

# Improving Adversarial Robustness for Recommendation Model via Cross-Domain Distributional Adversarial Training

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## ABSTRACT

Recommendation models based on deep learning are fragile when facing adversarial examples (AE). Adversarial training (AT) is the existing mainstream method to promote the adversarial robustness of recommendation models. However, these AT methods often have two drawbacks. First, they may be ineffective due to the ubiquitous sparsity of interaction data. Second, point-wise perturbation used by these AT methods leads to suboptimal adversarial robustness, because not all examples are equally susceptible to such perturbations. To overcome these issues, we propose a novel method called *Cross-domain Distributional Adversarial Training* (CDAT) which utilizes a richer auxiliary domain to improve the adversarial robustness of a sparse target domain. CDAT comprises a *Domain adversarial network* (Dan) and a *Cross-domain adversarial example generative network* (Cdan). Dan learns a domain-invariant preference distribution which is obtained by aligning user embeddings from two domains and paves the way to leverage the knowledge from another domain for the target domain. Then, by adversarially perturbing the domain-invariant preference distribution under the guidance of a discriminator, Cdan captures an aggressive and imperceptible AE distribution. In this way, CDAT can transfer distributional adversarial robustness from the auxiliary domain to the target domain. The extensive experiments conducted on real datasets demonstrate the remarkable superiority of the proposed CDAT in improving the adversarial robustness of the sparse domain. The codes and datasets are available on <https://github.com/HymanLoveGIN/CDAT>.

## CCS CONCEPTS

- Information systems → Recommender systems;

## KEYWORDS

Cross-Domain Recommendation, Adversarial Robustness, Adversarial Training

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## 1 INTRODUCTION

Deep learning-based recommendation models are widely deployed on online service platforms to deliver tailored recommendations to users. But, these models are vulnerable to adversarial attacks when facing with adversarial examples (AE) [9, 27]. AE is a form of input data that has been meticulously designed to introduce minor yet purposeful perturbations to the original input samples, which can lead to diminished recommendation performance. Therefore, the improvement of adversarial robustness in recommendation models, namely, the ability to defend against AE, has become a focal point of interest for researchers. Adversarial training (AT) [1, 5, 10, 28, 33–35] is the predominant method for enhancing the adversarial robustness of recommendation models, which dynamically generates AEs and integrates them into the training process, equipping recommendation models with adversarial robustness. However, it still faces the following challenges.

Substantial data are needed for AT of a model, otherwise, the model will be suboptimal in adversarial robustness [23]. This is especially true in recommendation models, where the data sparsity issue is widespread. An effective approach to mitigate this issue is cross-domain recommendation (CDR) [3, 11, 14, 38, 40], which enhances the recommendation performance of the sparse target domain by utilizing the knowledge from another auxiliary domain. However, traditional CDRs focus on transferring the knowledge that can improve the recommendation accuracy, without considering the knowledge benefitting adversarial robustness. On the other hand, to bolster the adversarial robustness of recommendation models, the availability of more powerful AEs is crucial, as they present the models with more formidable attack scenarios. However, prevalent AT methods [10, 34, 36] generally adopt the point-wise perturbation strategy to generate AEs, which ignores the varying susceptibility of the samples to such adversarial attacks, thus yielding suboptimal adversarial robustness [2, 25].

To address the above challenges, we propose a novel AT method called *Cross-domain Distributional Adversarial Training* (CDAT). CDAT encompasses a *Domain adversarial network* (Dan) and a *Cross-domain adversarial example generative network* (Cdan). The Dan focuses on capturing a domain-invariant user preference distribution. Specifically, the Dan includes a domain-invariant preference

encoder and a domain discriminator. This encoder takes all user data from both domains as input and aligns user preference embeddings from the two different domains within the same embedding space with the assistance of the domain discriminator. This alignment results in a domain-invariant preference distribution, thereby paving the way for the target domain to leverage the knowledge from another domain. Cdan consists of a cross-domain adversarial example generator and a cross-domain adversarial example discriminator. The target of the generator is to learn a distribution of *Cross-Domain Adversarial Example* (CDAE) which is imperceptible and possesses strong attack capability. To be specific, the generator takes the domain-invariant preference distribution obtained by Dan as input and then adversarially perturbs it to get the CDAE distribution. To ensure the imperceptibility of CDAEs, the discriminator enforces a constraint on the distance between the CDAE distribution and the domain-invariant preference distribution and the generator minimizes the distance. Concurrently, to guarantee the aggressiveness of CDAEs, CDAEs generated by the generator are fed into the recommenders of both auxiliary and target domains, and the generator is optimized to maximize the recommendation losses. Finally, we can generate jointly perturbed and imperceptible CDAEs from the CDAE distribution for CDAT. And in this manner, the adversarial robustness from the auxiliary domain can be transferred to the sparse target domain.

The main contributions of this paper can be summarized as follows:

- We propose a Cross-domain Distributional Adversarial Training (CDAT) method, which enhances the adversarial robustness of a recommendation model in the sparse target domain by transferring adversarial robustness from the auxiliary domain.
- We propose a Cross-domain Adversarial Example Generative Network (Cdan). This network takes a domain-invariant preference distribution obtained by Dan as input and captures a high-quality CDAE distribution to support CDAT, under the constraint of the cross-domain adversarial example discriminator and the guidance of maximizing the recommendation losses.
- We conduct extensive experiments in three scenarios constructed by two real datasets to verify the effectiveness of CDAT.

## 2 PRELIMINARIES

### 2.1 Base Model

We design a basic recommendation model called base model to combine with CDAT to show its performance. The base model is made up of a preference encoder  $E$  and a recommender  $Rec$  taking lower user embeddings  $\{e_u \in \mathbb{R}^d\}$  and lower item embeddings  $\{e_v \in \mathbb{R}^d\}$  as input, where  $d$  is embedding dimensionality.

**2.1.1 User and Item Embedding.** Let  $\mathcal{U}$  and  $\mathcal{V}$  (of size  $m = |\mathcal{U}|$  and  $n = |\mathcal{V}|$ ) be the sets of users and items, respectively. We use the user one-hot encoding  $x_u \in \{0, 1\}^m$  and the item one-hot encoding  $x_v \in \{0, 1\}^n$  to represent a user  $u \in \mathcal{U}$  and an item  $v \in \mathcal{V}$ , respectively. A user  $u$ 's embedding  $e_u$  will be obtained

with a lookup over a learnable embedding matrix  $W_u \in \mathbb{R}^{d \times m}$ , i.e.,  $e_u = W_u x_u$ . Likewise, we can also obtain an item  $v$ 's embedding  $e_v$  by a lookup over a learnable embedding matrix  $W_v \in \mathbb{R}^{d \times n}$ , i.e.,  $e_v = W_v x_v$ . Furthermore, the preference encoder  $E$  parameterized by  $\theta_E$  will receive a user embedding  $e_u$  as input to gain a user's preference embedding  $z_u$ , which is implemented as a Multi-Layer Perceptron (MLP) with activation function ReLU.

**2.1.2 Interaction Prediction Network.** To predict the probability that a user  $u$  will interact with an item  $v$ , we employ a recommender  $Rec$  with an MLP and a sigmoid function as output:

$$r_{uv} = Rec(z_u \oplus e_v; \theta_{Rec}), \quad (1)$$

where  $\theta_{Rec}$  represents the learnable parameters of  $Rec$  and  $\oplus$  represents concat operation.

