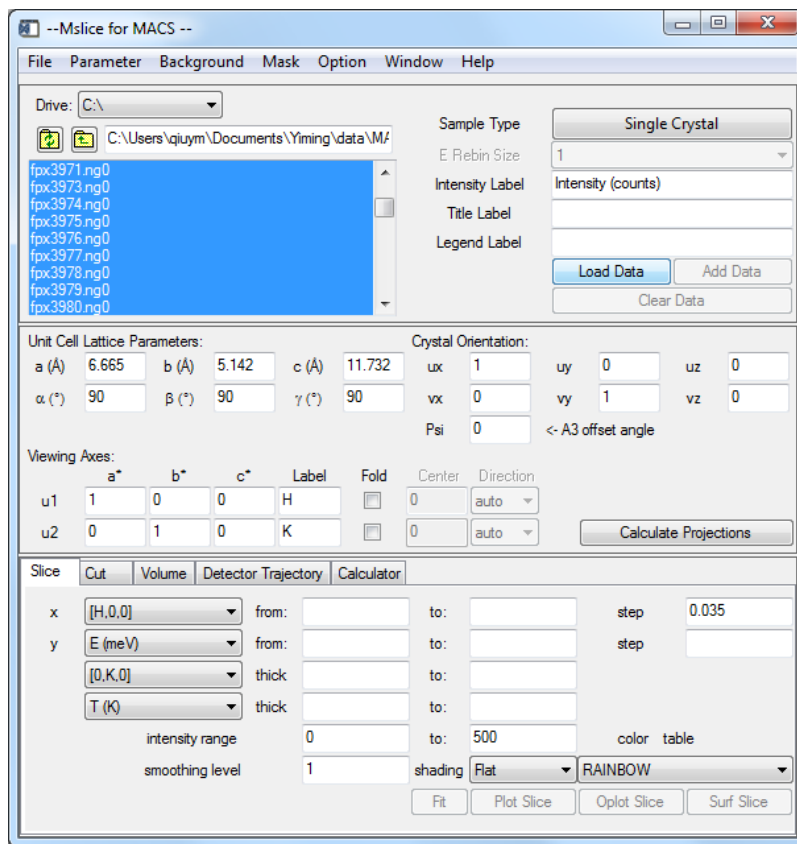
High-T: fpx18314-fpx18397

Empty can: fpx18023-fpx18100



Load Data

- Choose the data files in the file list panel. Right click to view file info. Press **Load Data** button. Press **Add Data** button to append data.
- For background files, choose them in the file list, then in the background menu, click **Load Empty Can File(s)**.



Constant-E A3 scan files:
 macs/201706/20170619/data
 72239-72249

Dispersion data files:
 macs/201304/20130425/data/
 Low-T: fpx17722-fpx17879
 High-T: fpx18314-fpx18397
 Empty can: fpx18023-fpx18100

Plot Constant-E Slice

- Load a3 scan files 72239-72249
- Make sure $u1=(1,0,0)$ and $u2=(0,1,0)$. Press **Calculate Projections** button.
- In the slice panel, choose $[H,0,0]$ as x axis, step 0.035, and $[0,K,0]$ as y axis, step 0.035. Press Plot Slice button to plot the H vs K contour plot.
- Keep the plot window.

--Mslice for MACS --

File Parameter Background Mask Option Window Help

Drive: C:\

C:\Users\qium\Documents\Yiming\work\Su

Sample Type: Single Crystal

Monitor Count: Automatic (3e4)

Intensity Label: Intensity (mon=3e4)

Title Label:

Legend Label:

PTAI Only: ☐

Load Data Add Data

Clear Data

Unit Cell Lattice Parameters:

a (Å) 6.71633 b (Å) 5.112 c (Å) 11.732

α (°) 90 β (°) 90 γ (°) 90

Crystal Orientation:

ux 0 uy 0 uz 0

vx 0 vy 1 vz 0

Psi 0 <- A3 offset angle

Viewing Axes:

	a*	b*	c*	Label	Fold	Center	Direction
u1	1	0	0	H	<input type="checkbox"/>	0	auto
u2	0	1	0	K	<input type="checkbox"/>	0	auto

