

# **Muon g-2, Dark Matter and MSSM**

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Univ. of Tokyo

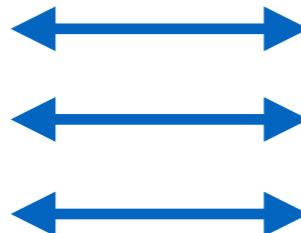
Preliminary work with M. Endo, S. Iwamoto, and K. Hamaguchi

# Physics beyond the SM

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Many hints!

- Hierarchy problem
- Dark Matter
- Muon g-2 ( $> 3\sigma$ )
- Baryon asymmetry, neutrino mass, GUT, etc...



## Supersymmetry

- Cancellation of loop correction
- Neutralino WIMP DM
- Neutralino/chargino - smuon loop

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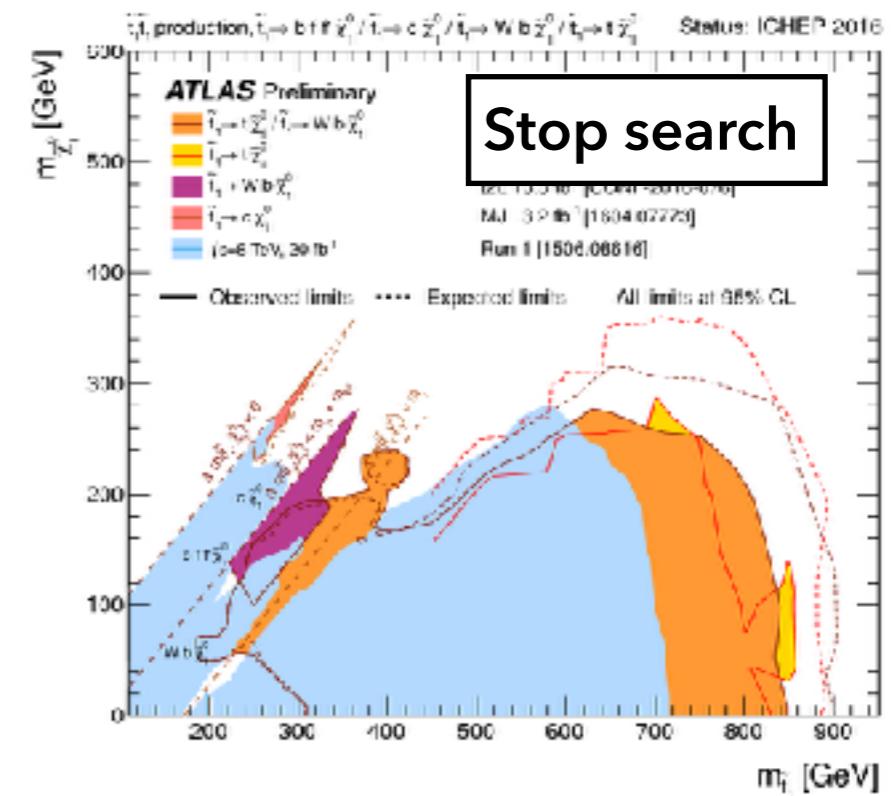
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- Colored superparticles  $> \mathcal{O}(1)$  TeV
- MSSM cannot solve EW hierarchy

Little hierarchy problem



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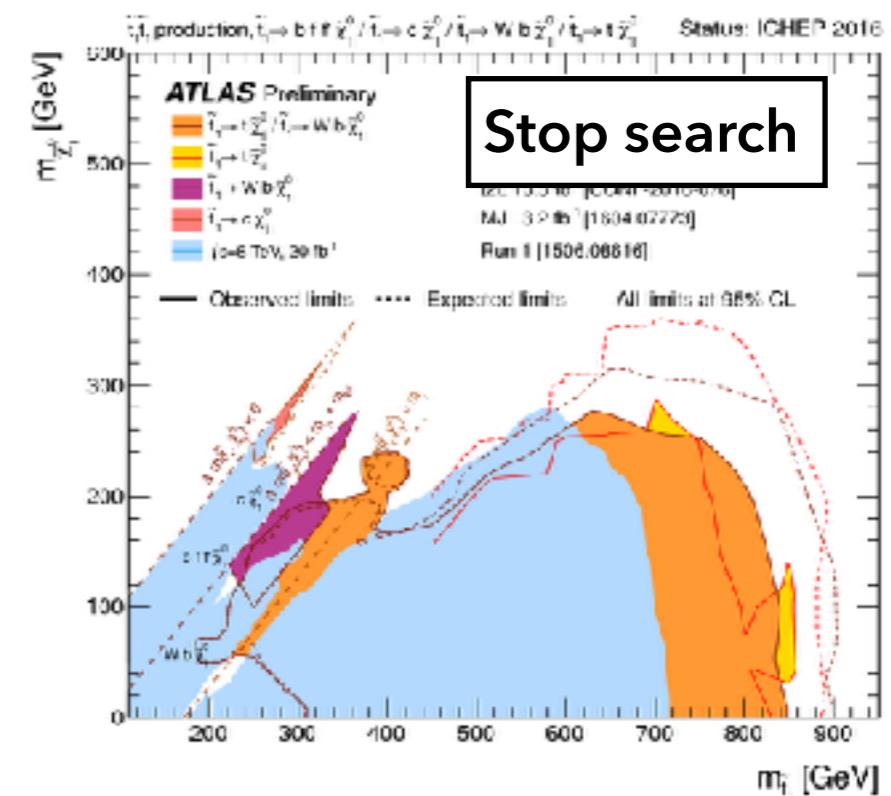
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But still,

SUSY can solve DM and Muon g-2 anomaly

Phenomenologically, SUSY is still attractive!



# Muon g-2 and DM in MSSM

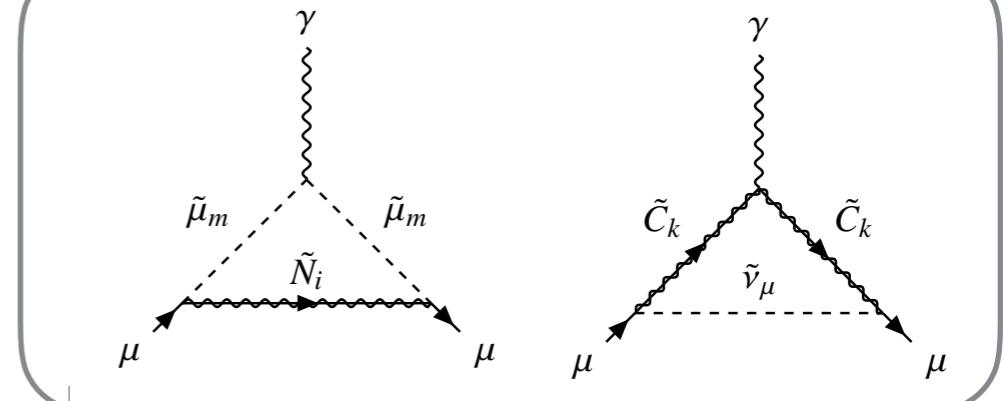
- 3 $\sigma$  discrepancy of muon g-2 between SM and the experiment

$$a_\mu(\text{exp}) - a_\mu(\text{SM}) = (261 \pm 80) \times 10^{-11}$$

[Hagiwara et.al. 2011]

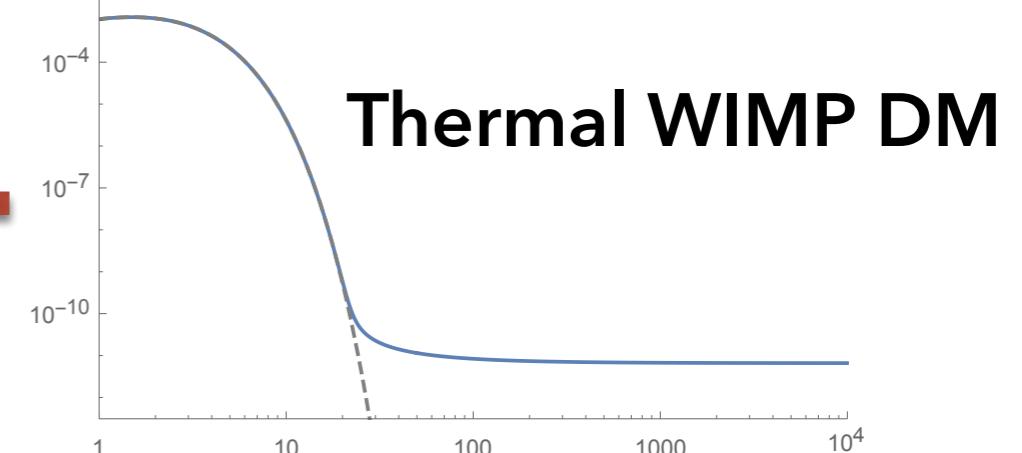
## MSSM

New loop contribution



- DM abundance today

$$\Omega_{\text{DM}} h^2 = 0.12$$



100 GeV - 1 TeV **neutralino/chargino** and **smuon** is necessary

bounds are not so strict as colored ones

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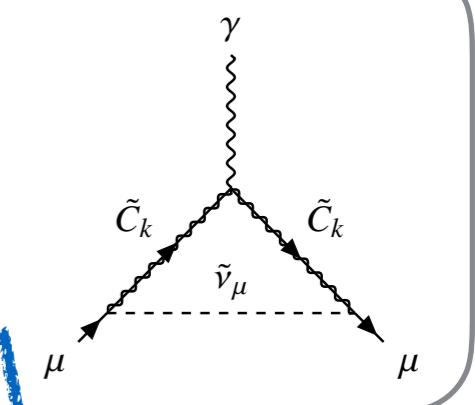
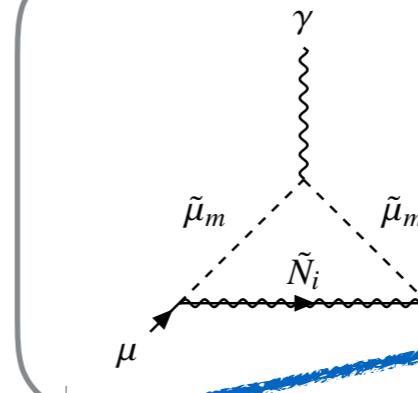
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Detectable by future experiments?

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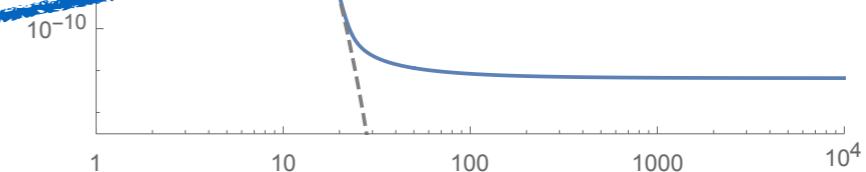
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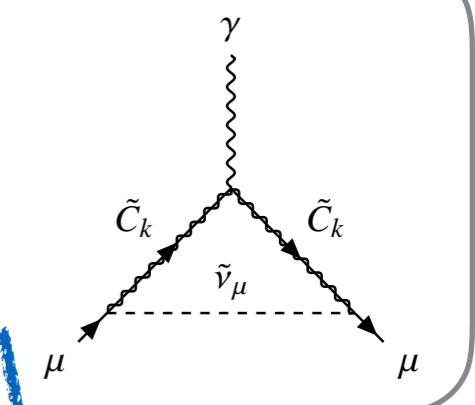
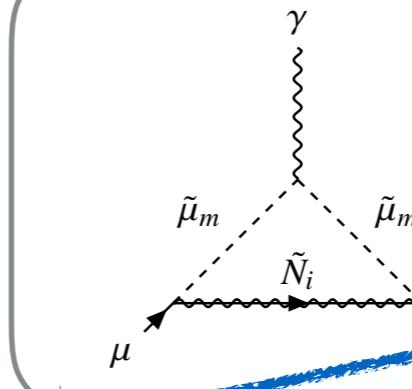
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Messages

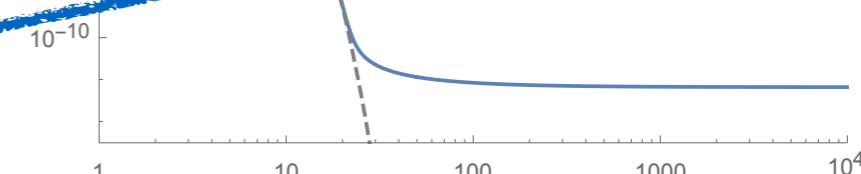
LHC or DM direct detection are not enough to study the parameter space!

## MSSM

New loop contribution



I WIMP DM



- 1. DM in each g-2 scenario**
- 2. Experimental bounds (Direct detection, LHC, ILC)**
- 3. Results**

