

Probing the origin of 750 GeV diphoton excess with the precision measurements at the ILC

K. J. Bae, K. Hamaguchi, T. Moroi, K. Y, PLB 759 (2016) 575 [arXiv:1604.08307]

Keisuke Yanagi
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Probing the $e^+e^- \rightarrow \gamma\gamma$ diphoton
New Physics

with the precision measurements at the ILC

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Precision measurement at the ILC

- The ILC is future electron-positron collider
- Center of Mass energy: $\sqrt{s} = 250\text{GeV} - 1\text{TeV} (3\text{TeV}??)$
- Clean environment compared with the LHC
- Even if $m > \sqrt{s}/2$, **new particle affects SM process** via loop correction

We focus on **the differential cross section** of $e^+e^- \rightarrow f\bar{f}$

Motivations for indirect probe

Powerful method to search new heavy (non-colored) particles with **large EW quantum number** and/or **large multiplicity**

Examples

- Several models for the diphoton excess:
SM + **singlet** scalar (750GeV) + **charged** scalars/fermions
- WIMP DM models [K. Harigaya et al., arXiv: 1504.03402]
(Wino/Higgsino DM, Minimal DM...)
- Other BSM particles ...

Indirect method is widely applicable!

(even though the 750 GeV diphoton excess is dead)

Motivations for indirect

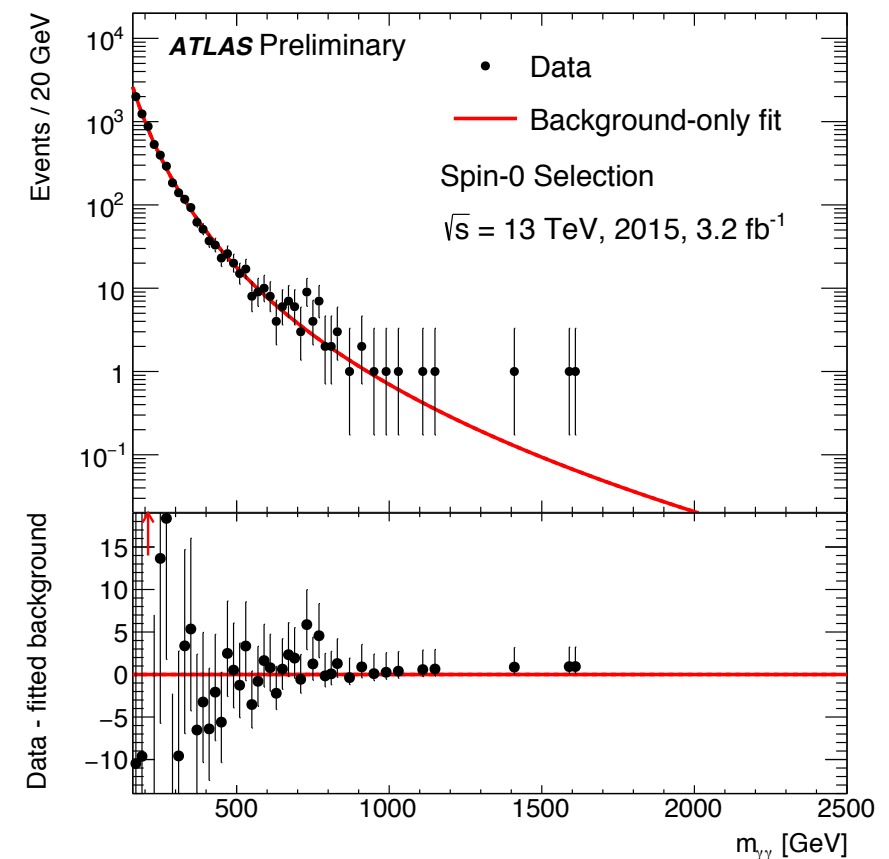
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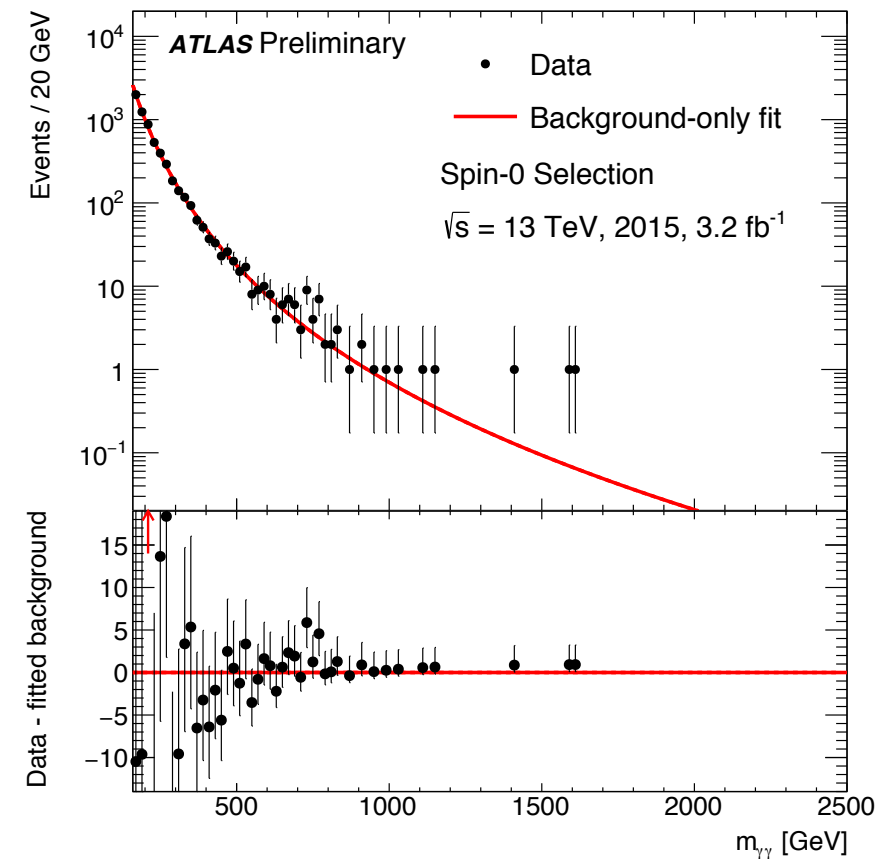
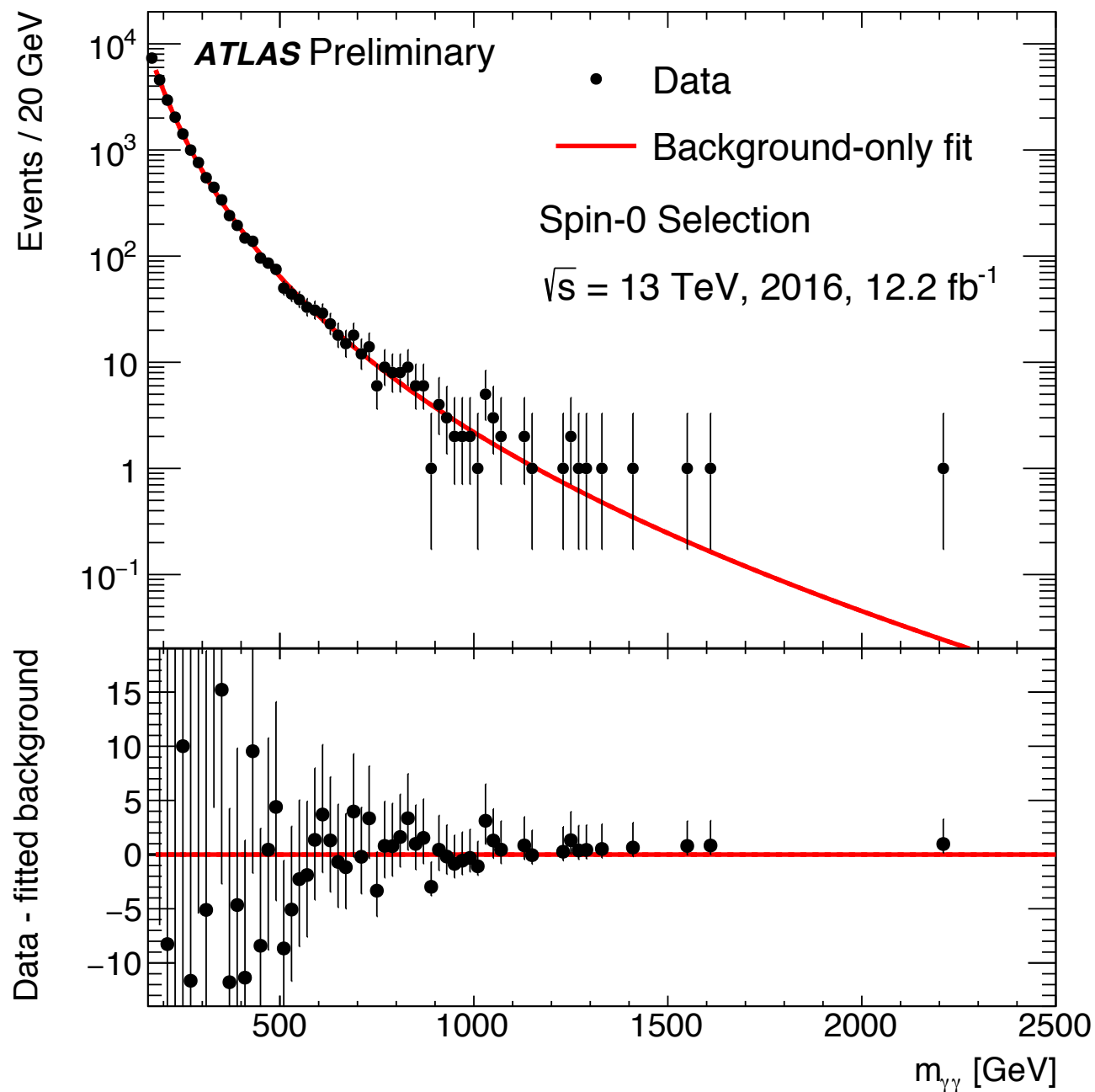
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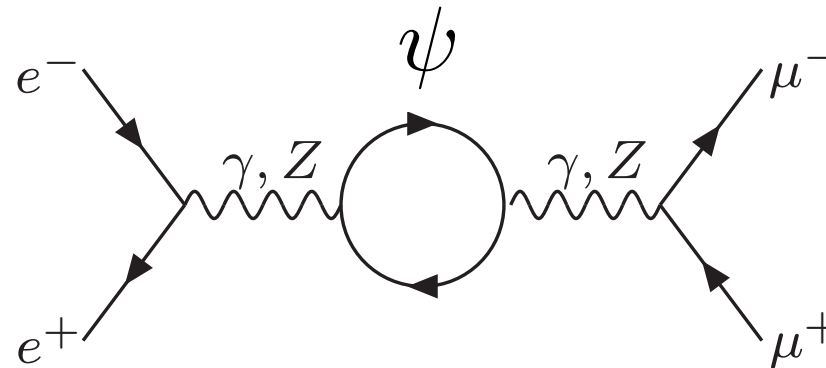
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Setup

