

# Non-Vertical Cultural Transmission, Assortment, and the Evolution of Cooperation

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## Abstract

Cultural evolution of cooperation under vertical and non-vertical cultural transmission is studied, and conditions are found for fixation and coexistence of cooperation and defection. The evolution of cooperation is facilitated by horizontal transmission and by an association between social interactions and horizontal transmission. The effect of oblique transmission depends on the horizontal transmission bias. Stable polymorphism of cooperation and defection can occur, and when it does, reduced association between social interactions and horizontal transmission evolves, which leads to a decreased frequency of cooperation and lower population mean fitness. The deterministic conditions are compared to outcomes of stochastic simulations of structured populations. Parallels are drawn with Hamilton's rule incorporating assortment and effective relatedness.

## 22 Introduction

Cooperative behavior can reduce an individual's fitness and increase the fitness of its conspecifics or competitors (Axelrod and Hamilton, 1981). Nevertheless, cooperative behavior appears to occur in many non-human animals (Dugatkin, 1997), including primates (Jaeggi and Gurven, 2013), rats (Rice and Gainer, 1962), birds (Stacey and Koenig, 1990; Krams et al., 2008), and lizards (Sinervo et al., 2006). Evolution of cooperative behavior remains an important conundrum in evolutionary biology (Haldane, 1932, Appendix).

Since the work of Hamilton (1964) and Axelrod and Hamilton (1981), theories for the evolution of cooperative and altruistic behaviors have been intertwined often under the rubric of *kin selection*. Kin selection theory posits that natural selection is more likely to favor cooperation between more closely related individuals. The importance of *relatedness* to the evolution of cooperation and altruism was demonstrated by Hamilton (1964), who showed that an allele that determines cooperative behavior will increase in frequency if the reproductive cost to the actor that cooperates,  $c$ , is less than the benefit to the recipient,  $b$ , times the relatedness,  $r$ , between the recipient and the actor. This condition is known as *Hamilton's rule*:

$$c < b \cdot r, \quad (1)$$

where the relatedness coefficient  $r$  measures the probability that an allele sampled from the cooperator is identical by descent to one at the same locus in the recipient.

Eshel and Cavalli-Sforza (1982) studied a related model for the evolution of cooperative behavior. Their model included *assortative meeting*, or non-random encounters, where a fraction  $m$  of individuals in the population each interact specifically with an individual of the same phenotype, and a fraction  $1 - m$  interacts with a randomly chosen individual. Such assortative meeting may be due, for example, to population structure or active partner choice. In their model, cooperative behavior can evolve if (Eshel and Cavalli-Sforza, 1982, eq. 3.2)

$$c < b \cdot m, \quad (2)$$

where  $b$  and  $c$  are the benefit and cost of cooperation<sup>1</sup>.

The role of assortment in the evolution of altruism was emphasized by Fletcher and Doebeli (2009). They found that in a *public-goods* game, altruism will evolve if cooperative individuals experience more cooperation, on average, than defecting individuals, and “thus, the evolution of altruism requires (positive) assortment between focal *cooperative* players and cooperative acts in their interaction environment.” With some change in parameters, this condition is summarized by (Fletcher and Doebeli, 2009, eq. 2.3)

$$c < b \cdot (p_C - p_D), \quad (3)$$

where  $p_C$  is the probability that a cooperator receives help, and  $p_D$  is the probability that a defector receives help.<sup>2</sup> Bijma and Aanen (2010) obtained a result related to inequality 3 for other types of games.

In this paper we study the evolution of a cooperative behavior that is subject to *cultural transmission*, which allows an individual to acquire attitudes or behavioral traits from other individuals in its social group through imitation, learning, or other modes of communication (Cavalli-Sforza and Feldman, 1981; Richerson and Boyd, 2008). Feldman et al. (1985) introduced the first model for the evolution of altruism by cultural transmission with kin selection and demonstrated that if the fidelity of cultural

<sup>1</sup>In an extended model, which allows an individual to encounter  $N$  individuals before choosing a partner, the right hand side is multiplied by  $E[N]$ , the expected number of encounters (Eshel and Cavalli-Sforza, 1982, eq. 4.6).

<sup>2</sup>Inequality 3 generalizes inequalities 1 and 2 by substituting  $p_C = r + p$ ,  $p_D = p$  and  $p_C = m + (1 - m)p$ ,  $p_D = (1 - m)p$ , respectively, where  $p$  is the frequency of cooperators.

transmission of altruism is  $\varphi$ , then the condition for evolution of altruism in the case of sib-to-sib  
64 altruism is (Feldman et al., 1985, Eq. 16)

$$c < b \cdot \varphi - \frac{1 - \varphi}{\varphi}. \quad (4)$$

66 In inequality 4,  $\varphi$  takes the role of relatedness ( $r$  in inequality 1) or assortment ( $m$  in inequality 2), but  
the effective benefit  $b \cdot \varphi$  is reduced by  $(1 - \varphi)/\varphi$ . This shows that under a combination of genetic  
68 and cultural transmission, the condition for the evolutionary success of altruism entails a modification  
of Hamilton's rule (inequality 1).

70 Cultural transmission may be modeled as vertical, horizontal, or oblique: vertical transmission occurs  
between parents and offspring, horizontal transmission occurs between individuals from the same  
72 generation, and oblique transmission occurs to offspring from the generation to which their parents  
belong (i.e. from non-parental adults). Evolution under either of these transmission models can  
74 be be more rapid than under pure vertical transmission (Cavalli-Sforza and Feldman, 1981; Lycett  
and Gowlett, 2008; Ram et al., 2018). Both Woodcock (2006) and Lewin-Epstein et al. (2017)  
76 demonstrated that non-vertical transmission can help explain the evolution of cooperative behavior  
(the former using simulations with cultural transmission, the latter using a model where cooperation is  
78 mediated by microbes that manipulate their host's behavior.) Some of the analyses by Lewin-Epstein  
et al. (2017) can be applied to cultural transmission, because models of cultural transmission are  
80 mathematically similar to those for transmission of infectious diseases (Cavalli-Sforza and Feldman,  
1981).

82 Here, we study models for the cultural evolution of cooperation that include both vertical and non-  
vertical transmission. In our models behavioral changes are mediated by cultural transmission that  
84 can occur specifically during social interactions. For instance, there may be an association between  
the choice of partner for social interaction and the choice of partner for cultural transmission, or when  
86 an individual interacts with an individual of a different phenotype, exposure to the latter may lead  
the former to convert its phenotype. Our results demonstrate that cultural transmission can enhance  
88 the evolution of cooperation even when genetic transmission cannot, partly because it can facilitate  
the generation of assortment (Fletcher and Doebeli, 2009), and partly because it can diminish the  
90 effect of natural selection (Ram et al., 2018). This further emphasizes that treatment of cooperation  
as a cultural trait, rather than a genetic one, can lead to a broader understanding of its evolutionary  
92 dynamics.

## Models

94 Consider a large population whose members can be one of two phenotypes:  $\phi = A$  for cooperators or  
 $\phi = B$  for defectors. An offspring inherits its phenotype from its parent via vertical transmission with  
96 probability  $v$  or from a random individual in the parental population via oblique transmission with  
probability  $(1 - v)$ . Following Ram et al. (2018), given that the parent's phenotype is  $\phi$  and assuming  
98 uni-parental inheritance (Zefferman, 2016), the conditional probability that the phenotype  $\phi'$  of the  
offspring is  $A$  is

$$100 \quad P(\phi' = A \mid \phi) = \begin{cases} v + (1 - v)p, & \text{if } \phi = A \\ (1 - v)p, & \text{if } \phi = B \end{cases}, \quad (5)$$

where  $p = P(\phi = A)$  is the frequency of  $A$  among all adults in the parental generation.

102 Not all adults become parents due to natural selection, and we denote the frequency of phenotype  $A$   
among parents by  $\tilde{p}$ . Therefore, the frequency  $\hat{p}$  of phenotype  $A$  among juveniles (after selection and  
104 vertical and oblique transmission) is

$$\hat{p} = \tilde{p}[v + (1 - v)p] + (1 - \tilde{p})[(1 - v)p] = v\tilde{p} + (1 - v)p . \quad (6)$$

106 Individuals are assumed to interact according to a *prisoner's dilemma*. Specifically, individuals  
 108 interact in pairs; a cooperator suffers a fitness cost  $0 < c < 1$ , and its partner gains a fitness benefit  
 $b$ , where we assume  $c < b$ . Table 1 shows the payoff matrix, i.e. the fitness of an individual with  
 phenotype  $\phi_1$  when interacting with a partner of phenotype  $\phi_2$ .

110 Social interactions occur randomly: two juvenile individuals with phenotype  $A$  interact with proba-  
 bility  $\hat{p}^2$ , two juveniles with phenotype  $B$  interact with probability  $(1 - \hat{p})^2$ , and two juveniles with  
 112 different phenotypes interact with probability  $2\hat{p}(1 - \hat{p})$ . Horizontal cultural transmission occurs  
 between pairs of individuals from the same generation. It occurs between socially interacting partners  
 114 with probability  $\alpha$ , or between a random pair with probability  $1 - \alpha$  (see Figure 1). However, hor-  
 izontal transmission is not always successful, as one partner may reject the other's phenotype. The  
 116 probability of successful horizontal transmission of phenotypes  $A$  and  $B$  are  $T_A$  and  $T_B$ , respectively  
 (Table 2). Then, the frequency  $p'$  of phenotype  $A$  among adults in the next generation, after horizontal  
 118 transmission, is

$$\begin{aligned} p' = & \hat{p}^2 [\alpha + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & \hat{p}(1 - \hat{p}) [\alpha(1 - T_B) + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & (1 - \hat{p})\hat{p} [\alpha T_A + (1 - \alpha)\hat{p} T_A] + \\ & (1 - \hat{p})^2 [(1 - \alpha)\hat{p} T_A] , \end{aligned} \quad (7)$$