# MSSM spectrum

---

Model-independent approach motivated by g-2 and DM

R-parity is conserved

- Slepton
  - Bino, Wino
  - Higgsino
  - Squark
  - Gluino
  - Heavy Higgs
- Neutralino DM**
- Muon g-2**
- Irrelevant**
- 
- ```
graph TD; A["Slepton  
Bino, Wino  
Higgsino"] --> B["Neutralino DM"]; C["Squark  
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```

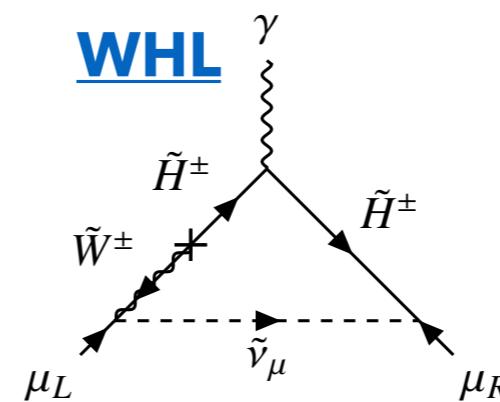
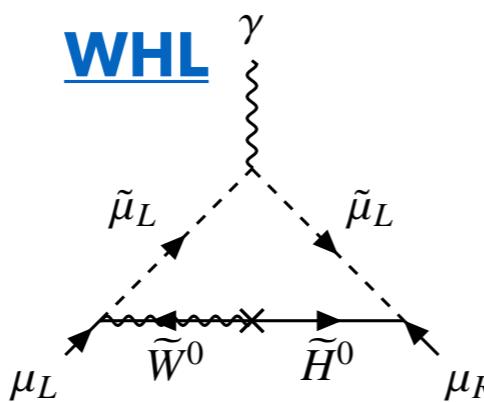
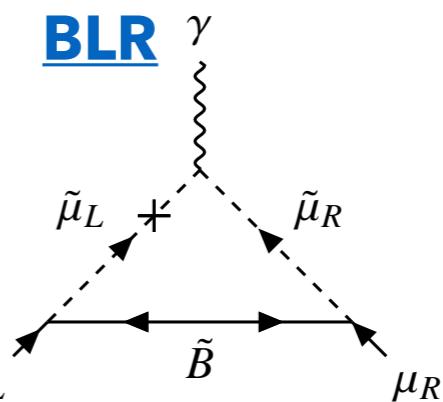
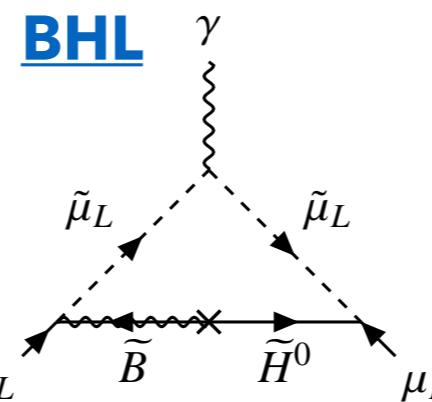
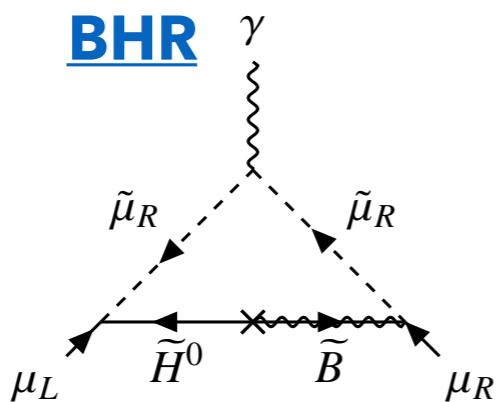
$$m_{H^0, \pm}, m_{A^0}, m_{\tilde{g}}, m_{\tilde{q}}, \gg m_{\tilde{N}}, m_{\tilde{C}^\pm}, m_{\tilde{l}}$$

We consider **only slepton, bino, wino, Higgsino**  
parameters:  **$M_1, M_2, \mu, m_L, m_R, \tan\beta$**

# Our strategy

We classify SUSY contribution to g-2 into 4 scenarios

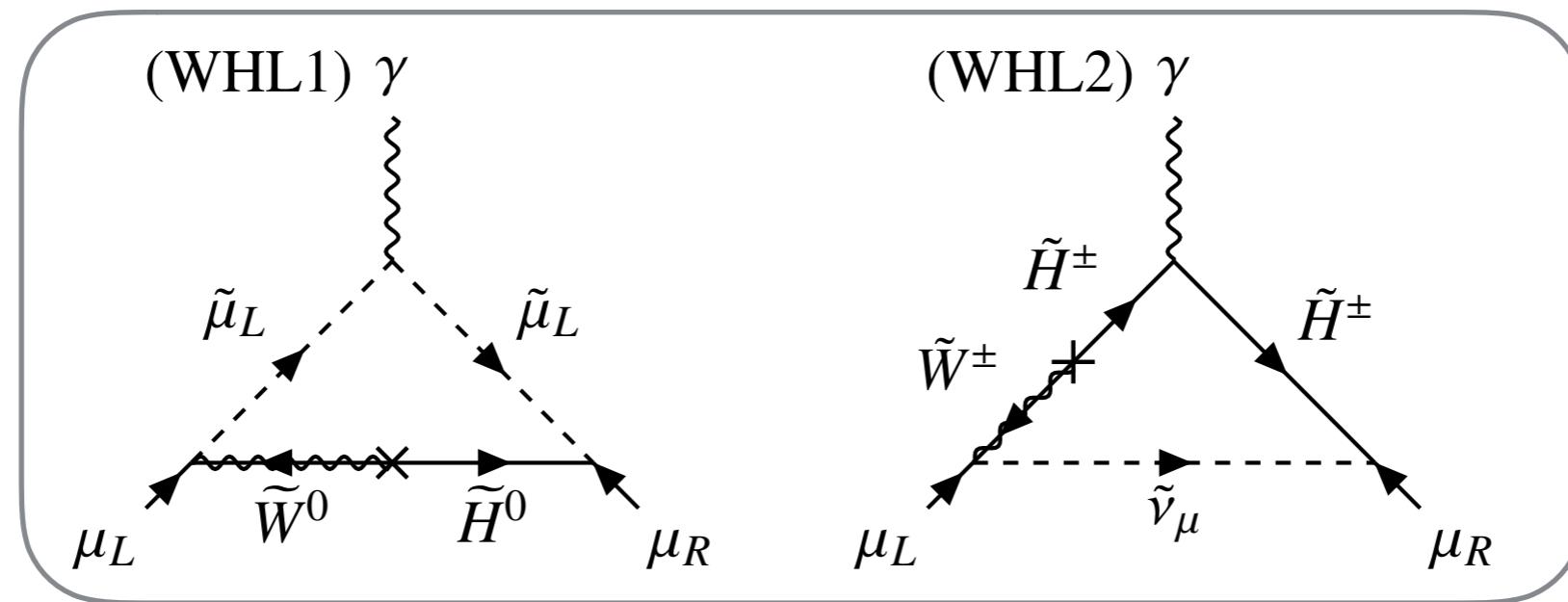
5 diagrams, 4 scenarios in gauge eigenstates  
(for large  $\tan\beta$ )



Is it possible to obtain DM abundance  $\Omega_{\text{DM}} h^2 = 0.12$  in each scenario ??

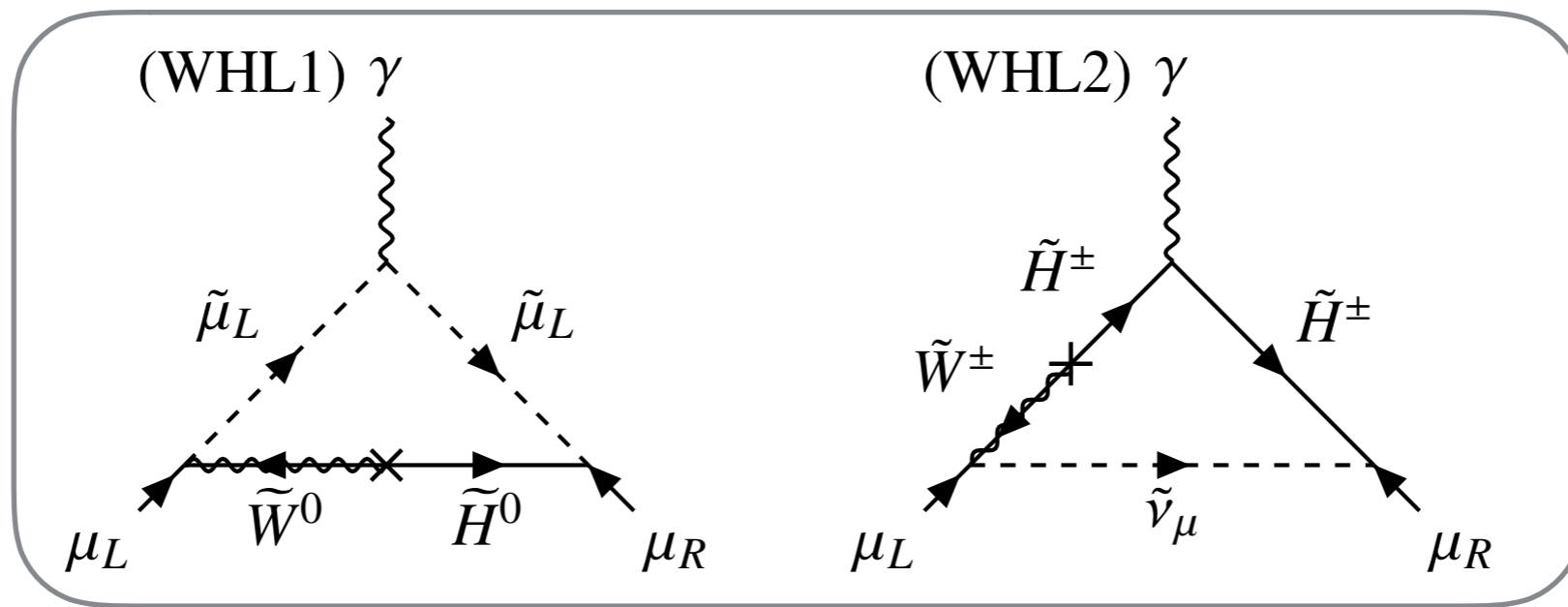
# DM in WHL scenario

- Wino, Higgsino, Left-handed smuon/sneutrino ( $\tilde{W}$ ,  $\tilde{H}$ ,  $\tilde{\mu}_L$ ,  $\tilde{\nu}_\mu$ )
- Assume  $M_2, \mu, m_L \ll M_1, m_R$



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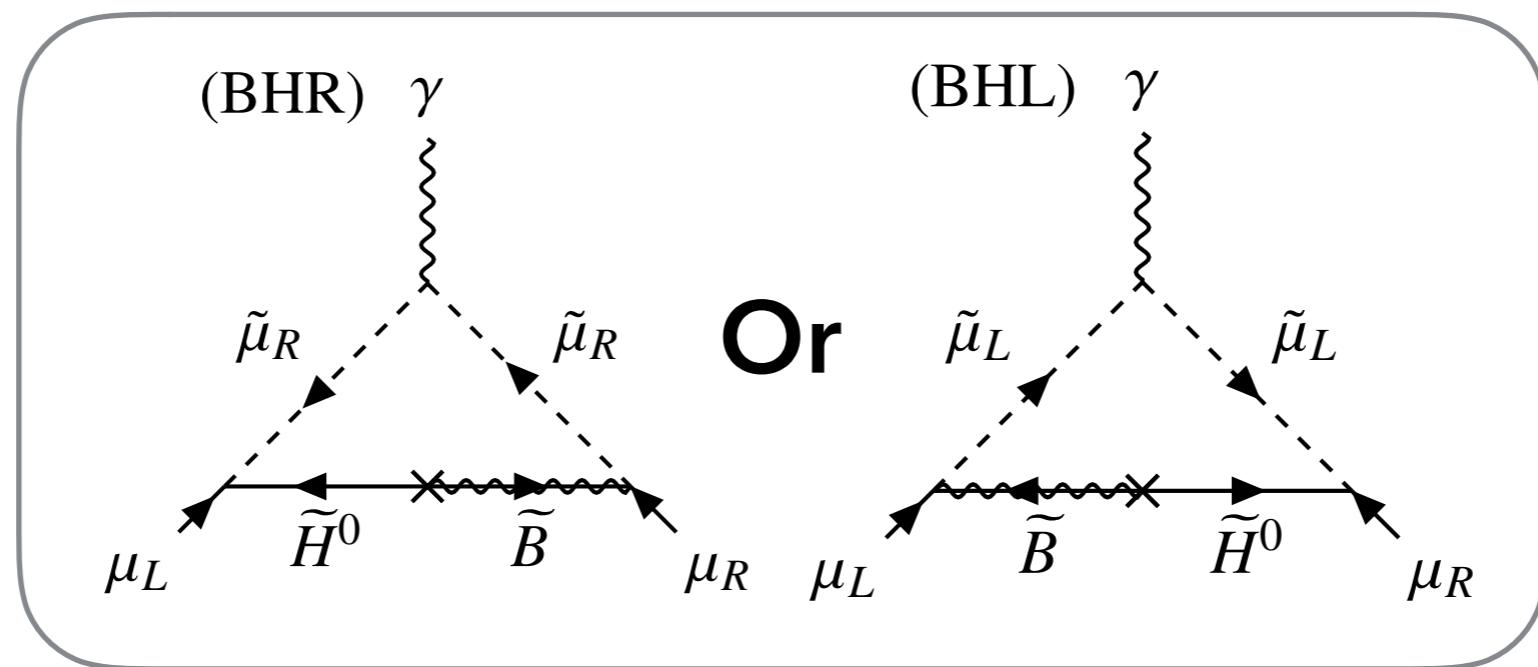


- For DM,  $M_2 \sim 3$  TeV (Wino DM), or  $\mu \sim 1$  TeV (Higgsino DM)
- But then,  $a_\mu(\text{WHL}) \ll \delta a_\mu = 261 \times 10^{-11}$
- $a_\mu(\text{WHL}) = 5.6 \times 10^{-11}$  ( $M_2 = \mu = m_R = 3$  TeV,  $\tan\beta=40$ )
- $a_\mu(\text{WHL}) = 50 \times 10^{-11}$  ( $M_2 = \mu = m_R = 1$  TeV,  $\tan\beta=40$ )

No solution...

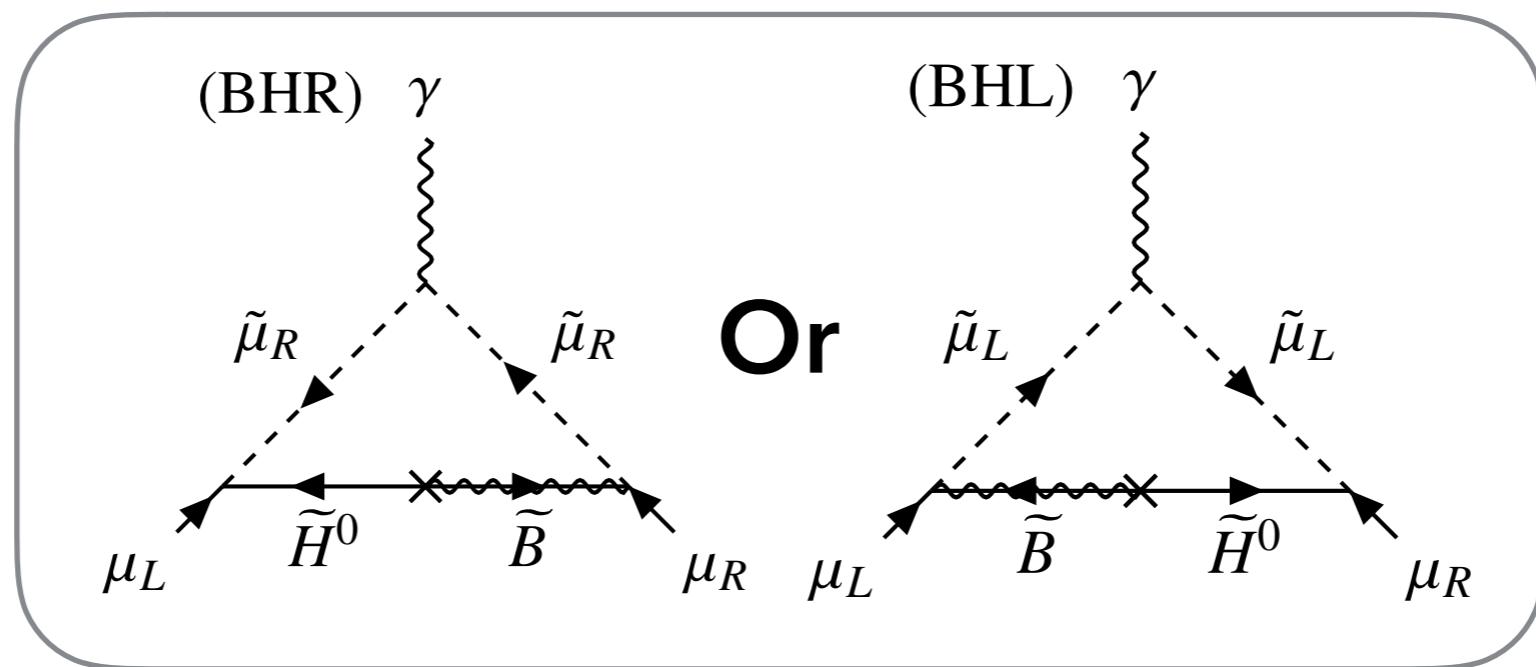
# DM in BHR or BHL scenario

- Bino, Higgsino, Right- or Left-handed smuon  $(\tilde{B}, \tilde{H}, \tilde{\mu}_R)$   $(\tilde{B}, \tilde{H}, \tilde{\mu}_L)$
- $M_1, \mu, m_R \ll M_2, m_L$  (BHR)
- $M_1, \mu, m_L \ll M_2, m_R$  (BHL)