Calculate Projections

Slice Cut Volume Detector Trajectory Calculator

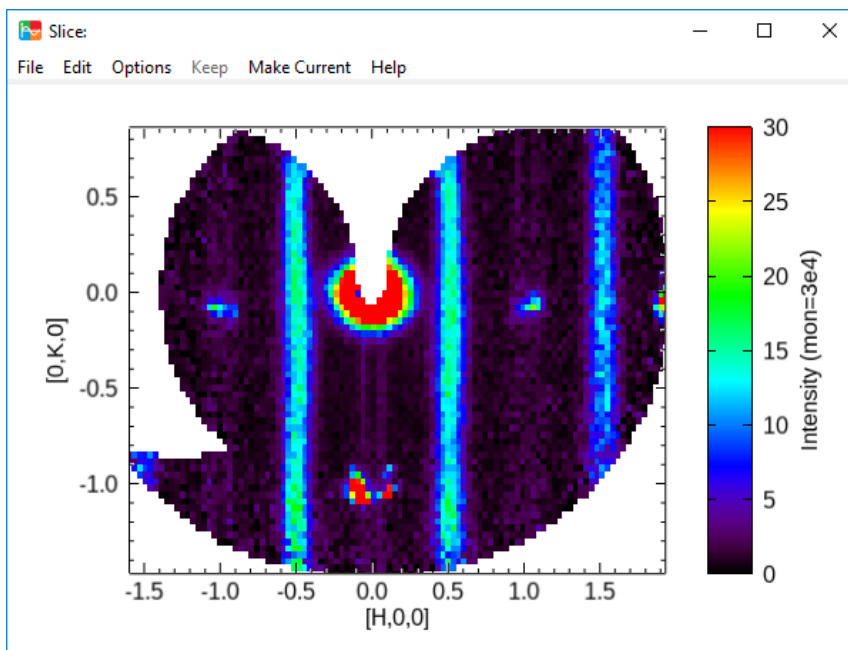
	Cut	Volume	Detector Trajectory	Calculator
x	[H,0,0]	from:	to:	step 0.035
y	[0,K,0]	from:	to:	step 0.035
E (meV)		thick	to:	
T (K)		thick	to:	

intensity range:

smoothing level: 0

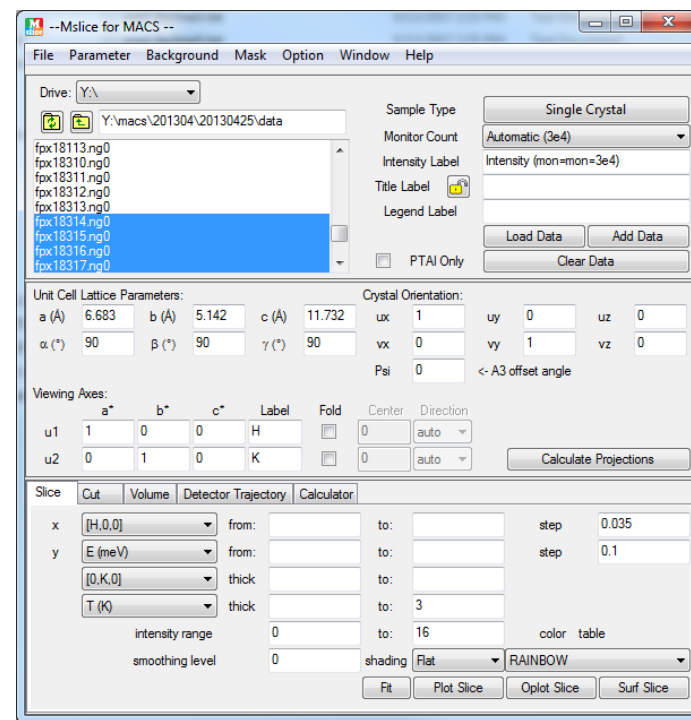
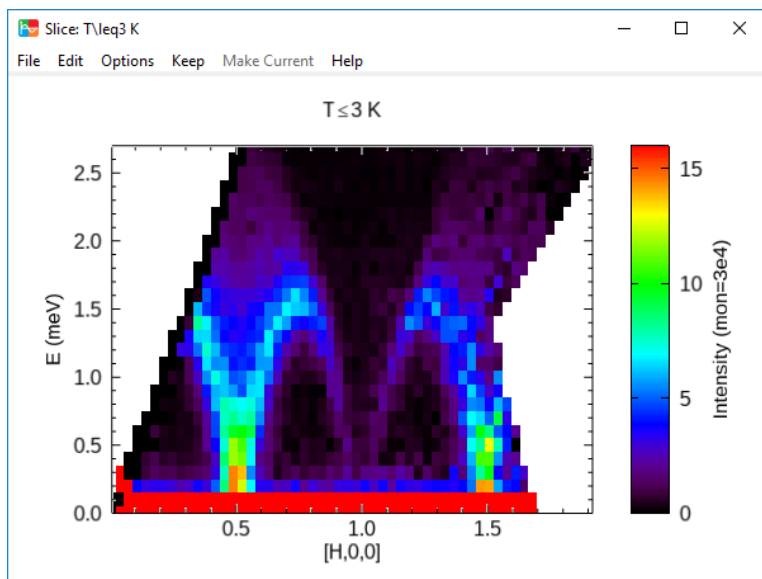
shading Flat RAINBOW

