Homework7

Yining Song

Problem 2 (a) library(quantreg) ## Warning: package 'quantreg' was built under R version 3.4.4 ## Loading required package: SparseM ## Warning: package 'SparseM' was built under R version 3.4.4 ## Attaching package: 'SparseM' ## The following object is masked from 'package:base': ## ## backsolve library(quantmod) ## Loading required package: xts ## Warning: package 'xts' was built under R version 3.4.4 ## Loading required package: zoo ## Warning: package 'zoo' was built under R version 3.4.4 ## Attaching package: 'zoo' ## The following objects are masked from 'package:base': ## as.Date, as.Date.numeric ## ## Loading required package: TTR ## Warning: package 'TTR' was built under R version 3.4.4 ## Version 0.4-0 included new data defaults. See ?getSymbols. data(barro) A=getSymbols('AAPL',from = '2008-1-1', to = "2008-12-31",auto.assign=FALSE)[,6] ## 'getSymbols' currently uses auto.assign=TRUE by default, but will ## use auto.assign=FALSE in 0.5-0. You will still be able to use ## 'loadSymbols' to automatically load data. getOption("getSymbols.env") ## and getOption("getSymbols.auto.assign") will still be checked for ## alternate defaults. ## ## This message is shown once per session and may be disabled by setting ## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details. b=getSymbols('^ixic', from = '2008-1-1', to = "2008-12-31", auto.assign=FALSE)[,6] summary(A) ## AAPL.Adjusted Index

Min.

:2008-01-02

Min.