# DM in BHR or BHL scenario

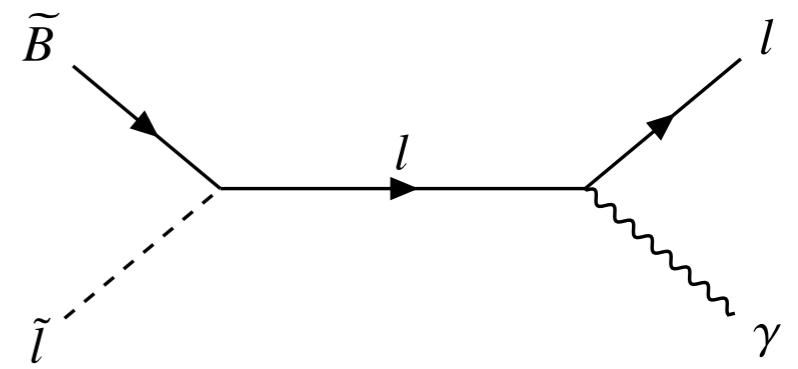
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- Bino DM is usually overproduced...
- **Bino-slepton coannihilation gives**

$$\Omega_{\text{Bino}} h^2 = \Omega_{\text{DM}} h^2$$

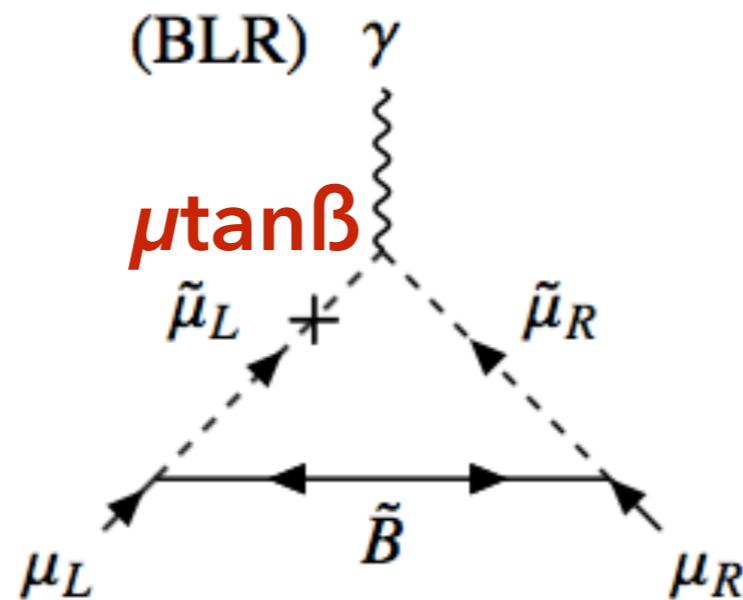
$$m_{\tilde{l}} - m_{\tilde{B}} \sim 10 \text{ GeV}$$



# DM in BLR scenario

---

- Bino, Left- and right-handed smuon  $(\tilde{B}, \tilde{\mu}_L, \tilde{\mu}_R)$
- Parameters:  $M_1, \mu, m_L, m_R$
- Looks similar to BHR or BHL

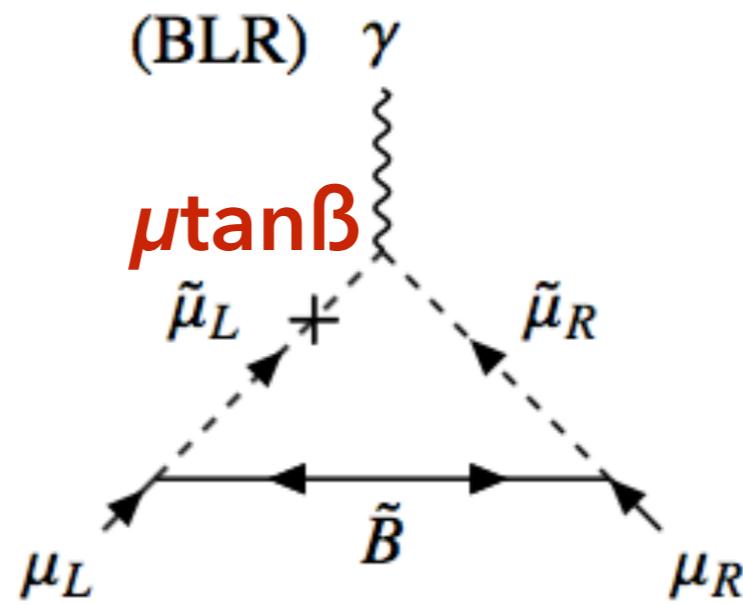


- $a_\mu(\text{BLR}) \propto \mu \tan \beta$
- Large  $\mu \tan \beta$  destabilize our vacuum
- Analysis becomes qualitatively different...

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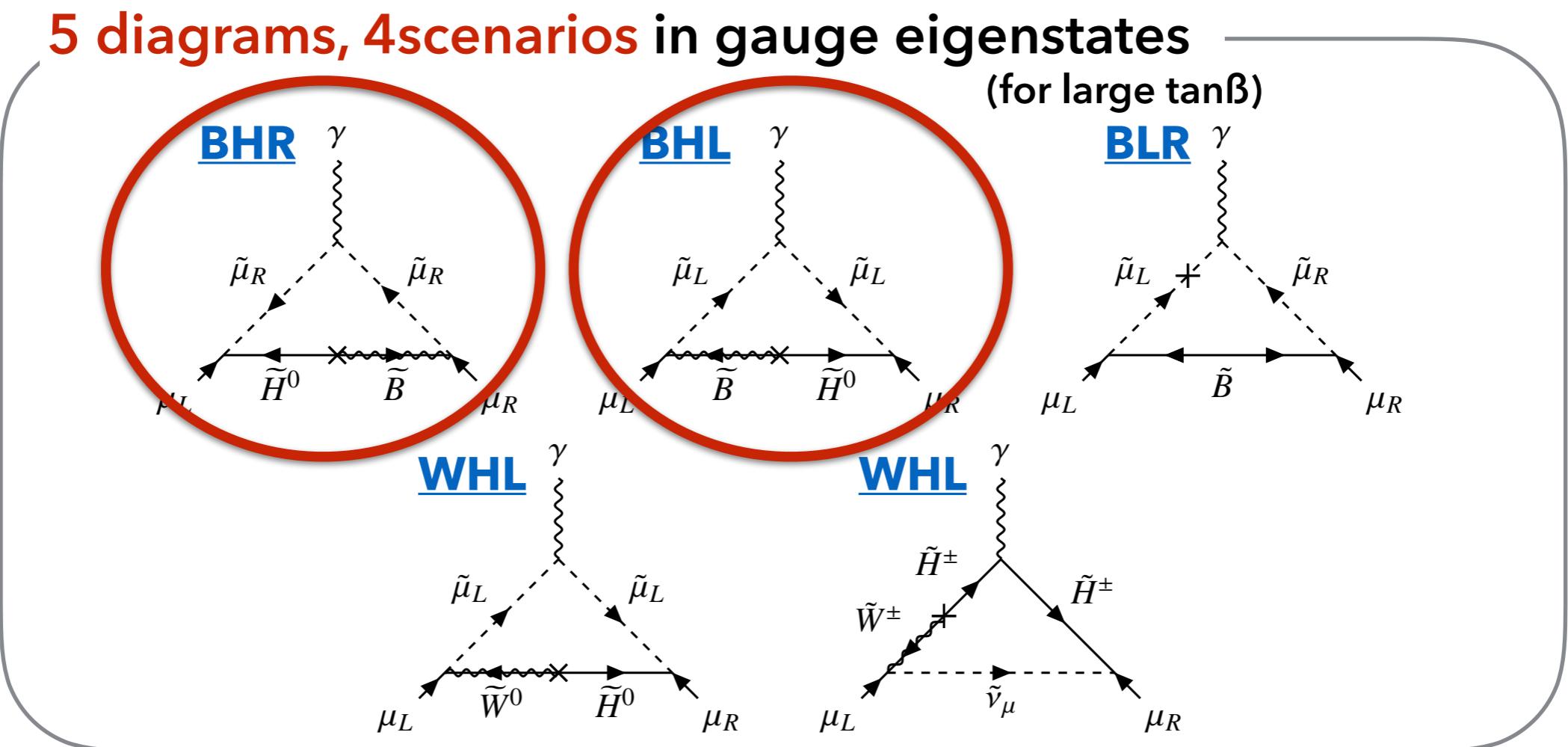


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Future work

# Our strategy

We can classify SUSY contribution to g-2 into 4 scenarios



We focus on BHR and BHL scenarios

1. DM in each g-2 scenario
2. Experimental bounds (Direct detection, LHC, ILC)
3. Results

# Various experimental inputs

---

## DM direct detection

$$(\tilde{B}, \tilde{H}, \tilde{\mu}_R) \quad (\tilde{B}, \tilde{H}, \tilde{\mu}_L)$$

- Spin-independent scattering

LUX, XENON1T

- Spin-dependent scattering

Weaker bounds than spin-independent

## LHC

- Slepton production



Small mass difference  
makes it difficult...

$$m_{\tilde{l}} - m_{\tilde{B}} \sim 10 \text{ GeV}$$

- Neutralino/chargino production

- decay to slepton

- decay to  $WZ$  or  $Wh$

Future high-luminosity LHC is important!

## ILC

Environment is clean!

- Slepton production

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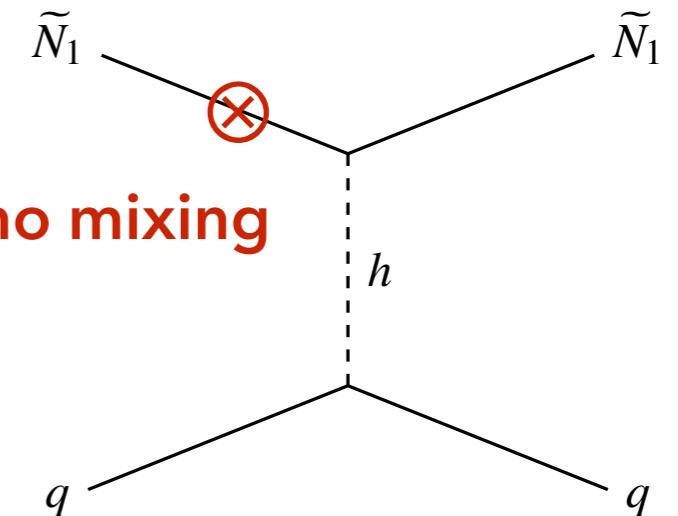
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# LUX and XENON1T

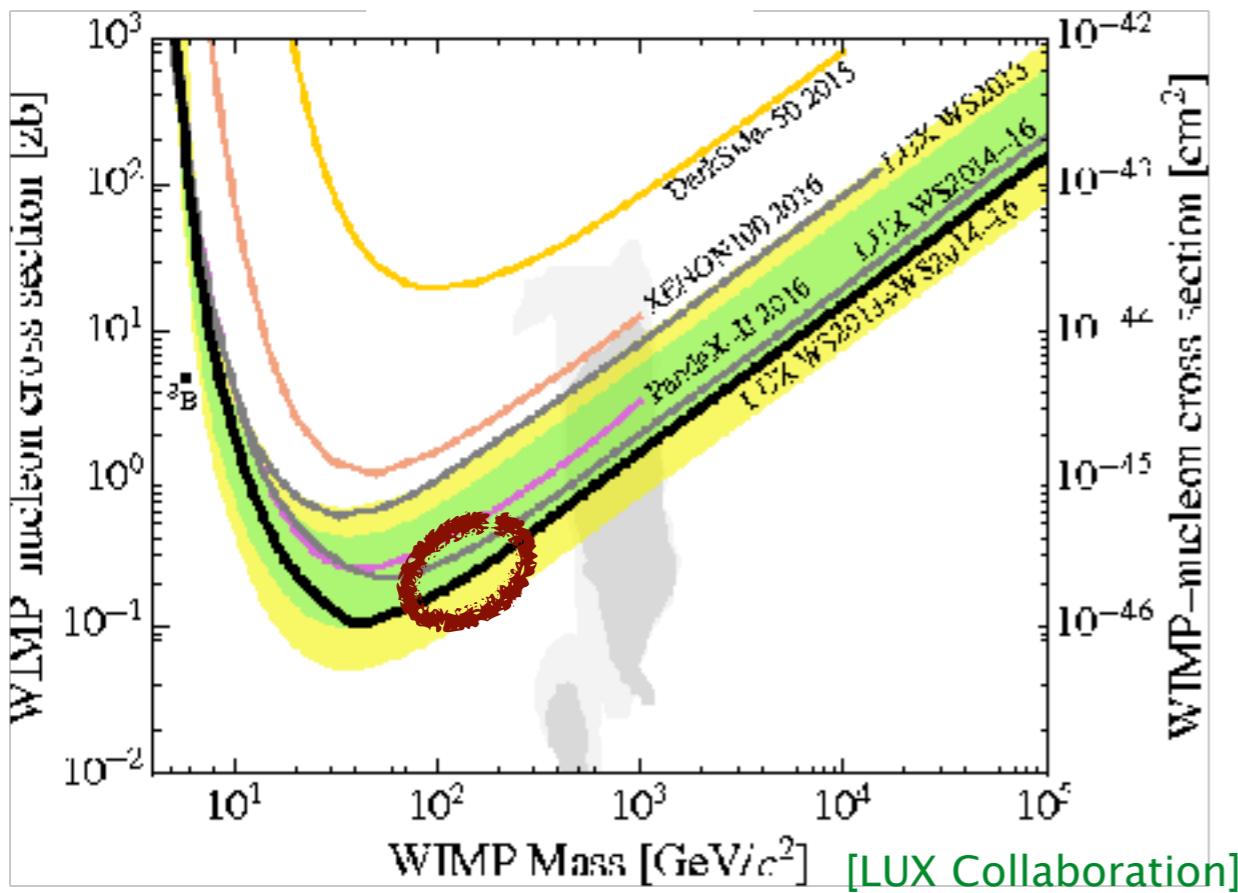
Spin-independent scattering

Muon g-2 favors  $M_1 = 100 - 200$  GeV  
in BHR or BHL scenario



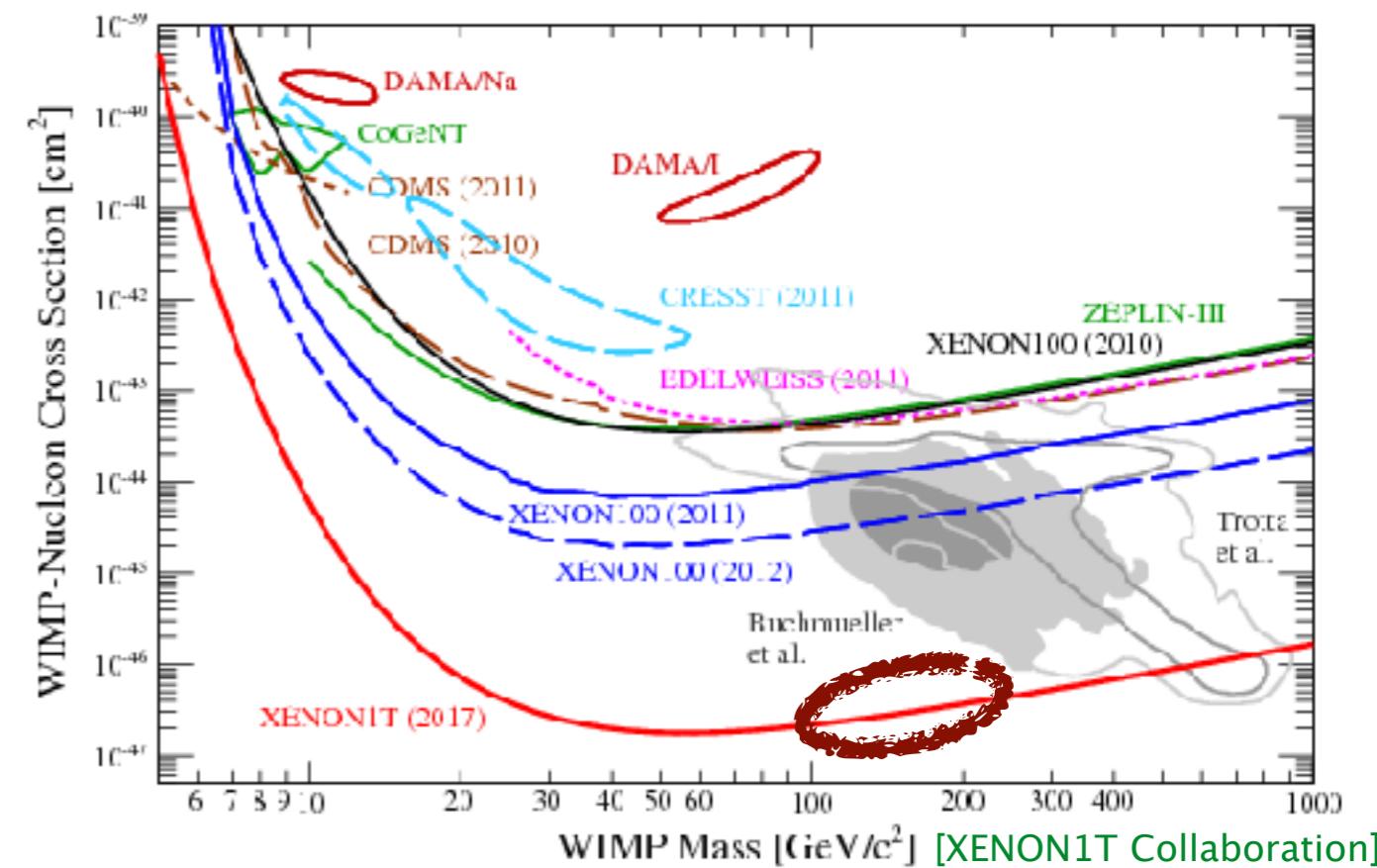