120 which simplifies to

$$p' = \hat{p}^2(T_B - T_A) + \hat{p}(1 + T_A - T_B) . \quad (8)$$

122 The frequency of  $A$  among parents (i.e. after selection) follows a similar dynamic, but also includes  
 the effect of natural selection, and is therefore

$$\begin{aligned} \bar{w}\tilde{p}' = & \hat{p}^2(1 + b - c) [\alpha + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & \hat{p}(1 - \hat{p})(1 - c) [\alpha(1 - T_B) + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ 124 & (1 - \hat{p})\hat{p}(1 + b) [\alpha T_A + (1 - \alpha)\hat{p} T_A] + \\ & (1 - \hat{p})^2 [(1 - \alpha)\hat{p} T_A] , \end{aligned} \quad (9)$$

where fitness values are taken from Table 1 and Table 2, and the population mean fitness is  $\bar{w} =$   
 126  $1 + \hat{p}(b - c)$ . Eq. 9 can be simplified to

$$\begin{aligned} \bar{w}\tilde{p}' = & \hat{p}^2(1 + b - c) [1 - (1 - \hat{p})(1 - \alpha)T_B] + \\ & \hat{p}(1 - \hat{p})(1 - c) [\hat{p}(1 - \alpha)T_B + 1 - T_B] + \\ & (1 - \hat{p})\hat{p}(1 + b) [\hat{p}(1 - \alpha) + \alpha] T_A + \\ & (1 - \hat{p})^2 \hat{p}(1 - \alpha) T_A . \end{aligned} \quad (10)$$

128 Starting from Eq. 6 with  $\hat{p}' = v\tilde{p}' + (1 - v)p'$ , we substitute  $p'$  from Eq. 8 and  $\tilde{p}'$  from Eq. 10 and

obtain

$$\begin{aligned}
\hat{p}' = & \frac{v}{\bar{w}} \left[ \hat{p}^2 (1 + b - c) \left( 1 - (1 - \hat{p})(1 - \alpha)T_B \right) \right] + \\
& \frac{v}{\bar{w}} \left[ \hat{p}(1 - \hat{p})(1 - c)(\hat{p}(1 - \alpha)T_B + 1 - T_B) \right] + \\
& \frac{v}{\bar{w}} \left[ \hat{p}(1 - \hat{p})(1 + b)(\hat{p}(1 - \alpha) + \alpha)T_A \right] + \\
& \frac{v}{\bar{w}} (1 - \hat{p})^2 \hat{p}(1 - \alpha)T_A + \\
& (1 - v)\hat{p}^2(T_B - T_A) + \\
& (1 - v)\hat{p}(1 + T_A - T_B) .
\end{aligned} \tag{11}$$

Table 3 lists the model variables and parameters.

## Results

In the following sections, we determine the equilibria of the model in Eq. 11, namely, solutions of  $\hat{p}' = \hat{p}$ , and analyze their local stability. We then analyze the evolution of a modifier of social association. Finally, we compare derived conditions to outcomes of stochastic simulations with a structured population.

### Evolution of cooperation

The fixed points (equilibria) of the recursion (Eq. 11) are  $\hat{p} = 0$ ,  $\hat{p} = 1$ , and (see Eq. B5)

$$\hat{p}^* = \frac{\alpha b v T_A - c v (1 - T_B) + (T_A - T_B)}{[c(1 - v) - b(1 - \alpha v)](T_A - T_B)} . \tag{12}$$

Define the following cost thresholds,  $\gamma_1$  and  $\gamma_2$ , and the vertical transmission threshold,  $\hat{v}$ ,

$$\gamma_1 = \frac{b v \alpha T_A + (T_A - T_B)}{v(1 - T_B)}, \quad \gamma_2 = \frac{b v \alpha T_B + (1 + b)(T_A - T_B)}{v(1 - T_B) + (1 - v)(T_A - T_B)}, \quad \hat{v} = \frac{T_B - T_A}{1 - T_A} . \tag{13}$$

Then we have the following result.

**Result 1** (Equilibria and stability). *With vertical, horizontal, and oblique transmission, the cultural evolution of a cooperation follows one of the following scenarios in terms of the cost thresholds  $\gamma_1$  and  $\gamma_2$  and the vertical transmission threshold  $\hat{v}$  (Eq. 13) :*

1. Fixation of cooperation: if (i)  $T_A \geq T_B$  and  $c < \gamma_1$ ; or if (ii)  $T_A < T_B$  and  $v > \hat{v}$  and  $c < \gamma_2$ .
2. Fixation of defection: if (iii)  $T_A \geq T_B$  and  $\gamma_2 < c$ ; or if (iv)  $T_A < T_B$  and  $\gamma_1 < c$ .
3. Stable polymorphism: if (v)  $T_A < T_B$  and  $v < \hat{v}$  and  $c < \gamma_1$ ; or if (vi)  $T_A < T_B$  and  $v > \hat{v}$  and  $\gamma_2 < c < \gamma_1$ .
4. Unstable polymorphism: if (vii)  $T_A > T_B$  and  $\gamma_1 < c < \gamma_2$ .

These conditions are illustrated in Figures 2a, 2b, 3a, and 3b, and full analysis is in Appendix B.

Much of the literature on evolution of cooperation focuses on conditions for an initially rare cooperative phenotype to invade a population of defectors. The following remarks address this condition.

156 **Remark 1** (Condition on  $c$  for cooperation to increase when rare, i.e.,  $\hat{p}' > p$  near  $p = 0$ ). *If the*  
 158 *initial frequency of cooperation is very close to zero, then its frequency will increase if the cost of*  
*cooperation is low enough,*

$$c < \gamma_1 = \frac{bv\alpha T_A + (T_A - T_B)}{v(1 - T_B)} . \quad (14)$$

160 This unites the conditions for fixation of cooperation and for stable polymorphism, both of which  
 entail instability of the state where defection is fixed,  $\hat{p} = 0$ .

162 Importantly, increasing social association  $\alpha$  increases the cost threshold ( $\partial\gamma_1/\partial\alpha > 0$ ), making it  
 easier for cooperation to increase from rarity. Similarly, increasing the horizontal transmission of  
 164 cooperation,  $T_A$ , increases the threshold ( $\partial\gamma_1/\partial T_A > 0$ ), facilitating the evolution of cooperation  
 ((Figure 3a and 3b). However, increasing the horizontal transmission of defection,  $T_B$ , can increase or  
 166 decrease the cost threshold, but it increases the cost threshold when the threshold is already above one  
 ( $c < 1 < \gamma_1$ ):  $\partial\gamma_1/\partial T_B$  is positive when  $T_A > \frac{1}{1+\alpha bv}$ , which gives  $\gamma_1 > 1/v$ . Therefore, increasing  $T_B$   
 168 decreases the cost threshold and limits the evolution of cooperation, but only if  $T_A < \frac{1}{1+\alpha bv}$ .

Increasing the vertical transmission rate,  $v$ , can either increase or decrease the cost threshold, depending  
 170 on the horizontal transmission bias,  $T_A - T_B$ , because  $\text{sign}(\partial\gamma_1/\partial v) = -\text{sign}(T_A - T_B)$ . When  $T_A < T_B$   
 we have  $\partial\gamma_1/\partial v > 0$ , and as the vertical transmission rate increases, the cost threshold increases,  
 172 making it easier for cooperation to increase when rare (Figure 2b). In contrast, when  $T_A > T_B$  we get  
 $\partial\gamma_1/\partial v < 0$ , and therefore as the vertical transmission rate increases, the cost threshold decreases,  
 174 making it harder for cooperation to increase when rare (Figure 2a).

In general, this condition cannot be formulated in the form of Hamilton's rule due to the bias in  
 176 horizontal transmission, represented by  $T_A - T_B$ . When there is no horizontal transmission bias,  
 $T_A = T_B$ , the following applies.

178 From Result 1 and inequality 14, if horizontal transmission is unbiased,  $T = T_A = T_B$ , then cooperation  
 will take over the population from any initial frequency if the cost is low enough,

$$c < b \cdot \frac{\alpha T}{1 - T} , \quad (15)$$

and regardless of the vertical transmission rate,  $v$ . This condition can be interpreted as a version of  
 182 Hamilton's rule ( $c < b \cdot r$ , inequality 1) or as a version of inequality 3, where  $\alpha T/(1 - T)$  can be  
 regarded as the *effective relatedness* or *effective assortment*, respectively. Figure S2a illustrates this  
 184 condition. Note that the right-hand side of inequality 15 equals  $\gamma_1$  when  $T = T_A = T_B$ .

From inequality 14, without social association ( $\alpha = 0$ ), cooperation will increase when it is rare if  
 186 there is horizontal transmission bias for cooperation,  $T_A > T_B$ , and

$$c < \frac{T_A - T_B}{v(1 - T_B)} . \quad (16)$$

188 Figure 3a illustrates this condition (for  $v = 1$ ), which is obtained by setting  $\alpha = 0$  in inequality 14.  
 Importantly, the benefit of cooperation,  $b$ , does not affect the evolution of cooperation in the absence of  
 190 social association, and the outcome is determined only by cultural transmission. Further, inequality 14  
 shows that with perfect social association ( $\alpha = 1$ ), cooperation will increase when rare if

$$c < \frac{bvT_A + (T_A - T_B)}{v(1 - T_B)} . \quad (17)$$

In the absence of oblique transmission,  $v = 1$ , the only equilibria are the fixation states,  $\tilde{p} = 0$  and  
 194  $\tilde{p} = 1$ , and cooperation will evolve from any initial frequency (i.e.,  $\tilde{p}' > \tilde{p}$ ) if inequality 17 applies

(Figure 3). This is similar to case of microbe-associated cooperation studied by Lewin-Epstein et al. (2017); therefore when  $v = 1$ , this remark is equivalent to their eq. 1.

It is interesting to examine the general effect of social association  $\alpha$  on the evolution of cooperation. Define the social association thresholds,  $a_1$  and  $a_2$ , as

$$a_1 = \frac{c \cdot v(1 - T_A) - (T_A - T_B)(1 + b - c)}{b \cdot v \cdot T_B}, \quad a_2 = \frac{c \cdot v(1 - T_B) - (T_A - T_B)}{b \cdot v \cdot T_A}. \quad (18)$$

**Remark 2** (Condition on social association  $\alpha$  for cooperation to increase when it is rare). *Cooperation will increase when rare if social association is high enough, specifically if  $a_2 < \alpha$ .*

Figures 2c and 2d illustrate this condition. With horizontal transmission bias for cooperation,  $T_A > T_B$ , cooperation can fix from any initial frequency if  $a_2 < \alpha$  (green area in the figures). With horizontal bias favoring defection,  $T_A < T_B$ , cooperation can fix from any frequency if social association is high,  $a_1 < \alpha$  (green area with  $T_A < T_B$ ), and can also increase when rare and reach stable polymorphism if social association is intermediate,  $a_2 < \alpha < a_1$  (yellow area). Without horizontal bias,  $T_A = T_B$ , fixation of cooperation occurs if social association is high enough,  $\frac{c}{b \cdot v} \cdot \frac{1-T}{T} < \alpha$  (inequality 15; in this case  $a_1 = a_2$ ).