To optimize the model, we construct a training dataset  $\mathcal{D} = \{(u, v_+, v_-)\}$ , where  $v_+$  and  $v_-$  denote a positive sample and a negative sample of a user  $u$ , respectively. By applying the popular pair-wise ranking loss of BPR [22, 38], we define the following objective function:

$$\mathcal{L}_{Rec}(\theta_E, \theta_{Rec}) = -\frac{1}{|\mathcal{D}|} \sum_{(u, v_+, v_-) \in \mathcal{D}} \log(r_{uv_+} - r_{uv_-}). \quad (2)$$

## 2.2 Problem Definition

The target problem of this paper is that we want a recommendation model in the sparse target domain  $t$  to learn a set of adversarially robust parameters  $\theta_{Rec}^{(t)}$  which denotes the parameters of the recommender in the target domain  $t$  to defend the adversarial attack with the help of the auxiliary domain  $s$ .

## 2.3 Threat Model

**Attack Capability.** We consider the threat model as an evasion attack model, which attacks the target recommendation model during inference by crafting AEs. Although in the realm of computer vision, these perturbations are typically added to raw data, in the context of recommendation, they are instead applied to the model parameters that underlie the recommendation strategy. Specifically, we focus on the adversarial perturbations introduced to user embeddings.

**Attack Goal.** This threat model belongs to an untargeted attack, which seeks to degrade the overall recommendation performance rather than targeting one user or item.

**Attack Knowledge.** The threat model is regarded as a white-box attack, permitting the method full knowledge of the recommendation model, including its parameters and structures. Although white-box attacks represent an idealized state of attack, they provide the most challenging adversaries for AT, which is beneficial for enhancing the adversarial robustness of the recommendation model.

## 3 METHODOLOGY

### 3.1 Overview

Figure 1 shows the architecture of CDAT, where the solid lines represent the paths activated when training, while the gold solid lines represent the paths activated when applying. CDAT is composed of the Domain adversarial network (Dan) and Cross-domain adversarial example generative network (Cdan).

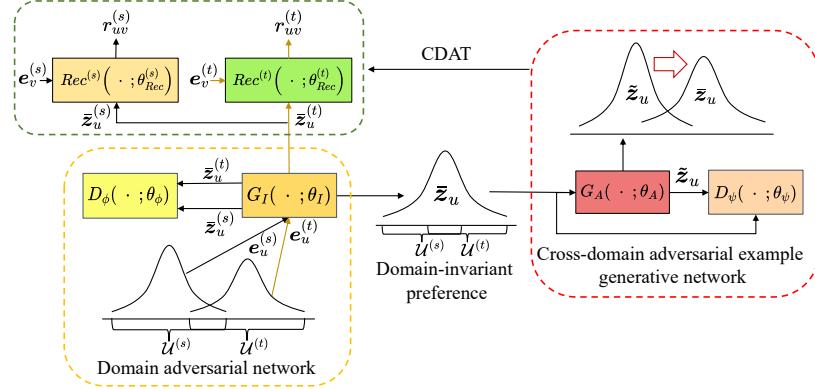


Figure 1: The overview of CDAT.

In Dan, CDAT first transforms the users' one-hot vectors  $\{x_u^{(\tau)}\}$  and the items' one-hot vectors  $\{x_v^{(\tau)}\}$  to their corresponding lower user embeddings  $\{e_u^{(\tau)}\}$  and lower item embeddings  $\{e_v^{(\tau)}\}$  by lookup method. And,  $\tau = \{s, t\}$  where  $s$  and  $t$  denote an auxiliary domain  $s$  and a target domain  $t$ , respectively. To align the users' preference embeddings from two different domains, CDAT lets domain-invariant preference encoder  $G_I$  to capture the distribution  $p_{\theta_I}(\bar{z}_u)$  containing users' domain-invariant preferences by means of domain discriminator, where  $\theta_I$  is the parameters of  $G_I$ . In Cdan, with the domain-invariant preference distribution as input, CDAT utilizes cross-domain adversarial example generator  $G_A$  parameterized by  $\theta_A$  to learn a harmful and imperceptible CDAE distribution  $p_{\theta_A}(\tilde{z}_u)$ .

Lastly, in domain  $t$ , the recommender  $Rec^{(t)}$  predicts the interaction probability  $r_{uv}^{(t)}$  by feeding a user's domain-invariant preference  $\bar{z}_u^{(t)}$  and an item embedding  $e_v^{(t)}$ . At the same time, CDAEs generated by  $G_A$  are also fed into the recommender. Then, we adversarially update the parameters of the recommender to obtain a recommendation model with adversarial robustness in the sparse target domain.

## 3.2 Domain Adversarial Network

Dan is composed of a domain-invariant preference encoder  $G_I$  and a domain discriminator  $D_\phi$ . Inspired by DANN [7], we leverage domain discriminator  $D_\phi$  to help encoder  $G_I$  to learn a users' domain-invariant preference distribution  $p_{\theta_I}(\bar{z}_u)$ , where  $\bar{z}_u \sim p_{\theta_I}(\bar{z}_u)$ , in preparation for further applying the knowledge benefitting AT from the auxiliary domain.

**3.2.1 Domain-invariant Preference Embedding.** Based on a user embedding  $e_u^{(\tau)}$ , we generate the domain-invariant preference  $\bar{z}_u$  by  $G_I$ , as follow:

$$\bar{z}_u = G_I(e_u^{(\tau)}; \theta_I), \tau \in \{s, t\}, \quad (3)$$

where  $\bar{z}_u \in \mathbb{R}^d$  and  $\theta_I$  is the learnable parameters of  $G_I$ .

**3.2.2 Optimization.** To make sure that  $\bar{z}_u$  is domain-invariant, we introduce a domain discriminator  $D_\phi$ , which takes  $\bar{z}_u$  as input. The

loss of the domain discriminator is defined as:

$$\begin{aligned} \mathcal{L}_\phi(\theta_I, \theta_\phi) = & - \left( \mathbb{E}_{\bar{z}_u^{(s)} \sim p_{\theta_I}(\bar{z}_u | e_u^{(s)})} \log(D_\phi(\bar{z}_u^{(s)})) \right. \\ & \left. + \mathbb{E}_{\bar{z}_u^{(t)} \sim p_{\theta_I}(\bar{z}_u | e_u^{(t)})} \log(1 - D_\phi(\bar{z}_u^{(t)})) \right), \end{aligned} \quad (4)$$

where  $\theta_\phi$  is the learnable parameters of the domain discriminator,  $\bar{z}_u^{(s)}$  and  $\bar{z}_u^{(t)}$  are the domain-invariant preference based on  $s$  and  $t$  domains' user embeddings, respectively. And if  $\tau = s$ , i.e. the domain-invariant preference is from the domain  $s$ , we let  $D_\phi(\bar{z}_u^{(s)}) = 1$  as groundtruth, otherwise  $D_\phi(\bar{z}_u^{(t)}) = 0$ . The role of the domain discriminator  $D_\phi$  is to help  $G_I$  learn an indistinguishable preference distribution. Therefore, the optimization objective of the  $G_I$  and  $D_\phi$  is defined as the following minmax game:

$$\min_{\theta_I} \max_{\theta_\phi} -\mathcal{L}_\phi. \quad (5)$$

The optimization objective of the domain discriminator  $D_\phi$  is to strengthen its discriminating ability by maximizing the negative discriminating loss ( $-\mathcal{L}_\phi$ ). The adversarial optimization of Equation (5) results in a good  $G_I$  by minimizing the loss to update its parameters. Hence,  $G_I$  is able to generate  $\{\bar{z}_u\}$  that are indistinguishable enough to fool a powerful domain discriminator.