Bino-Higgsino mixing  
 $\sim 1/(\mu^2 - M_1^2)$

Latest LUX



$$\sigma_{\text{upper}} = 0.2 - 0.3 \text{ zb}$$

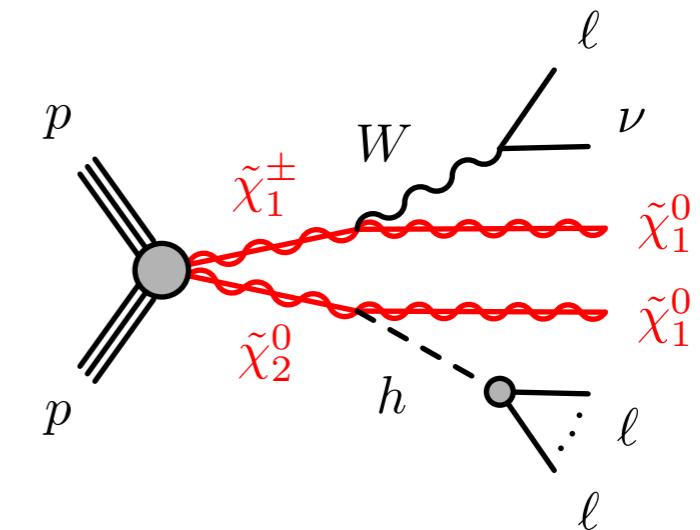
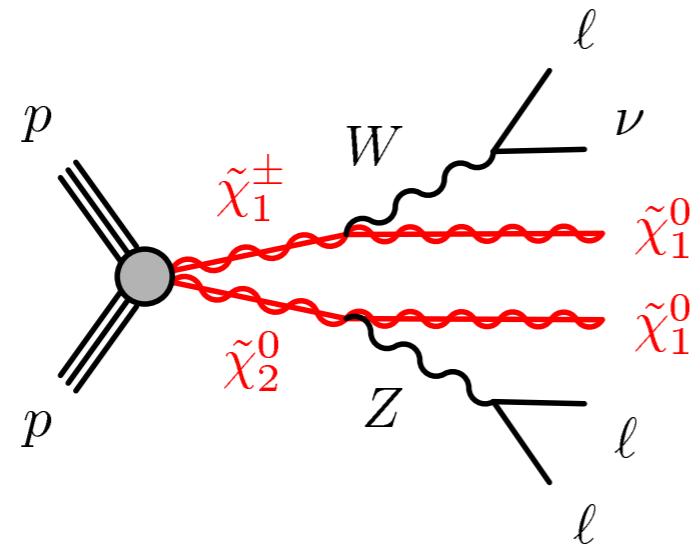
Future XENON1T



$$\sigma_{\text{upper}} = 0.02 - 0.03 \text{ zb}$$

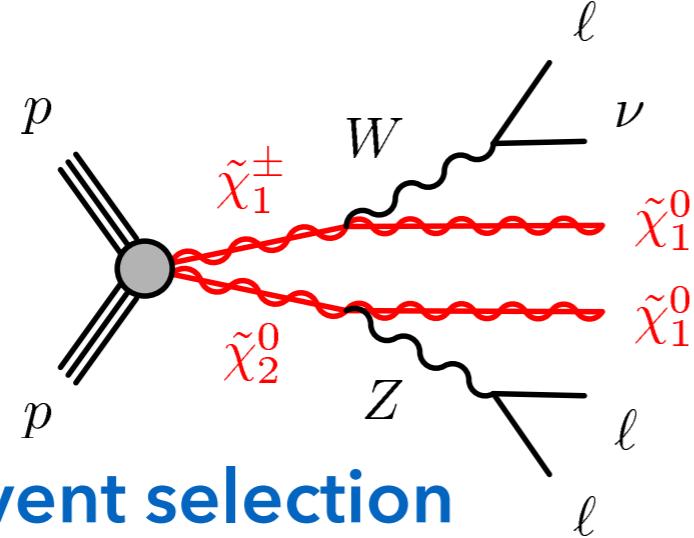
# High-Luminosity LHC

- Future prospect:  $\sqrt{s} = 14 \text{ TeV}$   $\int \mathcal{L} = 3000 \text{ fb}^{-1}$
- Higgsino pair production
- Decaying to 3 leptons +  $E_T^{\text{miss}}$  via  $WZ$  or  $Wh$



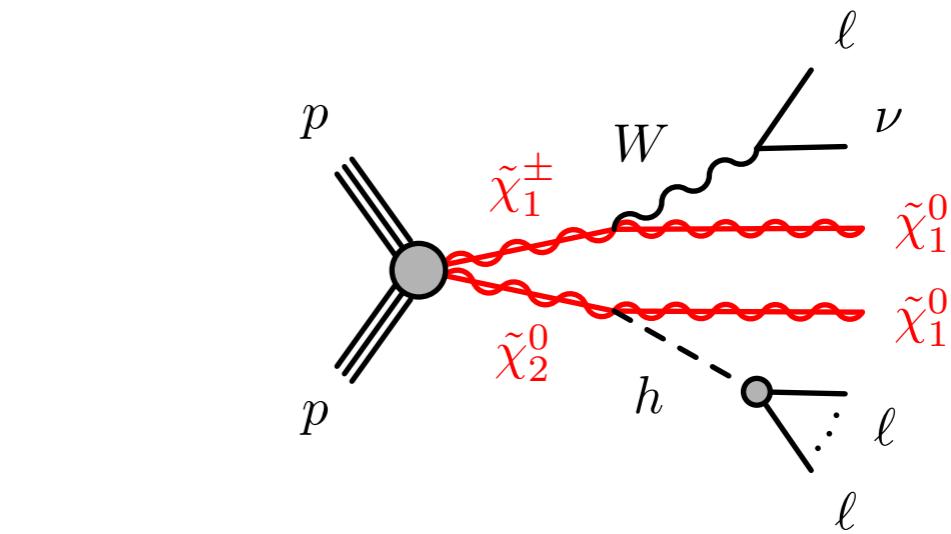
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ATLAS's event selection

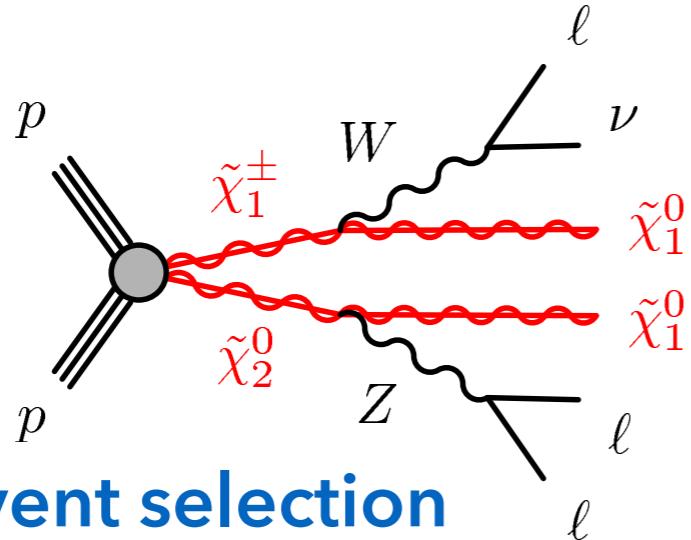
| Selection                             | SRA     | SRB     | SRC     | SRD     |
|---------------------------------------|---------|---------|---------|---------|
| $ m_{\text{SFOZ}} - m_Z [\text{GeV}]$ |         |         | $< 10$  |         |
| # of b-tagged jets                    |         |         | 0       |         |
| lepton $p_T(1, 2, 3)[\text{GeV}]$     |         |         | $> 50$  |         |
| $\cancel{E}_T[\text{GeV}]$            | $> 250$ | $> 300$ | $> 400$ | $> 500$ |
| $m_T[\text{GeV}]$                     | $> 150$ | $> 200$ | $> 200$ | $> 200$ |
| $N_{95\text{exp}}^{\text{SRX}}$       | 111     | 38.8    | 17.8    | 9.6     |



| Selection                                   | SRE     | SRF     | SRG     | SRH     |
|---------------------------------------------|---------|---------|---------|---------|
| SFOS pair                                   |         |         |         | veto    |
| # of b-tagged jets                          |         |         |         | 0       |
| $\cancel{E}_T[\text{GeV}]$                  |         |         |         | $> 100$ |
| $m_{\text{OS}}^{\min \Delta R}[\text{GeV}]$ |         |         |         | $< 75$  |
| $m_T(l_1)[\text{GeV}]$                      | $> 200$ | $> 200$ | $> 300$ | $> 400$ |