Interestingly, because  $\text{sign}(\partial a_2 / \partial v) = \text{sign}(T_A - T_B)$ , the effect of the vertical transmission rate  $v$  on  $a_1$  and  $a_2$  depends on the horizontal transmission bias. That is, with horizontal bias for cooperation,  $T_A > T_B$ , evolution of cooperation is facilitated by oblique transmission, whereas with horizontal bias for defection,  $T_A < T_B$ , evolution of cooperation is facilitated by vertical transmission. This is demonstrated in Figures 2c and 2d.

Next, we look at the roles of vertical and oblique transmission in the evolution of cooperation. Fixation of cooperation is possible only if the vertical transmission rate is high enough,

$$v > \hat{v} = \frac{T_B - T_A}{1 - T_A}. \quad (19)$$

This condition does not guarantee fixation of cooperation; rather, if this condition does not apply then cooperation cannot fix. If horizontal transmission is biased for cooperation,  $T_A > T_B$ , cooperation can fix with any vertical transmission rate (because  $\hat{v} < 0$ ). In contrast, if horizontal transmission is biased for defection,  $T_A < T_B$ , cooperation can fix only if the vertical transmission rate is high enough: in this case oblique transmission can prevent fixation of cooperation (see Figures 2b and 2d).

With only vertical transmission ( $v = 1$ ), inequality 14 entails that cooperation will increase when rare if

$$c < \frac{b\alpha T_A + (T_A - T_B)}{1 - T_B}, \quad (20)$$

which can also be written as

$$\frac{c(1 - T_B) - (T_A - T_B)}{bT_A} < \alpha. \quad (21)$$

In the absence of vertical transmission ( $v = 0$ ), from recursion 11 we see that the frequency of the cooperator phenotype among adults increases every generation, i.e.  $p' > p$ , if there is a horizontal transmission bias in favor of cooperation, namely  $T_A > T_B$ . That is, in the absence of vertical transmission, selection plays no role in the evolution of cooperation (i.e.,  $b$  and  $c$  do not affect  $\hat{p}'$ ). The dynamics are determined solely by differential horizontal transmission of the two phenotypes, namely, the relative tendency of each phenotype to be horizontally transmitted to peers. With no bias in horizontal transmission,  $T_A = T_B$ , phenotype frequencies do not change,  $\hat{p}' = \hat{p}$ .

Cooperation and defection can coexist at frequencies  $\hat{p}^*$  and  $1 - \hat{p}^*$  (Eq. 12). When it is feasible, this equilibrium is stable or unstable under the conditions of Result 1, parts 3 and 4, respectively. The yellow and blue areas in Figures 3 and 2 show cases of stable and unstable polymorphism, respectively. When  $\hat{p}^*$  is unstable, cooperation will fix if its initial frequency is  $\hat{p} > \hat{p}^*$ , and defection will fix if  $\hat{p} < \hat{p}^*$ ; this occurs when there is horizontal transmission bias for cooperation,  $T_A > T_B$ , and the cost is intermediate,  $\gamma_1 < c < \gamma_2$ . Figure S1 shows the mapping  $\hat{p} \rightarrow \hat{p}' - \hat{p}$ .

## Evolution of social association

We now focus on the evolution of social association under perfect vertical transmission,  $v = 1$ , assuming that the population is initially at a stable polymorphism of the two phenotypes, cooperation  $A$  and defection  $B$ , where the frequency of  $A$  among juveniles is  $\hat{p}^*$  (Eq. 12). Note that for a stable polymorphism, there must be horizontal bias for defection,  $T_A < T_B$ , and an intermediate cost of cooperation,  $\gamma_2 < c < \gamma_1$  (Eq. 13), see Figure 3b. The equilibrium population mean fitness is  $\bar{w}^* = 1 + \hat{p}^*(b - c)$ , which is increasing in  $\hat{p}^*$ , and  $\hat{p}^*$  is increasing in  $\alpha$  (Appendix C). Therefore, if social association increases, the population mean fitness also increases. But can an allele that increases social association evolve?

To answer this question, we extend our model to include a “modifier locus” (Feldman, 1972; Liberman and Feldman, 1986a,b; Liberman, 1988) that determines social association, but has no direct effect on fitness. The modifier locus has two alleles,  $M$  and  $m$ , which induce social associations  $\alpha_1$  and  $\alpha_2$ , respectively. Suppose that the population has evolved to a stable equilibrium  $\hat{p}^*$  when only allele  $M$  is present. We study the local stability of this equilibrium to invasion by the modifier allele  $m$ ; this is called “external stability” (Liberman and Feldman, 1986b; Altenberg et al., 2017) and obtain the following result.

**Result 2** (Reduction principle for social association). *From a stable polymorphism between cooperation and defection, a modifier allele can successfully invade the population if it decreases the social association  $\alpha$ .*

The full analysis is in Appendix D. Note that this reduction principle entails that successful invasions will reduce the frequency of cooperation, as well as the population mean fitness (Figure 4). Furthermore, if we assume that modifier alleles with decreased social association appear and invade the population from time to time, then social association will continue to decrease, further reducing the frequency of cooperation and the population mean fitness. This evolution will proceed as long as there is a stable polymorphism, that is, as long as  $a_2 < \alpha < a_1$  (Remark 2, Figure 3c). Thus, we can expect social association to eventually approach  $a_2$ , the frequency of cooperation to fall to zero, and the population mean fitness to decrease to one (Figure 4).

## Population structure

Social association may also emerge from population structure. Consider a population colonizing a two-dimensional grid of size 100-by-100, where each site is inhabited by one individual, similarly to the model of Lewin-Epstein and Hadany (2020). Each individual is characterized by its phenotype: either cooperator,  $A$ , or defector,  $B$ . Initially, each site in the grid is randomly colonized by either a cooperator or a defector, with equal probability. In each generation, half of the individuals are randomly chosen to “initiate” interactions, and these initiators interact with a random neighbor (i.e. individual in a neighboring site) in a prisoners’ dilemma game (Table 1) and a random neighbor (with replacement) for horizontal cultural transmission (Figure 1). The expected number of each of these interactions per individual per generation is one. The effective social association  $\alpha$  in this model is the probability that the same neighbor is picked for both interactions, or  $\alpha = 1/m$ , where  $m$  is



280 the number of neighbors. On an infinite grid,  $m = 8$ , but on a finite grid  $m$  can be lower in edge  
neighborhoods close to the grid border. As before,  $T_A$  and  $T_B$  are the probabilities of successful  
282 horizontal transmission of phenotypes  $A$  and  $B$ , respectively.

The order of the interactions across the grid at each generation is random. After all interactions take  
284 place, an individual's fitness is determined by  $w = 1 + b \cdot n_b - c \cdot n_c$ , where  $n_b$  is the number of  
interactions that individual had with cooperative neighbors, and  $n_c$  is the total number of interactions  
286 that that individual had ( $n_b \leq n_c$ ). Then, a new generation is produced, and the sites can be settled by  
offspring of any parent, not just the neighboring parents. Thus, selection is global, rather than local, in  
288 accordance with our deterministic model. The parent is randomly drawn with probability proportional  
to its fitness, divided by the average fitness of all potential parents. Offspring are assumed to have the  
290 same phenotype as their parents (i.e.  $v = 1$ ).

The outcomes of stochastic simulations with such a structured population are shown in Figure 5, which  
292 demonstrates that the highest cost of cooperation  $c$  that permits the evolution of cooperation agrees with  
the conditions derived above for our model without population structure or stochasticity. An example of  
294 stochastic stable polymorphism is shown in Figure 5c. Changing the simulation so that the population  
is structured to allow local selection (i.e., sites can only be settled by offspring of neighboring parents)  
296 had only a minor effect on the agreement with the derived conditions (Figure S3).

These comparisons between the deterministic unstructured model and the stochastic structured model  
298 show that the conditions derived for the deterministic model can be useful for predicting the dynamics  
under complex scenarios. Moreover, this structured population model demonstrates that our parameter  
300 for social association ( $\alpha$ ) can represent local interactions between individuals.

## Discussion

302 Under a combination of vertical, oblique, and horizontal transmission with payoffs in the form  
of a prisoner's dilemma game, cooperation or defection can either fix or coexist, depending on  
304 the relationship between the cost and benefit of cooperation, the horizontal transmission bias, and  
the association between social interaction and horizontal transmission (Result 1, Figures 2 and 3).  
306 Importantly, cooperation can increase when initially rare (i.e. invade a population of defectors) if and  
only if, rewriting inequality 14,

$$308 \quad c \cdot v(1 - T_B) < b \cdot v\alpha T_A + (T_A - T_B), \quad (22)$$

namely, the effective cost of cooperation (left-hand side) is smaller than the effective benefit plus the  
310 horizontal transmission bias (right-hand side). This condition cannot be formulated in the form of  
Hamilton's rule,  $c < b \cdot r$ , due to the effect of biased horizontal transmission, represented by  $(T_A - T_B)$ .  
312 Remarkably, a polymorphism of cooperation and defection can be stable if horizontal transmission  
is biased in favor of defection ( $T_A < T_B$ ) and both the cost of cooperation and social association are  
314 intermediate (yellow areas in Figures 2 and 3).

We find that stronger social association  $\alpha$  leads to evolution of higher frequency of cooperation and  
316 increased population mean fitness. Nevertheless, when cooperation and defection coexist, social  
association is expected to be reduced by natural selection, leading to extinction of cooperation and  
318 decreased population mean fitness (Result 2, Figure 4). Without social association, the benefit of  
cooperation cannot facilitate its evolution, and cooperation can only succeed if horizontal transmission  
320 is biased in its favor.

Indeed, in our model, horizontal transmission plays a major role in the evolution of cooperation:  
322 increasing the transmission of cooperation,  $T_A$ , or decreasing the transmission of defection,  $T_B$ , facili-  
tates the evolution of cooperation. However, the effect of oblique transmission is more complicated.