$SU(3) \times SU(2)_L \times U(1)_Y$

- SM + **N** vector-like fermions ψ of mass **m**, and rep. (**1**, **n**, **Y**)
- $e^+e^- \rightarrow \mu^+\mu^-$ process



- Define

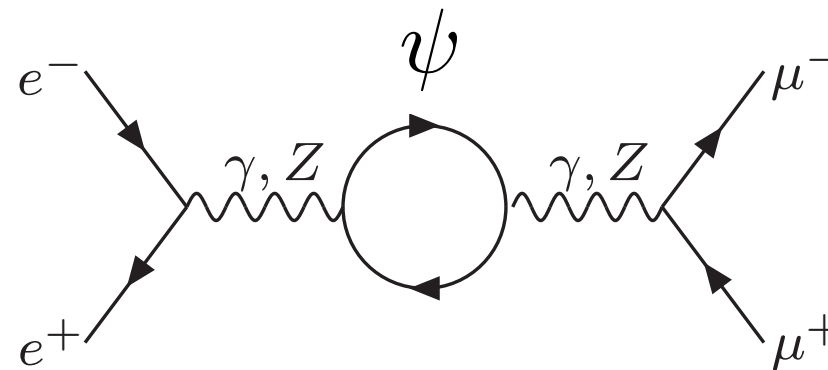
$$\Delta\chi^2 = \sum_{i: \text{bins}} \frac{(N_i^{\text{SM}+\psi} - N_i^{\text{SM}})^2}{N_i^{\text{SM}} + (\epsilon N_i^{\text{SM}})^2}$$

- Bins: 10 uniform intervals for the scattering angle $\cos\theta \in [-1, 1]$

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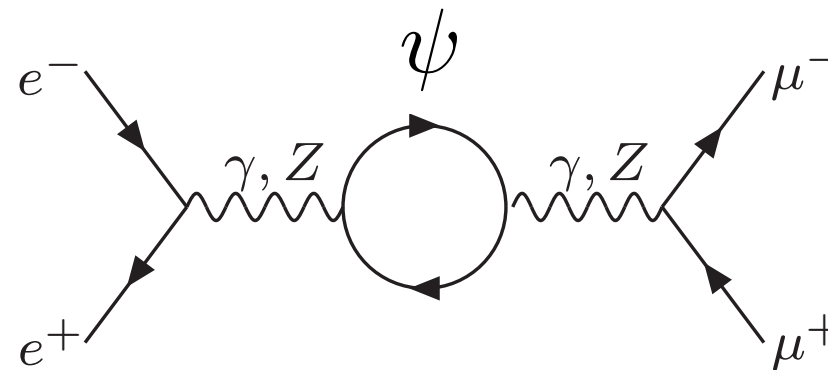
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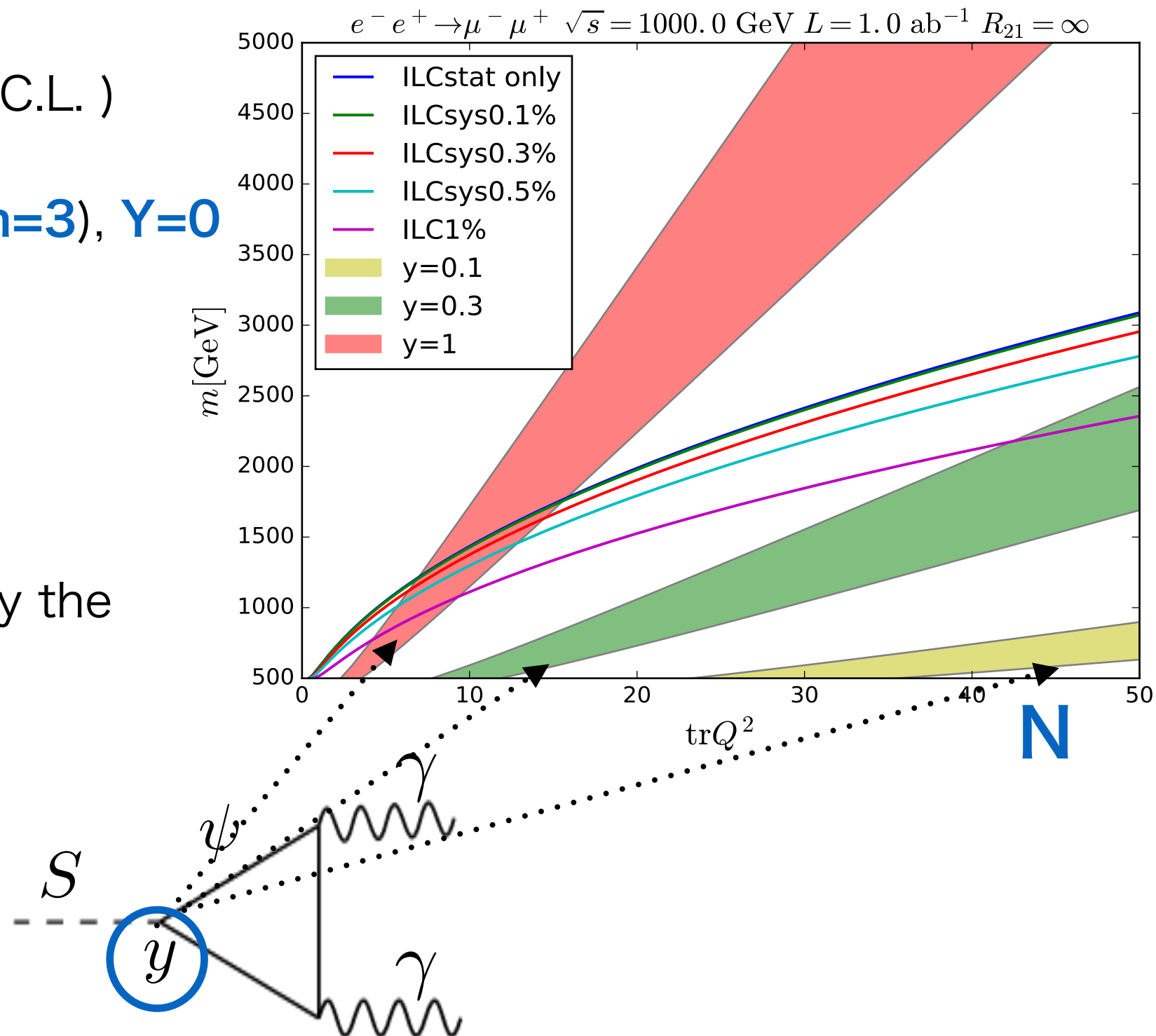
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Systematic uncertainty