| $m_T(l_2)[\text{GeV}]$                      | $> 100$ | $> 150$ | $> 150$ | $> 150$ |
| $m_T(l_3)[\text{GeV}]$                      | $> 100$ | $> 100$ | $> 100$ | $> 100$ |
| $N_{95\text{exp}}^{\text{SRX}}$             | 85      | 33      | 8.3     | 4.5     |

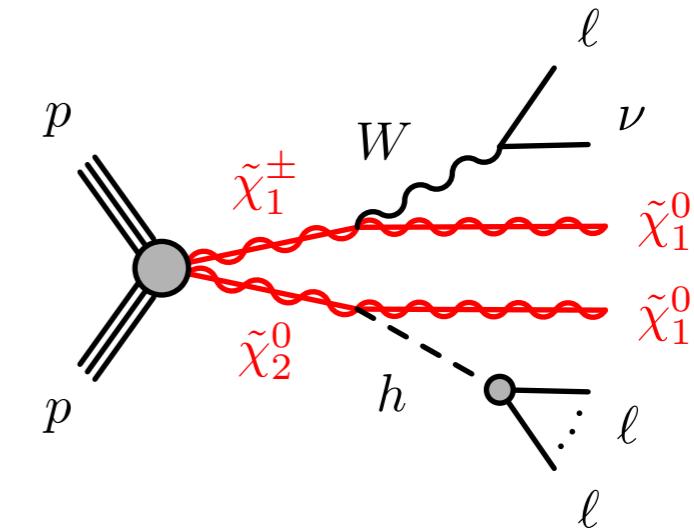
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[ATL-PHYS-PUB-2014-010]

We compare these numbers to our SUSY simulation

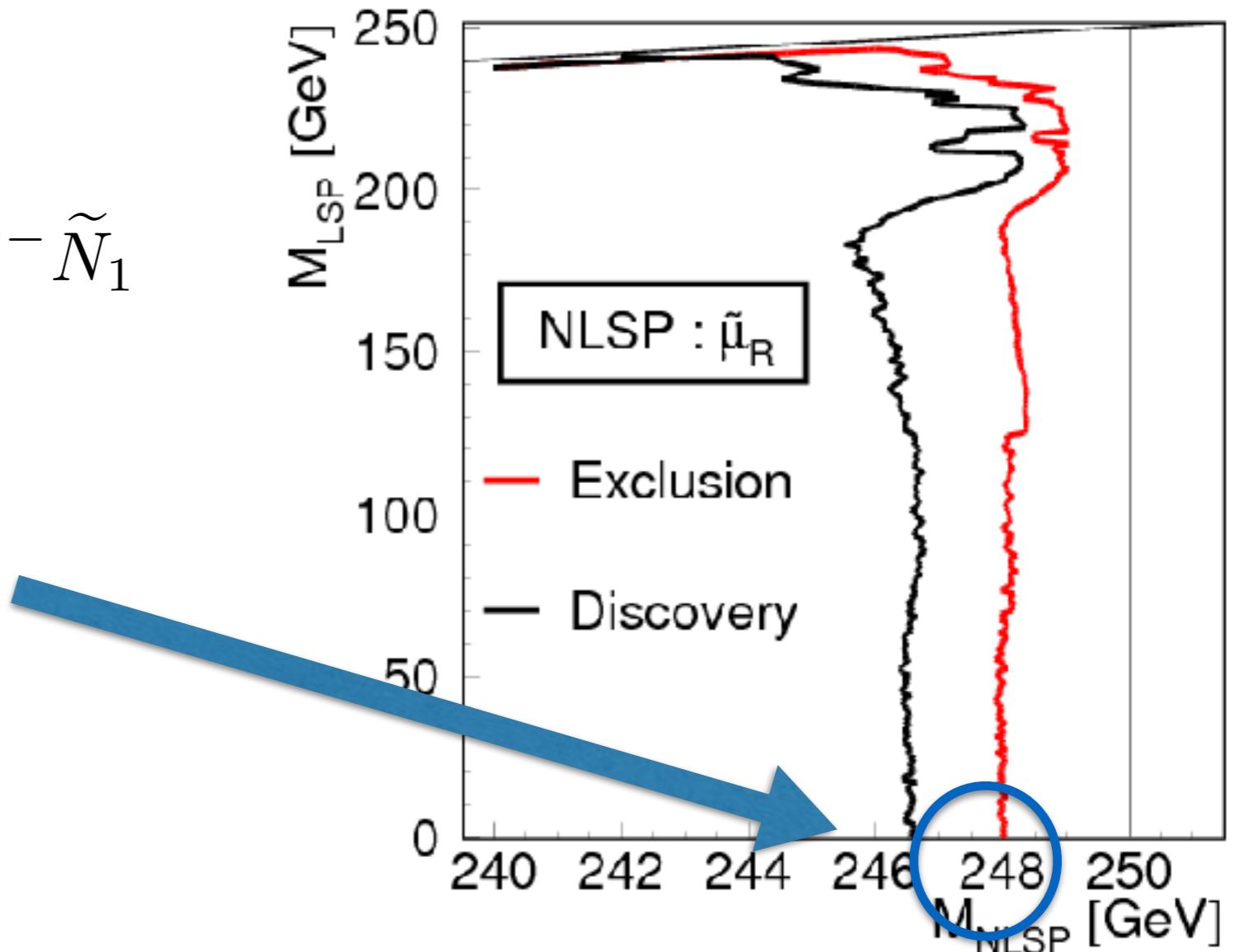
# ILC 500 GeV

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## Slepton production

$$e^+ e^- \rightarrow \tilde{l}^+ \tilde{l}^- \rightarrow l^+ \tilde{N}_1 l^- \tilde{N}_1$$

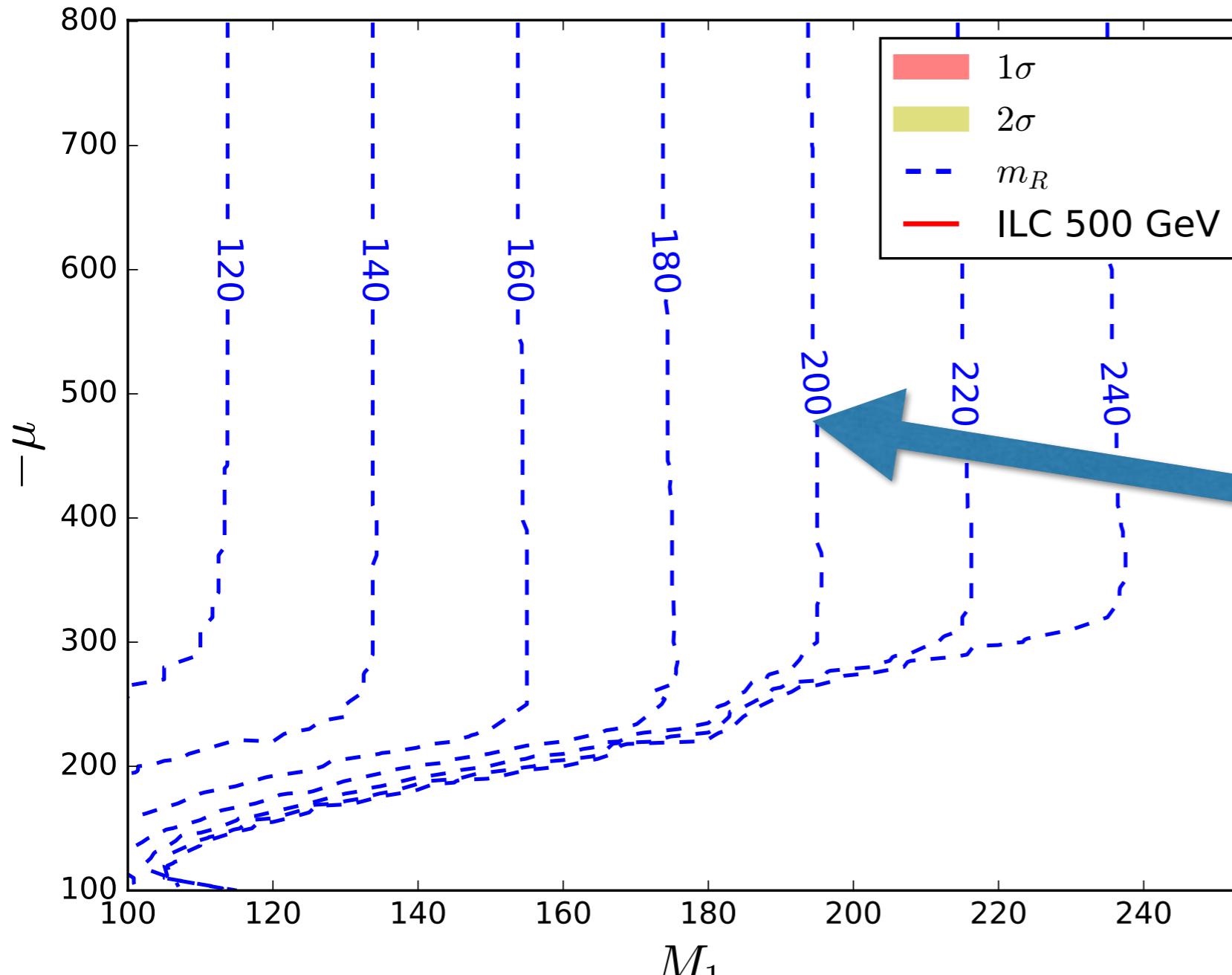
- ILC can probe small mass deference!



[arXiv:1307.5248]

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2. Experimental bounds (Direct detection, LHC, ILC)
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# BHR scenario

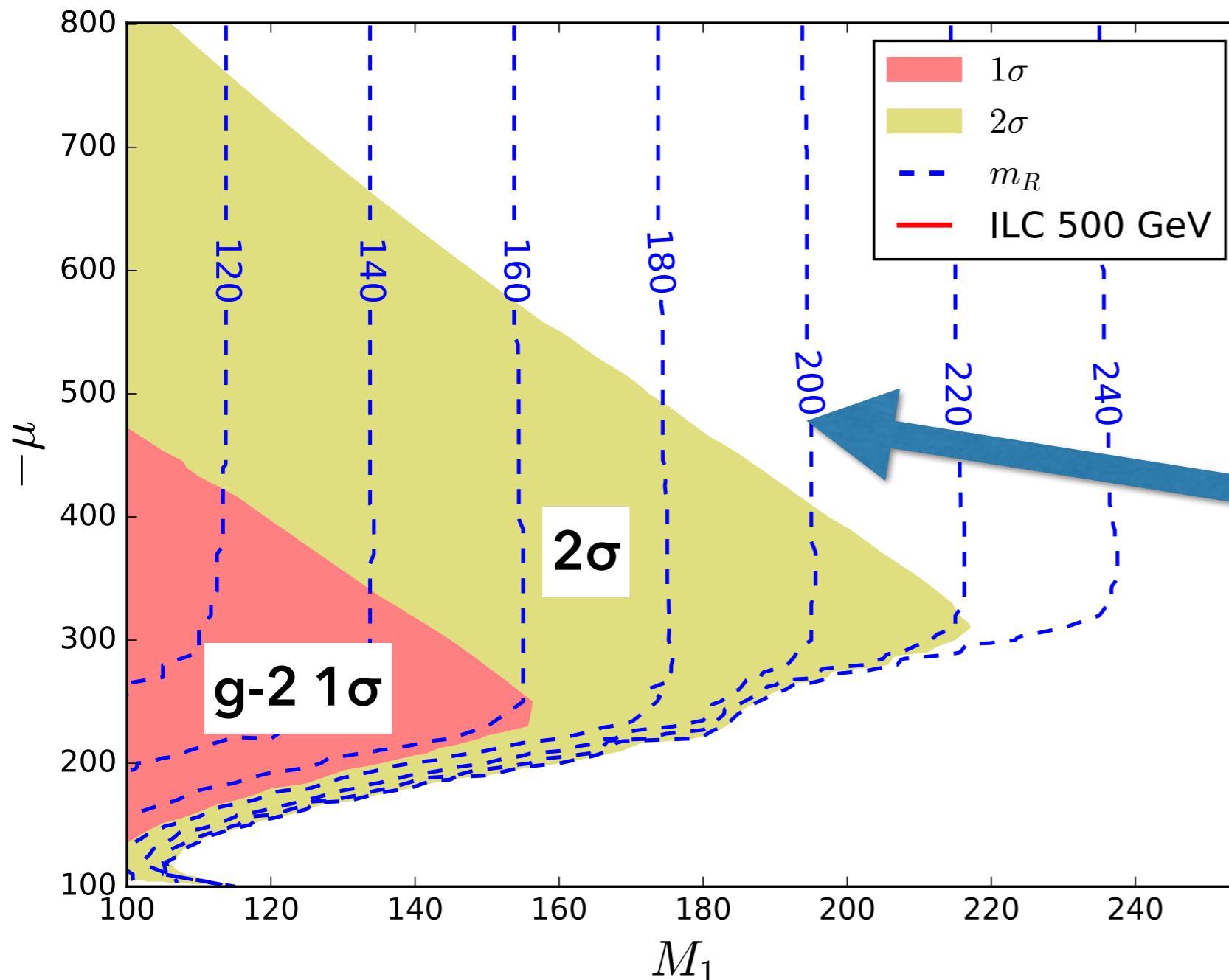


Parameters:  
 $M_1, \mu, m_R, \tan\beta=40$

$m_R$  that gives  
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Bino-slepton coannihilation

[Preliminary]

# BHR scenario



[Preliminary]

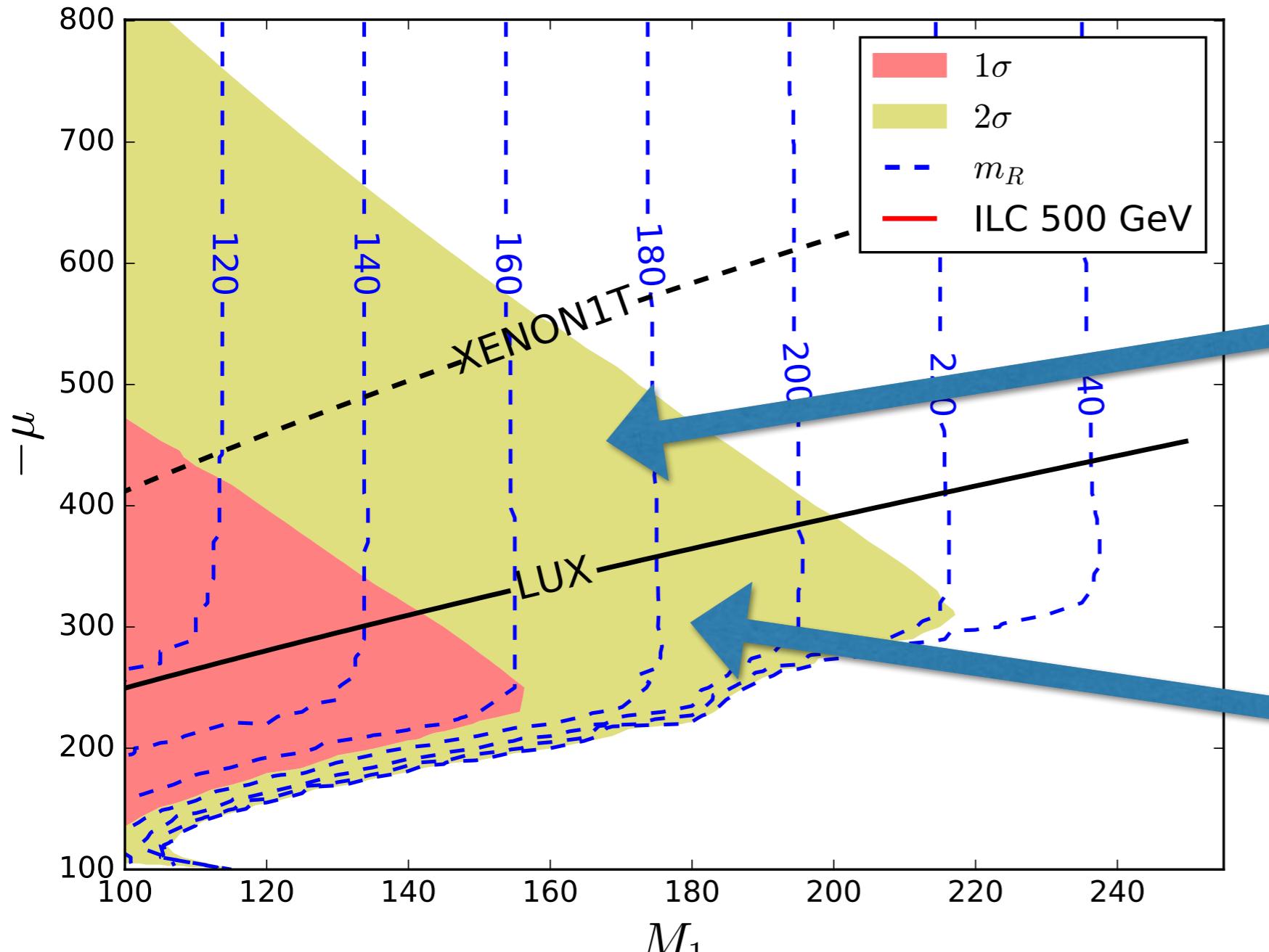
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Bino-slepton coannihilation

We can calculate  
 $a_\mu(\text{BHR}) = a_\mu(M_1, \mu, m_R)$

$\mu M_1 < 0$  is favored by g-2

# BHR scenario

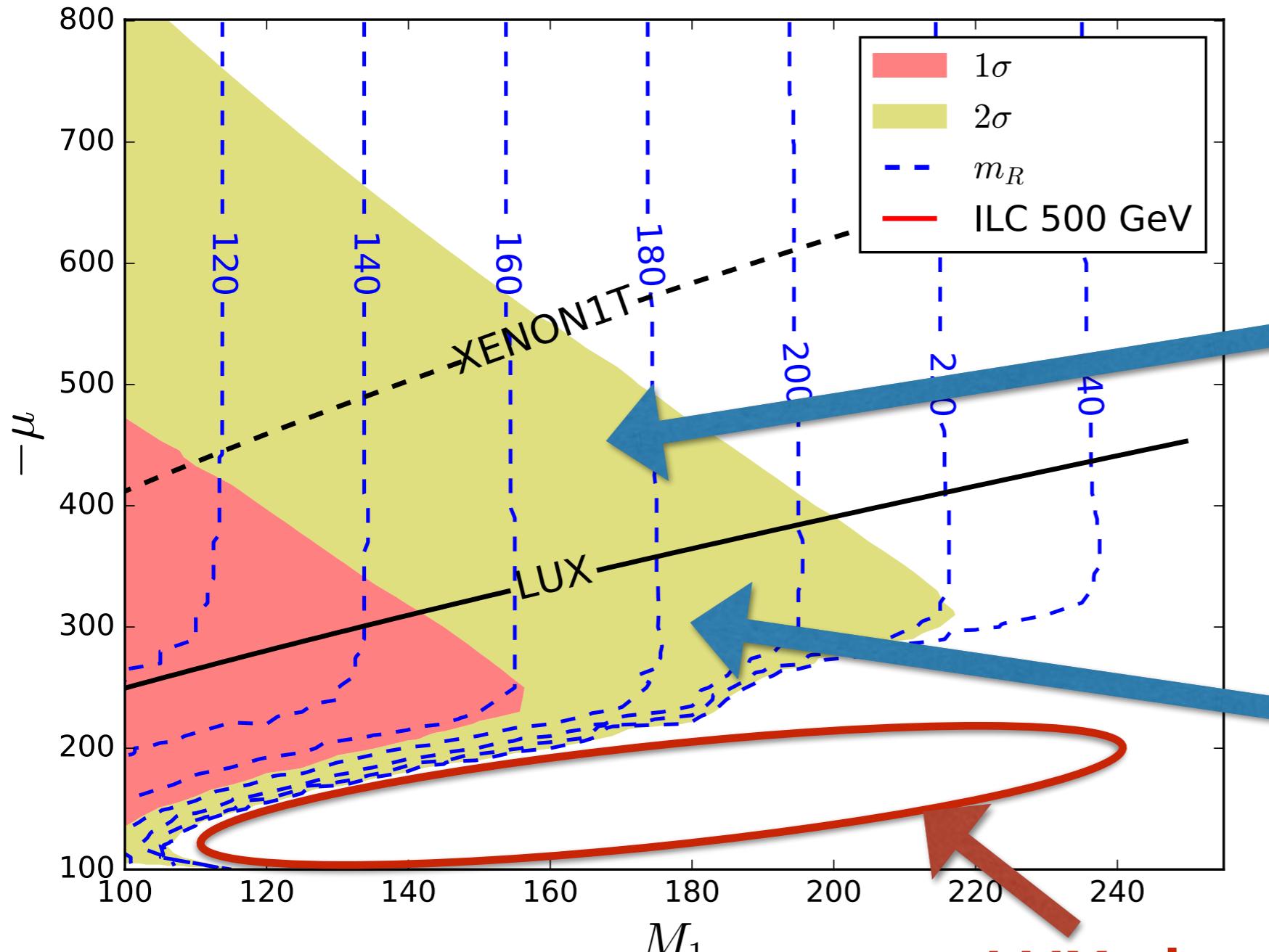


**XENON1T will  
probe here  
(this year?)**

**Excluded by LUX**

[Preliminary]

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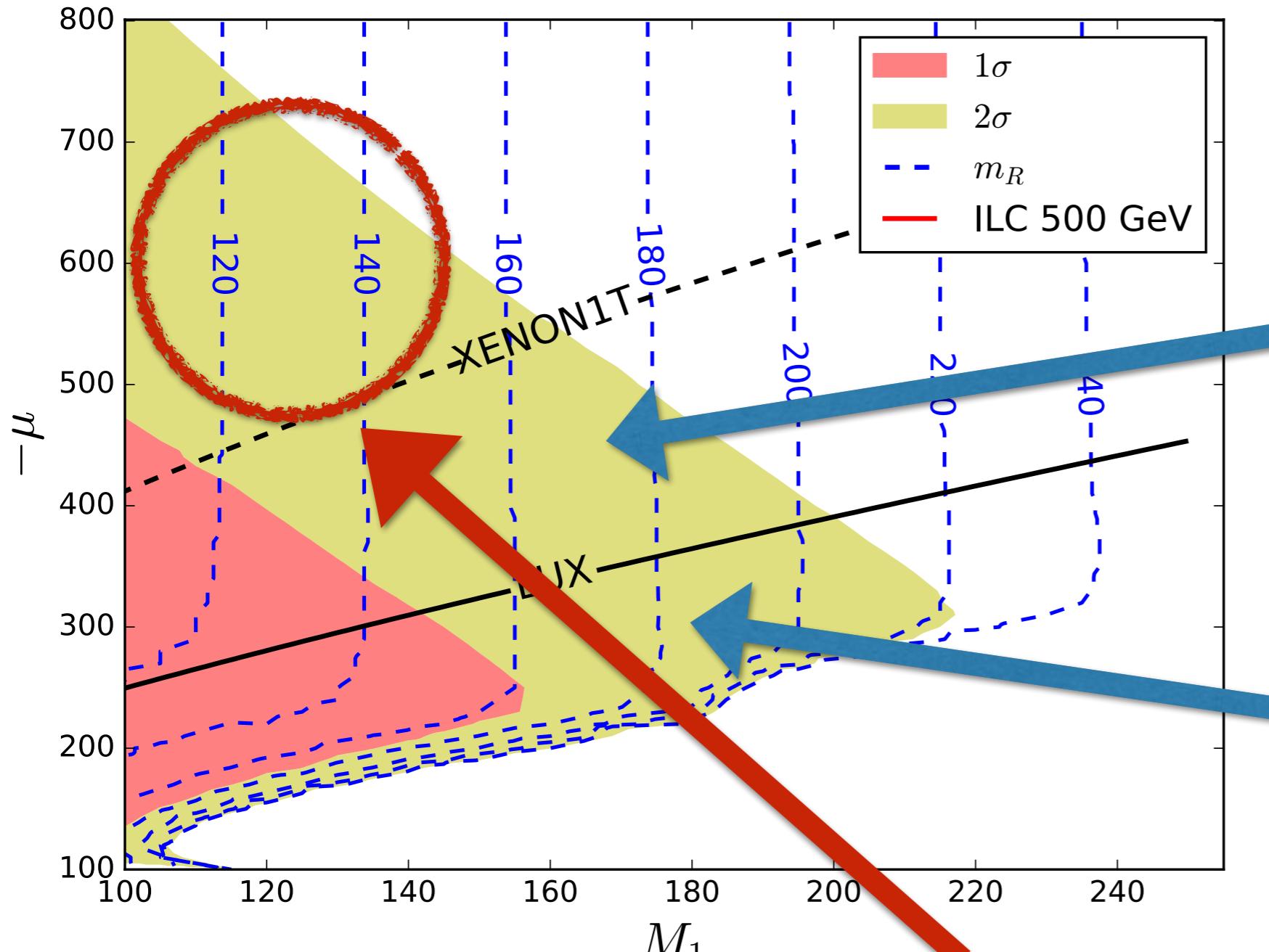
[Preliminary]

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**LUX already excluded  
well-tempered bino-Higgsino  
in this scenario!**

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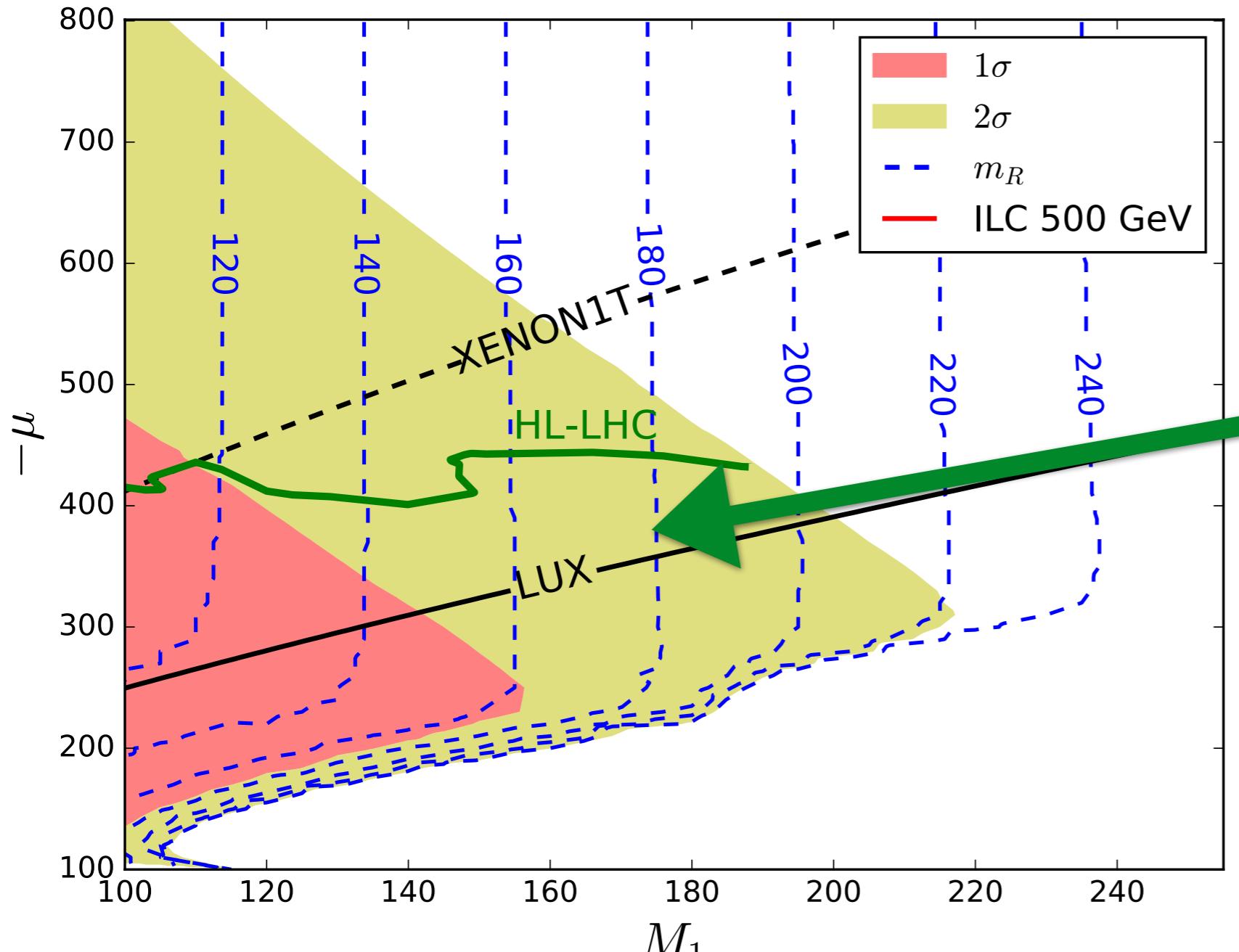
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[Preliminary]

**Can LHC probe here?**

# BHR scenario



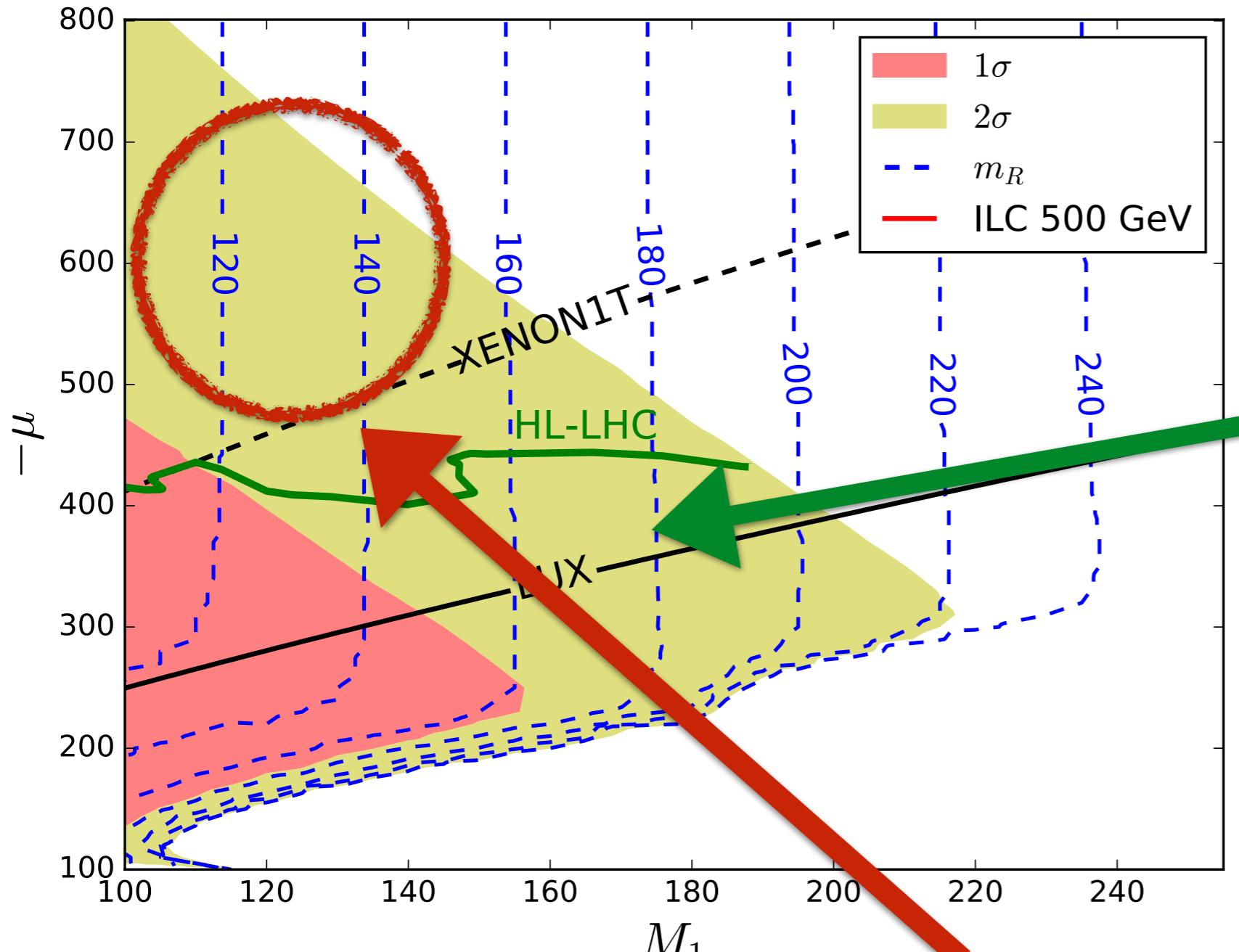
[Preliminary]