:10.00

```
## 1st Qu.:2008-04-02
                       1st Qu.:13.80
## Median :2008-07-01 Median :18.48
## Mean
         :2008-07-01 Mean :17.68
## 3rd Qu.:2008-09-30
                        3rd Qu.:21.54
## Max.
           :2008-12-30
                        Max.
                               :24.23
summary(b)
##
        Index
                        IXIC.Adjusted
## Min.
          :2008-01-02 Min. :1316
## 1st Qu.:2008-04-02
                        1st Qu.:2048
## Median :2008-07-01 Median :2305
## Mean
         :2008-07-01 Mean :2164
## 3rd Qu.:2008-09-30
                        3rd Qu.:2402
## Max.
          :2008-12-30 Max. :2610
1A = ROC(A) * 100
1b = ROC(b) * 100
beta1=coefficients(lm(lA~lb))[2]
beta1
##
         1b
## 1.078192
data1=cbind(lA,lb)
f=function(r){
  set.seed(r)
  sample=data1[sample(nrow(data1), size = nrow(A), replace = TRUE),]
 return (coef(summary(lm(AAPL.Adjusted~IXIC.Adjusted, data = sample)))[2,2])
mean(sapply(c(1:100), f))
## [1] 0.05956966
 (b)
library(dplyr)
## Warning: package 'dplyr' was built under R version 3.4.4
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:xts':
##
##
       first, last
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(ggplot2)
## Warning: package 'ggplot2' was built under R version 3.4.4
C=matrix(0,nrow = 1000,ncol = 5)
data2=read.table("Sensory.dat.txt",fill = T)
```

```
data2=as.matrix(data2[-c(1:2), ])
for (i in 1:10) {
  data2[3*i-1,]=c(i,data2[3*i-1,1:5])
  data2[3*i,]=c(i,data2[3*i,1:5])
print(data2)
                 VЗ
##
      V1
           V2
                       V4
                             V5
           "4.3" "4.9" "3.3" "5.3" "4.4"
## 3
     "1"
           "4.3" "4.5" "4.0" "5.5" "3.3"
## 4
           "4.1" "5.3" "3.4" "5.7" "4.7"
## 5
      "1"
## 6
     "2"
           "6.0" "5.3" "4.5" "5.9" "4.7"
## 7
      "2"
           "4.9" "6.3" "4.2" "5.5" "4.9"
           "6.0" "5.9" "4.7" "6.3" "4.6"
      "2"
## 8
           "2.4" "2.5" "2.3" "3.1" "2.4"
## 9
     "3"
           "3.9" "3.0" "2.8" "2.7" "1.3"
## 10 "3"
           "1.9" "3.9" "2.6" "4.6" "2.2"
## 11 "3"
## 12 "4"
           "7.4" "8.2" "6.4" "6.8" "6.0"
## 13 "4"
           "7.1" "7.9" "5.9" "7.3" "6.1"
## 14 "4"
           "6.4" "7.1" "6.9" "7.0" "6.7"
           "5.7" "6.3" "5.4" "6.1" "5.9"
## 15 "5"
           "5.8" "5.7" "5.4" "6.2" "6.5"
## 16 "5"
## 17 "5"
           "5.8" "6.0" "6.1" "7.0" "4.9"
## 18 "6"
           "2.2" "2.4" "1.7" "3.4" "1.7"
           "3.0" "1.8" "2.1" "4.0" "1.7"
## 19 "6"
## 20 "6"
           "2.1" "3.3" "1.1" "3.3" "2.1"
          "1.2" "1.5" "1.2" "0.9" "0.7"
## 21 "7"
## 22 "7"
           "1.3" "2.4" "0.8" "1.2" "1.3"
## 23 "7"
           "0.9" "3.1" "1.1" "1.9" "1.6"
## 24 "8"
           "4.2" "4.8" "4.5" "4.6" "3.2"
           "3.0" "4.5" "4.7" "4.9" "4.6"
## 25 "8"
           "4.8" "4.8" "4.7" "4.8" "4.3"
## 26 "8"
           "8.0" "8.6" "9.0" "9.4" "8.8"
## 27 "9"
## 28 "9"
           "9.0" "7.7" "6.7" "9.0" "7.9"
## 29 "9"
          "8.9" "9.2" "8.1" "9.1" "7.6"
## 30 "10" "5.0" "4.8" "3.9" "5.5" "3.8"
## 31 "10" "5.4" "5.0" "3.4" "4.9" "4.6"
## 32 "10" "2.8" "5.2" "4.1" "3.9" "5.5"
data2=data2 %>% as.data.frame() %>% rename(item = V1,I1 = V2, I2= V3, I3= V4, I4= V5,I5 = V6) %>%
 mutate_if(is.factor, as.character) %>% mutate_if(is.character, as.numeric )
## Warning: package 'bindrcpp' was built under R version 3.4.4
print(data2)
      item I1 I2 I3 I4 I5
## 1
         1 4.3 4.9 3.3 5.3 4.4
## 2
         1 4.3 4.5 4.0 5.5 3.3
## 3
         1 4.1 5.3 3.4 5.7 4.7
## 4
         2 6.0 5.3 4.5 5.9 4.7
         2 4.9 6.3 4.2 5.5 4.9
## 6
         2 6.0 5.9 4.7 6.3 4.6
## 7
         3 2.4 2.5 2.3 3.1 2.4
## 8
         3 3.9 3.0 2.8 2.7 1.3
```

```
## 9
         3 1.9 3.9 2.6 4.6 2.2
## 10
         4 7.4 8.2 6.4 6.8 6.0
         4 7.1 7.9 5.9 7.3 6.1