324 When there is horizontal transmission bias in favor of cooperation,  $T_A > T_B$ , increasing the rate of  
oblique transmission,  $1 - v$ , will facilitate the evolution of cooperation. In contrast, when the bias is  
326 in favor of defection,  $T_A < T_B$ , higher rates of vertical transmission,  $v$ , are advantageous for cooper-  
ation, and the rate of vertical transmission must be high enough ( $v > \hat{v}$ ) for cooperation to fix in the  
328 population.

The conditions derived from our deterministic model provide a good approximation to outcomes of  
330 simulations of a complex stochastic model with population structure in which individuals can only  
interact with and transmit to their neighbors. In these structured populations social association arises  
332 due to both social interactions and horizontal cultural transmission being local (Figure 5).

Feldman et al. (1985) studied the dynamics of an altruistic phenotype with vertical cultural transmission  
334 and a gene that modifies the transmission of the phenotype. Their results are very sensitive to  
this genetic modification: without it, the conditions for invasion of the altruistic phenotype reduce  
336 to Hamilton’s rule. Further work is needed to incorporate such genetic modification of cultural  
transmission into our model. Woodcock (2006) stressed the significance of non-vertical transmission  
338 for the evolution of cooperation and carried out simulations with prisoner’s dilemma payoffs but  
without horizontal transmission or social association ( $\alpha = 0$ ). Nevertheless, his results demonstrated  
340 that it is possible to sustain altruistic behavior via cultural transmission for a substantial length of  
time. Our results provide strong evidence for his hypothesis that horizontal transmission can play an  
342 important role in the evolution of cooperation.

To understand the role of horizontal transmission, we first review the role of *assortment*. Eshel and  
344 Cavalli-Sforza (1982) showed that altruism can evolve when the tendency for *assortative meeting*, i.e.,  
for individuals to interact with others of their own phenotype, is strong enough. Fletcher and Doebeli  
346 (2009) further argued that a general explanation for the evolution of altruism is given by *assortment*:  
the correlation between individuals that carry an altruistic trait and the amount of altruistic behavior  
348 in their interaction group (see also Bijma and Aanen (2010)). They suggested that to explain the  
evolution of altruism, we should seek mechanisms that generate assortment, such as population  
350 structure, repeated interactions, and individual recognition. Our results highlight another mechanism  
for generating assortment: an association between social interactions and horizontal transmission that  
352 creates a correlation between one’s partner for interaction and the partner for transmission. This  
mechanism does not require repeated interactions, population structure, or individual recognition.  
354 We show that high levels of such social association greatly increase the potential for evolution of  
cooperation. With enough social association, cooperation can increase in frequency when initially  
356 rare even when there is horizontal transmission bias against it ( $T_A < T_B$ ).

How does non-vertical transmission generate assortment? Lewin-Epstein et al. (2017) and Lewin-  
358 Epstein and Hadany (2020) suggested that microbes that manipulate their hosts to act altruistically  
can be favored by selection, which may help to explain the evolution of cooperation. From the kin  
360 selection point-of-view, if microbes can be transmitted *horizontally* from one host to another during  
host interactions, then following horizontal transmission the recipient host will carry microbes that  
362 are closely related to those of the donor host, even when the two hosts are (genetically) unrelated.  
From the assortment point-of-view, infection by behavior-determining microbes during interactions  
364 effectively generates assortment because a recipient of help may be infected by a behavior-determining  
microbe and consequently become a helper. Cultural horizontal transmission can similarly generate  
366 assortment between cooperators and enhance the benefit of cooperation if cultural transmission and  
helping interactions occur between the same individuals, i.e. when there is social association, so  
368 that the recipient of help may also be the recipient of the cultural trait for cooperation. Thus, with  
horizontal transmission, “assortment between focal cooperative players and cooperative acts in their  
370 interaction environment” (Fletcher and Doebeli, 2009) is generated not because the helper is likely to  
be helped, but rather because the helped is likely to become a helper.

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## 376 Appendices

### Appendix A Local stability criterion

378 Let  $f(p) = \lambda \cdot (p' - p)$ , where  $\lambda > 0$ , and 0 and 1 are equilibria, that is,  $f(0) = 0$  and  $f(1) = 0$ .

Set  $p > p^* = 0$ . Using a linear approximation for  $f(p)$  near 0, we have

$$380 \quad p' < p \Leftrightarrow f(p)/p < 0 \Leftrightarrow \frac{f'(0) \cdot p + O(p^2)}{p} < 0 \Leftrightarrow f'(0) + O(p) < 0. \quad (\text{A1})$$

Therefore, by definition of big-O notation, if  $f'(0) < 0$  then there exists  $\epsilon > 0$  such that for any local perturbation  $382 \quad 0 < p < \epsilon$ , it is guaranteed that  $0 < p' < p$ ; that is,  $p'$  is closer to zero than  $p$ .

Set  $p < p^* = 1$  Using a linear approximation for  $f(p)$  near 1, we have

$$384 \quad 1 - p' < 1 - p \Leftrightarrow -\frac{f(p)}{1 - p} < 0 \Leftrightarrow \frac{f'(1)(p - 1) + O((p - 1)^2)}{p - 1} < 0 \Leftrightarrow f'(1) - O(1 - p) < 0. \quad (\text{A2})$$

Therefore, if  $f'(1) < 0$  then there exists  $\epsilon > 0$  such that for any  $1 - \epsilon < 1 - p < 1$  we have  $1 - p' < 1 - p$ ; that  $386 \quad$  is,  $p'$  is closer to one than  $p$ .

### Appendix B Equilibria and stability

388 Let  $f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p})$ . Then, using *SymPy* (Meurer et al., 2017), a Python library for symbolic mathematics, this simplifies to

$$390 \quad f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p}) = \beta_1 \hat{p}^3 + \beta_2 \hat{p}^2 + \beta_3 \hat{p}, \quad (\text{B1})$$

where

$$\begin{aligned} \beta_1 &= [c(1 - v) - b(1 - \alpha v)](T_A - T_B), \\ \beta_2 &= -\beta_1 - \beta_3, \\ \beta_3 &= \alpha b v T_A - c v (1 - T_B) + (T_A - T_B). \end{aligned} \quad (\text{B2})$$

If  $T = T_A = T_B$  then  $\beta_1 = 0$  and  $\beta_3 = -\beta_2 = \alpha b v T - c v (1 - T)$ , and  $f(\hat{p})$  becomes a quadratic polynomial,

$$394 \quad f(\hat{p}) = \hat{p}(1 - \hat{p})[\alpha b v T - c v (1 - T)]. \quad (\text{B3})$$

Clearly the only two equilibria are the fixations  $\hat{p} = 0$  and  $\hat{p} = 1$ , which are locally stable if  $f'(\hat{p}) < 0$  near  $396 \quad$  the equilibrium (see Appendix A), where  $f'(\hat{p}) = (1 - 2\hat{p})[\alpha b v T - c v (1 - T)]$ , so that

$$\begin{aligned} f'(0) &= \alpha b v T - c v (1 - T), \\ f'(1) &= -\alpha b v T + c v (1 - T). \end{aligned} \quad (\text{B4})$$

398 In the general case where  $T_A \neq T_B$ , the coefficient  $\beta_1$  is not necessarily zero, and  $f(\hat{p})$  is a cubic polynomial. Therefore, three equilibria may exist, two of which are  $\hat{p} = 0$  and  $\hat{p} = 1$ , and the third is

$$400 \quad \hat{p}^* = \frac{\beta_3}{\beta_1} = \frac{\alpha b v T_A - c v (1 - T_B) + (T_A - T_B)}{[c(1 - v) - b(1 - \alpha v)](T_A - T_B)}. \quad (\text{B5})$$

Note that the sign of the cubic (Eq. B1) at positive (negative) infinity is equal (opposite) to the sign of  $\beta_1$ . If  $T_A > T_B$ , then

$$\beta_1 < [c(1 - \alpha v) - b(1 - \alpha v)](T_A - T_B) = (1 - \alpha v)(c - b)(T_A - T_B) < 0, \quad (\text{B6})$$

since  $c < b$  and  $\alpha v < 1$ . Hence the signs of the cubic at positive and negative infinity are negative and positive, respectively. First, if  $\beta_3 < \beta_1$  then  $1 < \hat{p}^*$ . Also,  $f'(0) < 0$  and  $f'(1) > 0$ ; that is, fixation of the defector phenotype  $B$  is the only locally stable feasible equilibrium. Second, if  $\beta_1 < \beta_3 < 0$  then  $0 < \hat{p}^* < 1$  and therefore  $f'(0) < 0$  and  $f'(1) < 0$  so that both fixations are locally stable and  $\hat{p}^*$  separates the domains of attraction. Third, if  $0 < \beta_3$  then  $\hat{p}^* < 0$  and therefore  $f'(0) > 0$  and  $f'(1) < 0$ ; that is, fixation of the cooperator phenotype  $A$  is the only locally stable legitimate equilibrium.

Similarly, if  $T_A < T_B$ , then

$$\beta_1 > [c(1 - \alpha v) - b(1 - \alpha v)](T_A - T_B) = (1 - \alpha v)(c - b)(T_A - T_B) > 0, \quad (\text{B7})$$

since  $c < b$  and  $\alpha v < 1$ , and the signs of the cubic at positive and negative infinity are positive and negative, respectively. First, if  $\beta_3 < 0$  then  $\hat{p}^* < 0$  and therefore  $f'(0) < 0$  and  $f'(1) > 0$ ; that is, fixation of the defector phenotype  $A$  is the only locally stable legitimate equilibrium. Second, if  $0 < \beta_3 < \beta_1$  then  $0 < \hat{p}^* < 1$  and therefore  $f'(0) > 0$  and  $f'(1) > 0$ ; that is, both fixations are locally unstable and  $\hat{p}^*$  is a stable polymorphic equilibrium. Third, if  $\beta_1 < \beta_3$  then  $\hat{p}^* > 1$  and therefore  $f'(0) > 0$  and  $f'(1) < 0$ , and fixation of the cooperator phenotype  $A$  is the only locally stable feasible equilibrium.