**3.2.3 Constraint.** Shared users are both in  $s$  and  $t$  domains. We can get a user's two domain-invariant preferences from different domains. Then, it is essential to keep the two domain-invariant preferences of a user close in the same space. To achieve this, we introduce an auxiliary loss  $\mathcal{L}_{su}$  to constrain them. The  $\mathcal{L}_{su}$  is defined as:

$$\mathcal{L}_{su}(\theta_I) = \|\bar{z}_u^{(s)} - \bar{z}_u^{(t)}\|, u \in \{\mathcal{U}^{(s)} \cap \mathcal{U}^{(t)}\}. \quad (6)$$

We will update  $G_I$  by minimizing  $\mathcal{L}_{su}$  to resist the distance between  $\bar{z}_u^{(s)}$  and  $\bar{z}_u^{(t)}$ .

In the end, we can get the following loss of Dan by combining  $\mathcal{L}_\phi$  and  $\mathcal{L}_{su}$ :

$$\mathcal{L}_{Dan}(\theta_I, \theta_\phi) = -\mathcal{L}_\phi + \mathcal{L}_{su}. \quad (7)$$

To ensure that the  $G_I$  can capture the recommendation information, we combine  $\mathcal{L}_{Dan}$  and the loss of recommender with domain-invariant preferences as input to guide the optimization process of Dan jointly. As a result, the optimization objective of Dan can be concluded as follow:

$$\min_{\theta_I} \max_{\theta_\phi} \left( \mathcal{L}_{Dan} + \mathcal{L}_{Rec}^{(s)} + \mathcal{L}_{Rec}^{(t)} \right), \quad (8)$$

where  $\mathcal{L}_{Rec}^{(s)}$  is the recommendation loss of the recommender in the auxiliary domain and  $\mathcal{L}_{Rec}^{(t)}$  is the recommendation loss of the recommender in the target domain.

### 3.3 Cross-domain Adversarial Example Generative Network

Inspired by generative adversarial network [8, 38], we propose a novel cross-domain adversarial example generative network (Cdan) containing cross-domain adversarial example generator  $G_A$  and cross-domain adversarial example discriminator  $D_\psi$  to jointly perturb all samples.  $G_A$  will learn a satisfactory distribution of CDAE constrained by  $D_\psi$  and maximized recommendation losses.

**3.3.1 CDAE.** The goal of  $G_A$  is to perturb all input samples jointly to generate an imperceptible CDAEs' distribution  $p_{\theta_A}(\tilde{z}_u)$  which has enough harmfulness, where  $\tilde{z}_u \sim p_{\theta_A}(\tilde{z}_u)$ . To realize this, we take domain-invariant preference distribution as input of  $G_A$  and generate CDAE  $\tilde{z}_u$ :

$$\tilde{z}_u = G_A(\bar{z}_u; \theta_A), \quad u \in \{\mathcal{U}^{(s)} \cup \mathcal{U}^{(t)}\}, \quad (9)$$

where  $\bar{z}_u$  implies a user's domain-invariant preference who is from  $s$  or  $t$  domain and  $\theta_A$  is the learnable parameters of  $G_A$ .

**3.3.2 Optimization.** In order to guarantee that CDAEs' distribution is imperceptible, we introduce a cross-domain adversarial example discriminator  $D_\psi$  parameterized by  $\theta_\psi$ , with  $\tilde{z}_u$  and  $\tilde{z}_u$  as input. Consequently, the loss of Cdan is defined as:

$$\begin{aligned} \mathcal{L}_{Cdan}(\theta_A, \theta_\psi) = & - \left( \mathbb{E}_{\tilde{z}_u \sim p_{\theta_I}(\tilde{z}_u)} \log(D_\psi(\tilde{z}_u)) \right. \\ & \left. + \mathbb{E}_{\tilde{z}_u \sim p_{\theta_A}(\tilde{z}_u)} \log(1 - D_\psi(\tilde{z}_u)) \right). \end{aligned} \quad (10)$$

If  $\tilde{z}_u$  acts as input of  $D_\psi$ , we set  $D_\psi(\tilde{z}_u) = 1$ , otherwise  $D_\psi(\tilde{z}_u) = 0$ .

To make certain that the CDAE distribution possesses adequate aggressivity while avoiding obtaining a trivial Cdan, it is required to maximize the recommendation losses of the auxiliary and target domains' recommender taking CDAEs as input to direct the optimization of Cdan. As a result, we define the following minmax optimization objective for Cdan:

$$\min_{\theta_\psi} \max_{\theta_A} \left( \mathcal{L}_{Cdan} + \lambda \left( \tilde{\mathcal{L}}_{Rec}^{(s)} + \tilde{\mathcal{L}}_{Rec}^{(t)} \right) \right), \quad (11)$$

where  $\lambda$  is a factor to control the contribution of CDAT,  $\tilde{\mathcal{L}}_{Rec}^{(s)}$  is the adversarial recommendation loss of the auxiliary domain and  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  is the adversarial recommendation loss of the target domain.

In this way, we train the discriminator  $D_\psi$  to minimize the cross entropy  $\mathcal{L}_{Cdan}$  to yield a strong discriminator to ensure CDAEs' imperceptibility. That CDAEs own imperceptibility indicates that domain-invariant preference distribution and CDAE distribution