## 11
         4 6.4 7.1 6.9 7.0 6.7
## 12
## 13
         5 5.7 6.3 5.4 6.1 5.9
## 14
         5 5.8 5.7 5.4 6.2 6.5
## 15
         5 5.8 6.0 6.1 7.0 4.9
         6 2.2 2.4 1.7 3.4 1.7
## 16
## 17
         6 3.0 1.8 2.1 4.0 1.7
## 18
         6 2.1 3.3 1.1 3.3 2.1
## 19
         7 1.2 1.5 1.2 0.9 0.7
         7 1.3 2.4 0.8 1.2 1.3
## 20
## 21
         7 0.9 3.1 1.1 1.9 1.6
## 22
         8 4.2 4.8 4.5 4.6 3.2
## 23
         8 3.0 4.5 4.7 4.9 4.6
## 24
         8 4.8 4.8 4.7 4.8 4.3
## 25
         9 8.0 8.6 9.0 9.4 8.8
## 26
         9 9.0 7.7 6.7 9.0 7.9
## 27
         9 8.9 9.2 8.1 9.1 7.6
        10 5.0 4.8 3.9 5.5 3.8
## 28
## 29
        10 5.4 5.0 3.4 4.9 4.6
## 30
        10 2.8 5.2 4.1 3.9 5.5
g=function(r){
  sample=data2[sample(nrow(data2), size = 100, replace = TRUE),2:6]
  return (coef(summary(lm(I1~I2+I3+I4+I5, data=data2)))[,1])
}
t1=Sys.time()
res=sapply(c(1:100),g)
t2=Sys.time()
t2-t1
## Time difference of 0.5350311 secs
res=res %>% as.data.frame() %>% rename(I2=V2,I3=V3,I4=V4,I5=V5,
                                           Intercep = V1)
summary(res)
##
                              12
                                                  I3
       Intercep
    Min.
           :-0.57913
                               :-0.57913
                                                   :-0.57913
                       Min.
                                           Min.
##
    1st Qu.:-0.12963
                       1st Qu.:-0.12963
                                           1st Qu.:-0.12963
    Median: 0.25241
                       Median : 0.25241
                                           Median: 0.25241
##
    Mean
           : 0.09043
                       Mean
                               : 0.09043
                                           Mean
                                                  : 0.09043
    3rd Qu.: 0.34132
                        3rd Qu.: 0.34132
                                           3rd Qu.: 0.34132
##
    Max.
           : 0.56720
                       Max.
                               : 0.56720
                                           Max.
                                                   : 0.56720
##
          14
                              15
                                                  V6
##
          :-0.57913
                               :-0.57913
                                                  :-0.57913
   Min.
                       Min.
                                           Min.
   1st Qu.:-0.12963
                       1st Qu.:-0.12963
                                           1st Qu.:-0.12963
##
  Median: 0.25241
                       Median : 0.25241
                                           Median: 0.25241
##
   Mean
           : 0.09043
                       Mean
                               : 0.09043
                                           Mean
                                                  : 0.09043
    3rd Qu.: 0.34132
                        3rd Qu.: 0.34132
                                           3rd Qu.: 0.34132
##
    Max.
           : 0.56720
                               : 0.56720
                                                  : 0.56720
                       Max.
                                           Max.
##
          ۷7
                              V8
                                                  V9
##
           :-0.57913
                               :-0.57913
                                                  :-0.57913
    Min.
                       Min.
                                           Min.
    1st Qu.:-0.12963
                        1st Qu.:-0.12963
                                           1st Qu.:-0.12963
   Median : 0.25241
                       Median : 0.25241
                                           Median: 0.25241
```