Fit Plot Slice Oplot Slice Surf Slice



Plot H vs E dispersion Slice

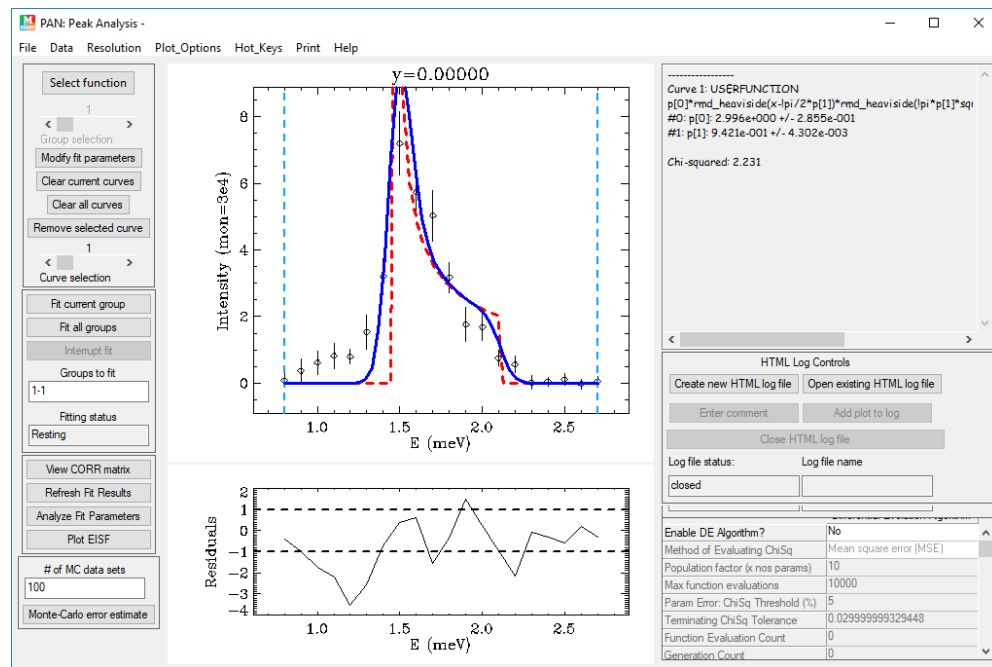
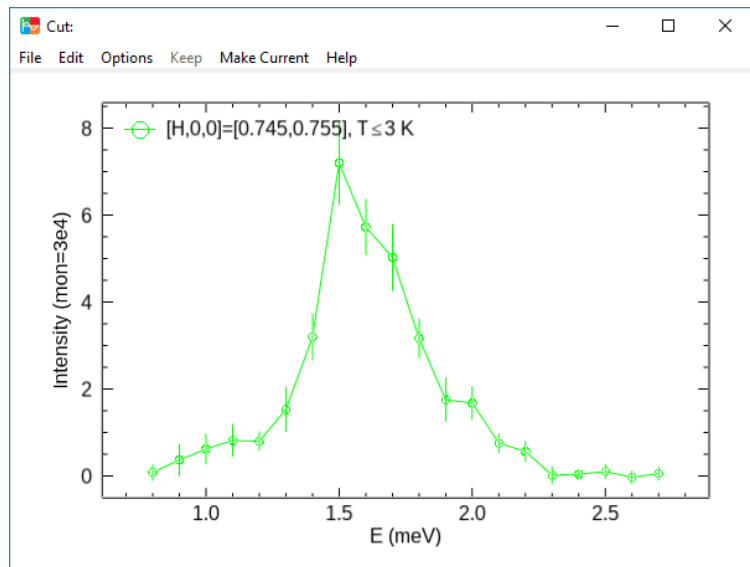
- Load low-T (17722-17879) and high-T (18314-18397) data files. Load empty can files (18023-18100) as background.
- Disable the monitor lambda/2 correction in the **Option** menu. Calculate projection. Increase the empty can subtraction tolerance in the **Parameter** menu to 0.015 for energy and 0.15 for kidney.
- In the slice panel, choose [H,0,0] as x axis, step 0.035, and E as y axis, step **0.1**. Specify the temperature range. Press **Plot Slice** button to plot the H vs E contour plot.
- Keep the plot window.