HL-LHC can probe  
here  
Weaker than XENON1T!

$\text{Br}(\tilde{H} \rightarrow \tilde{\tau} + \tau(\nu_\tau))$   
 $> \text{Br}(\tilde{H} \rightarrow \tilde{B} + Z(W))$

We assume universal  
 $m_R$  for  $\tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R$

# BHR scenario



[Preliminary]

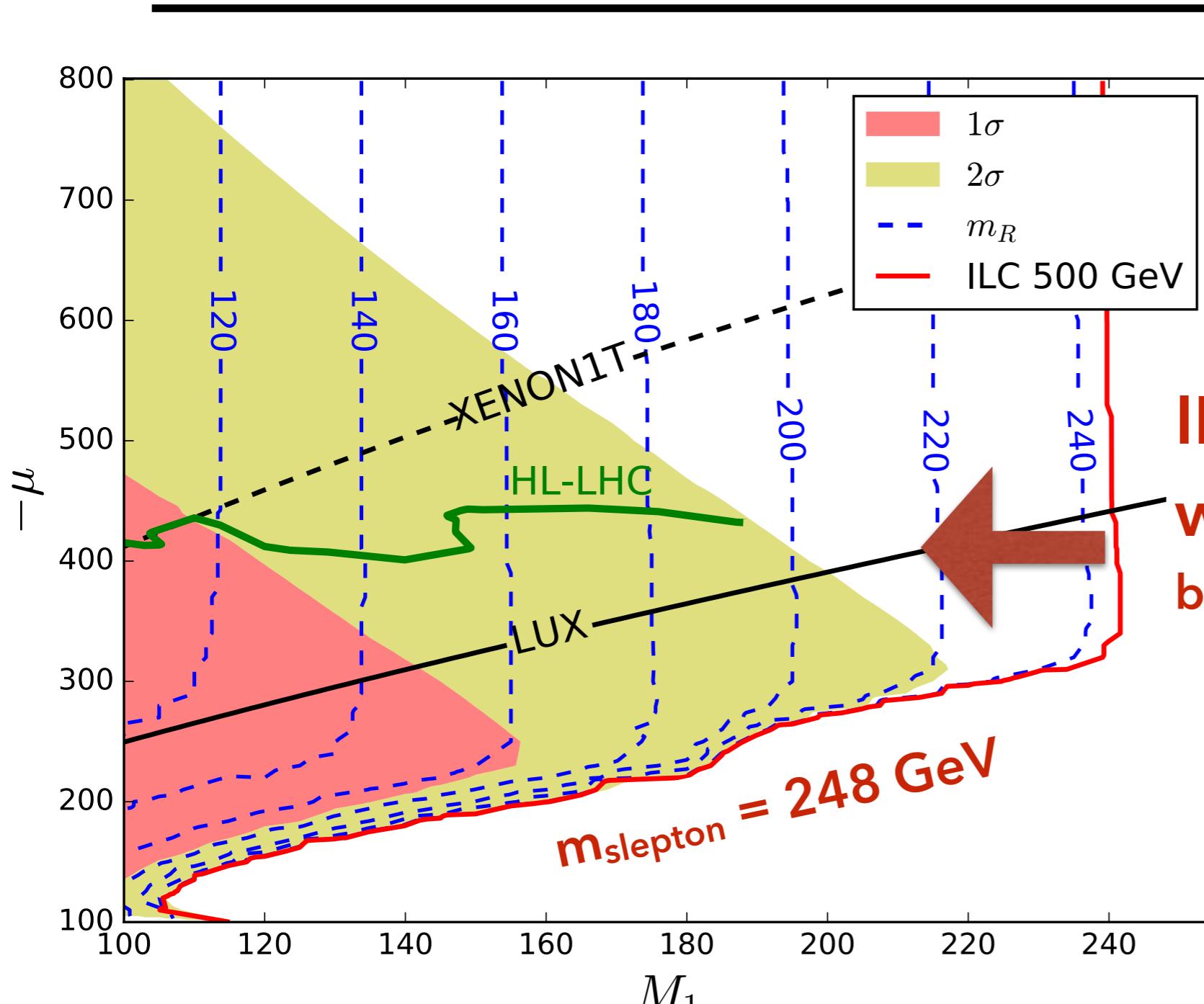
This region cannot be studied!

HL-LHC can probe  
here  
Weaker than XENON1T!

$\text{Br}(\tilde{H} \rightarrow \tilde{\tau} + \tau(\nu_\tau))$   
 $> \text{Br}(\tilde{H} \rightarrow \tilde{B} + Z(W))$

We assume universal  
 $m_R$  for  $\tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R$

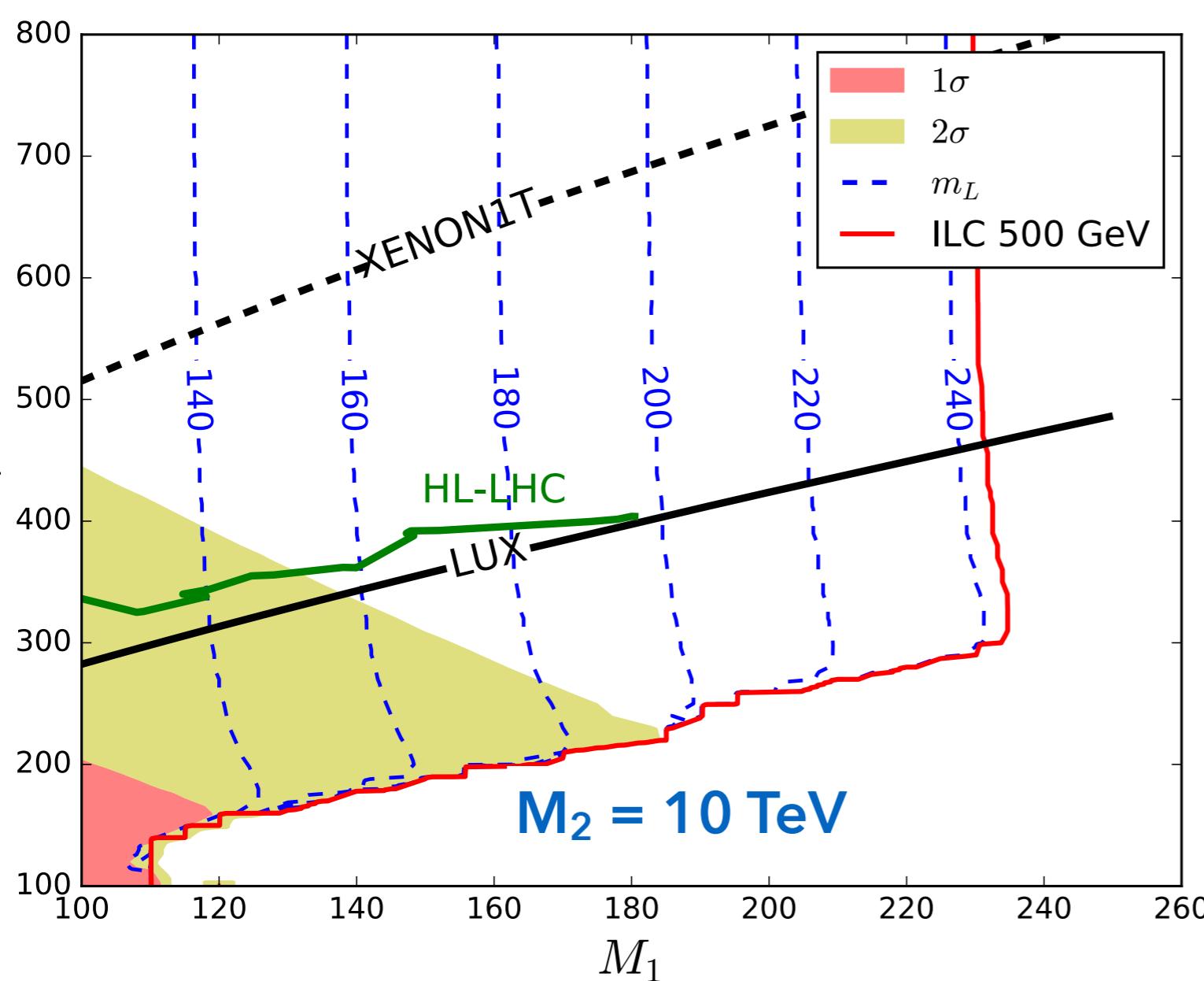
# BHR scenario



ILC 500 GeV can probe  
whole parameter space!  
by slepton production

[Preliminary]

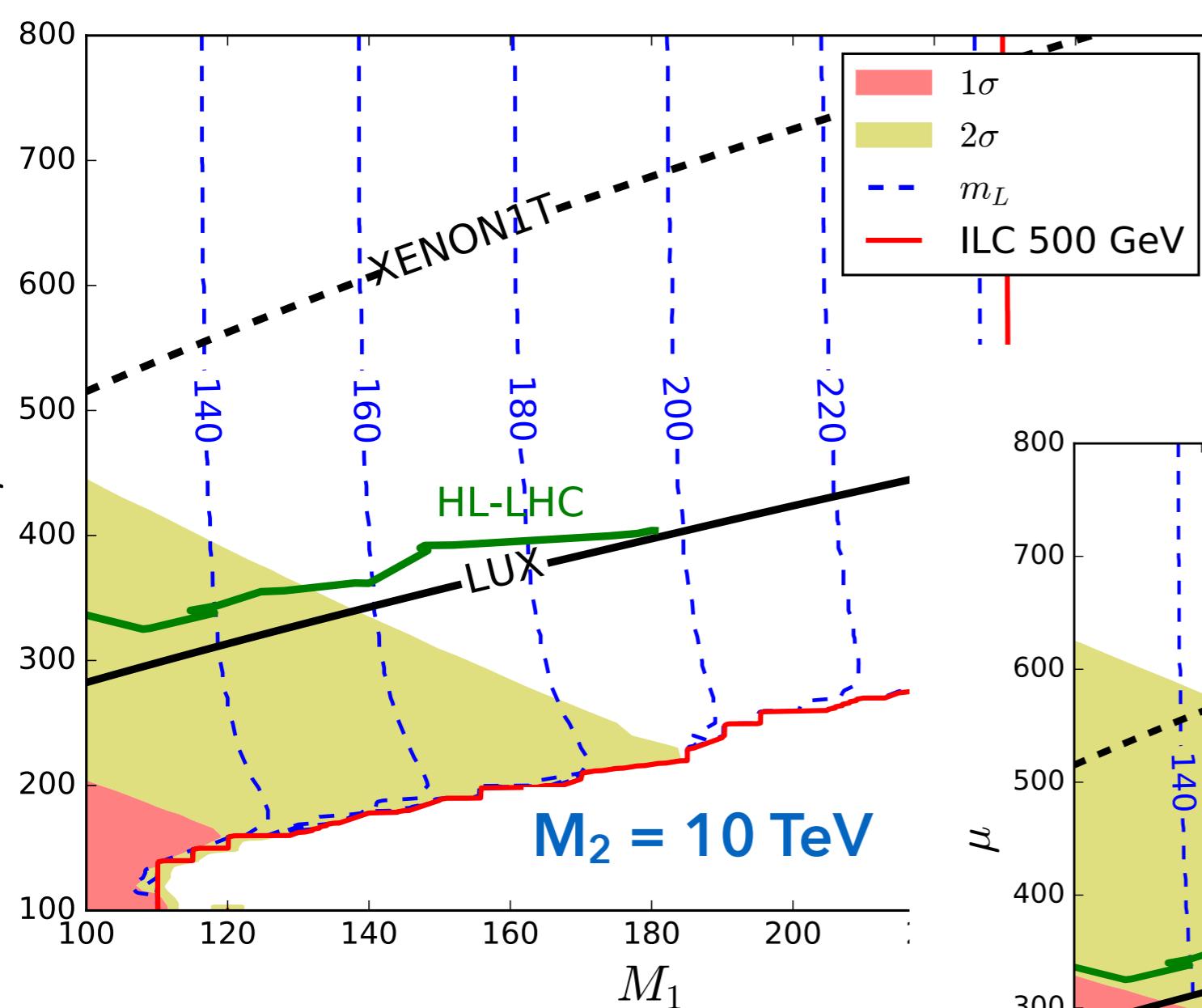
# BHL scenario



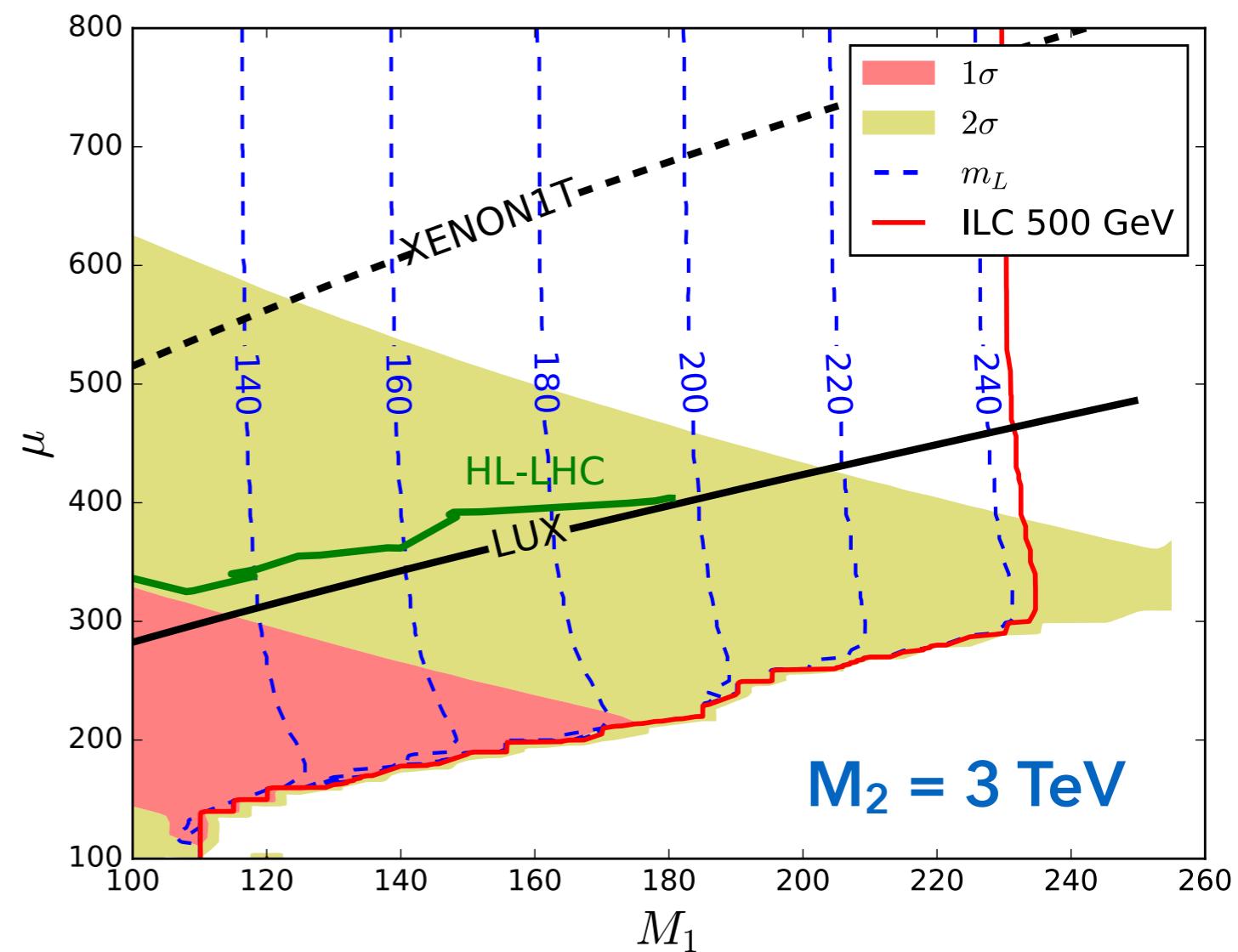
Looks similar to BHR scenario  
But  $M_2$  is important  
since WHL contribution  
is large

[Preliminary]

# BHL scenario

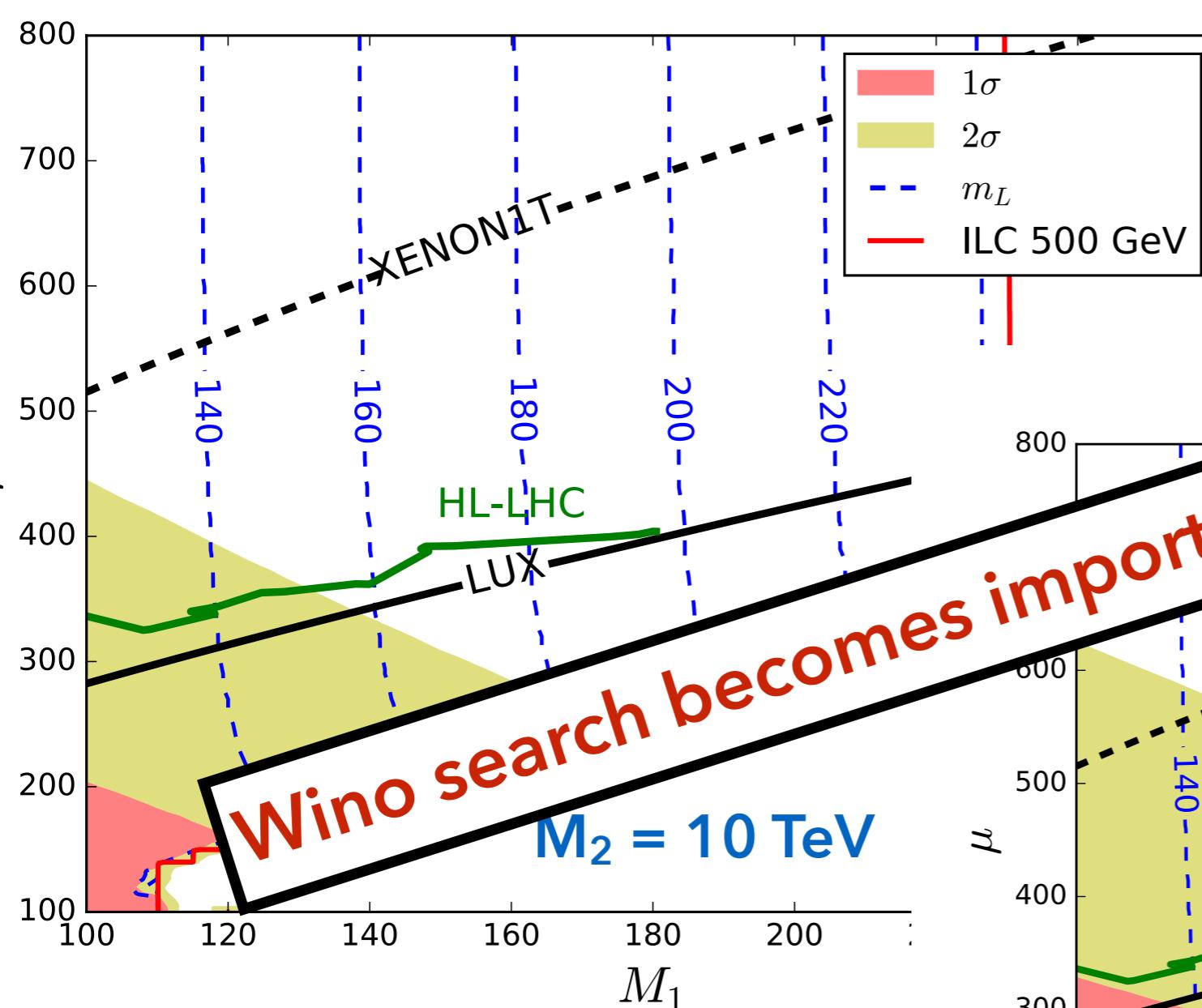


[Preliminary]

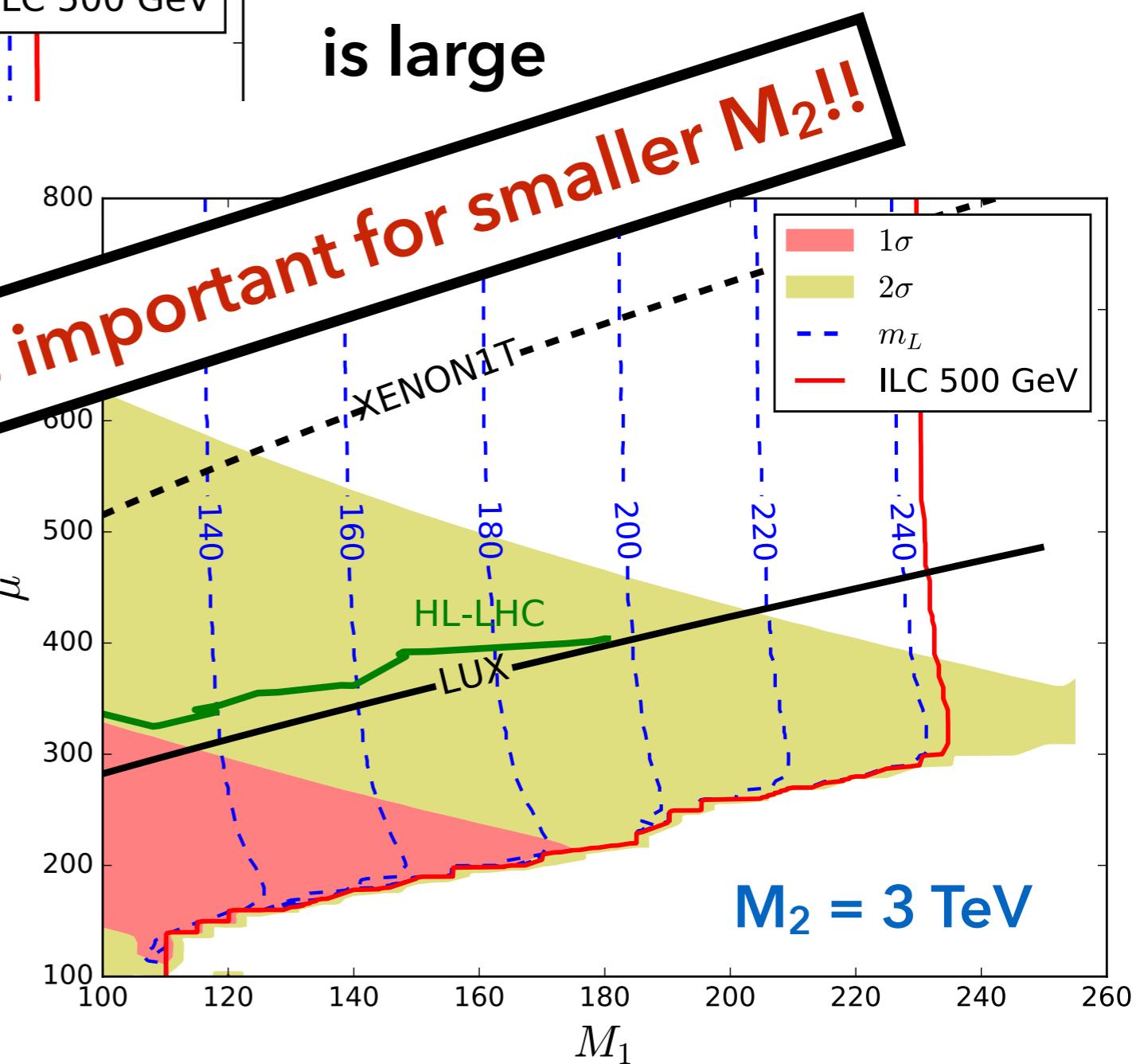


Looks similar to BHR scenario  
But  $M_2$  is important  
since WHL contribution  
is large

# BHL scenario



[Preliminary]



Looks similar to BHR scenario  
But  $M_2$  is important  
since WHL contribution  
is large

# Summary

- **MSSM can solve both the DM and muon g-2 anomaly**
- **We classify MSSM contributions into 4 scenarios**
- **BHR scenario cannot be covered even at the HL-LHC**
- **ILC is important!**

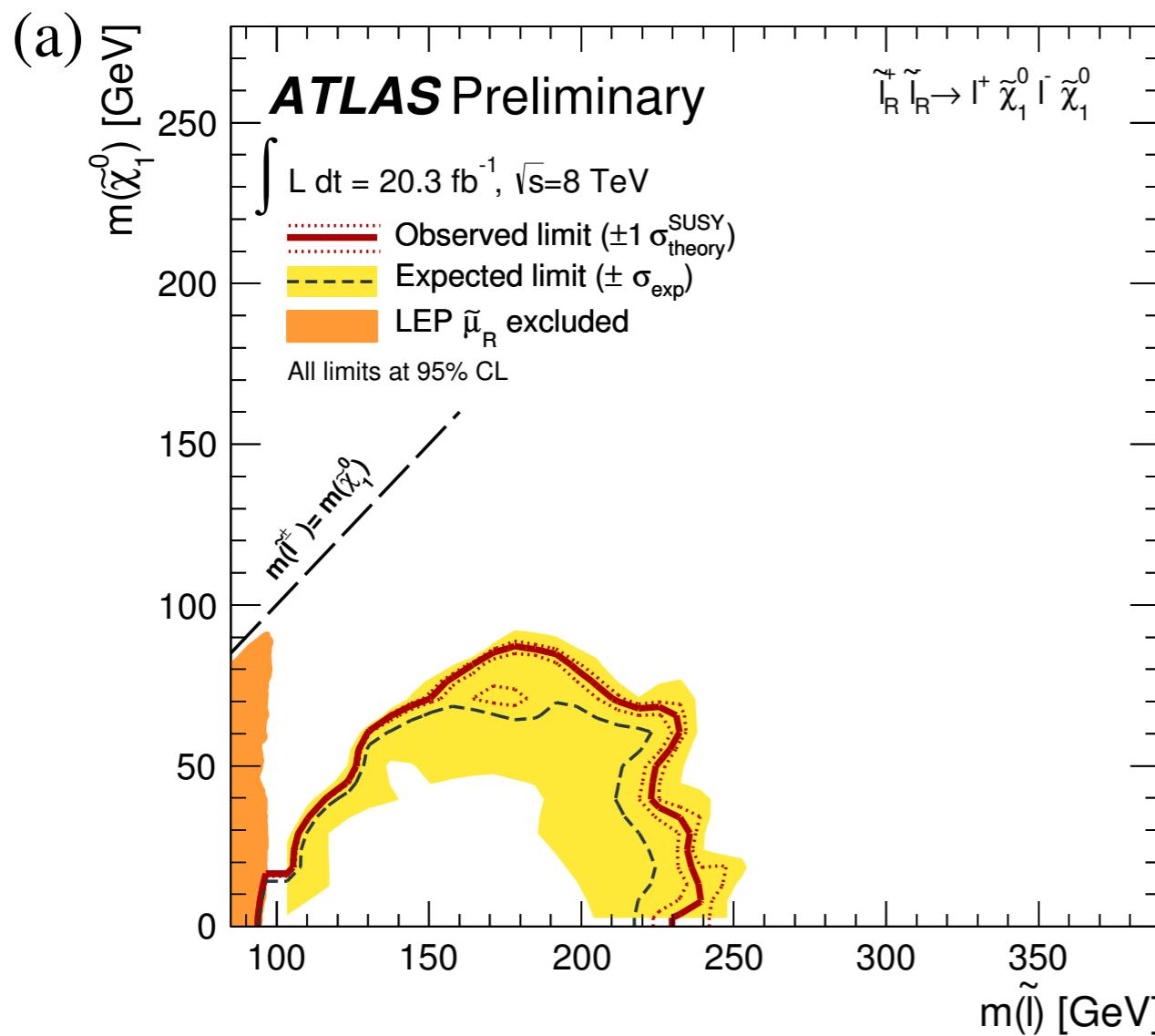
# Backup

# 8 TeV: 2l + $E_T^{\text{miss}}$

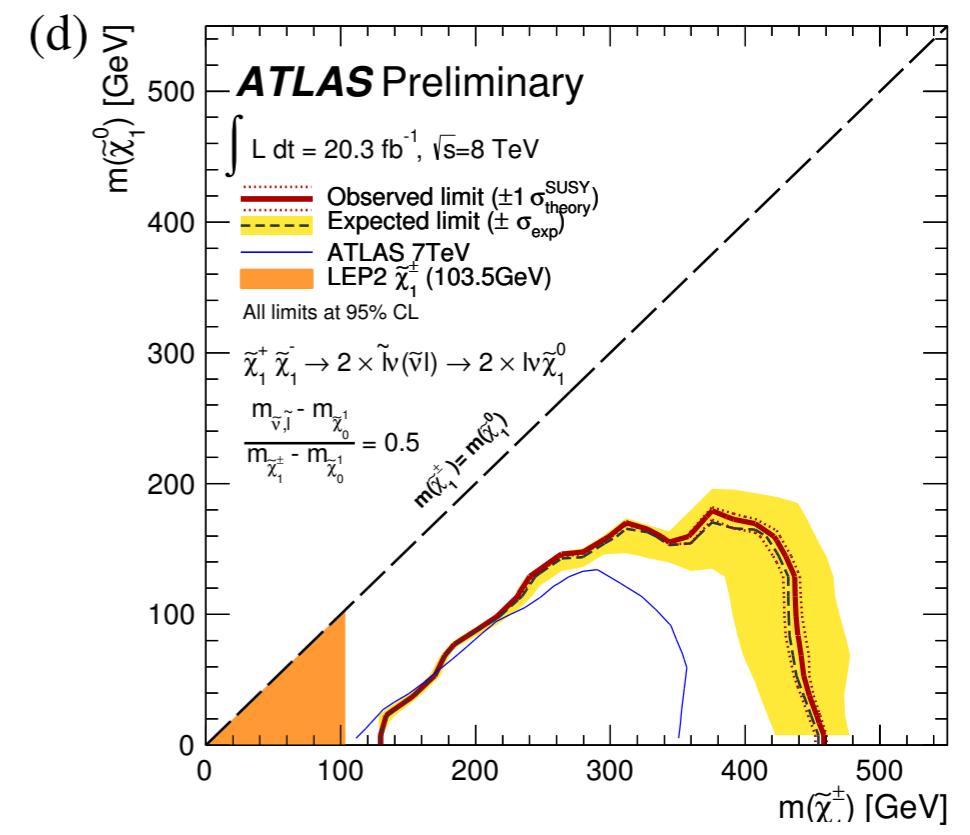
## Slepton production

Mass bounds on bino-like LSP is  $\sim 100$  GeV

Difficult to probe small mass difference



From chargino decay??



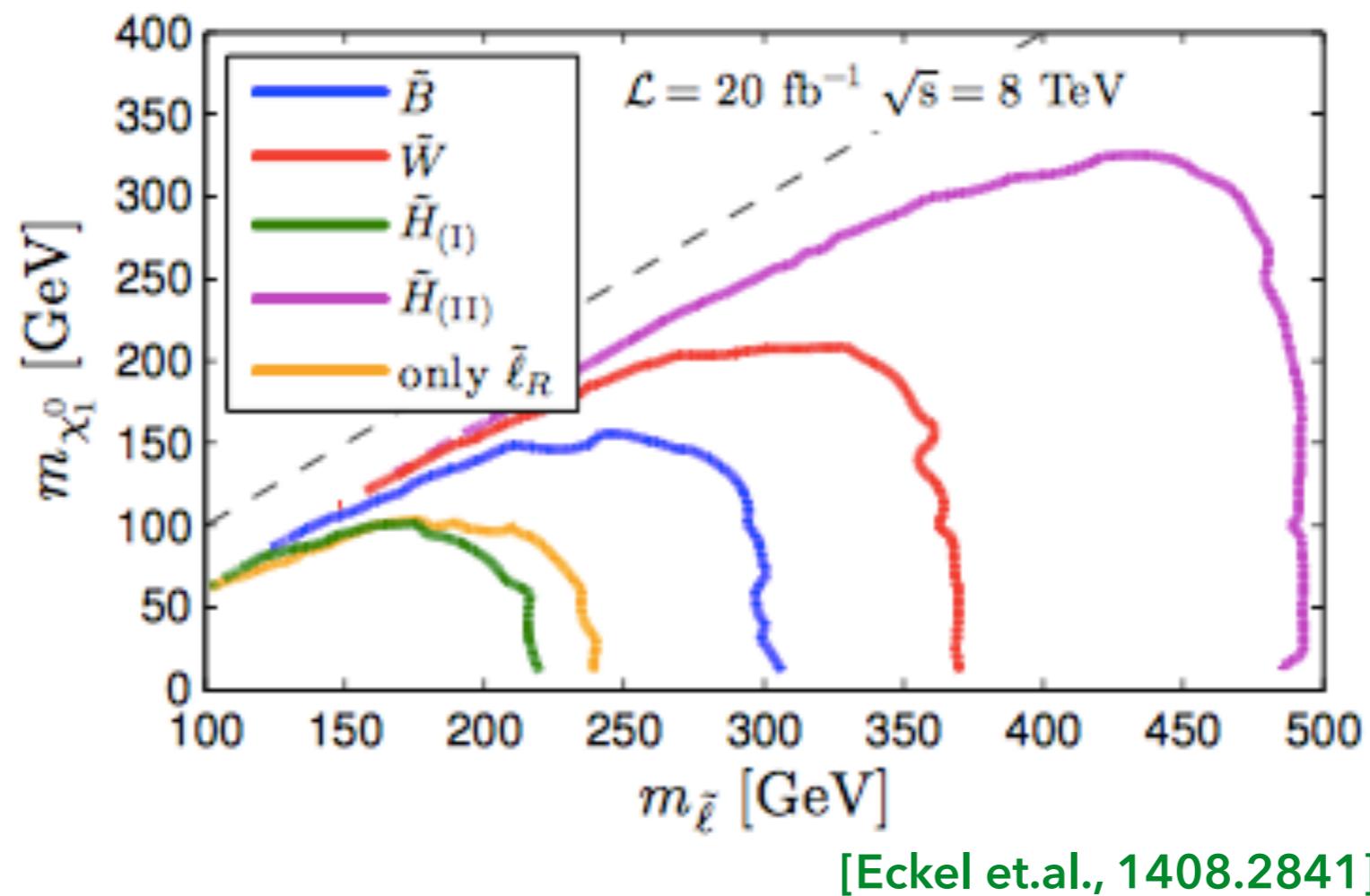
[ATLAS-CONF-2013-049]

# 8 TeV: 2l + $E_T^{\text{miss}}$

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## Slepton production

In the case of left-handed slepton,  