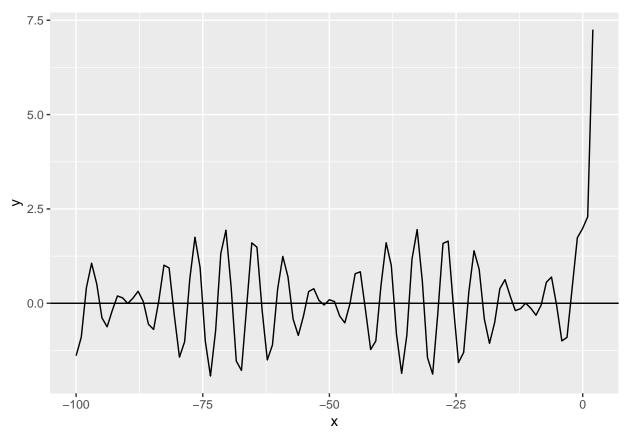
```
Mean : 0.09043
                      Mean
                             : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
                      Max. : 0.56720
##
   Max. : 0.56720
                                         Max. : 0.56720
##
        V10
                           V11
                                             V12
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V13
                           V14
                                             V15
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
##
        V16
                           V17
                                             V18
                                         Min. :-0.57913
                      Min. :-0.57913
##
   Min. :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V19
##
                           V20
                                             V21
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V22
                           V23
                                             V24
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
##
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V25
                           V26
                                              V27
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
        V28
                           V29
                                              V30
##
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min.
                                               :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median : 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V31
                           V32
                                              V33
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
```

```
1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median : 0.25241
##
                                         Median: 0.25241
                      Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V34
                           V35
                                             V36
   Min. :-0.57913
                      Min. :-0.57913
                                         Min.
                                               :-0.57913
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
    3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
##
        V37
                           V38
                                             V39
##
   Min.
         :-0.57913
                      Min.
                           :-0.57913
                                         Min.
                                             :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
    3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
##
        V40
                           V41
                                             V42
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
    1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V43
                           V44
                                             V45
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
        V46
                           V47
                                             V48
##
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V49
                           V50
##
                                             V51
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max.
         : 0.56720
                      Max. : 0.56720
                                         Max.
                                              : 0.56720
##
        V52
                                             V54
                           V53
   Min. :-0.57913
                      Min. :-0.57913
##
                                         Min. :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median : 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
                      3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
```

```
##
        V55
                           V56
                                              V57
                      Min. :-0.57913
                                         Min. :-0.57913
##
   Min.
         :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median : 0.25241
##
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
                      Max. : 0.56720
                                         Max. : 0.56720
##
   Max. : 0.56720
        V58
                           V59
##
                                              V60
##
   Min.
          :-0.57913
                             :-0.57913
                                         Min.
                                               :-0.57913
                      Min.
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
                      Max. : 0.56720
                                         Max. : 0.56720
##
   Max. : 0.56720
##
        V61
                           V62
                                              V63
##
          :-0.57913
                      Min. :-0.57913
                                               :-0.57913
   Min.
                                         Min.
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
##
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
        V64
                           V65
                                              V66
##
##
   Min. :-0.57913
                             :-0.57913
                                               :-0.57913
                      Min.
                                         Min.
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
##
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
        V67
                           V68
                                              V69
##
##
          :-0.57913
                      Min.
                             :-0.57913
                                               :-0.57913
   Min.
                                         Min.
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median : 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
                      3rd Qu.: 0.34132
##
   3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V70
                           V71
                                              V72
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                                         Mean : 0.09043
##
                      Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V73
                           V74
                                             V75
##
##
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median: 0.25241
                                         Median : 0.25241
##
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V76
                           V77
                                              V78
##
                      Min. :-0.57913
   Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
```

```
3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
                                         Max. : 0.56720
   Max. : 0.56720
                      Max. : 0.56720
##
##
        V79
                           V80
                                              V81
          :-0.57913
                             :-0.57913
                                         Min.
                                                :-0.57913
##
   Min.
                      Min.
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median : 0.25241
                      Median : 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
        V82
                           V83
                                              V84
##
##
   Min.
          :-0.57913
                      Min.
                             :-0.57913
                                         Min.
                                                :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
##
   Median: 0.25241
                      Median: 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V85
                           V86
                                              V87
          :-0.57913
                             :-0.57913
                                               :-0.57913
##
   Min.
                      Min.
                                         Min.
                      1st Qu.:-0.12963
##
   1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median : 0.25241
                      Median : 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
                      Max. : 0.56720
   Max. : 0.56720
                                         Max. : 0.56720
##
        887
                           V89
                                              V90
##
##
   Min.
         :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median : 0.25241
                                         Median: 0.25241
##
                      Mean : 0.09043
##
   Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V91
                           V92
                                              V93
##
   Min.
         :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
    1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   Median: 0.25241
                      Median : 0.25241
                                         Median: 0.25241
##
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V94
                           V95
                                              V96
   Min. :-0.57913
                      Min. :-0.57913
                                         Min. :-0.57913
##
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
   1st Qu.:-0.12963
##
   Median: 0.25241
                      Median : 0.25241
                                         Median: 0.25241
   Mean : 0.09043
                      Mean : 0.09043
                                         Mean : 0.09043
##
   3rd Qu.: 0.34132
##
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
   Max. : 0.56720
##
                      Max. : 0.56720
                                         Max. : 0.56720
        V97
                           V98
                                              V99
##
   Min. :-0.57913
##
                      Min. :-0.57913
                                         Min.
                                               :-0.57913
##
   1st Qu.:-0.12963
                      1st Qu.:-0.12963
                                         1st Qu.:-0.12963
##
   Median: 0.25241
                      Median: 0.25241
                                         Median : 0.25241
                                         Mean : 0.09043
##
   Mean : 0.09043
                      Mean : 0.09043
##
   3rd Qu.: 0.34132
                      3rd Qu.: 0.34132
                                         3rd Qu.: 0.34132
##
   Max. : 0.56720
                      Max. : 0.56720
                                         Max. : 0.56720
##
        V100
##
   Min.
          :-0.57913
##
   1st Qu.:-0.12963
```

```
## Median: 0.25241
## Mean : 0.09043
## 3rd Qu.: 0.34132
## Max. : 0.56720
 (c)
library(parallel)
library(foreach)
library(doParallel)
## Loading required package: iterators
cs=detectCores()
cl=makeCluster(cs[1]-1)
registerDoParallel(cl)
h=function(r){
  set.seed(r)
  sample=data2[sample(nrow(data2), size = 100, replace = TRUE),2:6]
  return (coef(summary(lm(I1~I2+I3+I4+I5, data =data2)))[,1])
tt1=Sys.time()
res=sapply(c(1:100),h)
tt2=Sys.time()
tt2-tt1
## Time difference of 0.558032 secs
stopCluster(cl)
Problem 3
 (a)
library(ggplot2)
f=function(x){
  y=3^x-\sin(x)+\cos(5*x)
  return(y)
g=function(x){
  y=3^x*log(3)-cos(x)-5*sin(5*x)
  return(y)
ggplot(data=data.frame(x = 0,y = 0), mapping = aes(x = x)) +
  stat_function(fun=f) +
  xlim(-100, 2) +
  geom_abline(intercept = 0, slope = 0)
```



```
froot=function(x) {while (abs(f(x)-0) > 1e-6) {
   z=x-f(x)/g(x)
   return(z)
}}
froot(2.5)
```