Plot & Fit Cut

- Make a cut along E, with [H,0,0] thickness range of [0.745,0.755] and $T < 3$ K. x range starts from 0.79, step 0.1.
- Keep the plot window.
- Press Fit button in the Cut panel to fit the data. Use Müller Ansatz equ. as the user function (in one line, initial $p[0]=3$, $p[1]=0.9$):

$$p[0] * \text{rmd_heaviside}(x - !\pi/2 * p[1]) * \text{rmd_heaviside}(!\pi * p[1] * \sqrt{2}/2 - x) / \sqrt{\text{abs}(x^2 - 0.25 * (!\pi * p[1])^2)}$$
- Load pre-generated resolution data from [Resolution->Load ASCII Res File](#).



Quantum spin dynamics of the antiferromagnetic linear chain in zero and nonzero magnetic field

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Applying the sum rules (1.38), (1.42), and (1.45) to our analytic expression (1.16) for the dynamic correlation function of the HB AF

$$S_{\pm\pm}(q, \omega) = \frac{A}{(\omega^2 - \frac{1}{4}\pi^2 J^2 \sin^2 q)^{1/2}} \Theta\left(\omega - \frac{\pi}{2} J \sin q\right) \\ \times \Theta\left[\pi J \sin\left(\frac{q}{2}\right) - \omega\right] \quad (1.48)$$

where $\Theta(x)$ is the step function.

- Add a line to the plot from **Edit->Add Line** :

```
p=[2.996, 0.9421] & y = gauss_smooth(p[0]*rmd_heaviside(x-!pi/2*p[1])*
rmd_heaviside(!pi*p[1]*sqrt(2)/2-x)/sqrt(abs(x^2-0.25*(!pi*p[1])^2)),
0.15/(x[1]-x[0])/sqrt(8.*alog(2)))
```

Add line

formula:

p=[2.996,0.9421] & y = ga

x_start:

0.610059

x_end:

2.8893533

of points:

101

line style:

solid

color:

red

thickness:

2

legend:

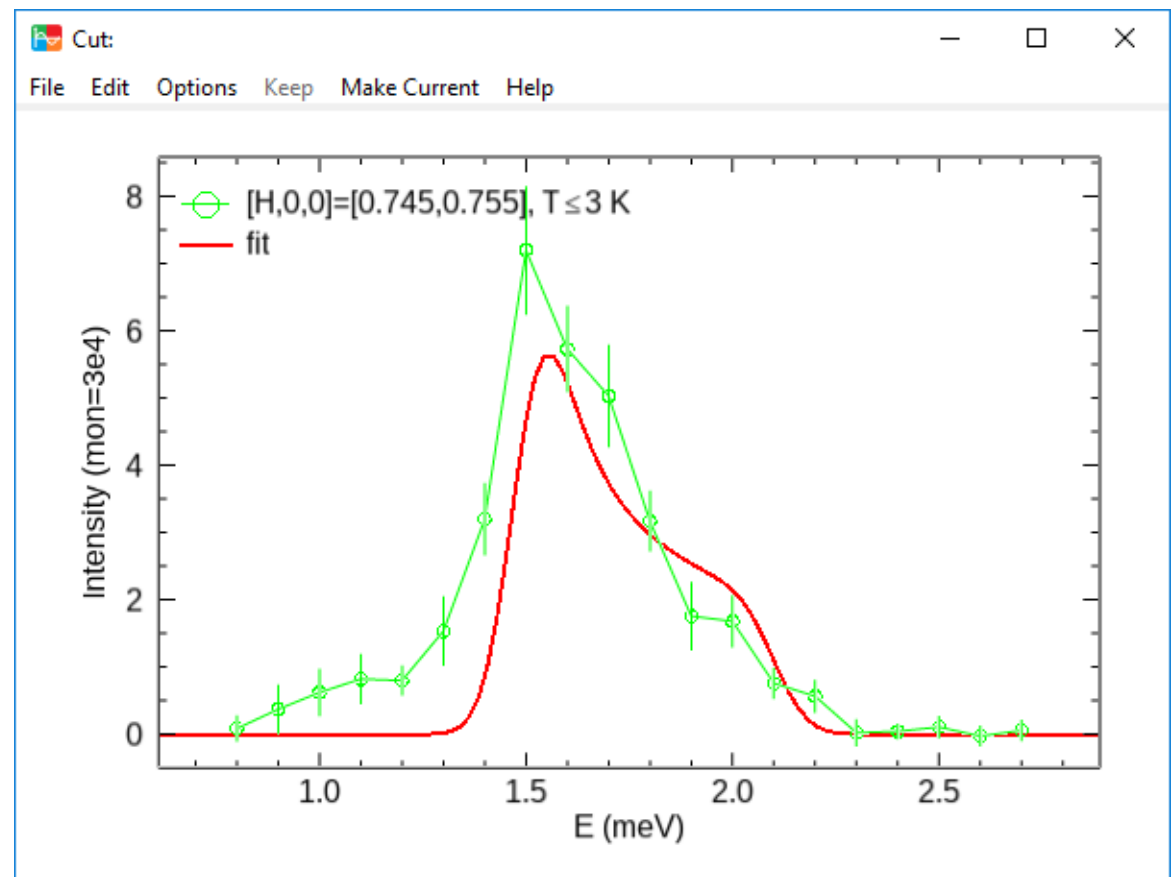
fit

The formula must be a valid IDL expression, for example:
y=x^2+sin(x)
Use & to combine multiple statements in one line.

Clear

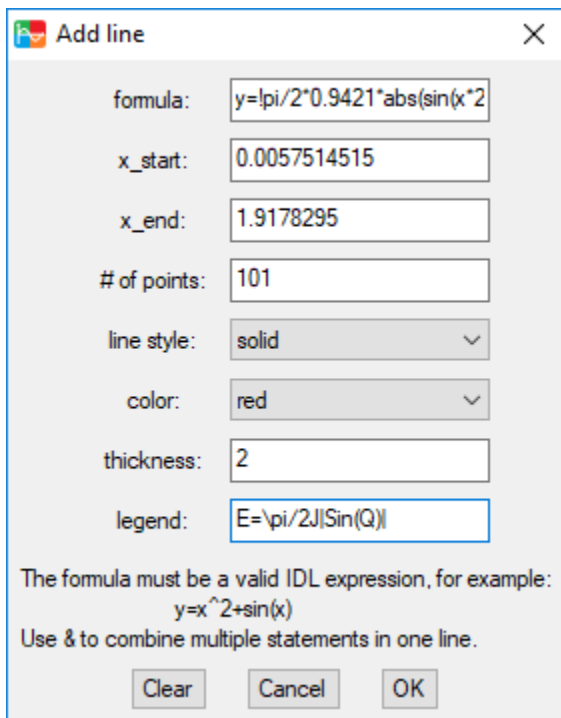
Cancel

OK



Overplot the Dispersion Curve

- Overplot the lower and upper bound of the continuum in the H vs E window from [Edit->Add Line](#). The formula for the lower bound is $y = \pi/2 * 0.9421 * \text{abs}(\sin(x * \pi))$. Use $E = \pi/2 J |\sin(Q)|$ as legend. The formula for the upper bound is $y = \pi * 0.9421 * \text{abs}(\sin(x * \pi))$. Use $E = \pi J |\sin(Q/2)|$ as legend.