It depends on the character of the LSP

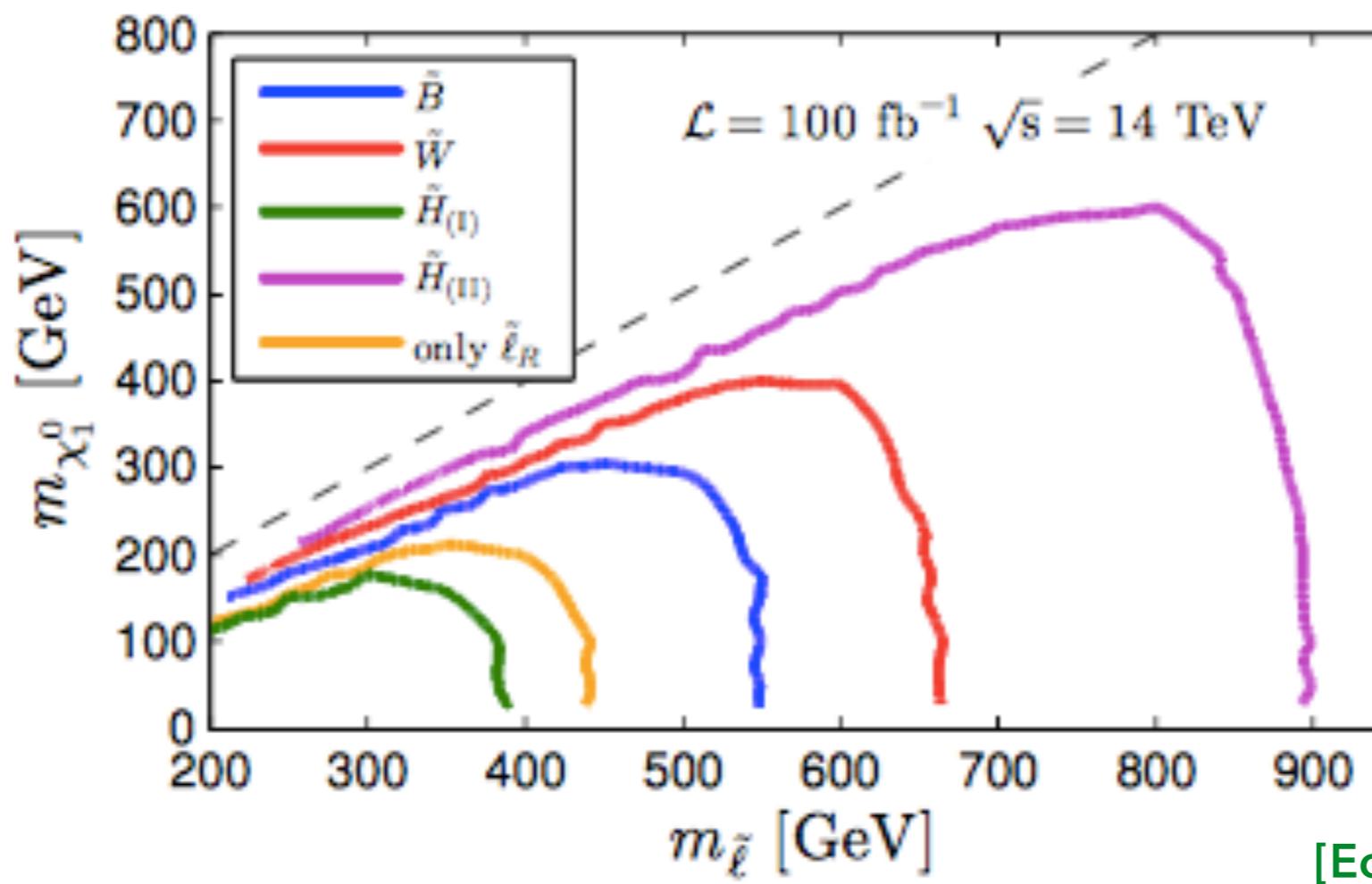


# 14 TeV: 2l + $E_T^{\text{miss}}$

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Slepton production

Even at 14 TeV, it is difficult to probe small mass difference

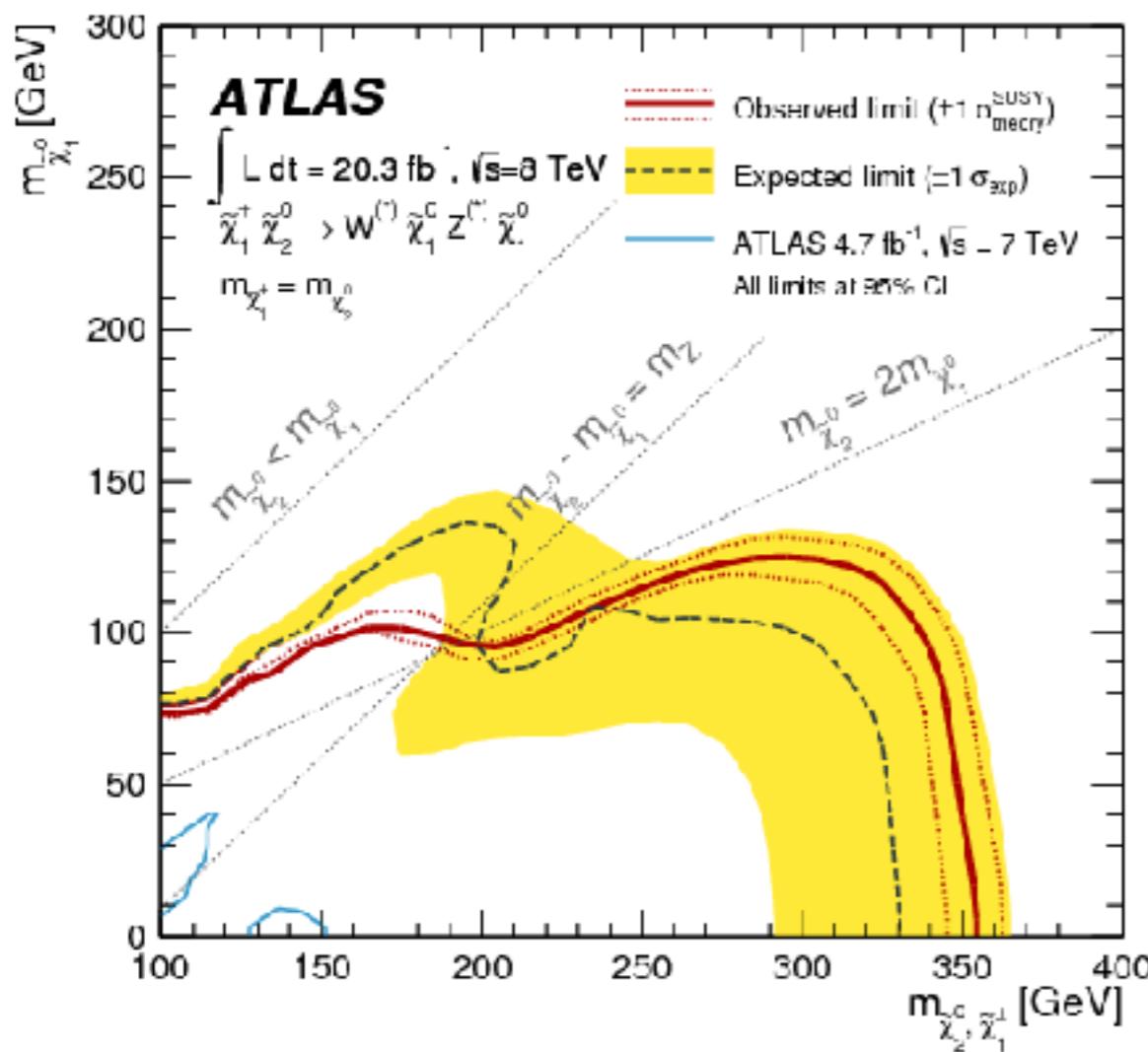


# 8 TeV: 3l + $E_T^{\text{miss}}$

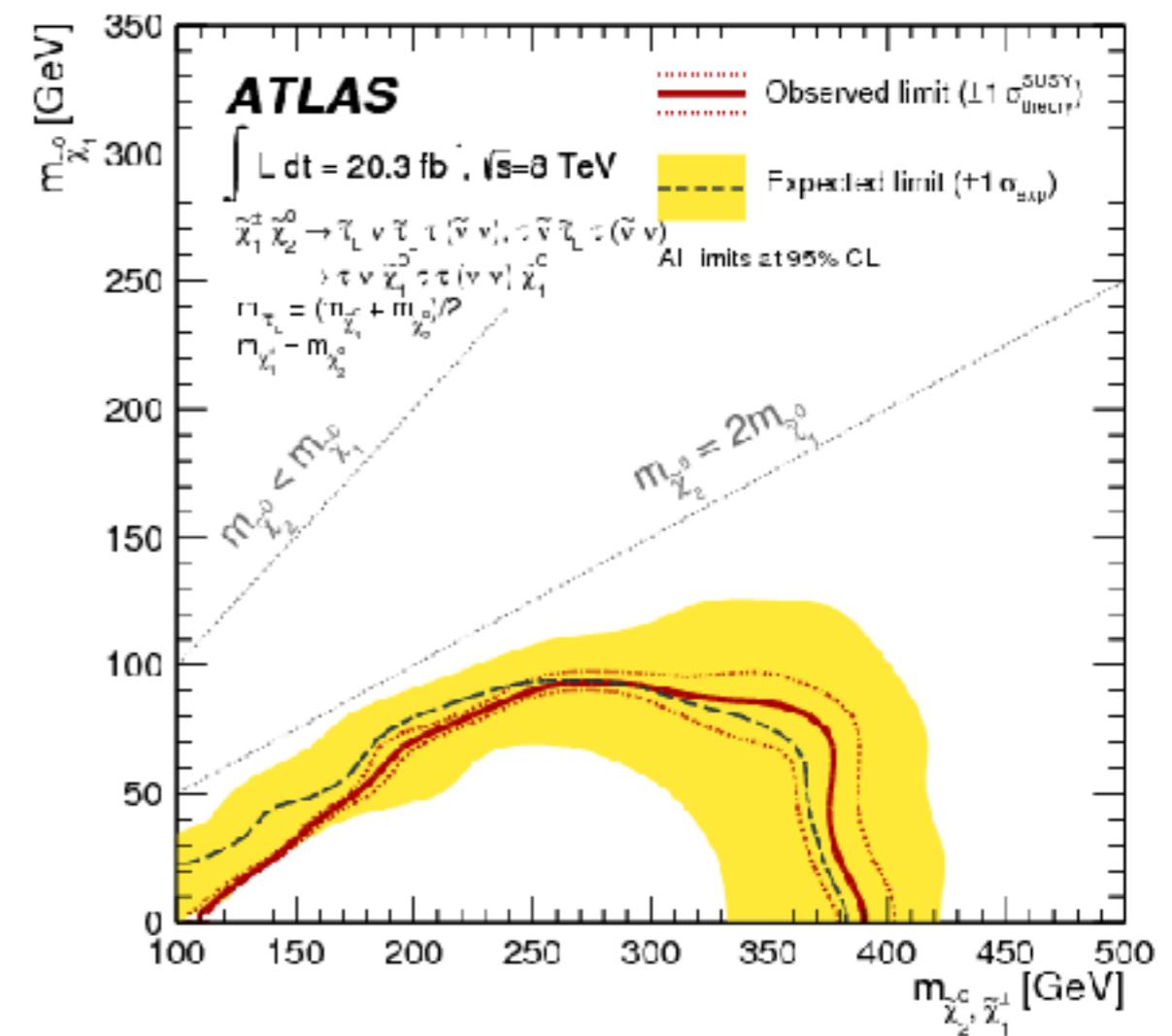
Neutralino/chargino production

In BHR or BHL scenario, neutralino/chargino decay to WZ, Wh, or stau

WZ



Stau

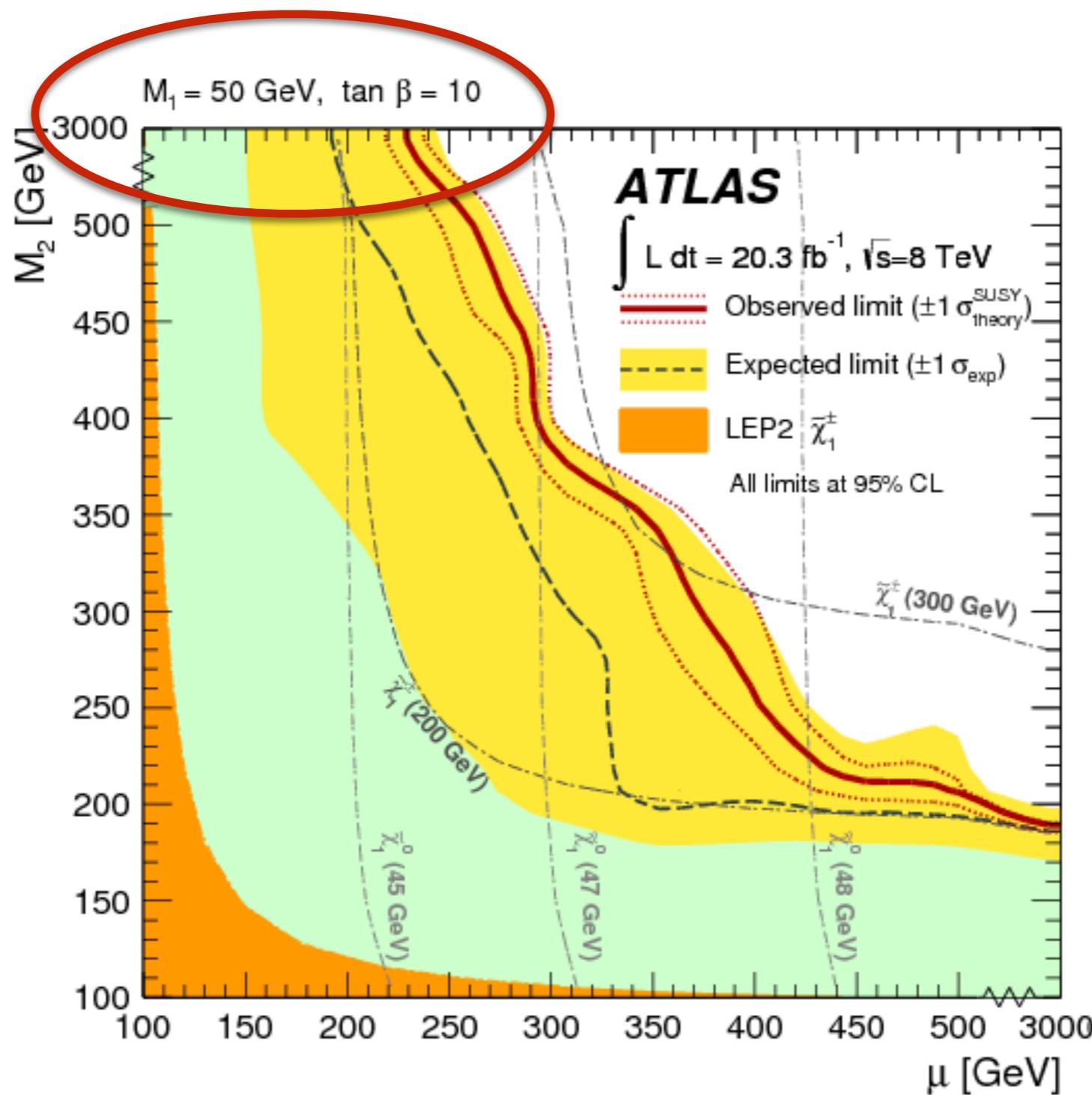


Mass bounds on LSP is  $\sim 100$  GeV

# 8 TeV: 3l + $E_T^{\text{miss}}$

---

Neutralino/chargino production  
Highly depends on the spectrum...

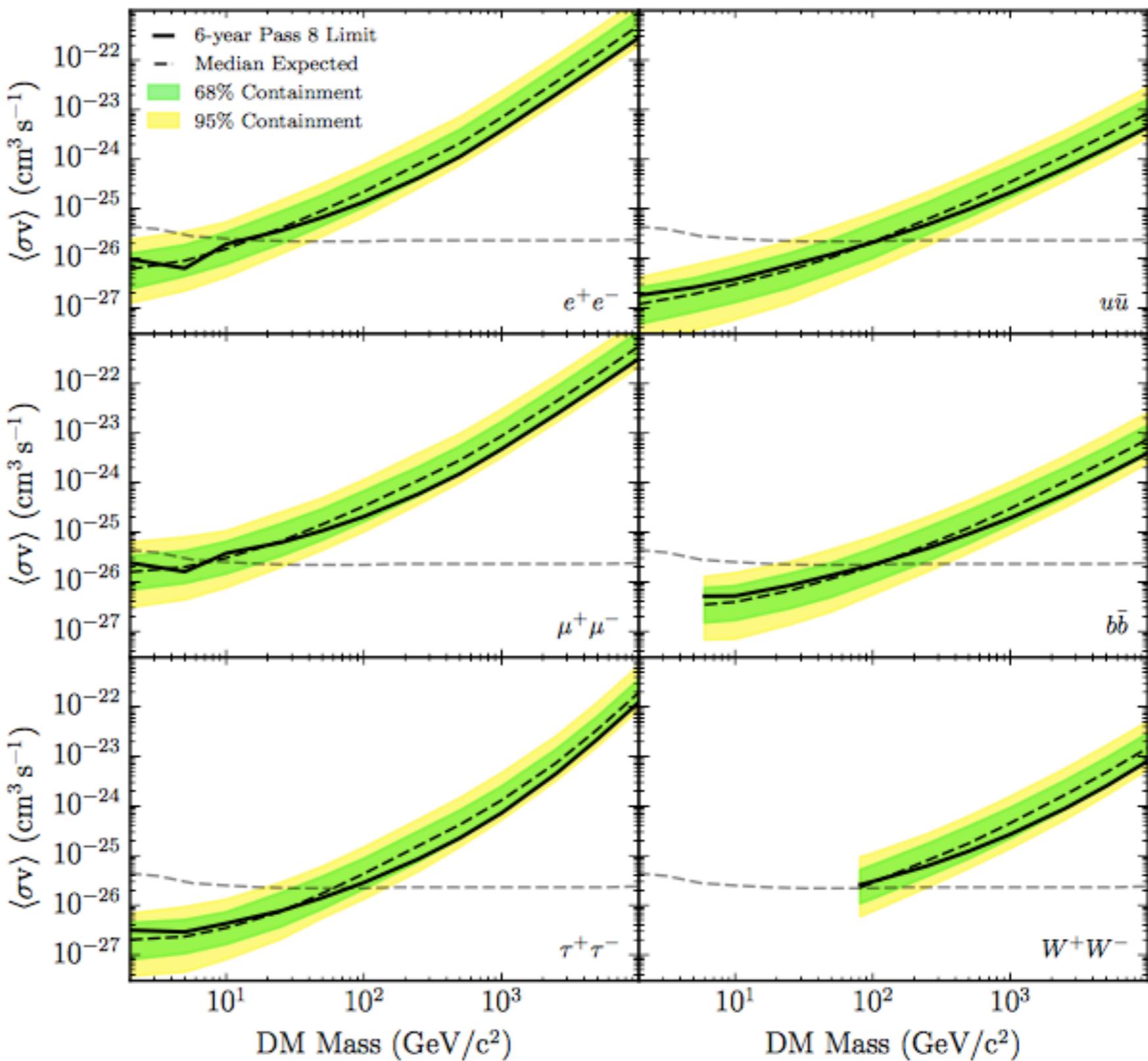


# DM Indirect search

Annihilation  
is p-wave suppressed

No bounds

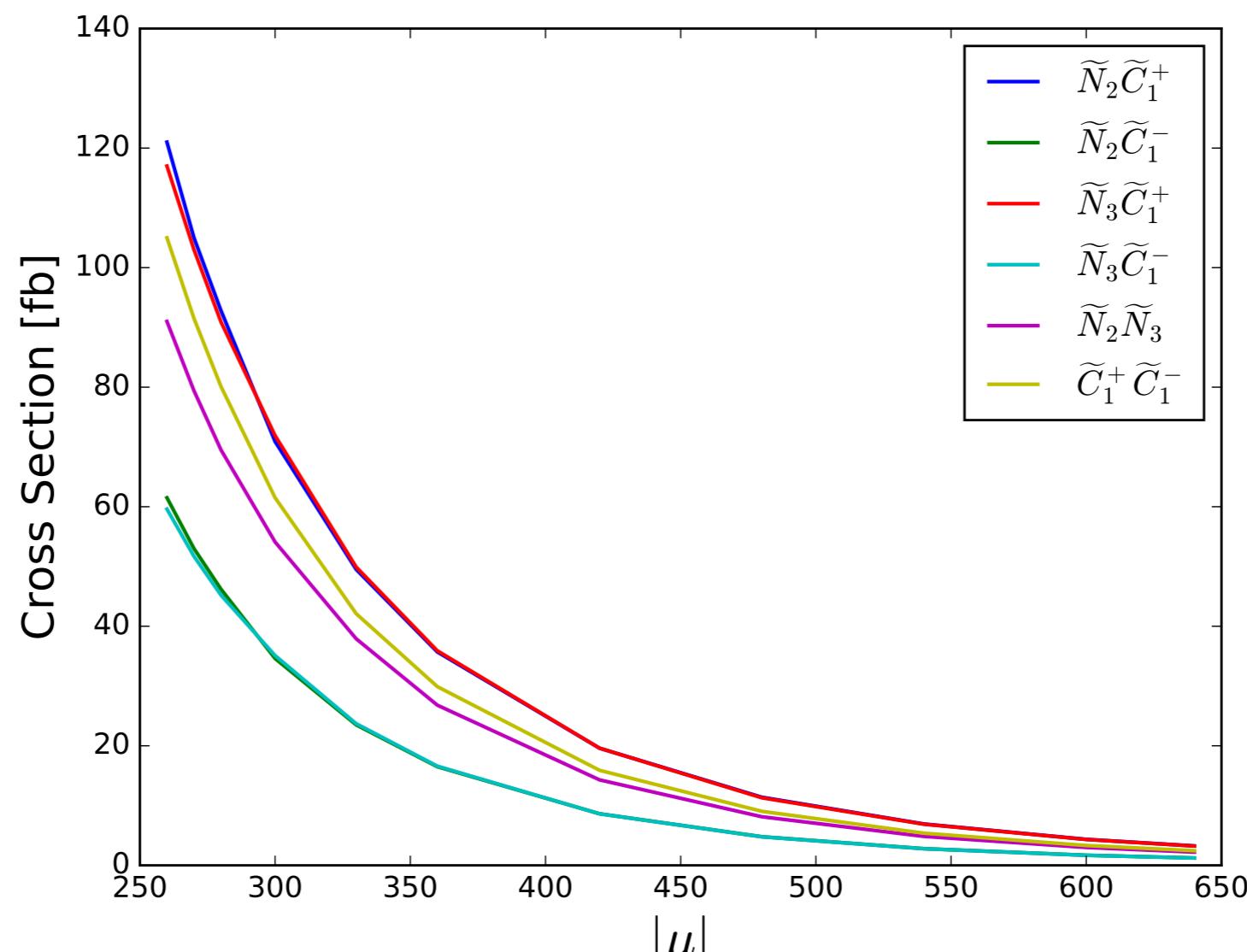
Fermi-LAT



# Production cross section of Higgsino-like neutralino/chargino

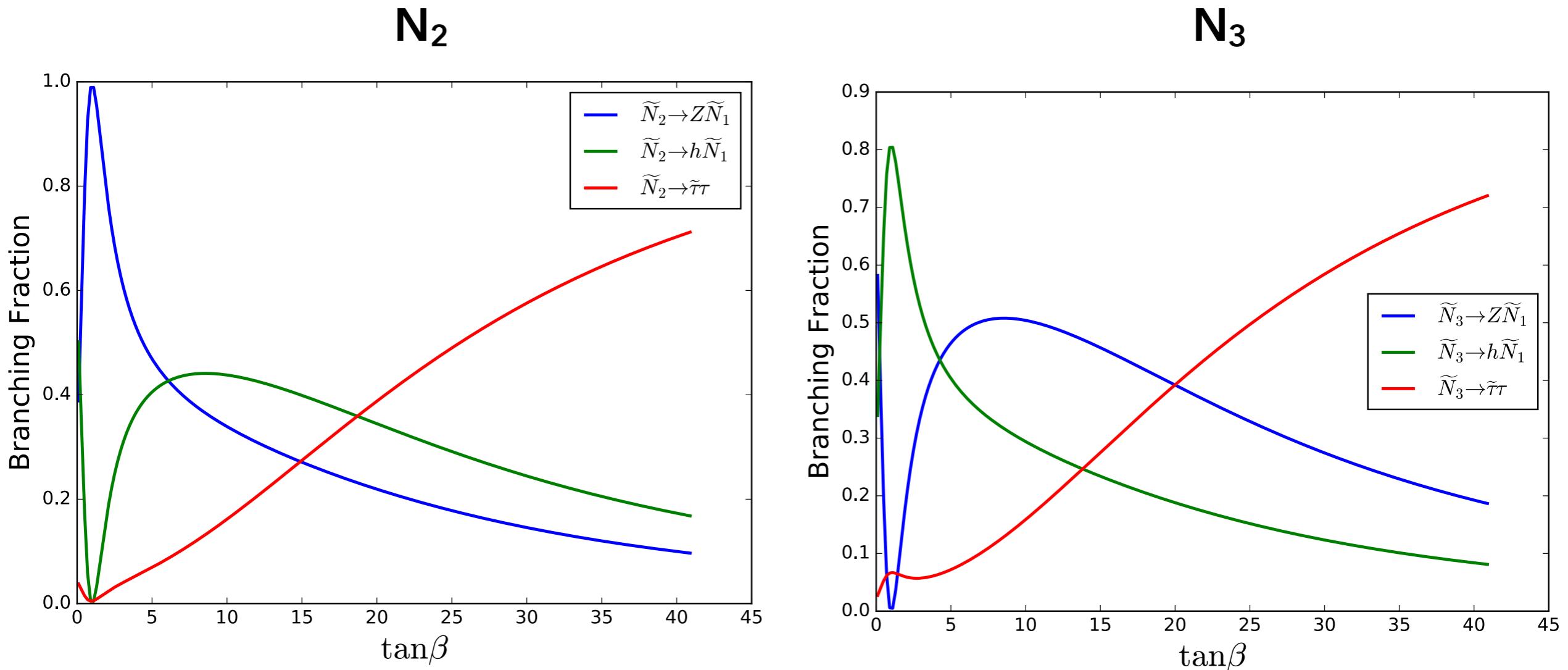
---

NLO production cross section of  $pp \rightarrow \tilde{N}_{2,3}\tilde{C}_1^\pm$



$M_1 = 100 \text{ GeV}, \mu < 0$

# Branching fractions of Higgsino-like neutralinos

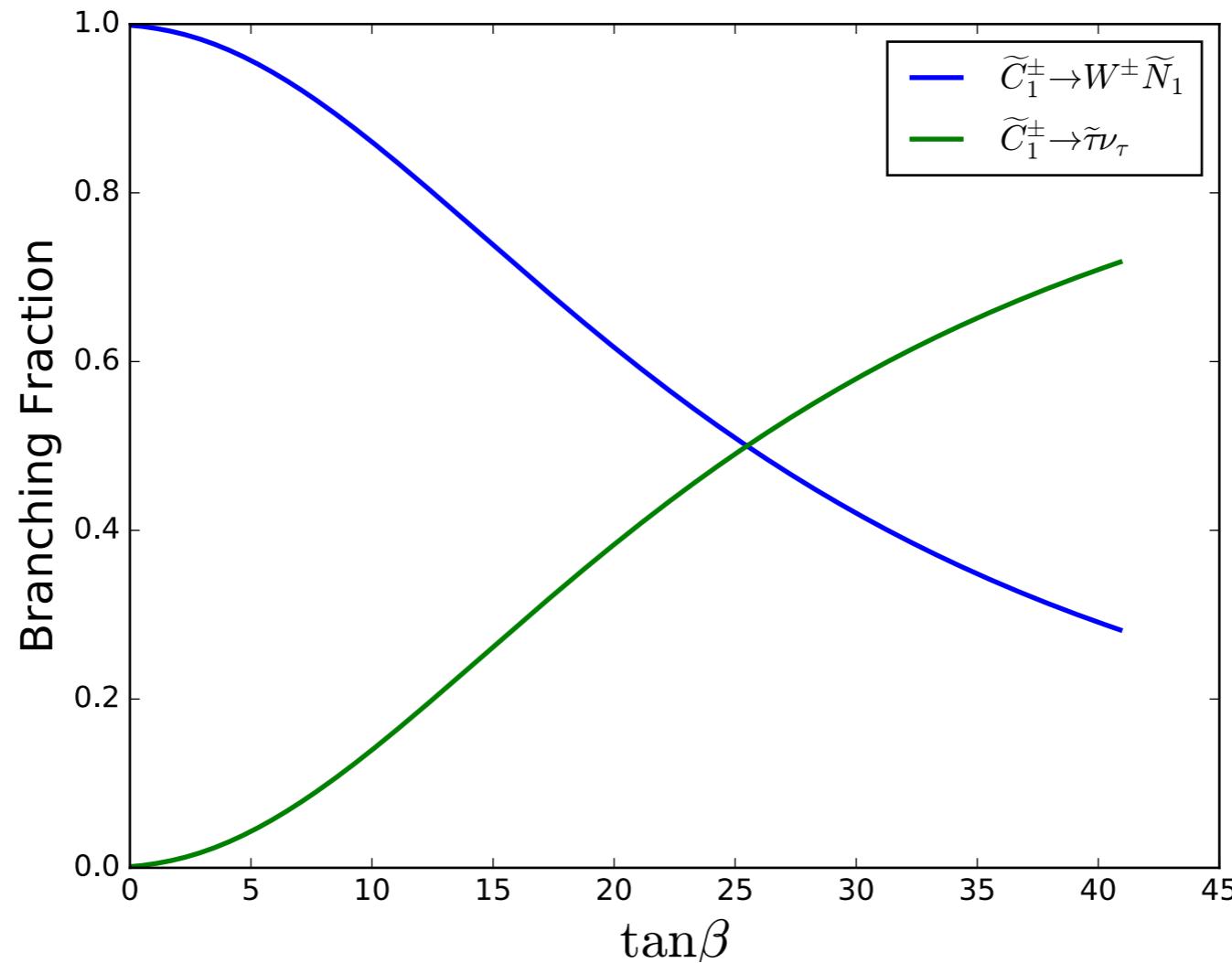


- $M_1 = 100 \text{ GeV}$ ,  $\mu = -500 \text{ GeV}$ ,  $m_R = 110 \text{ GeV}$  (which give  $\Omega_{\text{DM}}h^2 = 0.12$ )
- The Higgsino coupling to stau is Yukawa:  $y_\tau = m_\tau / v \cos\beta$
- Braching fraction to stau is enhanced for large  $\tan\beta$

# Branching fractions of Higgsino-like charginos

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$C_1^\pm$



The Higgsino coupling to stau is Yukawa:  $y_\tau \sim m_\tau / v \cos\beta$   
Enhanced for large  $\tan\beta$

# LHC simulation

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- Generate 50000 events for each **neutralino/chargino** production channel by Herwig++
- Their decay modes are restricted to  **$WZ$**  or  **$Wh$**
- Detector simulation and event selection are done by CheckMATE