[1] 1.624361

```
T1=Sys.time()
sapply(c(-100:0), froot)
```

```
-97.1339503
     [1] -100.4342823
                                                                  -96.0600686
##
                        -99.1621869
                                      -99.1194764
##
          -95.0360278
                        -93.9858536
                                      -92.4718422
                                                    -91.9017118
                                                                  -90.7854984
     [6]
##
          -89.9448030
                        -88.7373202
                                      -79.4194620
                                                    -86.8382937
                                                                  -85.2054910
    [11]
##
    [16]
          -85.2805280
                        -83.6248825
                                      -84.5068908
                                                    -82.0718857
                                                                  -78.0191884
##
    [21]
          -80.3665802
                        -78.9212411
                                      -78.4727334
                                                    -77.1700302
                                                                  -78.6124263
    [26]
          -75.1450525
                        -74.0658592
                                      -73.0469512
                                                    -71.9948163
                                                                  -70.8415352
##
##
    [31]
          -69.9096796
                        -68.8049472
                                      -67.9508221
                                                    -66.7513732
                                                                  -62.9865812
##
    [36]
          -64.8463570
                        -63.2799074
                                      -63.3045042
                                                    -61.6468717
                                                                  -62.8322827
##
    [41]
          -60.0807903
                        -56.8890831
                                      -58.3873681
                                                    -56.9335988
                                                                  -56.5168884
##
    [46]
          -55.1781686
                        -45.6419139
                                      -53.1566295
                                                    -52.0716457
                                                                  -51.0586646
##
    [51]
                                      -47.9175624
                                                    -46.8227015
                                                                  -45.9569161
          -50.0036762
                        -48.9132195
##
    [56]
          -44.7646308
                        -42.1826879
                                      -42.8541247
                                                    -41.3425789
                                                                  -41.3315821
    [61]
##
          -39.6669051
                        -41.3348749
                                      -38.0899064
                                                    -35.3656540
                                                                  -36.4100880
##
    [66]
          -34.9450991
                        -34.5682344
                                      -33.1866305
                                                    -30.3864667
                                                                  -31.1687461
##
    [71]
          -30.0774495
                        -29.0713459
                                      -28.0124650
                                                    -26.9458953
                                                                  -25.9253854
##
    [76]
          -24.8390328
                       -23.9631295
                                      -22.7771810
                                                    -20.7057779
                                                                 -20.8616251
```

```
## [81] -19.3961502 -19.3625183 -17.6852583 -20.2150144 -16.0992802
## [86] -13.6668824 -14.4350523 -12.9559035 -12.6288192 -11.1954467
## [91] -9.1096109 -9.1814838
                                  -8.0833255 -7.0850801 -6.0209859
## [96]
         -4.9613203
                       -3.9357074 -2.8641956 -1.9168900 -0.7064704
## [101] -20.2814480
T2=Sys.time()
T2-T1
## Time difference of 0.03600216 secs
 (b)
T3=Sys.time()
mclapply(-100:0, froot, mc.cores = 1)
## [[1]]
## [1] -100.4343
##
## [[2]]
## [1] -99.16219
## [[3]]
## [1] -99.11948
##
## [[4]]
## [1] -97.13395
##
## [[5]]
## [1] -96.06007
## [[6]]
## [1] -95.03603
##
## [[7]]
## [1] -93.98585
## [[8]]
## [1] -92.47184
##
## [[9]]
## [1] -91.90171
##
## [[10]]
## [1] -90.7855
##
## [[11]]
## [1] -89.9448
##
## [[12]]
## [1] -88.73732
## [[13]]
## [1] -79.41946
##
## [[14]]
```

```
## [1] -86.83829
##
## [[15]]
## [1] -85.20549
## [[16]]
## [1] -85.28053
##
## [[17]]
## [1] -83.62488
## [[18]]
## [1] -84.50689
##
## [[19]]
## [1] -82.07189
##
## [[20]]
## [1] -78.01919
## [[21]]
## [1] -80.36658
##
## [[22]]
## [1] -78.92124
## [[23]]
## [1] -78.47273
##
## [[24]]
## [1] -77.17003
##
## [[25]]
## [1] -78.61243
## [[26]]
## [1] -75.14505
##
## [[27]]
## [1] -74.06586
## [[28]]
## [1] -73.04695
##
## [[29]]
## [1] -71.99482
##
## [[30]]
## [1] -70.84154
## [[31]]
## [1] -69.90968
##
```