Add line

formula:

x_start:

x_end:

of points:

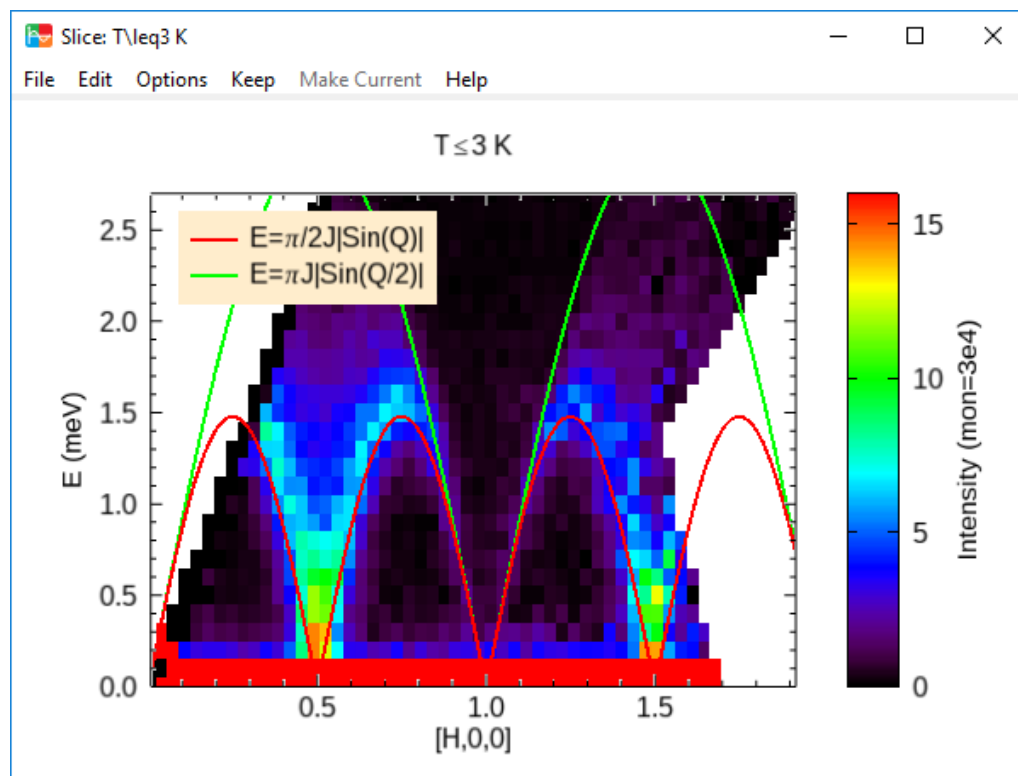
line style:

color:

thickness:

legend:

The formula must be a valid IDL expression, for example:
 $y = x^2 + \sin(x)$
 Use & to combine multiple statements in one line.