This analysis can be summarized as follows:

1. *Fixation of cooperation*: if (i)  $T = T_A = T_B$  and  $c < b \cdot \frac{\alpha T}{1-T}$ ; or if (ii)  $T_A > T_B$  and  $0 < \beta_3$ ; or if (iii)  $T_A < T_B$  and  $\beta_1 < \beta_3$ .
2. *Fixation of the defection*: if (iv)  $T = T_A = T_B$  and  $c > b \cdot \frac{\alpha T}{1-T}$ ; or if (v)  $T_A > T_B$  and  $\beta_3 < \beta_1 < 0$ ; or if (vi)  $T_A < T_B$  and  $\beta_3 < 0$ .
3. *polymorphism of both phenotypes at  $\hat{p}^*$* : if (vii)  $T_A < T_B$  and  $0 < \beta_3 < \beta_1$ .
4. *Fixation of either phenotype depending on initial frequency*: if (viii)  $T_A > T_B$  and  $\beta_1 < \beta_3 < 0$ .

We now proceed to use the cost thresholds,  $\gamma_1$  and  $\gamma_2$ , and the vertical transmission threshold,  $\hat{v}$  (Eq. 13). First, assume  $T_A < T_B$ .  $\beta_3 < 0$  requires  $\gamma_1 < c$ . For  $\beta_3 < \beta_1$  we need  $c[v(1 - T_B) + (1 - v)(T_A - T_B)] > b v \alpha T_B + (1 + b)(T_A - T_B)$ . Note that the expression in the square brackets is positive if and only if  $v > \hat{v}$ . Thus, for  $\beta_3 < \beta_1$  we need  $v > \hat{v}$  and  $\gamma_2 < c$  or  $v < \hat{v}$  and  $c < \gamma_2$ , and for  $0 < \beta_3 < \beta_1$  we need  $v > \hat{v}$  and  $\gamma_2 < c < \gamma_1$ , or  $v < \hat{v}$  and  $c < \min(\gamma_1, \gamma_2)$ . For  $\beta_1 < \beta_3$  we need  $v > \hat{v}$  and  $c < \gamma_2$  or  $v < \hat{v}$  and  $\gamma_2 < c$ . However, some of these conditions cannot be met, since  $v < \hat{v}$  implies  $c < 1 < \gamma_2$ .

Second, assume  $T_A > T_B$ .  $\beta_3 > 0$  requires  $\gamma_1 > c$ . For  $\beta_1 < \beta_3$  we need  $c[v(1 - T_B) + (1 - v)(T_A - T_B)] < b v \alpha T_B + (1 + b)(T_A - T_B)$ . Thus for  $\beta_1 < \beta_3$  we need  $v > \hat{v}$  and  $c < \gamma_2$  or  $v < \hat{v}$  and  $c > \gamma_2$ . But  $\hat{v} < 0$  when  $T_A > T_B$ , and therefore we have  $\beta_1 < \beta_3$  if  $c < \gamma_2$ . Similarly, we have  $\beta_3 < \beta_1$  if  $c > \gamma_2$ .

This analysis is summarized in Result 1.

## Appendix C Effect of social association on mean fitness

To determine the effect of increasing  $\alpha$  on the stable population mean fitness,  $\bar{w}^* = 1 + (b - c)\hat{p}^*$ , we must analyze its effect on  $\hat{p}^*$ ,

$$\frac{\partial \hat{p}^*}{\partial \alpha} = \frac{b T_A - c(1 - T_B) + (T_A - T_B)}{b(1 - \alpha)^2(T_B - T_A)}. \quad (\text{C1})$$

Note that stable polymorphism implies  $c < \gamma_1$ , and because  $\alpha < 1$ , we have

$$c < \gamma_1 = \frac{b \alpha T_A + (T_A - T_B)}{1 - T_B} < \frac{b T_A + (T_A - T_B)}{1 - T_B}. \quad (\text{C2})$$

Therefore, the numerator in Eq. C1 is positive. Since  $T_A < T_B$ , the denominator in Eq. C1 is also positive, and hence the derivative  $\partial \hat{p}^* / \partial \alpha$  is positive. Thus, the population mean fitness increases as social association  $\alpha$  increases.

## Appendix D Reduction principle

We assume here that  $v = 1$ , i.e. no oblique transmission, and therefore  $\hat{p} = \tilde{p}$ . Denote the frequencies of the pheno-genotypes  $AM$ ,  $BM$ ,  $Am$ , and  $Bm$  by  $\tilde{\mathbf{p}} = (\tilde{p}_1, \tilde{p}_2, \tilde{p}_3, \tilde{p}_4)$ . The frequencies of the pheno-genotypes in the next generation are defined by the recursion system,

$$\begin{aligned}
 \bar{w}\tilde{p}'_1 &= \tilde{p}_1x(1+b-c)(1-(1-\alpha_1)(1-x)T_B) + \\
 &\quad \tilde{p}_1(1-x)(1-c)(1-\alpha_1T_Bx - T_B(1-x)) + \\
 &\quad \tilde{p}_2x(1+b)T_A(x+\alpha_1(1-x)) + \\
 &\quad \tilde{p}_2(1-x)x(1-\alpha_1)T_A, \\
 \bar{w}\tilde{p}'_2 &= \tilde{p}_1x(1+b-c)(1-\alpha_1)(1-x)T_B + \\
 &\quad \tilde{p}_1(1-x)(1-c)(\alpha_1T_B + (1-\alpha_1)(1-x)T_B) + \\
 &\quad \tilde{p}_2x(1+b)(1-\alpha_1T_A(1-x) - T_Ax) + \\
 &\quad \tilde{p}_2(1-x)(1-(1-\alpha_1)xT_A), \\
 \bar{w}\tilde{p}'_3 &= \tilde{p}_3x(1+b-c)(1-(1-\alpha_2)(1-x)T_B) + \\
 &\quad \tilde{p}_3(1-x)(1-c)(1-\alpha_2T_Bx - T_B(1-x)) + \\
 &\quad \tilde{p}_4x(1+b)T_A(x+\alpha_2(1-x)) + \\
 &\quad \tilde{p}_4(1-x)x(1-\alpha_2)T_A, \\
 \bar{w}\tilde{p}'_4 &= \tilde{p}_3x(1+b-c)(1-\alpha_2)(1-x)T_B + \\
 &\quad \tilde{p}_3(1-x)(1-c)(\alpha_2T_B + (1-\alpha_2)(1-x)T_B) + \\
 &\quad \tilde{p}_4x(1+b)(1-\alpha_2T_A(1-x) - T_Ax) + \\
 &\quad \tilde{p}_4(1-x)(1-(1-\alpha_2)xT_A),
 \end{aligned} \tag{D1}$$

where  $x = \tilde{p}_1 + \tilde{p}_3$  is the total frequency of the cooperative phenotype  $A$ , and  $\bar{w} = 1 + (b-c)x$  is the population mean fitness.

The equilibrium where only allele  $M$  is present is  $\tilde{\mathbf{p}}^* = (\tilde{p}^*, 1 - \tilde{p}^*, 0, 0)$ , where

$$\tilde{p}^* = \frac{c(1-T_B) - b\alpha_1T_A - (T_A - T_B)}{b(1-\alpha_1)(T_A - T_B)}, \tag{D2}$$

setting  $\alpha = \alpha_1$  and  $v = 1$  in Eq. 12. When  $v = 1$ ,  $\tilde{p}^*$  is a feasible polymorphism ( $0 < \tilde{p}^* < 1$ ) if  $T_A < T_B$  and  $\gamma_2 < c < \gamma_1$  (Result 1).

The local stability of  $\tilde{\mathbf{p}}^*$  to the introduction of allele  $m$  is determined by the linear approximation  $\mathbf{L}^*$  of the transformation in Eq. D1 near  $\tilde{\mathbf{p}}^*$  (i.e., the Jacobian of the transformation at the equilibrium).  $\mathbf{L}^*$  is known to have a block structure, with the diagonal blocks occupied by the matrices  $\mathbf{L}_{in}^*$  and  $\mathbf{L}_{ex}^*$  (Lieberman and Feldman, 1986b; Altenberg et al., 2017). The latter is the external stability matrix: the linear approximation to the transformation near  $\tilde{\mathbf{p}}^*$  involving only the pheno-genotypes  $Am$  and  $Bm$ , derived from Eq. D1 as

$$\mathbf{L}_{ex}^* = \frac{1}{\bar{w}^*} \begin{bmatrix} X & Y \\ Z & Q \end{bmatrix} = \frac{1}{\bar{w}^*} \begin{bmatrix} \frac{\partial \bar{w}\tilde{p}'_3}{\partial \tilde{p}_3}(\tilde{\mathbf{p}}^*) & \frac{\partial \bar{w}\tilde{p}'_4}{\partial \tilde{p}_4}(\tilde{\mathbf{p}}^*) \\ \frac{\partial \bar{w}\tilde{p}'_3}{\partial \tilde{p}_4}(\tilde{\mathbf{p}}^*) & \frac{\partial \bar{w}\tilde{p}'_4}{\partial \tilde{p}_3}(\tilde{\mathbf{p}}^*) \end{bmatrix} = \tag{D3}$$

$$\frac{1}{\bar{w}^*} \begin{bmatrix} (1+b\tilde{p}^*-c)(1-T_B(1-\tilde{p}^*)) + b\tilde{p}^*\alpha_2T_B(1-\tilde{p}^*) & (1+b\tilde{p}^*)T_A\tilde{p}^* + b\tilde{p}^*\alpha_2T_A(1-\tilde{p}^*) \\ (1+b\tilde{p}^*-c)T_B(1-\tilde{p}^*) - b\tilde{p}^*\alpha_2T_B(1-\tilde{p}^*) & (1+b\tilde{p}^*)(1-T_A\tilde{p}^*) - b\tilde{p}^*\alpha_2T_A(1-\tilde{p}^*) \end{bmatrix}.$$