- Bins: 10 uniform intervals for the scattering angle $\cos\theta \in [-1, 1]$

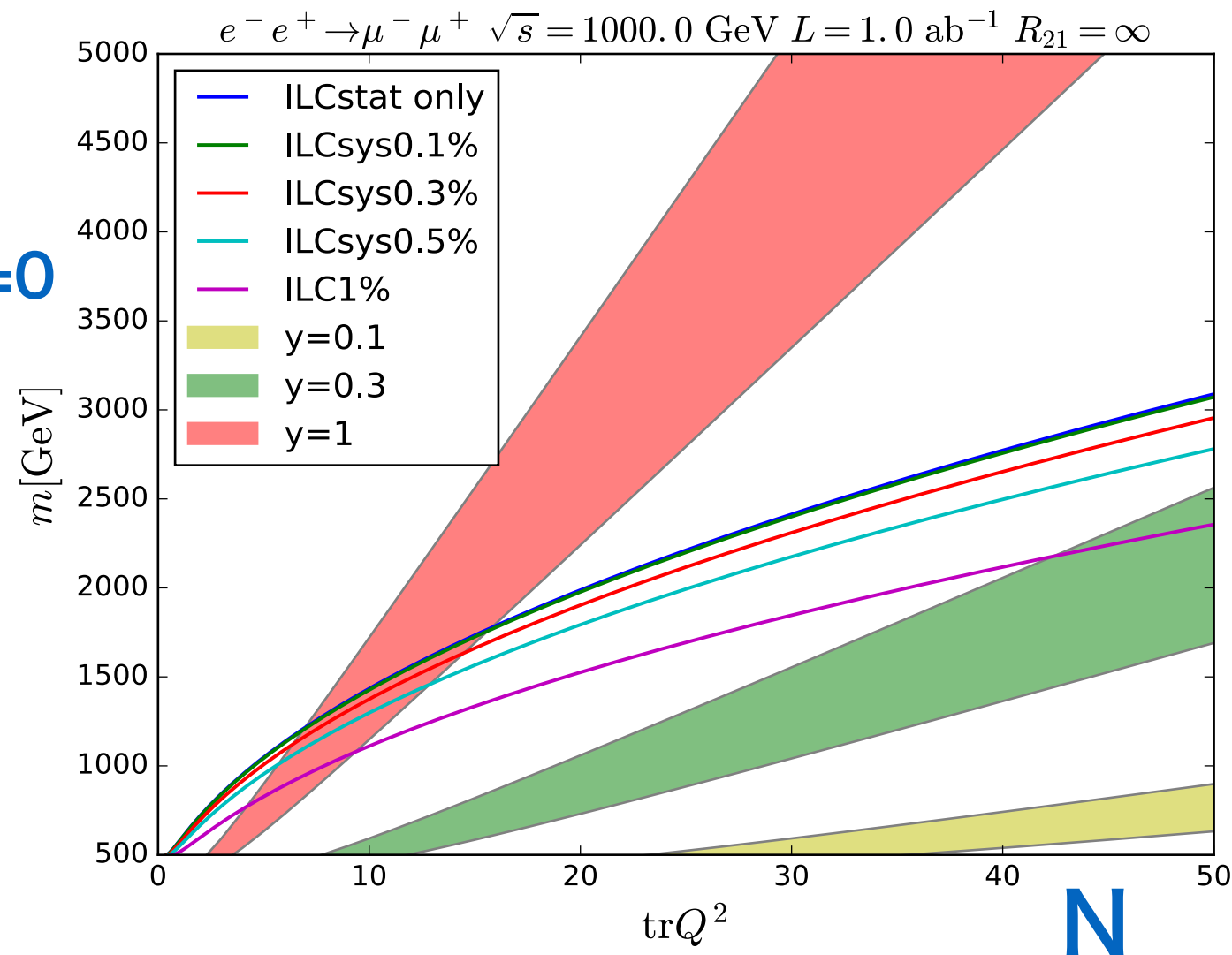
Mass reach

- Expected mass reach (95% C.L.)
- New particle: SU(2) triplet (**$n=3$**), **$Y=0$**
- $\sqrt{s} = 1 \text{ TeV}$
- $m > \sqrt{s}/2$ can be probed!
- (Shaded region is favored by the diphoton excess)



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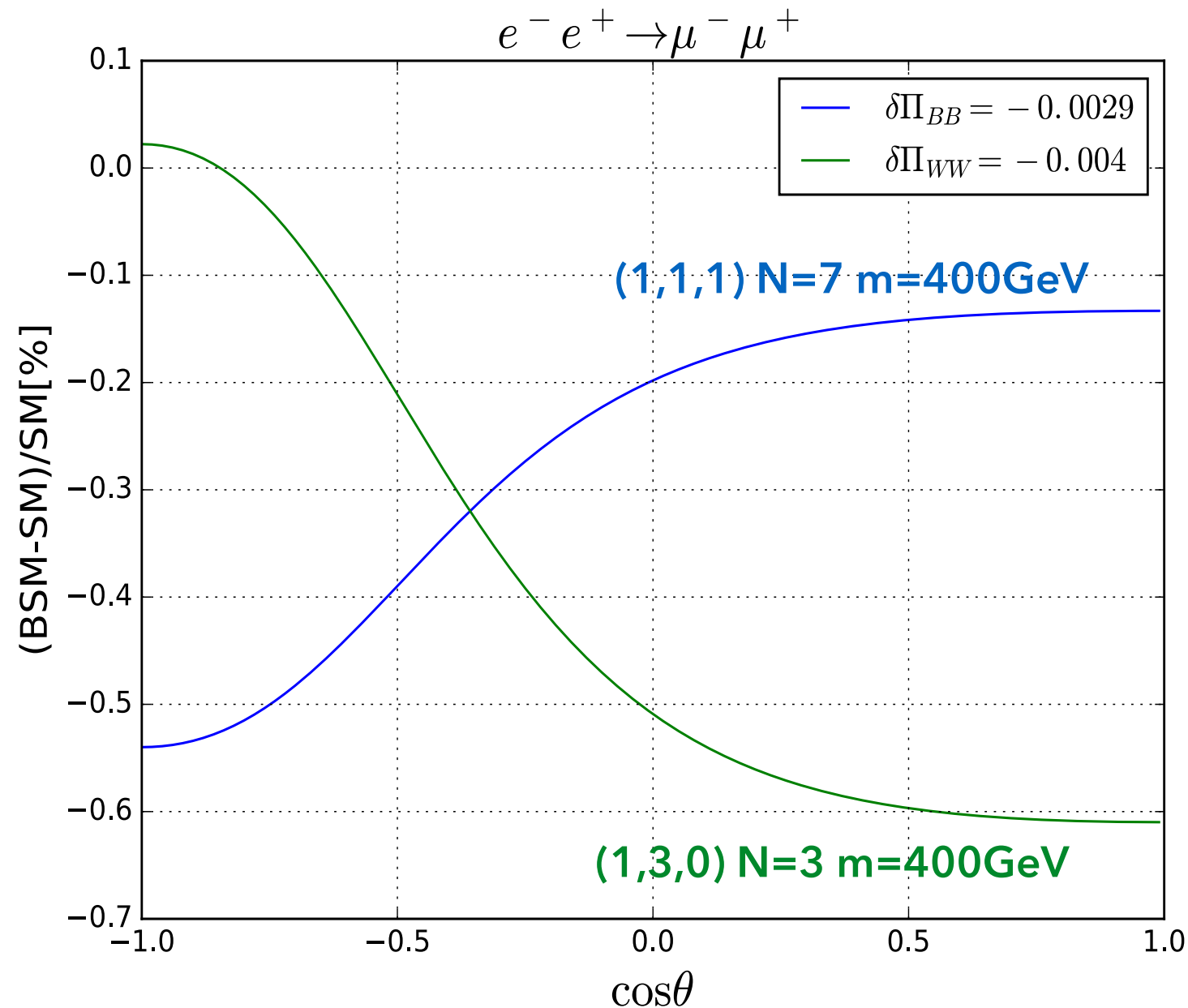
How about quantum number of $SU(2)_L \times U(1)_Y$?