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### Algorithm 1 Training Algorithm of CDAT.

```

Input: Datasets  $\mathcal{D} = \mathcal{D}^{(s)} \cup \mathcal{D}^{(t)}$ ,  $\lambda, \eta$ ;
Output: Well-trained  $G_I, Rec^{(t)}$ ;
1: Random initialize  $G_I, D_\phi, G_A, D_\psi, Rec^{(s)}$  and  $Rec^{(t)}$ ;
2: for  $T$  epochs do
3:   Randomly draw samples  $\{(u, v_+, v_-)\}$  from  $\mathcal{D}$ ;
4:   for  $T_{Dan}$  epochs do
5:     Compute gradient  $\nabla_{\theta_\phi} (\mathcal{L}_{Dan})$ 
       and  $\nabla_{\theta_I} (\mathcal{L}_{Dan} + \mathcal{L}_{Rec}^{(s)} + \mathcal{L}_{Rec}^{(t)})$ ;
6:      $\theta_\phi^{(T+1)} = \theta_\phi^{(T)} + \eta \nabla_{\theta_\phi} (\mathcal{L}_{Dan})$ ;
7:      $\theta_I^{(T+1)} = \theta_I^{(T)} - \eta \nabla_{\theta_I} (\mathcal{L}_{Dan} + \mathcal{L}_{Rec}^{(s)} + \mathcal{L}_{Rec}^{(t)})$ ;
8:   end for
9:   Get  $\tilde{z}_u \sim p_{\theta_I}(\tilde{z}_u)$ ;
10:  for  $T_{Cdan}$  epochs do
11:    Compute gradient  $\nabla_{\theta_\psi} (\mathcal{L}_{Cdan})$ 
       and  $\nabla_{\theta_A} (\mathcal{L}_{Cdan} + \lambda (\tilde{\mathcal{L}}_{Rec}^{(s)} + \tilde{\mathcal{L}}_{Rec}^{(t)}))$ ;
12:     $\theta_\psi^{(T+1)} = \theta_\psi^{(T)} - \eta \nabla_{\theta_\psi} (\mathcal{L}_{Cdan})$ ;
13:     $\theta_A^{(T+1)} = \theta_A^{(T)} + \eta \nabla_{\theta_A} (\mathcal{L}_{Cdan} + \lambda (\tilde{\mathcal{L}}_{Rec}^{(s)} + \tilde{\mathcal{L}}_{Rec}^{(t)}))$ ;
14:  end for
15:  Get  $\tilde{z}_u \sim p_{\theta_A}(\tilde{z}_u)$ ;
16:  Compute gradient  $\nabla_{\theta_{Rec}^{(s)}} (\mathcal{L}_{Rec}^{(s)} + \lambda \tilde{\mathcal{L}}_{Rec}^{(s)})$ 
       and  $\nabla_{\theta_{Rec}^{(t)}} (\mathcal{L}_{Rec}^{(t)} + \lambda \tilde{\mathcal{L}}_{Rec}^{(t)})$ ;
17:   $(\theta_{Rec}^{(s)})^{(T+1)} = (\theta_{Rec}^{(s)})^{(T)} - \eta \nabla_{\theta_{Rec}^{(s)}} (\mathcal{L}_{Rec}^{(s)} + \lambda \tilde{\mathcal{L}}_{Rec}^{(s)})$ ;
18:   $(\theta_{Rec}^{(t)})^{(T+1)} = (\theta_{Rec}^{(t)})^{(T)} - \eta \nabla_{\theta_{Rec}^{(t)}} (\mathcal{L}_{Rec}^{(t)} + \lambda \tilde{\mathcal{L}}_{Rec}^{(t)})$ ;
19: end for

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are close. Apart from this, we also adversarially train  $G_A$  with the aim of maximizing the loss  $\mathcal{L}_{Cdan} + \lambda (\tilde{\mathcal{L}}_{Rec}^{(s)} + \tilde{\mathcal{L}}_{Rec}^{(t)})$  to gain aggressive CDAEs for enhancing adversarial robustness of recommendation model in the sparse target domain.

### 3.4 Cross-domain Distributional Adversarial Training

We leverage these well-pleasing CDAEs captured by Cdan to adversarially attack the recommender  $Rec^{(t)}$  in the target domain and update the parameters of  $Rec^{(t)}$  to obtain a more robust recommendation model. In this process, the adversarial robustness will be transferred from the rich auxiliary domain to the sparse target domain by CDAEs.

To be specific, a CDAE  $\tilde{z}_u$  is sampled from  $p_{\theta_A}(\tilde{z}_u)$  which fits by  $G_A$ . And then, we predict the attacked interaction probability  $\tilde{r}_{\tilde{u}v}^{(t)}$  that an attacked user  $\tilde{u}$  will interact with an item  $v$ :

$$\tilde{r}_{\tilde{u}v}^{(t)} = Rec^{(t)} \left( \tilde{z}_u^{(t)} \oplus e_v^{(t)}; \theta_{Rec}^{(t)} \right), \quad (12)$$

where  $\tilde{z}_u^{(t)} \sim p_{\theta_A}(\tilde{z}_u | \tilde{z}_u^{(t)})$  and  $e_v^{(t)}$  is an item embedding in domain  $t$ .

To accomplish CDAT, we build an adversarial training set  $\tilde{\mathcal{D}}^{(t)} = \{(\tilde{u}, v_+, v_-)\}$ , where  $v_+$  and  $v_-$  represent a positive sample and a negative sample of an attacked user  $\tilde{u}$ , respectively. We define the following adversarial recommendation loss of the recommender

for attacked domain  $t$  like Equation (2):

$$\tilde{\mathcal{L}}_{Rec}^{(t)}(\theta_A, \theta_{Rec}^{(t)}) = -\frac{1}{|\tilde{\mathcal{D}}^{(t)}|} \sum_{(\tilde{u}, v_+, v_-) \in \tilde{\mathcal{D}}^{(t)}} \log \left( \tilde{r}_{\tilde{u}v_+}^{(t)} - \tilde{r}_{\tilde{u}v_-}^{(t)} \right). \quad (13)$$

In order to strengthen the adversarial robustness of the recommendation model in the sparse target domain  $t$  by CDAT, the optimization objective is defined as the following minmax game:

$$\min_{\theta_{Rec}^{(t)}} \max_{\theta_A} \tilde{\mathcal{L}}_{Rec}^{(t)}. \quad (14)$$

$\theta_A$  is updated by maximizing the loss  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  to destroy the performance of  $Rec^{(t)}$ . Meanwhile,  $\theta_{Rec}^{(t)}$  is also updated by minimizing the loss  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  to make  $Rec^{(t)}$  be able to defend the adversarial attack.

### 3.5 Overall Optimization Objective

Finally, by combining  $\mathcal{L}_{Dan}$ ,  $\mathcal{L}_{Cdan}$ ,  $\mathcal{L}_{Rec}^{(s)}$ ,  $\mathcal{L}_{Rec}^{(t)}$ ,  $\tilde{\mathcal{L}}_{Rec}^{(s)}$  and  $\tilde{\mathcal{L}}_{Rec}^{(t)}$ , we can get the following overall optimization objective:

$$\begin{aligned} \min_{\theta_I, \theta_\psi, \theta_{Rec}^{(s)}, \theta_{Rec}^{(t)}} \max_{\theta_\phi, \theta_A} & \left( \mathcal{L}_{Dan} + \mathcal{L}_{Cdan} + \mathcal{L}_{Rec}^{(s)} + \mathcal{L}_{Rec}^{(t)} \right. \\ & \left. + \lambda \left( \tilde{\mathcal{L}}_{Rec}^{(s)} + \tilde{\mathcal{L}}_{Rec}^{(t)} \right) \right). \end{aligned} \quad (15)$$

We summarize the training procedure of CDAT in Algorithm 1.

**Table 1: Statistics of datasets.**

Datasets	Douban			Amazon		
Scenarios	Movie-Book   Movie-Music			TV-CD		
Domains	Movie	Book	Movie	Music	TV	CD
#Users	1,873	2,063	2,049	1,624	17,894	15,733
#Shared users	1,231		967		1,859	
#Items	9,468	6,703	9,496	5,508	9,881	12,482
#Interactions	460,028	69,211	487,122	51,985	520,166	262,709
Density	2.59%	0.50%	2.51%	0.58%	0.29%	0.13%