**Acceptance** is obtained for each neutralino/chargino, each decay mode, and each signal region

$$A_{i,\pm}^{Z,\text{SRX}} = \frac{\text{\# of events which pass the cuts of SRX}}{\text{\# of generated events in } pp \rightarrow \tilde{N}_i \tilde{C}_1^\pm \rightarrow W \tilde{N}_1 Z \tilde{N}_1},$$

$$A_{23}^{Z,\text{SRX}} = \frac{\text{\# of events which pass the cuts of SRX}}{\text{\# of generated events in } pp \rightarrow \tilde{N}_2 \tilde{N}_3 \rightarrow Z \tilde{N}_1 Z \tilde{N}_1}.$$

# Expected number of events and evaluation

---

## Expected number of events for each signal region

$$N_{i,\pm}^{\text{SRX}} = \int \mathcal{L} \cdot \sigma(pp \rightarrow \tilde{N}_i \tilde{C}_1^\pm) \cdot \text{Br}(\tilde{N}_i \rightarrow Z\tilde{N}_1) \cdot \text{Br}(\tilde{C}_1^\pm \rightarrow W^\pm \tilde{N}_1) \cdot A_{i,\pm}^{Z,\text{SRX}}$$

$$+ \int \mathcal{L} \cdot \sigma(pp \rightarrow \tilde{N}_i \tilde{C}_1^\pm) \cdot \text{Br}(\tilde{N}_i \rightarrow h\tilde{N}_1) \cdot \text{Br}(\tilde{C}_1^\pm \rightarrow W^\pm \tilde{N}_1) \cdot A_{i,\pm}^{h,\text{SRX}},$$

$$N_{23}^{\text{SRX}} = \int \mathcal{L} \cdot \sigma(pp \rightarrow \tilde{N}_2 \tilde{N}_3) \cdot \text{Br}(\tilde{N}_2 \rightarrow Z\tilde{N}_1) \cdot \text{Br}(\tilde{N}_3 \rightarrow Z\tilde{N}_1) \cdot A_{23}^{Z,\text{SRX}}$$

$$+ \int \mathcal{L} \cdot \sigma(pp \rightarrow \tilde{N}_2 \tilde{N}_3) \cdot \text{Br}(\tilde{N}_2 \rightarrow h\tilde{N}_1) \cdot \text{Br}(\tilde{N}_3 \rightarrow h\tilde{N}_1) \cdot A_{23}^{h,\text{SRX}},$$

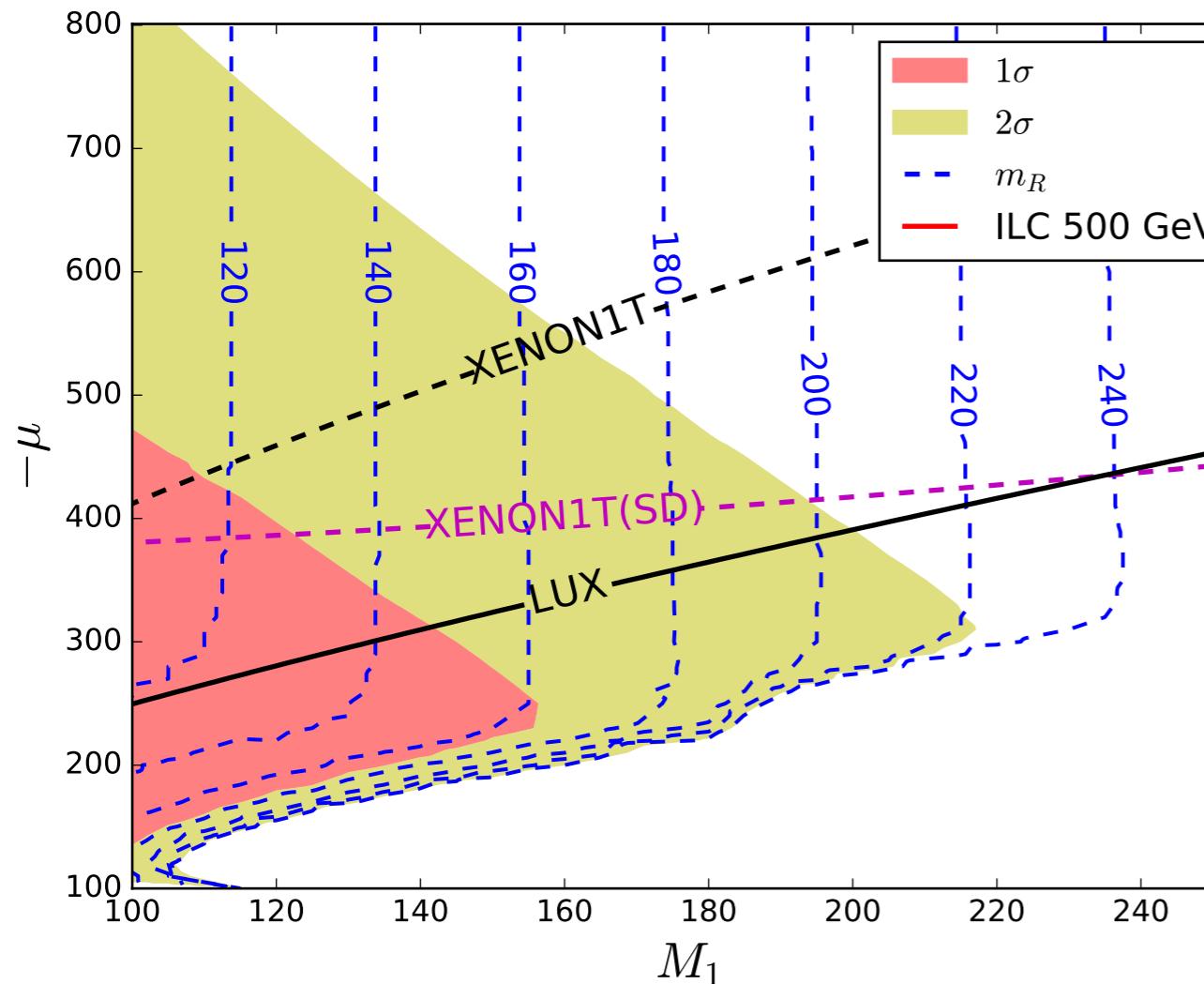
$$N^{\text{SRX}} \equiv \sum_{\text{ch}} N_{\text{ch}}^{\text{SRX}}$$

$$r^{\text{SRX}} \equiv \frac{N^{\text{SRX}} - 1.96\Delta N^{\text{SRX}}}{N_{95\text{exp}}^{\text{SRX}}}, \quad \text{is used for evaluation}$$

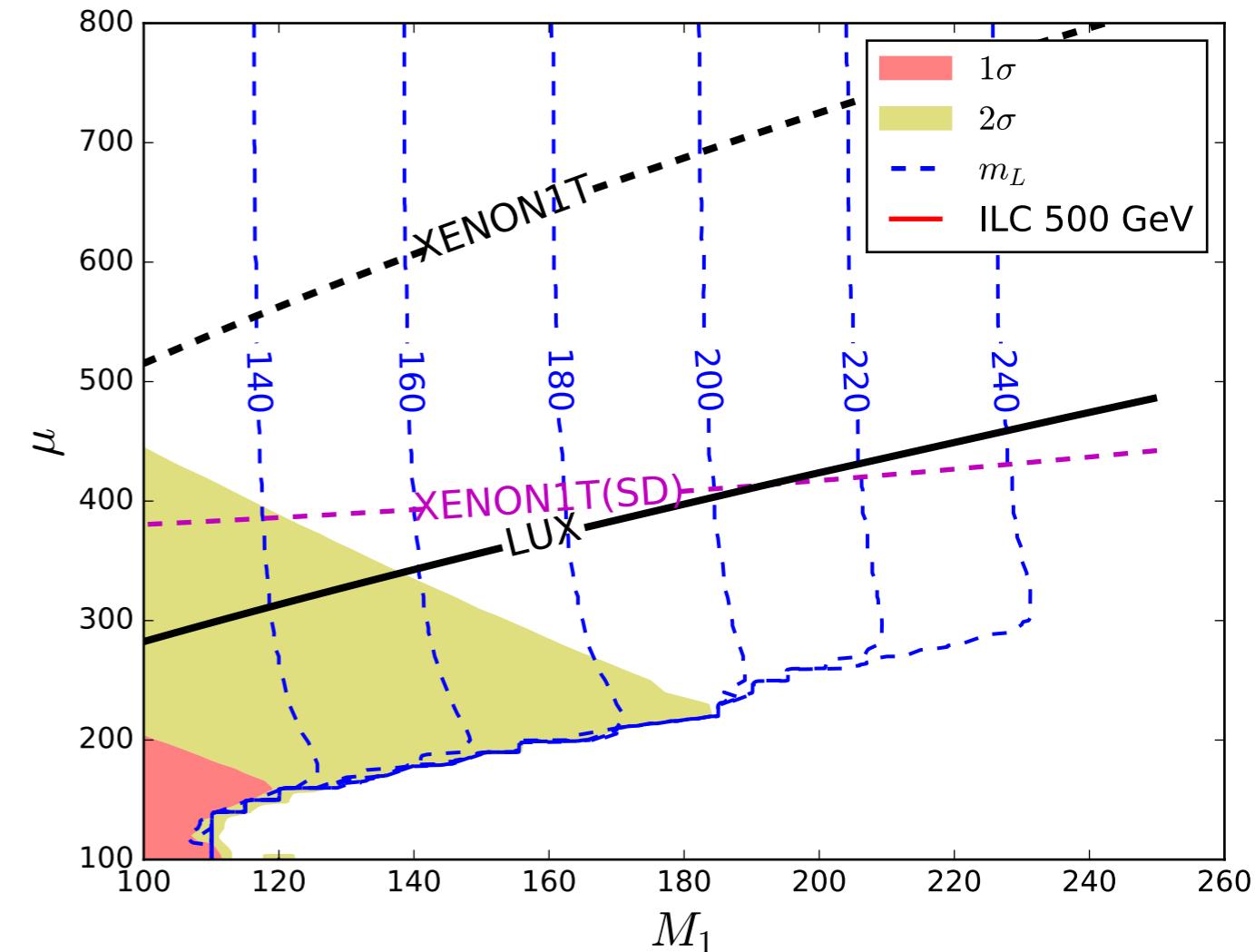
If  $r_{\max} \equiv \max_{\text{SR}}\{r^{\text{SRX}}\} > 1$  the model point is excluded at 95% CL.

# Spin-dependent scattering

BHR



BHL



Weaker expected limits than spin-independent  
No limits from XENON100