Is it possible to **discriminate different BSM particles?**

Angular distribution

- The deviation of the differential cross section from SM
- $e^+e^- \rightarrow \mu^+\mu^-$ process
- **Angular distribution is different** for different quantum number

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$P_+ = +30\%$ $P_- = -80\%$ (Beam polarization)

$\sqrt{s} = 500 \text{ GeV}$ (Beam energy)

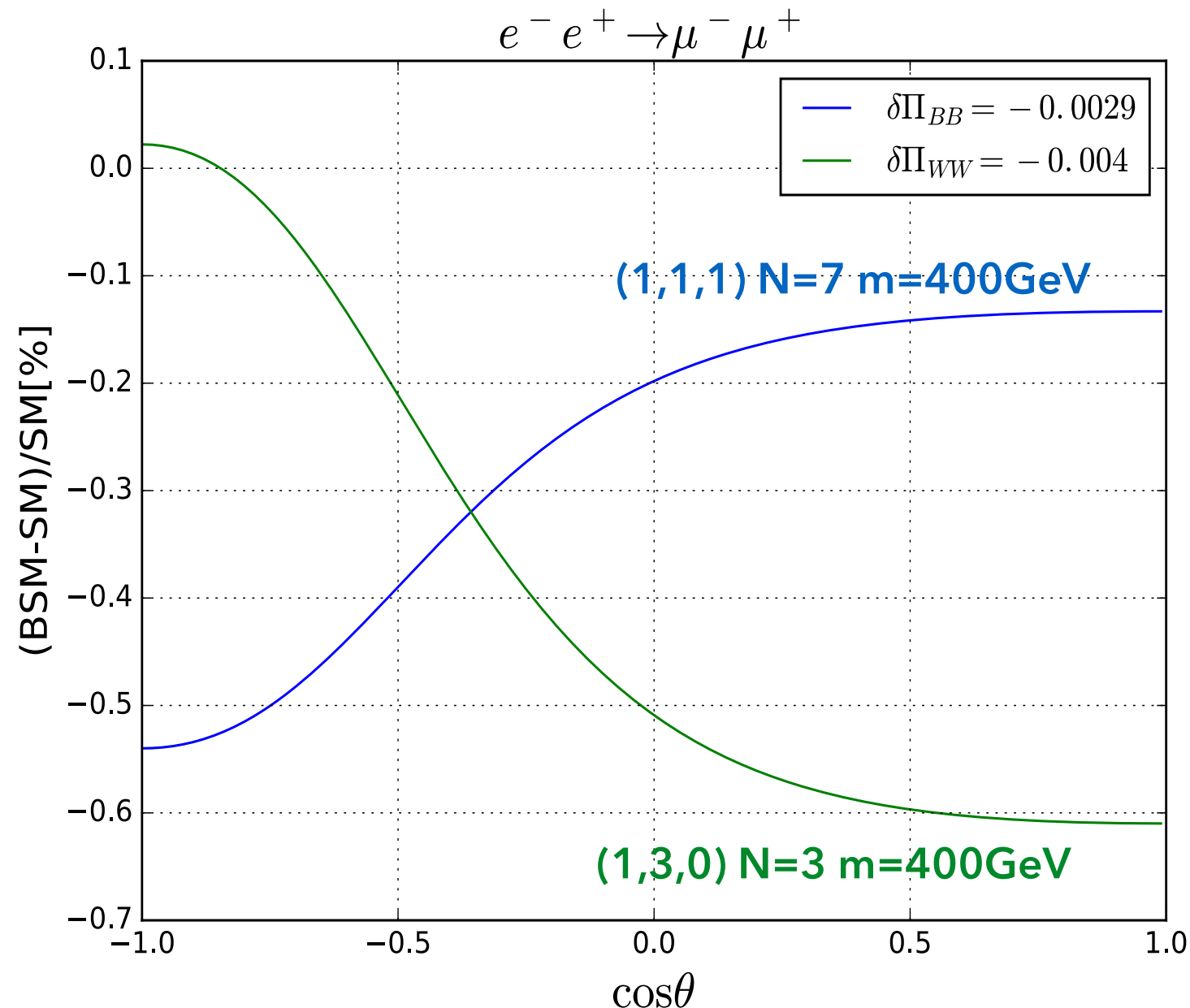
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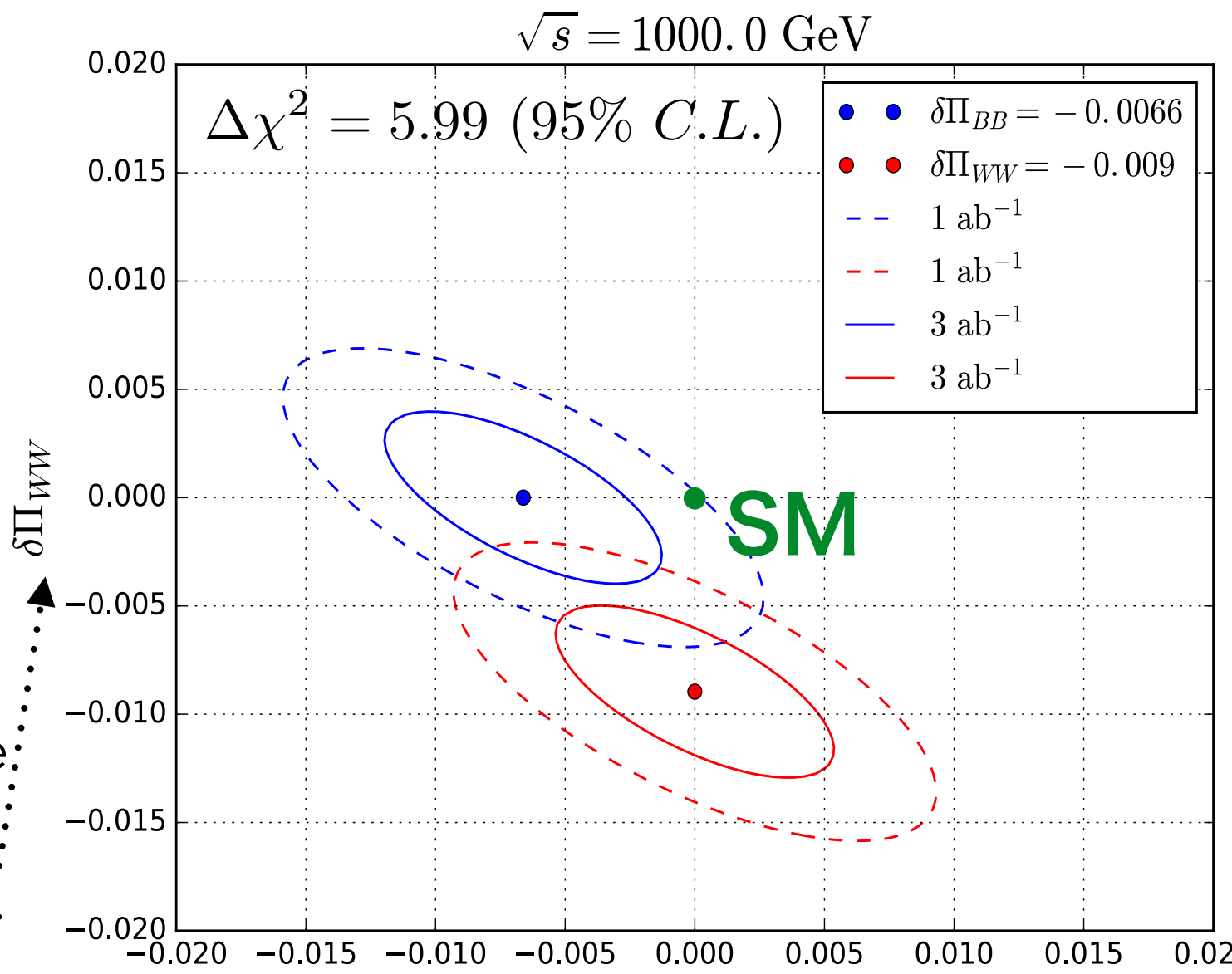
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SU(2)_L vs. U(1)_Y