## 4 EXPERIMENTS

The experiments aim to answer the following research questions:

- **RQ1** How does CDAT perform compared to the state-of-the-art baselines in terms of recommendation accuracy and adversarial robustness?
- **RQ2** How do the different parts of CDAT affect the performance?
- **RQ3** How to illustrate the superiority of CDAT with visualizable case studies?

### 4.1 Experimental Settings

**4.1.1 Datasets.** We conduct the experiments on two public datasets: Douban [39] and Amazon [21]. Specifically, we build three cross-domain scenarios: Movie-Book and Movie-Music in Douban, and TV-CD in Amazon, where Book, Music and CD are the target domains. Table 1 shows the statistics of the three cross-domain scenarios (after all pre-processing steps), where the density is defined as

the ratio of the observed interactions over all possible interactions. For the interaction data of the target domain in different scenarios, the data is randomly divided into training set, validation set, and testing set. For each user, we randomly select an interacted history to the validation set, another one to the testing set and the remaining ones to the training set. We repeat such procedure three times and report the average results with standard deviation.

**4.1.2 Baseline Methods.** We compare our CDAT with the following baseline methods, comprising one basic recommendation model, three AT methods in recommendation (APR, DAT, ACDN), and two CDR methods (MLP++, ACDR) which are briefly described as follows:

- **Base Model** is a basic recommendation model including an encoder and a recommender, which are both implemented as an MLP with activation function ReLU.
- **APR** [10] is an AT method, which generates AEs based on the user embeddings to maximize the BPR loss and then forces the recommendation model to minimize the BPR loss on AEs.
- **DAT** [33] further considers to add perturbations to both user and item embeddings with proper restriction.
- **ACDN** [34] leverages the users shared by the target and auxiliary domains to construct AEs for AT.
- **MLP++** [11] combines two MLPs by sharing user embedding matrix to realize cross-domain recommendation.
- **ACDR** [14] incorporates global user preferences and domain-specific user preferences via adversarial learning.

For fairness, APR, DAT, ACDN and proposed CDAT use the same Base Model to compare their performances.

**4.1.3 Evaluation Protocols.** We adopt the widely used metrics Hit Ratio (HR) and Normalized Discounted Cumulative Gain (NDCG) to evaluate the recommendation accuracy of CDAT and the baseline methods. HR measures whether the testing item is in the top-K list. While NDCG is a position-sensitive metric, which assigns higher weights to hits at higher positions. In a word, for both metrics, the higher values, the better performance can indicate. We also employ the popular *leave-one-out* evaluation protocol [4, 10]. Specifically, we rank a positive item of a testing user among her 99 negative items which are randomly sampled.

In order to fully evaluate the defense capability of these methods against different attacks, we employ three attacking methods FGSM [9], PGD [20] and advGAN [31] to attack the recommendation model trained by CDAT and baseline methods. Then, we evaluate the adversarial robustness also by HR and NDCG. For FGSM and PGD, we set up two attack intensities, e.g.  $\epsilon \in \{0.1, 1\}$ , to test the robustness against different attack strengths, which are denoted as FGSM-0.1, FGSM-1, PGD-0.1 and PGD-1. The detailed settings of all attacks are presented in Table 2.

**4.1.4 Hyper-Parameter Setting.** All the hyper-parameters of baselines and CDAT are tuned on validation sets. The specific settings of CDAT are presented in Table 3. All modules in CDAT are implemented as an MLP with activation function ReLU. We choose Adam as the optimizer. To ensure the stability of the adversarial process, we employ the hinge gan loss [17, 41].

**Table 2: Hyper-parameters setting of different attacking methods in different scenarios**

Attacking Method	Scenarios		
	Movie-Book	Movie-Music	TV-CD
advGAN	$\alpha=0.3, \beta=0.1, c=10$	$\alpha=0.3, \beta=0.1, c=10$	$\alpha=0.5, \beta=0.1, c=10$
FGSM-0.1	$\epsilon=0.1$ , step size=0.1		
FGSM-1	$\epsilon=1$ , step size=1		
PGD-0.1	$\epsilon=0.1$ , step size=0.01, iterations=20		
PGD-1	$\epsilon=1$ , step size=0.1, iterations=20		

**Table 3: Hyper-parameters setting of CDAT in different scenarios**

Hyper-parameter	Scenarios		
	Movie-Book	Movie-Music	TV-CD
learning rate of $D_\phi$ and $G_I$	0.0003	0.0003	0.0001
learning rate of $D_\psi$ and $G_A$	0.0001	0.0001	0.0001
learning rate of $Rec^{(t)}$	0.0001	0.0001	0.0001
$\lambda$	0.1	0.3	0.1
size of embedding	128		
size of domain-invariant preference	32		
size of CDAE	32		

## 4.2 Performance Comparison (RQ1)

Tables 4 and 5 present the target domain's performance in different scenarios from which we can make the following observations and analyses.

First, in all scenarios, CDAT almost consistently outperforms the baselines in terms of all the metrics under adversarial robustness evaluation. These results verify the superiority of CDAT which can enhance the adversarial robustness of the sparse target domain by transferring distributional robustness from a denser auxiliary domain.

And, these results also imply that our CDAT using joint perturbation is superior to the baselines using point-wise perturbation.

Then, notably, in certain cases, the performance of APR and DAT, designed for single-domain recommendations, slightly outperforms our CDAT. We argue that it may be attributed to negative transfer of recommendation information in CDAT in certain sparse cases.

