§ 4. Compactifications of 6d (20) SCFT's

We want to look at compactifications on Riemann surfaces to 4d N=1 theories

Yet us review some facts about 4d W=1 SCFT's: • B-function:

where M is the energy scale, to T_r and T_r b = $T_2(r_i)$ 8 ab. quadratic Casimir $Y(g_p)$: anomalous dimension of Φ ; sum is over matter fields normalization: $T_2(\square) = \frac{1}{2}$, $T_2(ad_p) = N$

· chiral primary operator O with dimension D[O] has R-charge

$$R[O] = \frac{1}{3}D[O] = \frac{1}{3}\left(D_{uv}[G] + \frac{Y[O]}{2}\right)$$

Consider a non-Tagrangian theory which has a flavor symmetry with current superfield Ja I 2 Sd40 Ja Va + (terms for gauge invariance)

 J^a is a real linear superfield: $D^2 J^a = \overline{D}^2 J^a = 0$ containing j^a

OPE: $j_{n}^{q}(x) j_{n}^{b}(0) = \frac{3k_{G}}{4\pi^{4}} S^{ab} \frac{x^{2}g_{nv} - 1x_{n}x_{v}}{x^{6}} + \frac{1}{\pi^{2}} f^{abc} \frac{x_{n}x_{v} \times f^{c}(0)}{x^{6}}$

KG is called central charge of the flavor sym.

In free chiral multiplets have Ku(n) = 1

For GCU(n) we have

$$k_G = 2 \sum T_2(v_i)$$

where $u = \sum_{i} r_{i}$

For GCH: KGCH= IGCSHKH
weakly
ganged flavor embedding index

A-function receives contributions of one-loop and higher-loop:

Define

Examples:

R-symmetry of N=2 SCFT:
$$SU(2) \times U(1)$$
 and R-sym. of N=1 SCFT:

$$R_{N=1} = \frac{1}{3}R_{N=2} + \frac{4}{3}I_{3}$$

$$U(i)_{R} \qquad \text{Cartan of SU(2)}_{R}$$

for any flavor sym. G Setting $K = K_G/2 \longrightarrow \text{exact } / \text{-function for}$ N=1 stops at one-loop

· Argyres-Seiberg theory: consider SU(1) N=2 gange theory with

one hypermultiplet

Take Su(1) C Es flavor of Minaham-Nemeshansky SCFT

 $\neg \beta = \exists T_1(adj) + \exists \sum_i R_i T_2(r_i) - \frac{\kappa_6}{2}$ Tuse $T_2(su(2)) = 2$ $T_2(\square) = \frac{1}{2}$

 $K_{E_6} = 6 , I_{S4(2)} c_{5}E_{6} = 1$

=3.2-1-3=0

consider 54(2) C E 2 MN SCFT (KSu(2) = =8)

-2/5 = 3.2 - 2 - 4 = 0

· Mass deformed Argyres-Seiberg theory add SW=m &2, where & is chiral

superfield inside
$$W=1$$
 VM

$$-3 R_{IR} = \frac{1}{2} R_{W=2} + I_3 = \frac{3}{2} R_{W=1} - I_3$$

$$K = \frac{3}{4} K_G$$

$$-3 S - function of SU(2) is$$

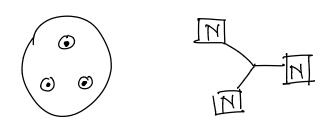
$$S = 3 \cdot 2 - \frac{3}{2} - \frac{3}{4} \cdot 6 = 6$$

TN theory

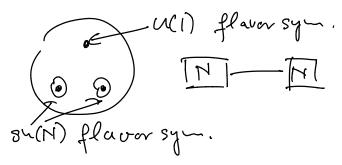
This is an N=2 SCFT with no marginal couplings and flavor sym. > SU(N)3

- . To is the theory of eight free chiral multiplets Qijk
- . To is MN SCFT

To theory is obtained by wrapping N M5-branes on a sphere with I maximal punctures



By comparison, a bifundamental of $SU(N) \times SU(N)$ arises by wrapping N M5-branes on sphere with 2 maximal punctures and I simple puncture:



The theory can be used as "building blocks" by ganging their flavor symmetries;