- $\delta\Pi_{WW}, \delta\Pi_{BB}$ are the vacuum polarizations of new particles
- Each point corresponds to a new physics model
- Integrated luminosity **1 ab⁻¹** and **3 ab⁻¹** are considered
- **SM+U(1)_Y** or **SM+SU(2)_L** can be distinguished from **models outside the contour** at 95 % C.L.:

$$\delta\Pi_{WW} = \begin{array}{c} \psi \\ \circlearrowleft \\ W \quad W \end{array}$$

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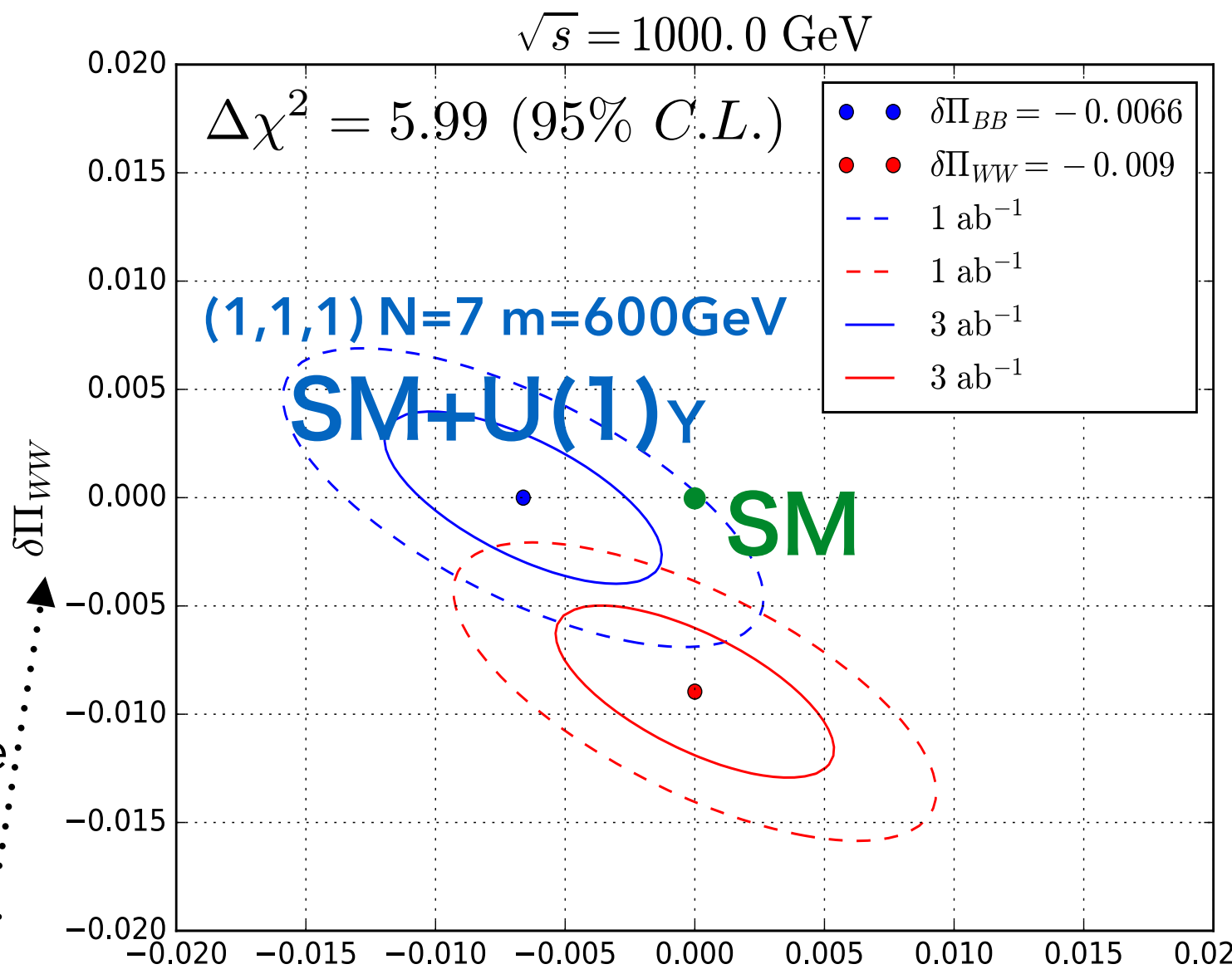


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$$\delta\Pi_{WW} = \text{Diagram: A fermion loop with a fermion line labeled } \psi \text{ and two external wavy lines labeled } W.$$