Finally, in Figure 2, we can observe that the performance of general CDR in the target domain declines significantly with the PGD's perturbation constrain  $\epsilon$  increasing. Consequently, we confirm that the general CDRs just transfer recommendation information to have a reliable recommendation performance and cannot transfer the knowledge benefiting adversarial robustness, which leads to unpromising adversarial robustness of the general CDR model.

## 4.3 Ablation Study (RQ2)

**4.3.1 Performance of Different Parts.** Now we investigate the effectiveness of the Cdan, unshared users, and  $D_\psi$ . For this purpose, we compare CDAT with its three variants as follows:

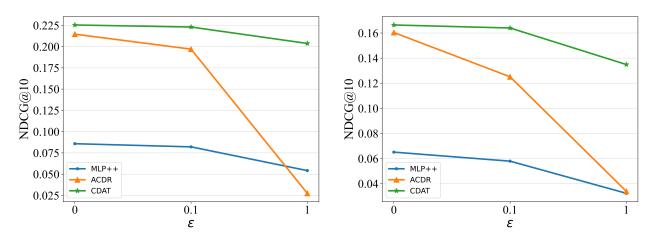
- **CDAT-w/o-Cdan** is the variant without Cdan, where  $\mathcal{L}_{Cdan}$ ,  $\tilde{\mathcal{L}}_{Rec}^{(s)}$ , and  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  are removed from the Equation (15).

**Table 4: Performance comparison in different scenarios.** Clean represents the performance of the recommendation model trained by the proposed CDAT and baselines without adversarial attacks on the test set. The metric is HR@10 in this table.

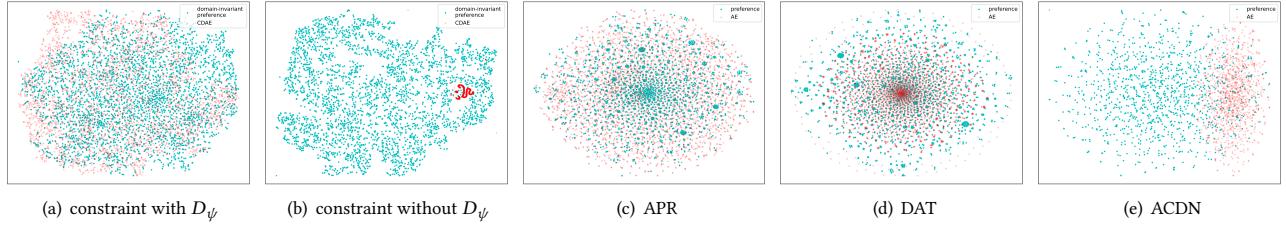
Scenarios	Attack	Base Model	APR	DAT	ACDN	CDAT
Movie-Book	Clean	0.3652 $\pm$ 0.0087	0.3822 $\pm$ 0.0127	0.3844 $\pm$ 0.0120	0.3404 $\pm$ 0.0256	<b>0.3940<math>\pm</math>0.0066</b>
	FGSM-0.1	0.3081 $\pm$ 0.0153	0.3714 $\pm$ 0.0125	0.3774 $\pm$ 0.0108	0.3390 $\pm$ 0.0244	<b>0.3920<math>\pm</math>0.0063</b>
	FGSM-1	0.1640 $\pm$ 0.0141	0.3313 $\pm$ 0.0187	0.3510 $\pm$ 0.0086	0.3364 $\pm$ 0.0247	<b>0.3850<math>\pm</math>0.0042</b>
	PGD-0.1	0.3013 $\pm$ 0.0117	0.3614 $\pm$ 0.0117	0.3708 $\pm$ 0.0102	0.3394 $\pm$ 0.0233	<b>0.3904<math>\pm</math>0.0061</b>
	PGD-1	0.1067 $\pm$ 0.0143	0.2529 $\pm$ 0.0313	0.2739 $\pm$ 0.0346	0.3263 $\pm$ 0.0259	<b>0.3698<math>\pm</math>0.0039</b>
	advGAN	0.1403 $\pm$ 0.0244	0.1015 $\pm$ 0.0118	0.1472 $\pm$ 0.0174	0.3360 $\pm$ 0.0237	<b>0.3886<math>\pm</math>0.0079</b>
Movie-Music	Clean	0.2789 $\pm$ 0.0167	0.3018 $\pm$ 0.0027	0.3135 $\pm$ 0.0184	0.2802 $\pm$ 0.0117	<b>0.3180<math>\pm</math>0.0146</b>
	FGSM-0.1	0.2252 $\pm$ 0.0120	0.2956 $\pm$ 0.0013	0.3126 $\pm$ 0.0180	0.2743 $\pm$ 0.0042	<b>0.3169<math>\pm</math>0.0159</b>
	FGSM-1	0.0877 $\pm$ 0.0056	0.2805 $\pm$ 0.0025	0.2928 $\pm$ 0.0259	0.2208 $\pm$ 0.0612	<b>0.3004<math>\pm</math>0.0156</b>
	PGD-0.1	0.2184 $\pm$ 0.0092	0.2928 $\pm$ 0.0022	0.3120 $\pm$ 0.0185	0.2710 $\pm$ 0.0073	<b>0.3155<math>\pm</math>0.0141</b>
	PGD-1	0.0488 $\pm$ 0.0018	0.2244 $\pm$ 0.0102	0.2502 $\pm$ 0.0494	0.1906 $\pm$ 0.0884	<b>0.2724<math>\pm</math>0.0170</b>
	advGAN	0.0570 $\pm$ 0.0133	0.1115 $\pm$ 0.0221	0.1563 $\pm$ 0.0055	0.2271 $\pm$ 0.0741	<b>0.2976<math>\pm</math>0.0148</b>
TV-CD	Clean	0.3079 $\pm$ 0.0052	0.3025 $\pm$ 0.0222	0.2959 $\pm$ 0.0098	0.2326 $\pm$ 0.0153	<b>0.3176<math>\pm</math>0.0047</b>
	FGSM-0.1	0.2826 $\pm$ 0.0084	0.2814 $\pm$ 0.0095	0.2067 $\pm$ 0.0310	0.3162 $\pm$ 0.0047	
	FGSM-1	0.1946 $\pm$ 0.0112	<b>0.3265<math>\pm</math>0.0246</b>	0.2538 $\pm$ 0.0088	0.1409 $\pm$ 0.0420	0.3100 $\pm$ 0.0074
	PGD-0.1	0.2819 $\pm$ 0.0081	0.2860 $\pm$ 0.0504	0.2803 $\pm$ 0.0094	0.2032 $\pm$ 0.0350	<b>0.3159<math>\pm</math>0.0049</b>
	PGD-1	0.1765 $\pm$ 0.0094	0.2072 $\pm$ 0.1381	0.2382 $\pm$ 0.0089	0.1017 $\pm$ 0.0396	<b>0.3027<math>\pm</math>0.0073</b>
	advGAN	0.2100 $\pm$ 0.0047	0.2515 $\pm$ 0.1077	0.2827 $\pm$ 0.0076	0.1883 $\pm$ 0.0676	<b>0.3167<math>\pm</math>0.0049</b>

**Table 5: Performance comparison in different scenarios.** Clean represents the performance of the recommendation model trained by the proposed CDAT and baselines without adversarial attacks on the test set. The metric is NDCG@10 in this table.

Scenarios	Attack	Base Model	APR	DAT	ACDN	CDAT
Movie-Book	Clean	0.2086 $\pm$ 0.0076	0.2225 $\pm$ 0.0086	0.2251 $\pm$ 0.0066	0.2094 $\pm$ 0.0126	<b>0.2254<math>\pm</math>0.0061</b>
	FGSM-0.1	0.1767 $\pm$ 0.0112	0.2164 $\pm$ 0.0091	0.2208 $\pm$ 0.0058	0.2084 $\pm$ 0.0116	<b>0.2237<math>\pm</math>0.0060</b>
	FGSM-1	0.0885 $\pm$ 0.0059	0.1901 $\pm$ 0.0102	0.2068 $\pm$ 0.0057	0.2068 $\pm$ 0.0091	<b>0.2153<math>\pm</math>0.0056</b>
	PGD-0.1	0.1735 $\pm$ 0.0118	0.2122 $\pm$ 0.0084	0.2186 $\pm$ 0.0056	0.2085 $\pm$ 0.0113	<b>0.2230<math>\pm</math>0.0053</b>
	PGD-1	0.0623 $\pm$ 0.0050	0.1511 $\pm$ 0.0187	0.1664 $\pm$ 0.0187	0.2021 $\pm$ 0.0089	<b>0.2037<math>\pm</math>0.0090</b>
	advGAN	0.0973 $\pm$ 0.0155	0.0686 $\pm$ 0.0052	0.1034 $\pm$ 0.0127	0.2073 $\pm$ 0.1111	<b>0.2223<math>\pm</math>0.0058</b>
Movie-Music	Clean	0.1478 $\pm$ 0.0103	0.1576 $\pm$ 0.0041	0.1643 $\pm$ 0.0067	0.1491 $\pm$ 0.0059	<b>0.1664<math>\pm</math>0.0038</b>
	FGSM-0.1	0.1191 $\pm$ 0.0085	0.1547 $\pm$ 0.0032	0.1644 $\pm$ 0.0059	0.1442 $\pm$ 0.0117	<b>0.1646<math>\pm</math>0.0042</b>
	FGSM-1	0.0480 $\pm$ 0.0058	0.1453 $\pm$ 0.0033	<b>0.1545<math>\pm</math>0.0099</b>	0.1442 $\pm$ 0.0401	0.1508 $\pm$ 0.0023
	PGD-0.1	0.1165 $\pm$ 0.0073	0.1534 $\pm$ 0.0039	<b>0.1645<math>\pm</math>0.0058</b>	0.1422 $\pm$ 0.0142	0.1640 $\pm$ 0.0036
	PGD-1	0.0289 $\pm$ 0.0021	0.1193 $\pm$ 0.0029	0.1343 $\pm$ 0.0214	0.0995 $\pm$ 0.0534	<b>0.1349<math>\pm</math>0.0018</b>
	advGAN	0.0369 $\pm$ 0.0098	0.0719 $\pm$ 0.1111	0.0956 $\pm$ 0.0062	0.1172 $\pm$ 0.0495	<b>0.1559<math>\pm</math>0.0046</b>
TV-CD	Clean	0.1547 $\pm$ 0.0040	0.1589 $\pm$ 0.0102	<b>0.1618<math>\pm</math>0.0050</b>	0.1259 $\pm$ 0.0118	0.1609 $\pm$ 0.0018
	FGSM-0.1	0.1396 $\pm$ 0.0053	0.1512 $\pm$ 0.0233	0.1518 $\pm$ 0.0047	0.1112 $\pm$ 0.0188	<b>0.1602<math>\pm</math>0.0017</b>
	FGSM-1	0.0955 $\pm$ 0.0060	<b>0.1703<math>\pm</math>0.0131</b>	0.1335 $\pm$ 0.0050	0.0731 $\pm$ 0.0241	0.1561 $\pm$ 0.0030
	PGD-0.1	0.1405 $\pm$ 0.0050	0.1509 $\pm$ 0.0236	0.1516 $\pm$ 0.0049	0.1097 $\pm$ 0.0202	<b>0.1599<math>\pm</math>0.0018</b>