Plot $\chi''T$ vs $\hbar\omega/k_B T$

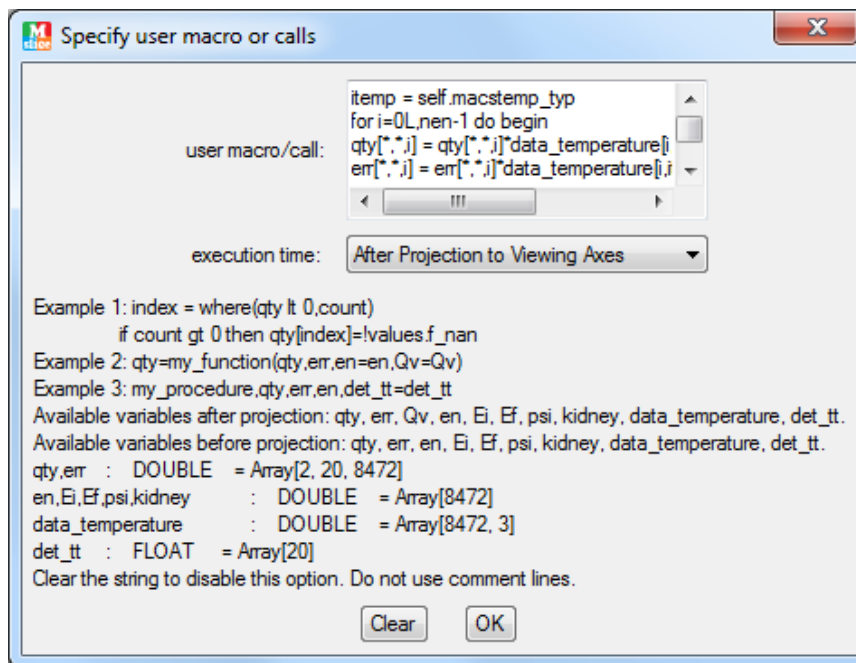
- In mslice menu **Option->User Macro**, enter the following script:

```

itemp = self.macstemp_typ
for i=0L,nen-1 do begin
    qty[*,*,i] = qty[*,*,i]*data_temperature[i,itemp]
    err[*,*,i] = err[*,*,i]*data_temperature[i,itemp]
endfor
data_temperature[*,itemp] = en/(kb*data_temperature[*,itemp])

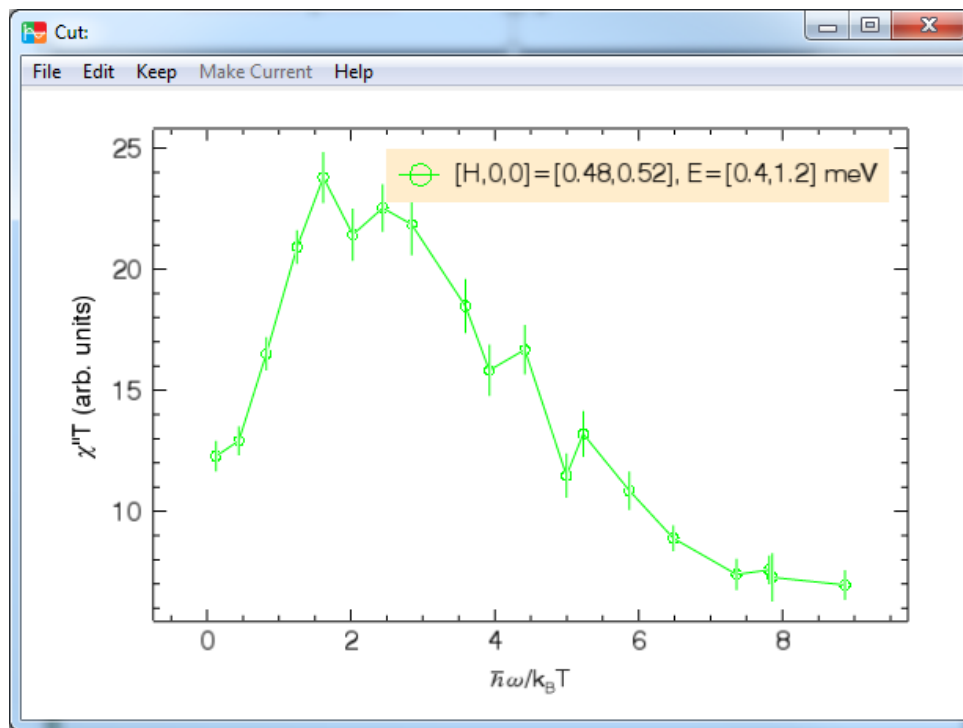
```

- Choose the execution time to be **After Projection to Viewing Axes**.



Plot $\chi''T$ vs $\hbar\omega/k_B T$

- Choose Option->View Intensity As-> Chi(Q,omega)
- Recalculate the projection.
- In the cut panel, cut along T, which is $E/k_B T$ now, step 0.4.
Set H thickness range [0.48,0.52], and E thickness range [0.4,1.2].
- Plot cut. In the plot window, change the x-axis title to $\hbar\omega/k_B T$, and y-axis title to $\chi''T$ (arb. units).