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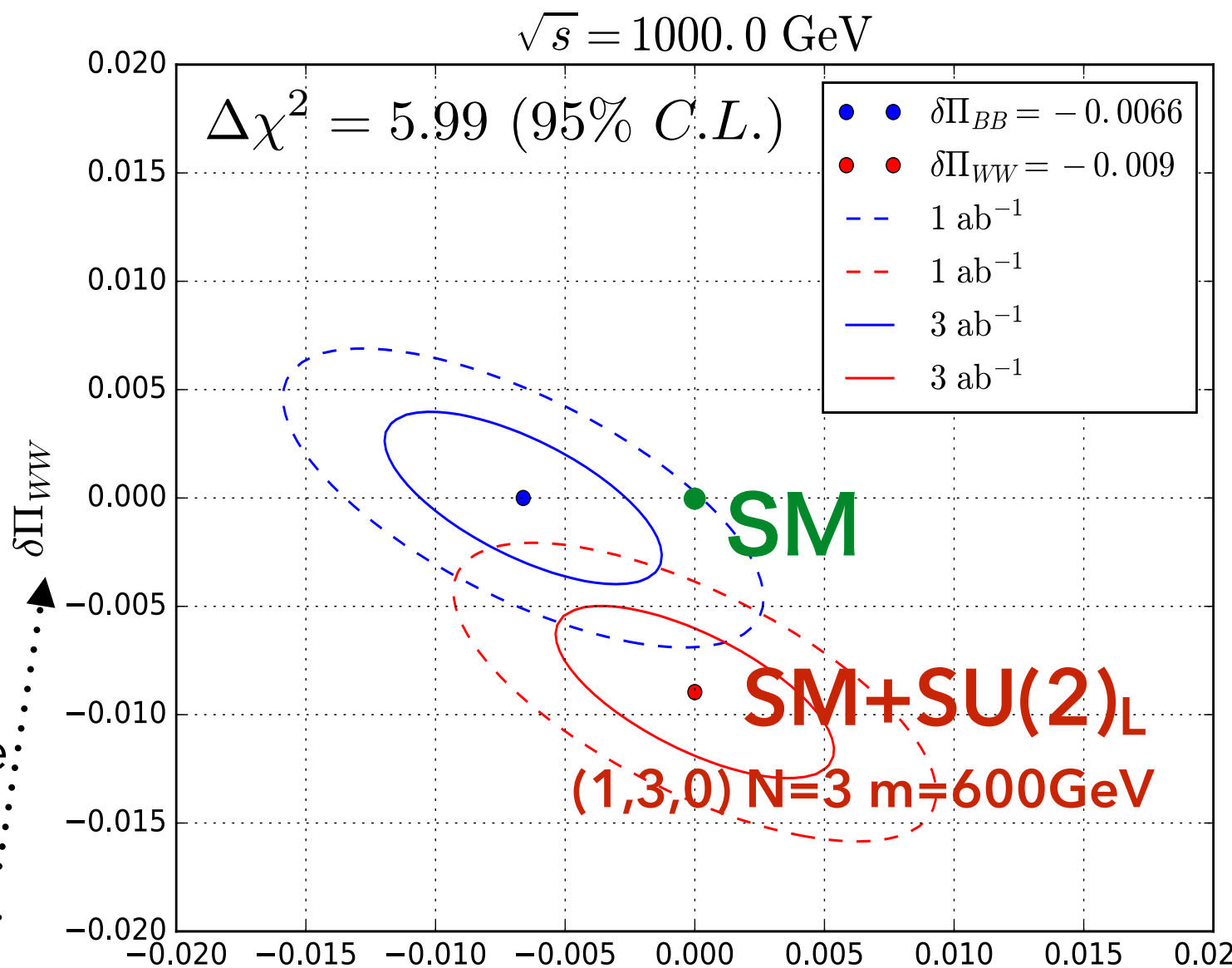


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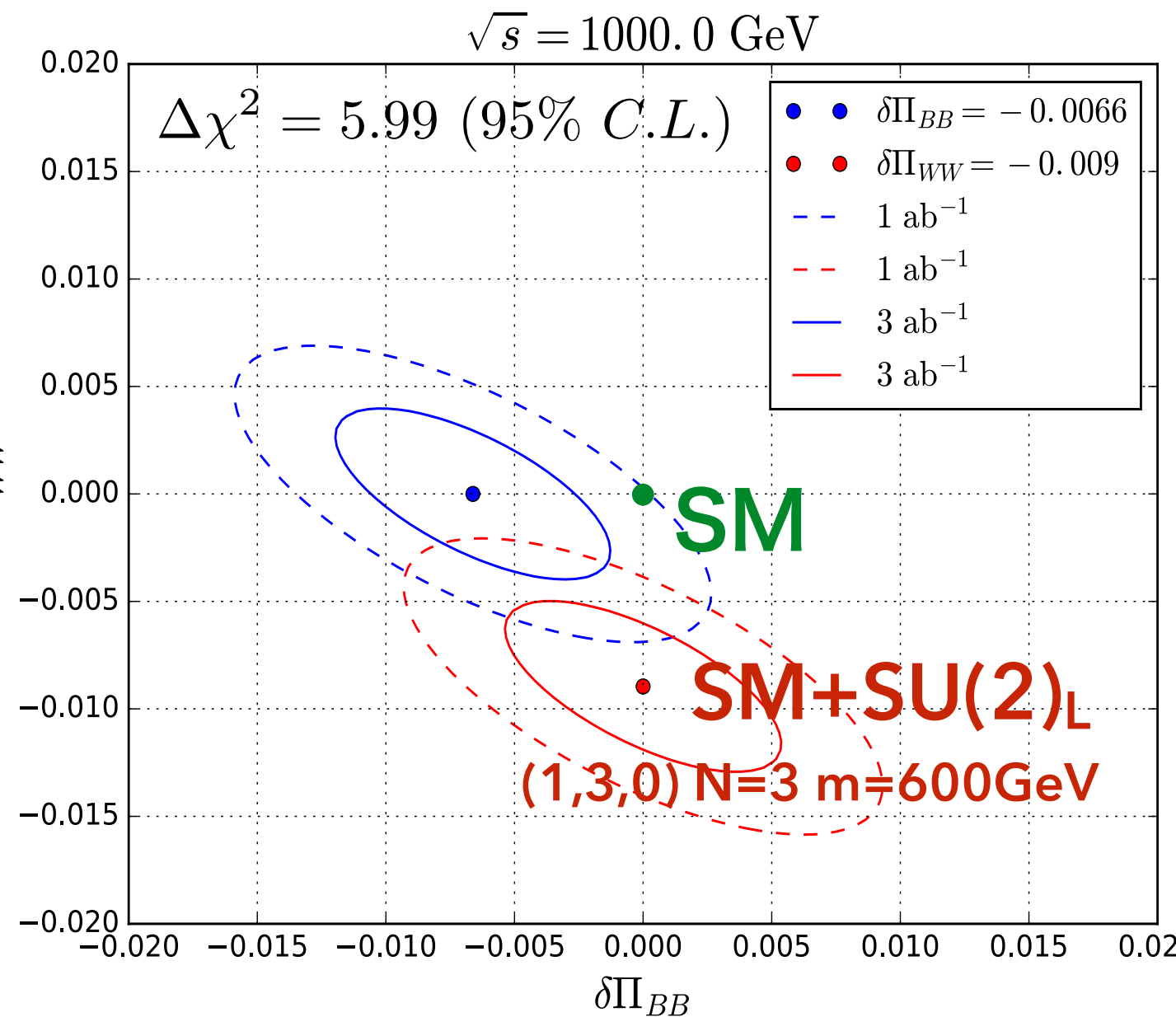
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It is possible to **discriminate $SU(2)_L \times U(1)_Y$ quantum number!**

Summary

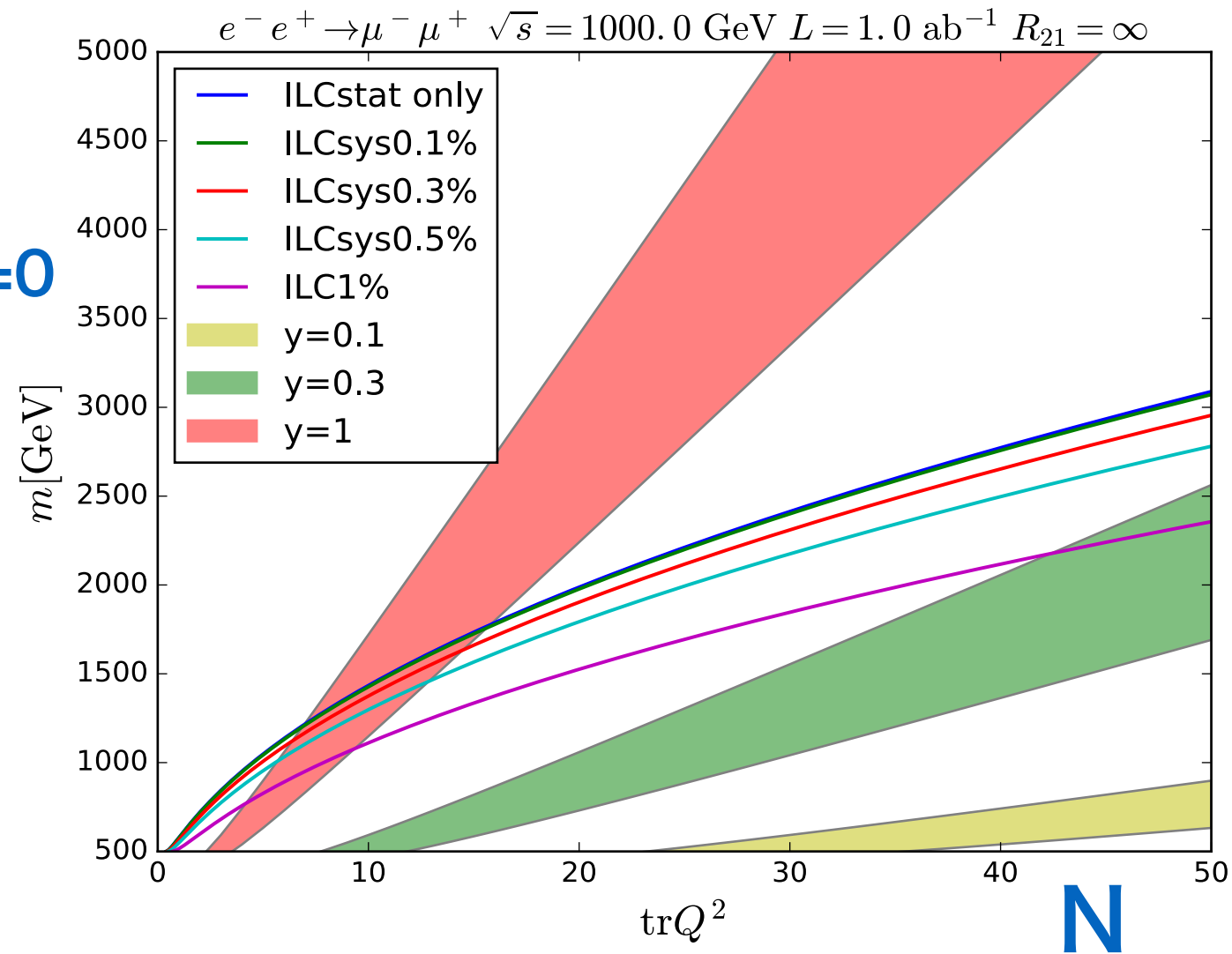
Precision measurement of the process $e^+e^- \rightarrow f\bar{f}$ provides a clue for the beyond standard physics.