	PGD-1	0.0886 $\pm$ 0.0046	0.1068 $\pm$ 0.0671	0.1231 $\pm$ 0.0058	0.0527 $\pm$ 0.0220	<b>0.1514<math>\pm</math>0.0031</b>
	advGAN	0.1138 $\pm$ 0.0024	0.1316 $\pm$ 0.0565	0.1544 $\pm$ 0.0043	0.1043 $\pm$ 0.0327	<b>0.1607<math>\pm</math>0.0019</b>

**Figure 2: Performance comparison with general cross-domain recommendation methods.**

- **CDAT-Shared** is the variant that only utilizes the shared users' data as input.
- **CDAT-w/o- $D_\psi$**  is the variant without the discriminator  $D_\psi$ , where  $\mathcal{L}_{Cdan}$  is removed from the Equation (15).



**Figure 3: Visualization comparison between AE distribution and preference distribution in Movie-Book.**

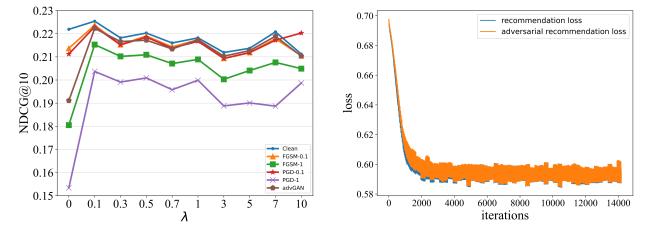
**Table 6: Ablation Studies in Movie-Book.** Clean represents the performance of the recommendation model trained by the variants without adversarial attacks on the test set.

Attack	Metric	CDAT-w/o-Cdan	CDAT-w/o- $D_\psi$	CDAT-Shared	CDAT
Clean	HR@10	0.3906±0.0087	0.3918±0.0044	0.3816±0.0086	<b>0.3940±0.0066</b>
	NDCG@10	0.2219±0.0061	0.2216±0.0061	0.2057±0.0082	<b>0.2254±0.0061</b>
FGSM-0.1	HR@10	0.3848±0.0119	0.3880±0.0054	0.3799±0.0076	<b>0.3920±0.0063</b>
	NDCG@10	0.2137±0.0070	0.2191±0.0056	0.2021±0.0053	<b>0.2237±0.0060</b>
FGSM-1	HR@10	0.3426±0.0530	0.3762±0.0103	0.3538±0.0171	<b>0.3850±0.0042</b>
	NDCG@10	0.1805±0.0397	0.2074±0.0096	0.1843±0.0093	<b>0.2153±0.0056</b>
PGD-0.1	HR@10	0.3828±0.0121	0.3866±0.0062	0.3786±0.0071	<b>0.3904±0.0061</b>
	NDCG@10	0.2112±0.0077	0.2182±0.0047	0.2011±0.0049	<b>0.2230±0.0053</b>
PGD-1	HR@10	0.2971±0.0623	0.3525±0.0100	0.3152±0.0107	<b>0.3698±0.0039</b>
	NDCG@10	0.1534±0.0411	0.1909±0.0064	0.1638±0.0030	<b>0.2037±0.0090</b>
advGAN	HR@10	0.3524±0.0141	0.3868±0.0060	0.3484±0.0081	<b>0.3886±0.0079</b>
	NDCG@10	0.1911±0.0193	0.2188±0.0065	0.1910±0.0120	<b>0.2223±0.0058</b>

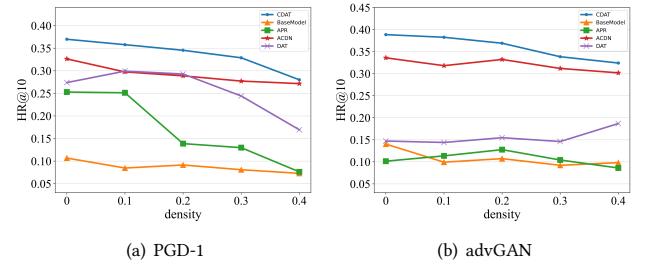
The results of the Movie-Book scenario are shown in Table 6. First, it can be observed that the performance of CDAT is remarkably better than CDAT-w/o-Cdan, which shows that Cdan generating high-quality CDAEs plays an important role in enhancing the sparse domain’s adversarial robustness. Second, we can see that CDAT also outperforms CDAT-Shared. This verifies that leveraging sufficient unshared users is better than only employing shared users’ data. In the end, it is observable that the performance of CDAT-w/o- $D_\psi$  is inferior to CDAT, indicating that CDAEs possessing imperceptibility are good for CDAT.

Figure 3 employs the t-SNE algorithm [29] to visualize the user preference distribution and AE distribution under CDAT, CDAT-w/o- $D_\psi$  and three baselines. By comparing subfigures (a) and (b) in Figure 3, we observe that with the constraint of the discriminator  $D_\psi$ , the CDAEs’ distribution and domain-invariant preference distribution are closer, indicating the imperceptibility of our CDAEs. Furthermore, comparing subfigures (a) with (c), (d), and (e), it is evident that the AEs produced by CDAT are more balanced in terms of quality compared to other point-wise perturbation-based methods. This result validates the effectiveness of our CDAT which jointly perturbs all samples for generating AEs.

**4.3.2 Hyper-parameter and Model Convergence Studies.** In this section, we study the influence of hyper-parameter, the balance factor  $\lambda$  between standard generalization and adversarial robustness generalization, of which the results are shown in Figure 4 in Movie-Book. We can see that the performance of CDAT under adversarial robustness evaluation significantly increases with the increasing of  $\lambda$  from 0 to 0.1, which demonstrates that the model’s adversarial robustness will get promoted with the increasing contribution of CDAT.



**Figure 4: Tuning of hyper-parameter  $\lambda$  in Movie-Book.** **Figure 5: Convergence analysis**



**Figure 6: Density Analysis in Movie-Book.**

However, when  $\lambda$  is bigger than 0.1, the performance gradually declines. This is attributed to the excessive contribution of CDAT, which hinders the model’s acquisition of adversarial robustness.

Additionally, Figure 5 presents the variation of recommendation loss  $\mathcal{L}_{Rec}^{(t)}$  and adversarial recommendation loss  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  during the training phase in Movie-Book with  $\lambda$  set to 0.1. It can be observed that both  $\mathcal{L}_{Rec}^{(t)}$  and  $\tilde{\mathcal{L}}_{Rec}^{(t)}$  decrease gradually with the increasing of iterations, eventually plateauing within a certain range with minor fluctuations. This trend reflects that our CDAT enables the model to achieve a balance between recommendation performance and adversarial robustness as the iterations increases.

**4.3.3 Density Analysis.** Figure 6 illustrates the variation in performance of our CDAT and baseline methods as the density decreases under different attacks, where the horizontal axes represent the proportion of the data that are randomly removed from the target domain’s training set. It can be observed that the performance of almost all methods declines as the density decreases. However, the performance of our CDAT remains superior to all baselines. The

		User ID	Top10 of Predicted Items									
CDAT	Clean	45	1339	729	200	4047	2430	1565	326	2110	2136	1902
	PGD-1	45	1339	729	200	4047	2430	1565	326	2110	2136	1902
	advGAN	45	1339	729	200	4047	2430	1565	326	2110	2136	1902
ACDN	Clean	45	963	1749	1338	1837	3830	1455	3741	4002	1165	4495
	PGD-1	45	963	1749	1338	1455	3830	1165	1837	3868	4976	3741
	advGAN	45	963	1749	1338	1837	1455	3830	3741	1165	4495	4002
DAT	Clean	45	729	1339	4047	200	5266	2136	2430	2110	326	1787
	PGD-1	45	729	1339	4047	2430	4898	1902	326	5266	200	2136