Because we assume that  $\tilde{\mathbf{p}}^*$  is internally stable (i.e. locally stable to small perturbations in the frequencies of  $AM$  and  $BM$ ), the stability of  $\tilde{\mathbf{p}}^*$  is determined by the eigenvalues of the external stability matrix  $\mathbf{L}_{ex}^*$ . This is

a positive matrix, and due to the Perron-Frobenius theorem, the leading eigenvalue of  $\mathbf{L}_{ex}^*$  is real and positive. Thus, if the leading eigenvalue is less (greater) than one, then the equilibrium  $\tilde{\mathbf{p}}^*$  is externally stable (unstable) and allele  $m$  cannot (can) invade the population of allele  $M$ . The eigenvalues of  $\mathbf{L}_{ex}^*$  are the roots of the characteristic polynomial,

$$R(\lambda) = \lambda^2 - \lambda \frac{(X + Q)}{w^*} + \frac{XQ - YZ}{w^{*2}}, \quad (D4)$$

where  $X, Y, Z$ , and  $Q$  are defined in Eq. D3. The characteristic polynomial  $R(\lambda)$  is a quadratic with a positive leading coefficient. Therefore,  $\lim_{\lambda \rightarrow \pm\infty} R(\lambda) = \infty$ , and the leading eigenvalue is less than one (implying stability) if and only if  $R(1) > 0$  and  $R'(1) > 0$ . Thus, a sufficient condition for external instability of  $\tilde{\mathbf{p}}^*$  is

$$R(1) < 0 \Leftrightarrow 1 - \frac{(X + Q)}{w^*} + \frac{XQ - YZ}{w^{*2}} < 0 \Leftrightarrow \bar{w}^{*2} - \bar{w}^*(X + Q) + XQ - YZ < 0. \quad (D5)$$

Using *SymPy* (Meurer et al., 2017), a Python library for symbolic mathematics, we find that inequality D5 is true if and only if

$$\alpha_2(bT_A + (T_A - T_B) - c(1 - T_B)) < \alpha_1(bT_A + (T_A - T_B) - c(1 - T_B)). \quad (D6)$$

We assumed  $c < \gamma_1$ , that is,

$$\begin{aligned} c < \gamma_1 &= \frac{b\alpha_1 T_A + (T_A - T_B)}{1 - T_B} \Leftrightarrow \\ 0 &< b\alpha_1 T_A + (T_A - T_B) - c(1 - T_B) \Rightarrow \\ 0 &< bT_A + (T_A - T_B) - c(1 - T_B), \end{aligned} \quad (D7)$$

since  $0 \leq \alpha_1 \leq 1$ . Therefore, combining inequalities D5, D6, and D7, we find that  $R(1) < 0$  if and only if  $\alpha_2 < \alpha_1$ . This is a sufficient condition for external instability. So, if  $\alpha_2$ , the social association of the invading modifier allele  $m$ , is less than  $\alpha_1$ , the social association of the resident allele  $M$ , then invasion will be successful.

Determining a necessary and sufficient condition for successful invasion is more complicated, requiring analysis of the sign of  $R'(1)$ . However, we numerically validated that the leading eigenvalue is greater than one if and only if  $\alpha_2 < \alpha_1$ .

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**Table 1: Payoff matrix for prisoner's dilemma.**

	$\phi_2 = A$	$\phi_2 = B$
$\phi_1 = A$	$1 + b - c$	$1 - c$
$\phi_1 = B$	$1 + b$	$1$

The fitness of phenotype  $\phi_1$  when interacting with phenotype  $\phi_2$ .  $A$  is a cooperative phenotype,  $B$  is a defector phenotype,  $b$  is the benefit gained by an individual interacting with a cooperator, and  $c$  is the cost of cooperation.  $0 < c < 1$  and  $c < b$ .

**Table 2: Interaction frequency, fitness, and transmission probabilities.**

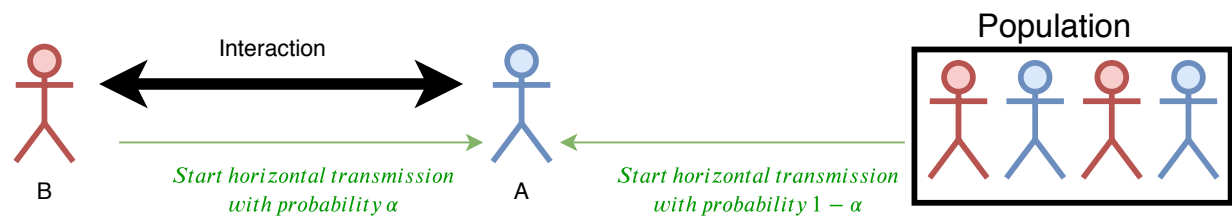
Phenotype $\phi_1$	Phenotype $\phi_2$	Frequency	Fitness of $\phi_1$	$P(\phi_1 = A)$ via horizontal transmission:	
				from partner, $\alpha$	from population, $(1 - \alpha)$
$A$	$A$	$\hat{p}^2$	$1 + b - c$	$1$	$\hat{p} + (1 - \hat{p})(1 - T_B)$
$A$	$B$	$\hat{p}(1 - \hat{p})$	$1 - c$	$1 - T_B$	$\hat{p} + (1 - \hat{p})(1 - T_B)$
$B$	$A$	$\hat{p}(1 - \hat{p})$	$1 + b$	$T_A$	$\hat{p}T_A$
$B$	$B$	$(1 - \hat{p})^2$	$1$	$0$	$\hat{p}T_A$

**Table 3: Model variables and parameters.**

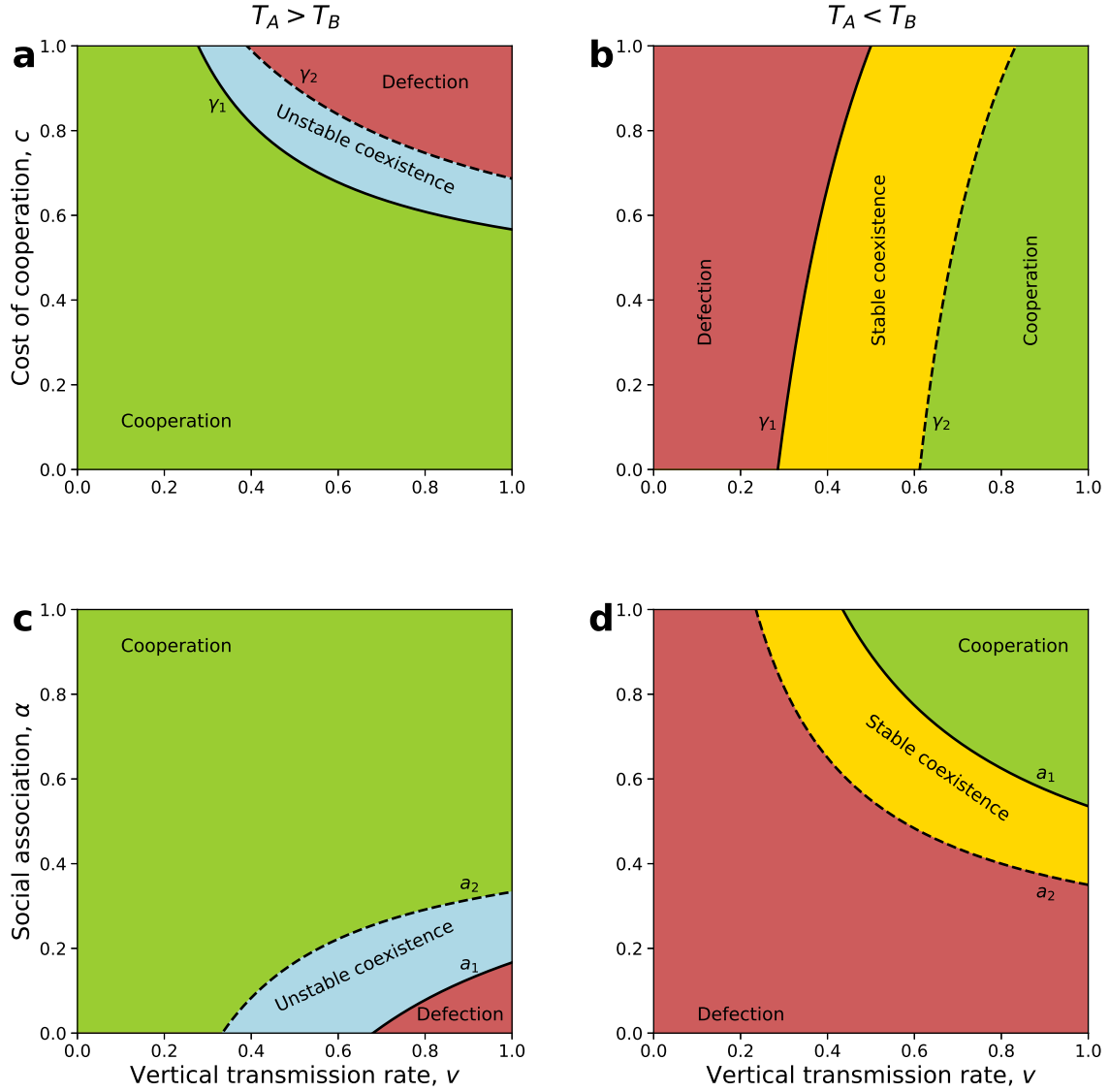
Symbol	Description	Values
$A$	Cooperator phenotype	
$B$	Defector phenotype	
$p$	Frequency of phenotype $A$ among adults	$[0, 1]$
$\tilde{p}$	Frequency of phenotype $A$ among parents	$[0, 1]$
$\hat{p}$	Frequency of phenotype $A$ among juveniles	$[0, 1]$
$v$	Vertical transmission rate	$[0, 1]$
$c$	Cost of cooperation	$(0, 1)$
$b$	Benefit of cooperation	$c < b$
$\alpha$	Probability of social association	$[0, 1]$
$T_A, T_B$	Horizontal transmission rates of phenotype $A$ and $B$	$(0, 1)$