[[32]]

```
## [1] -68.80495
##
## [[33]]
## [1] -67.95082
## [[34]]
## [1] -66.75137
##
## [[35]]
## [1] -62.98658
## [[36]]
## [1] -64.84636
##
## [[37]]
## [1] -63.27991
##
## [[38]]
## [1] -63.3045
## [[39]]
## [1] -61.64687
##
## [[40]]
## [1] -62.83228
## [[41]]
## [1] -60.08079
##
## [[42]]
## [1] -56.88908
##
## [[43]]
## [1] -58.38737
## [[44]]
## [1] -56.9336
##
## [[45]]
## [1] -56.51689
## [[46]]
## [1] -55.17817
##
## [[47]]
## [1] -45.64191
##
## [[48]]
## [1] -53.15663
## [[49]]
## [1] -52.07165
##
```

[[50]]

```
## [1] -51.05866
##
## [[51]]
## [1] -50.00368
## [[52]]
## [1] -48.91322
##
## [[53]]
## [1] -47.91756
## [[54]]
## [1] -46.8227
##
## [[55]]
## [1] -45.95692
##
## [[56]]
## [1] -44.76463
## [[57]]
## [1] -42.18269
##
## [[58]]
## [1] -42.85412
## [[59]]
## [1] -41.34258
##
## [[60]]
## [1] -41.33158
##
## [[61]]
## [1] -39.66691
## [[62]]
## [1] -41.33487
##
## [[63]]
## [1] -38.08991
## [[64]]
## [1] -35.36565
##
## [[65]]
## [1] -36.41009
##
## [[66]]
## [1] -34.9451
## [[67]]
## [1] -34.56823
##
```

[[68]]

```
## [1] -33.18663
##
## [[69]]
## [1] -30.38647
## [[70]]
## [1] -31.16875
##
## [[71]]
## [1] -30.07745
## [[72]]
## [1] -29.07135
##
## [[73]]
## [1] -28.01246
##
## [[74]]
## [1] -26.9459
## [[75]]
## [1] -25.92539
##
## [[76]]
## [1] -24.83903
## [[77]]
## [1] -23.96313
##
## [[78]]
## [1] -22.77718
##
## [[79]]
## [1] -20.70578
## [[80]]
## [1] -20.86163
##
## [[81]]
## [1] -19.39615
## [[82]]
## [1] -19.36252
##
## [[83]]
## [1] -17.68526
##
## [[84]]
## [1] -20.21501
## [[85]]
## [1] -16.09928
##
```

[[86]]

```
## [1] -13.66688
##
## [[87]]
## [1] -14.43505
## [[88]]
## [1] -12.9559
##
## [[89]]
## [1] -12.62882
## [[90]]
## [1] -11.19545
##
## [[91]]
## [1] -9.109611
##
## [[92]]
## [1] -9.181484
## [[93]]
## [1] -8.083326
##
## [[94]]
## [1] -7.08508
## [[95]]
## [1] -6.020986
##
## [[96]]
## [1] -4.96132
##
## [[97]]
## [1] -3.935707
## [[98]]
## [1] -2.864196
##
## [[99]]
## [1] -1.91689
## [[100]]
## [1] -0.7064704
##
## [[101]]
## [1] -20.28145
T4=Sys.time()
T3-T4
```

Time difference of -0.01200104 secs