	advGAN	45	729	2136	1902	4898	5266	1339	5839	4047	5973	573

**Figure 7: Visualization of adversarial robustness of the recommendation model comparison between our CDAT and two baselines ACDN and DAT in Movie-Book.**

result indicates that our CDAT which leverages the dense auxiliary domain to enhance the adversarial robustness of the sparse target domain is effective.

#### 4.4 Case Study (RQ3)

In Figure 7, we visually present the adversarial robustness of recommendation models trained by CDAT, ACDN and DAT in Movie-Book. We select a user whose ID is 45 at random. For this user, we obtain her top-10 predicted item lists from the recommendation models trained by CDAT, ACDN and DAT on the test set, respectively. We evaluate these predicted item lists through three evaluation methods which are clean, PGD-1 and advGAN.

For each AT method, in the PGD-1 and advGAN evaluation, if the cell is filled with blue, it signifies that the item at that position is consistent with the item in the corresponding position of the clean evaluation. If the cell is filled with orange, it indicates that the item at that position in the PGD-1 or advGAN evaluation appears in the clean evaluation but not in the corresponding position. A green fill means that the item at that position is present in the PGD-1 or advGAN evaluation but absent in the clean evaluation.

As we can see, the three evaluations in CDAT are identical, demonstrating that our CDAT method is able to enhance the adversarial robustness of the sparse recommendation model. By contrast, under the ACDN and DAT, the PGD-1 and advGAN evaluations exhibit significant changes compared to the clean evaluation, indicating that the two methods are less effective at improving the model's adversarial robustness.

## 5 RELATED WORKS

### 5.1 Adversarial Training Method in Recommendation

Adversarial training [28, 35, 36] is an effective method to promote the adversarial robustness of recommendation models. It typically

involves two steps: generating AEs and optimizing model's parameters. APR [10] is the first AT method proposed specifically for recommendation. It aims to strengthen the robustness and generalization capabilities of recommendations with BPR. Building upon APR, the DAT [33] approach further refines the perturbation by restricting its direction. Additionally, ACDN [34] dynamically generates adversarial examples based on shared user embeddings.

In summary, due to the widespread sparsity of data in recommendation, existing AT methods may not effectively improve the adversarial robustness of recommendation models in sparse settings. Moreover, existing AT methods generate AEs by point-wise perturbation, which can lead to uneven AEs' quality due to varying sensitivities to such perturbations, thus hindering the efficacy of AT. In this paper, we address these issues by utilizing the knowledge benefitting AT from the auxiliary domain and joint perturbation to generate AEs.

### 5.2 Cross-domain Recommendation

In the pursuit of mitigating data sparsity in recommendation models, researchers introduce CDR methods [11, 13, 18, 32, 37]. According to different CDR tasks, these methods can be categorized into single-target domain and dual-target domain recommendations.

The single-target domain recommendations are designed to enhance the recommendation performance in the sparse target domain by leveraging the richer data from the auxiliary domain. Early techniques employ joint factorization of the user-item interaction matrices from both the auxiliary and target domains to capture the common preferences among shared users [12, 16, 24]. In recent years, many methods based on deep neural networks have been proposed for better improving performance in the sparse target domain by transfer learning [6, 15]. Dual-target domain recommendations represent a burgeoning trend in recent years, aiming to simultaneously promote the recommendation performance in two relevant domains [11, 14, 38]. Early methods transfer the knowledge between two domains by jointly modeling a user's preference in two relevant domains like CoNet. However, the users' representations from such methods may be harmful to dual-CDR's performance due to mixed representations. Recently, researchers have also proposed some methods [3, 19, 26, 30] to disentangle preferences.

Although the above CDR methods demonstrate promising performance in generalization ability, they almost ignore transferring adversarial robustness from the auxiliary domain to the target domain, which leads to degraded performance of CDR when facing adversarial attacks. In this paper, we propose the CDAT to tackle this issue.

## 6 CONCLUSION

In this paper, we propose a novel AT method called Cross-domain Distributional Adversarial Training (CDAT) for enhancing the adversarial robustness of the sparse recommendation domain, which transfers distributional adversarial robustness from the dense auxiliary domain to the sparse target domain. In particular, we propose a *Domain adversarial network* (Dan) that captures a distribution containing domain-invariant preferences, aligning the user embeddings of two domains and paving the way for the use of the knowledge from another domain. We also propose a *Cross-domain adversarial*

*example generative network* (Cdan) that learns a strongly attacking CDAEs' distribution of good imperceptibility by joint perturbation with the guidance of maximizing recommendation losses and the constraint of the cross-domain adversarial example discriminator to support CDAT. At last, remarkable improvements in adversarial robustness on the sparse target domain demonstrate the superiority of our CDAT.

## ACKNOWLEDGMENTS

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