1. We can probe new charged fermions **even when they are out of kinematical reach** at the ILC.
2. We can **discriminate $SU(2)_L \times U(1)_Y$** quantum numbers of the new particles by **studying the angular distribution** at the ILC.

Backup

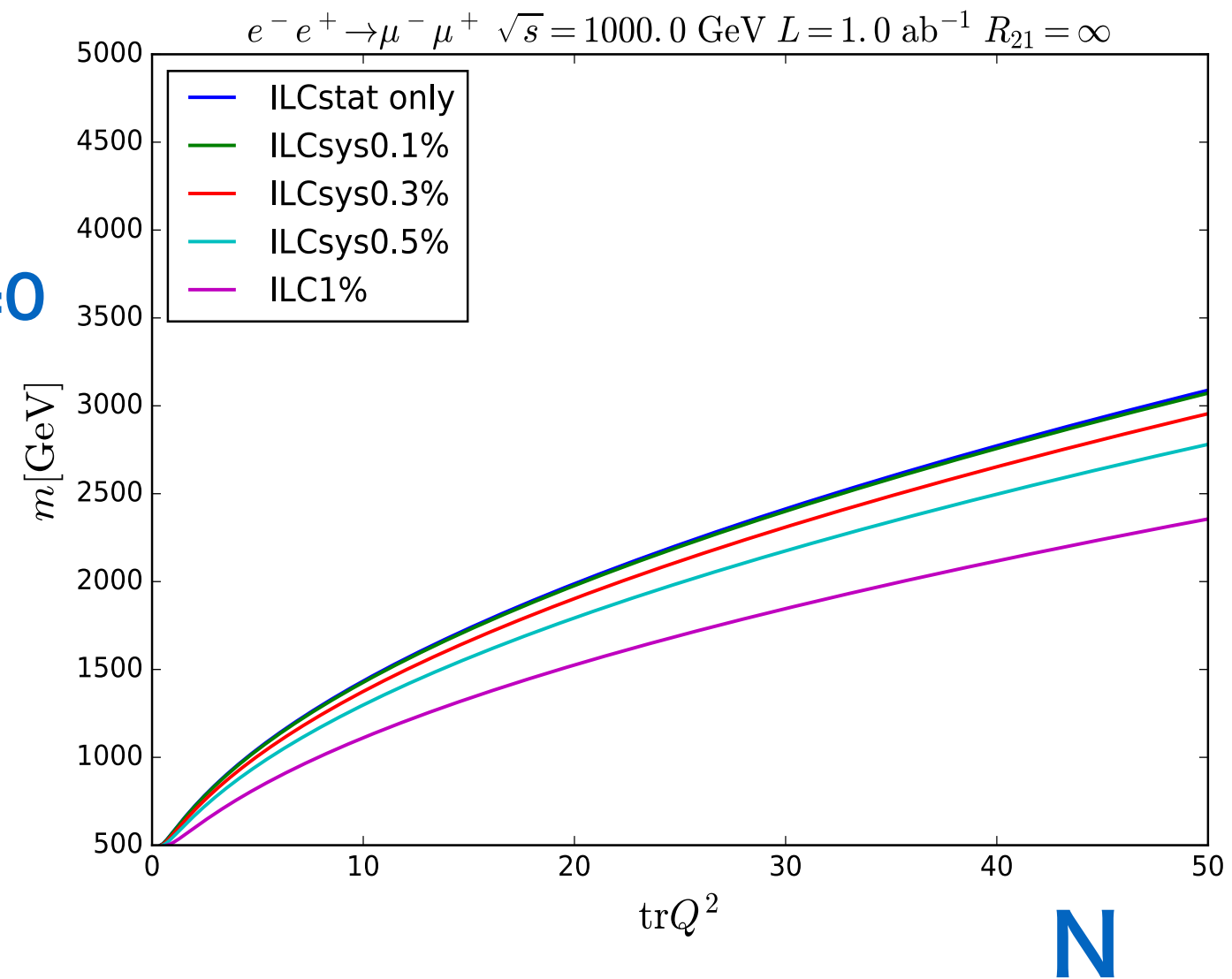
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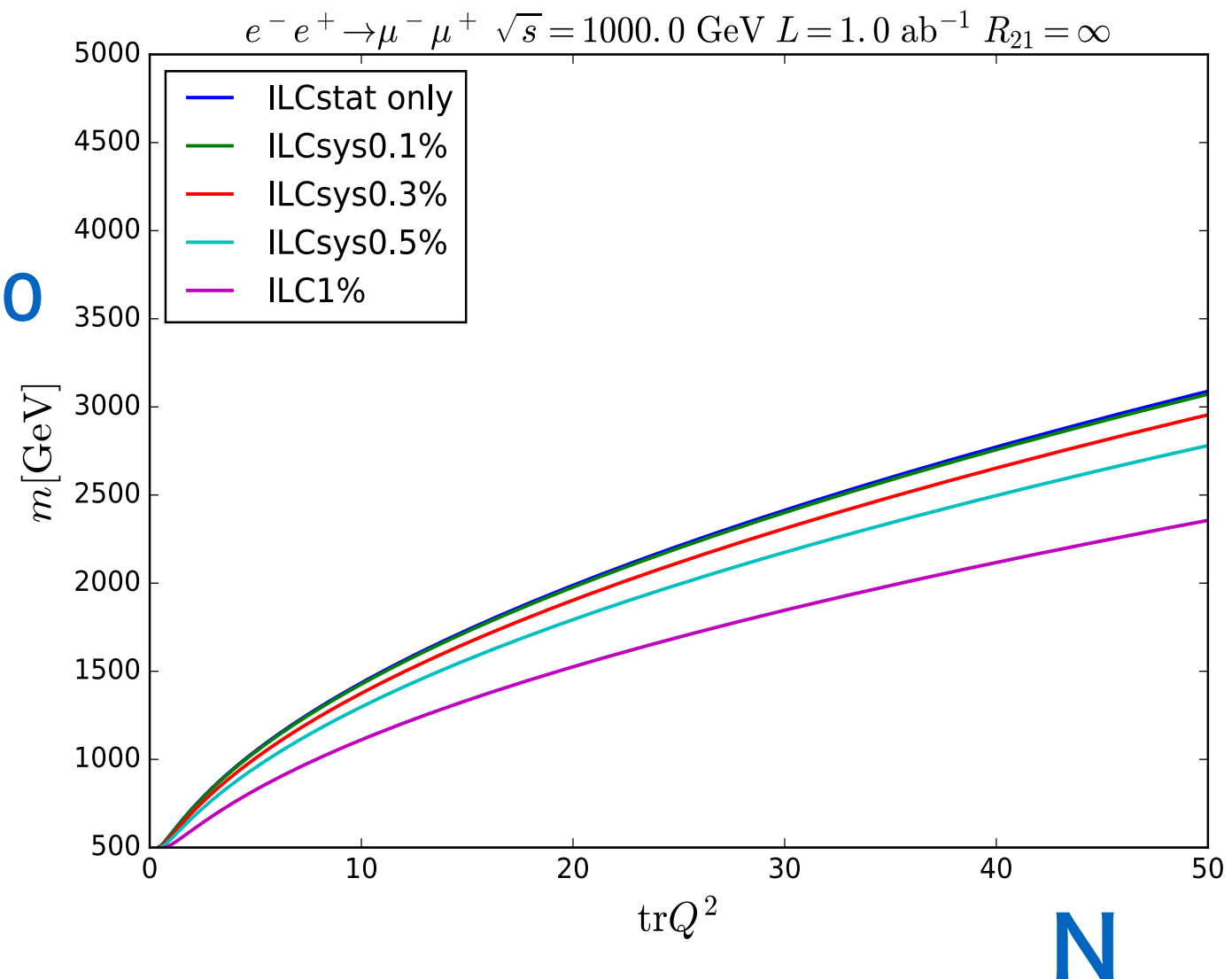
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How about quantum number of $SU(2) \times U(1)$?