# Figures

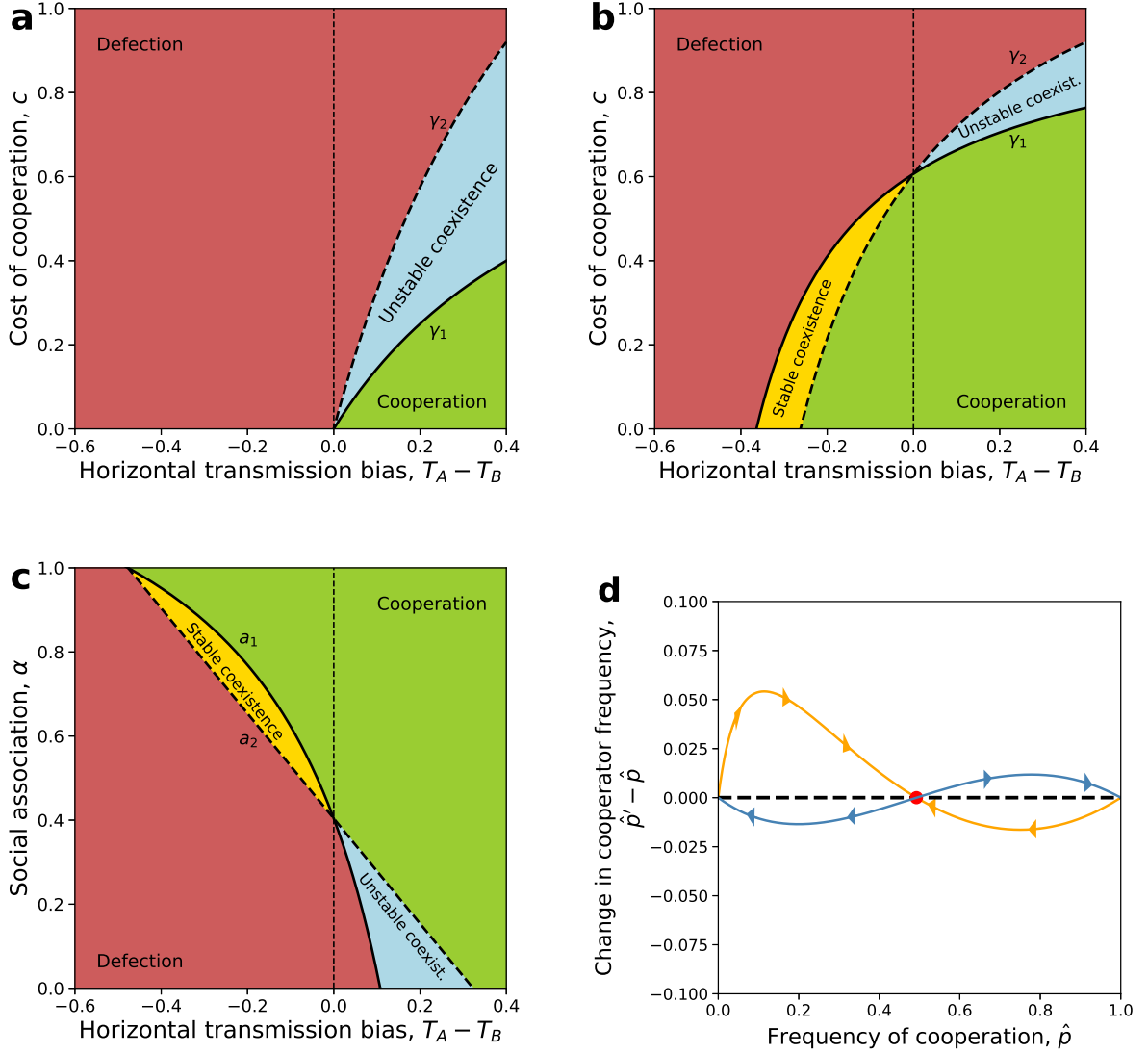


**Figure 1: Cultural horizontal transmission with assortment.** Transmission occurs between interacting partners with probability  $\alpha$  (left) or between two random peers with probability  $1 - \alpha$ , where  $\alpha$  is the *social association* parameter.

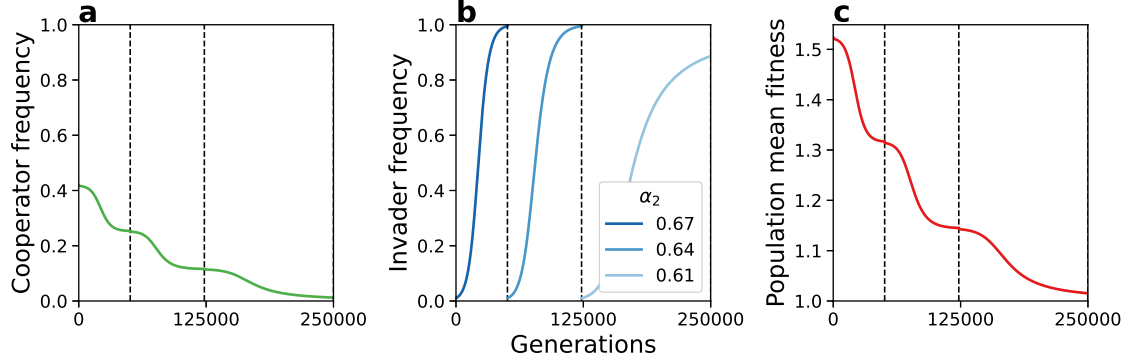


**Figure 2: Evolution of cooperation under vertical, oblique, and horizontal cultural transmission.**

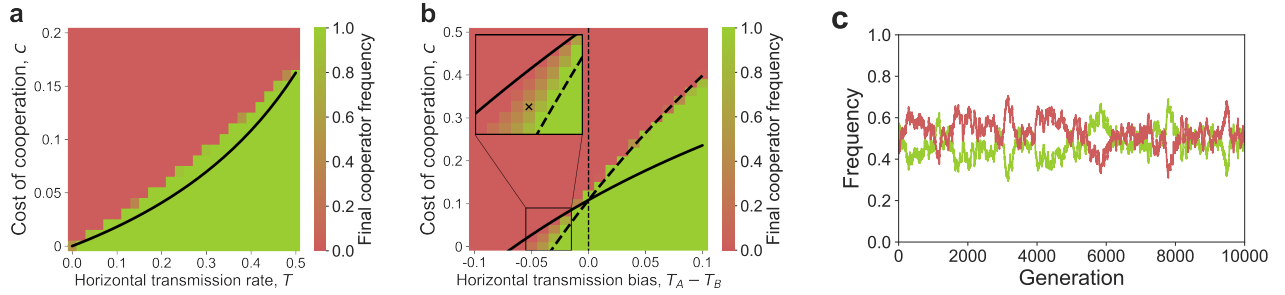
The figure shows the parameter ranges for global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable polymorphism (blue), and stable polymorphism of cooperation and defection (yellow). In all cases the vertical transmission rate  $\nu$  is on the x-axis. **(a-b)** Cost of cooperation  $c$  is on the y-axis and the cost thresholds  $\gamma_1$  and  $\gamma_2$  (Eq. 13) are represented by the solid and dashed lines, respectively. **(c-d)** Social association  $\alpha$  is on the y-axis and the social association thresholds  $a_1$  and  $a_2$  (Eq. 18) are represented by the solid and dashed lines, respectively. Horizontal transmission is biased in favor of cooperation,  $T_A > T_B$ , in **(a)** and **(c)**, or defection,  $T_A < T_B$ , in **(b)** and **(d)**. Here,  $T_A = 0.5$ , and **(a)**  $b = 1.2$ ,  $T_B = 0.4$ ,  $\alpha = 0.4$ ; **(b)**  $b = 2$ ,  $T_B = 0.7$ ,  $\alpha = 0.7$ ; **(c)**  $b = 1.2$ ,  $T_B = 0.4$ ,  $c = 0.5$ ; **(d)**  $b = 2$ ,  $T_B = 0.7$ ,  $c = 0.5$ .



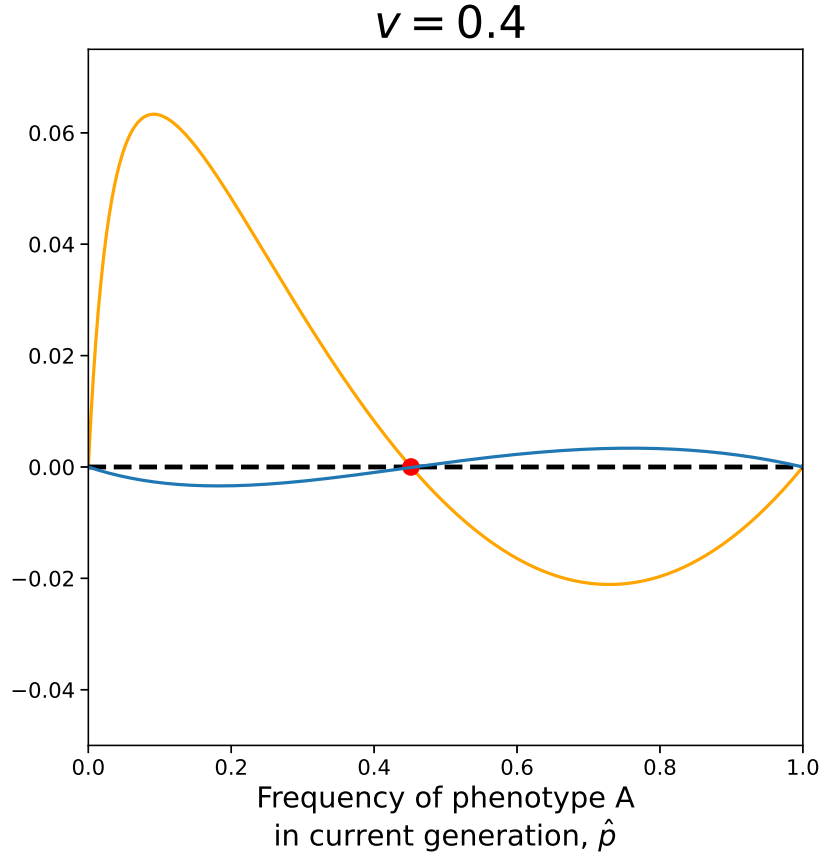
**Figure 3: Evolution of cooperation under vertical and horizontal cultural transmission ( $v=1$ ).** Figures (a)-(c) shows the parameter ranges for global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable polymorphism (blue), and stable polymorphism of cooperation and defection (yellow). In figures (a)-(c) the horizontal bias ( $T_A - T_B$ ) is on the x-axis. (a-b) Cost of cooperation  $c$  is on the y-axis; the cost thresholds  $\gamma_1$  and  $\gamma_2$  (Eq. 13) are the solid and dashed lines, respectively. (c) Social association  $\alpha$  is on the y-axis; the social association thresholds  $a_1$  and  $a_2$  (Eq. 18) are the solid and dashed lines, respectively. Here in figures (a)-(c),  $b = 1.3$ ,  $T_A = 0.4$ , (a)  $\alpha = 0$ , (b)  $\alpha = 0.7$ , (c)  $c = 0.35$ . In figure (d) shows stable and unstable polymorphism of cooperation and defection. The curves show the change in cooperators frequency,  $\hat{p}' - \hat{p}$ , as a function of the current frequency of cooperators among juveniles,  $\hat{p}$  (Eq. 11). A stable polymorphism (orange curve) is given by  $T_A = 0.4$ ,  $T_B = 0.9$ ,  $b = 12$ ,  $c = 0.35$ , and  $\alpha = 0.45$ . An unstable polymorphism (blue curve) is given by  $T_A = 0.5$ ,  $T_B = 0.1$ ,  $b = 1.3$ ,  $c = 0.904$ , and  $\alpha = 0.4$ .