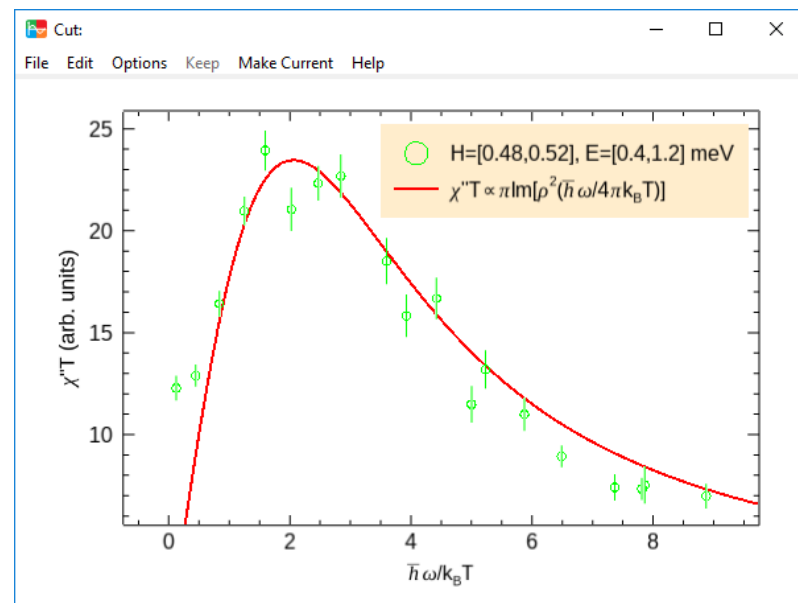
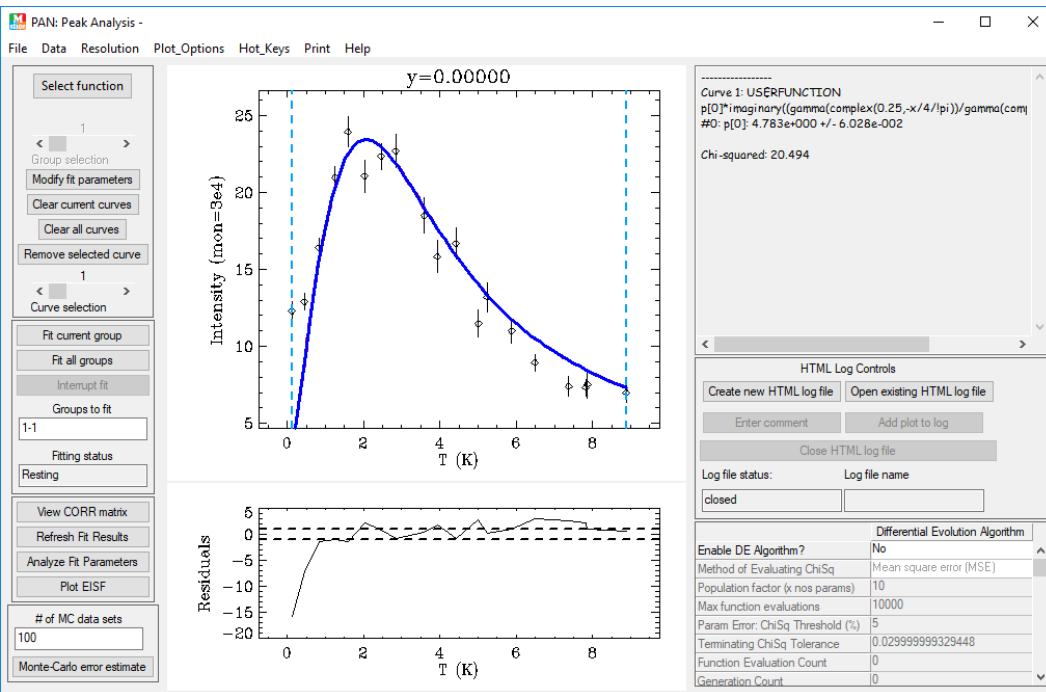


Fit to Scaling Function

- Press Fit button. In PAN, choose user function as the fitting function:

$$p[0] * \text{imaginary} \left(\frac{\gamma(\text{complex}(0.25, -x/4/\pi))}{\gamma(\text{complex}(0.75, -x/4/\pi))} \right)^2$$
- Add a line of the scaling function to the previous $\chi''T$ vs $\hbar\omega/k_B T$ plot.

$$y = 4.783 * \text{imaginary} \left(\frac{\gamma(\text{complex}(0.25, -x/4/\pi))}{\gamma(\text{complex}(0.75, -x/4/\pi))} \right)^2$$
with $\backslash \chi''T \propto \pi \text{Im}[\rho^2(\hbar\omega/4\pi k_B T)]$ as legend.



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Subject Categories: Magnetic materials | Computation, modelling and theory

Quantum criticality and universal scaling of a quantum antiferromagnet

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that at the antiferromagnetic zone centre (AFZC) $q_{\text{AFZC}} = \pi/c$, the dynamical structure factor is given by

$$S(\pi, E) = \frac{e^{E/kT}}{e^{E/kT} - 1} \frac{A}{T} \text{Im} \left[\rho \left(\frac{E}{4\pi T} \right)^2 \right] \quad (3)$$

where $\rho(x) = \Gamma(1/4 - ix)/\Gamma(3/4 - ix)$ and A is a constant¹⁶. It is clear from this equation that the structure factor multiplied by temperature depends only on the dimensionless ratio of E to T rather than on these quantities separately, and therefore obeys universal scaling. The ideal