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750 GeV diphoton Excess (1)

SM + **singlet** pseudo-scalar (750GeV) + **charged** scalars/fermions

$$\mathcal{L}_\psi = \sum_i \bar{\psi}_i (i \not{D} - m) \psi_i - i \sum_i y S \bar{\psi}_i \gamma_5 \psi_i$$

Narrow width approximation:

$$\sigma(pp \rightarrow S \rightarrow \gamma\gamma) \simeq \frac{C_{gg}}{s m_S} \Gamma(S \rightarrow \gamma\gamma)$$

Assuming

$$\sqrt{s} = 13 \text{ TeV} \quad \sigma = 3 - 10 \text{ fb} \quad C_{gg} \simeq 2.1 \times 10^3 \quad m_S = 750 \text{ GeV}$$

Decay width

$$\Gamma(S \rightarrow \gamma\gamma) = 0.45 - 1.5 \text{ MeV}$$

is necessary.

750 GeV diphoton excess (2)

Functions

$$C_{gg} = (\pi^2/8) \int_0^1 dx_1 \int_0^1 dx_2 \delta(x_1 x_2 - m_S^2/s) g(x_1) g(x_2)$$

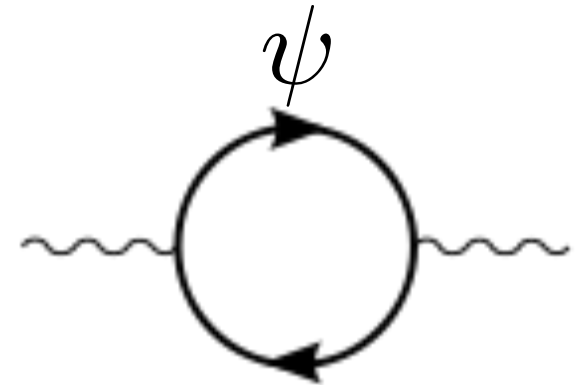
$$\Gamma(S \rightarrow \gamma\gamma) \simeq \frac{\alpha^2}{256\pi^3} m_S^3 \left[\frac{y}{m} \text{tr} Q^2 L \left(\frac{m_S^2}{4m^2} \right) \right]^2$$

$$L(\tau) = \begin{cases} 2\tau^{-2} (\tau + (\tau - 1) \arcsin^2 \sqrt{\tau}) & \text{for scalar } S, \\ 2\tau^{-1} \arcsin^2 \sqrt{\tau} & \text{for pseudo-scalar } S, \end{cases}$$

$$\text{tr} Q^2 = N \left[\frac{n(n-1)(n+1)}{12} + nY^2 \right]$$

Vacuum polarization

$$\delta\Pi_{VV}(q^2, m^2) \equiv \frac{1}{2}g_V^2 C_{VV} I(q^2/m^2)$$



$$C_{WW} = \frac{4}{3}Nn(n-1)(n+1),$$

$$C_{BB} = 16nNY^2.$$

$$I(x) \equiv \frac{1}{16\pi^2} \int_0^1 dy \, y(1-y) \ln(1-y(1-y)x) \quad \text{for fermion}$$

$$I(x) \equiv \frac{1}{16\pi^2} \int_0^1 dy \, (1-2y)^2 \ln(1-y(1-y)x) \quad \text{for scalar}$$

Particle representation

Electromagnetic charge can be written as follows,

$$\text{tr} Q^2 = \frac{1}{16} (C_{WW} + C_{BB})$$

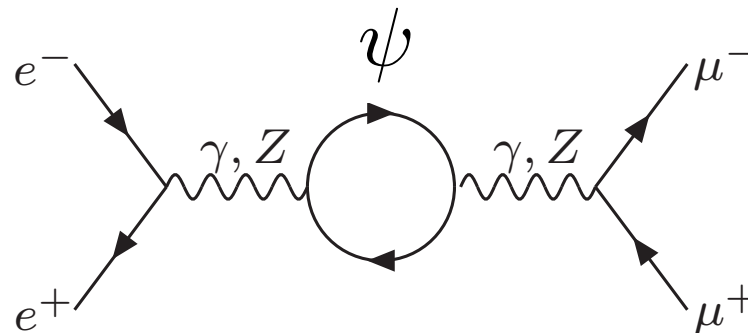
We parametrize the ratio of SU(2) and U(1) by

$$R_{21} \equiv C_{WW}/C_{BB} = \frac{n^2 - 1}{12Y^2}$$

Amplitudes (1)

$e^+e^- \rightarrow \mu^+\mu^-$ matrix element

$$\mathcal{M}^{\text{SM},\psi}(e_h^- e_h^+ \rightarrow \mu_{h'}^- \mu_{h'}^+) = \sum_{V,V'=\gamma,Z} C_{e_h V} C_{\mu_{h'} V'} D_{VV'}^{\text{SM},\psi}(s) [\bar{u}_{h'} \gamma^\mu v_{h'}] [\bar{v}_h \gamma_\mu u_h]$$



Coupling to gauge boson

$$C_{e_L Z} = C_{\mu_L Z} = g_Z (-1/2 + \sin^2 \theta_W),$$

$$C_{e_R Z} = C_{\mu_R Z} = g_Z \sin^2 \theta_W,$$

$$C_{e_L \gamma} = C_{e_R \gamma} = C_{\mu_L \gamma} = C_{\mu_R \gamma} = -e$$

$$g_Z = e/(\sin \theta_W \cos \theta_W)$$

Amplitude (2)

Photon and Z boson propagator

$$D_{VV'}^{\text{SM}}(q^2) = \frac{\delta_{VV'}}{q^2 - m_V^2},$$

$$D_{VV'}^{\psi}(q^2) = \frac{q^2}{(q^2 - m_V^2)(q^2 - m_{V'}^2)} \delta\Pi_{VV'}(q^2, m)$$

where,

$$\delta\Pi_{\gamma\gamma}(q^2, m) = \delta\Pi_{WW}(q^2, m) \sin^2 \theta_W + \delta\Pi_{BB}(q^2, m) \cos^2 \theta_W,$$

$$\delta\Pi_{ZZ}(q^2, m) = \delta\Pi_{WW}(q^2, m) \cos^2 \theta_W + \delta\Pi_{BB}(q^2, m) \sin^2 \theta_W,$$

$$\delta\Pi_{\gamma Z}(q^2, m) = [\delta\Pi_{WW}(q^2, m) - \delta\Pi_{BB}(q^2, m)] \sin \theta_W \cos \theta_W$$