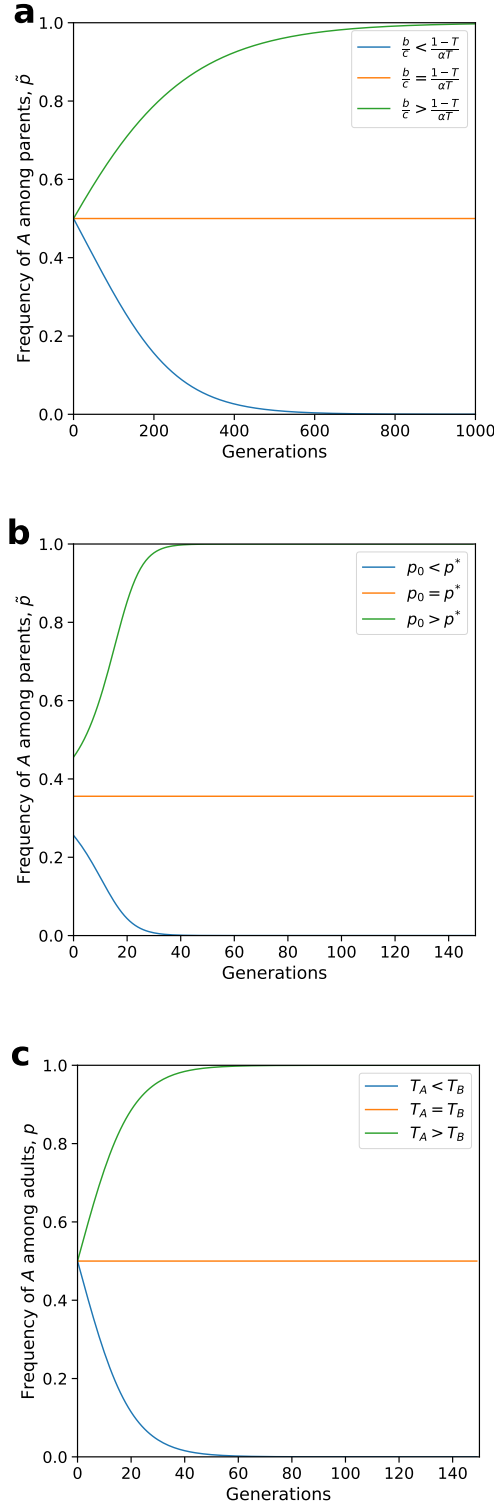
**Figure 4: Reduction principle for social association.** Consecutive fixation of modifier alleles that reduce social association in numerical simulations of evolution with two modifier alleles (Eq. D1). When an invading modifier allele is established in the population (frequency  $> 99.95\%$ ), a new modifier allele that reduces social association by 5% is introduced (at initial frequency 0.5%). **(a)** The frequency of the cooperative phenotype  $A$  over time. **(b)** The frequency of the invading modifier allele  $m$  over time. **(c)** The population mean fitness ( $\bar{w}$ ) over time. Here,  $c = 0.05$ ,  $b = 1.3$ ,  $T_A = 0.4 < T_B = 0.7$ , initial social association  $\alpha_1 = 0.7$ , lower social association threshold  $a_2 = 0.605$ .



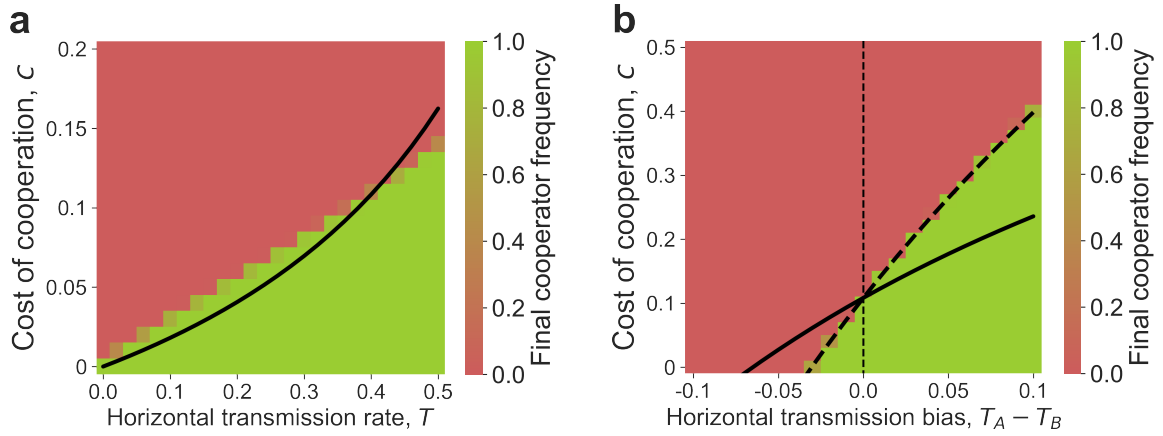
**Figure 5: Evolution of cooperation in a structured population.** **(a-b)** The expected frequency of cooperators in a structured population after 10,000 generations is shown (red for 0%, green for 100%) as a function of both the cost of cooperation,  $c$ , on the y-axis, and either the symmetric horizontal transmission rate,  $T = T_A = T_B$ , on the x-axis of panel (a), or the transmission bias,  $T_A - T_B$ , on the x-axis of panel (b). Black curves represent the cost thresholds for the evolution of cooperation in a well-mixed population with social association, where  $\alpha = 1/8$  in Eq. 15 for panel (a) and in Eq. 13 for (b). The inset in panel (b) focuses on an area of the parameter range in which neither phenotype is fixed throughout the simulation, maintaining a stochastic locally stable polymorphism (Karlin et al., 1975). This stochastic polymorphism is illustrated in panel (c), which shows the frequency of cooperators (green) and defectors (red) over time for the parameter set marked by an  $x$  in panel (b). In all cases, the population evolves on a 100-by-100 grid. Cooperation and horizontal transmission are both local between neighboring sites, and each site has 8 neighbors. Selection operates globally (see Figure S3 for results from a model with local selection). Simulations were stopped at generation 10,000 or if one of the phenotypes fixed. 50 simulations were executed for each parameter set. Benefit of cooperation,  $b = 1.3$ ; perfect vertical transmission  $v = 1$ ; **(a)** Symmetric horizontal transmission,  $T = T_A = T_B$ ; **(b)** Horizontal transmission rates  $T_A = 0.4$ ,  $0.3 < T_B < 0.5$ ; **(c)** Horizontal transmission rates  $T_A = 0.4 < T_B = 0.435$  and cost of cooperation  $c = 0.02$ .



**Figure S1: Stable and unstable polymorphism of cooperation and defection.** The curves show the change in cooperators frequency,  $\hat{p}' - \hat{p}$ , as a function of the current frequency of cooperators among juveniles,  $\hat{p}$  (Eq. 11). The dashed black line is  $\hat{p}' - \hat{p} = 0$ . The curves and the dashed line intersect at the polymorphic equilibrium  $\hat{p}^*$  (red circle). A stable polymorphism (orange curve) is given by  $T_A = 0.4$ ,  $T_B = 0.9$ ,  $b = 20$ ,  $c = 0.1$ ,  $\alpha = 1$ , and  $v = 0.4$ . An unstable polymorphism (blue curve) is given by  $T_A = 0.5$ ,  $T_B = 0.4$ ,  $b = 1.2$ ,  $c = 0.487$ ,  $\alpha = 0.09$  and  $v = 0.6$ .



**Figure S2: Dynamics of the frequency of cooperation.** The frequency  $\tilde{p}$  of cooperator parents in (a-b) and the frequency  $p$  of adults cooperators in (c). The different lines correspond to parameter values that lead to fixation of cooperation (green), extinction of cooperation (red), or stable polymorphism of cooperators and defectors (yellow). (a)  $v = 1$ ,  $T_A = T_B = T = 0.2$ ,  $\alpha = 0.5 \neq 0$ ,  $\tilde{p}_0 = 0.5$  and  $c = 0.1$ ; (b)  $v = 1$ ,  $\alpha = 0$ ,  $\tilde{p}^* \approx 0.35$ ,  $T_A = 0.65$ ,  $T_B = 0.1$ ,  $b = 1.3$  and  $c = 0.65$ ; (c)  $v = 0$ ,  $\alpha = 0.5$ ,  $p_0 = 0.5$ ,  $T_A = 0.5$ ,  $b = 1.3$  and  $c = 0.5$ .



**Figure S3: Evolution of cooperation in a structured population with local selection.** The expected frequency of cooperators in a structured population after 10,000 generations is shown (red for 0%, green for 100%) as function of both the cost of cooperation ( $c$ ) on the y-axis, and the symmetric horizontal transmission rate ( $T = T_A = T_B$ ) on the x-axis of panel (a), or the transmission bias  $T_A - T_B$  on the x-axis of panel (b). The population evolves on a 100-by-100 grid. Cooperation and horizontal transmission are both local between neighboring sites, and each site had 8 neighbors. Selection operates locally (see Figure 5 for results from a model with global selection). The black curves represent the cost thresholds for the evolution of cooperation in a well-mixed population with social association, where  $\alpha = 1/8$  in Eq. 15 for panel (a) and in Eq. 13 for panel (b). The population evolves on a 100-by-100 grid. Simulations were stopped at generation 10,000 or if one of the phenotypes fixed. 50 simulations were executed for each parameter set. Here, benefit of cooperation,  $b = 1.3$ ; perfect vertical transmission  $\nu = 1$ ; **(a)** Symmetric horizontal transmission,  $T = T_A = T_B$ ; **(b)** Horizontal transmission rates  $T_A = 0.4$ ,  $0.3 < T_B < 0.5$ ;