# Non-Vertical Cultural Transmission, Assortment, and the Evolution of Cooperation

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10 Abstract

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We construct models for the cultural evolution of cooperation in a well-mixed population with vertical, horizontal, and oblique transmission. Conditions are found for fixation and coexistence of cooperation and defection. The results show that association between cooperation and horizontal transmission facilitates the evolution of cooperation. A spatial model is constructed and its results are compared to the well-mixed model. Comparisons are drawn with Hamilton's rule and the concepts of relatedness and assortment.

### Introduction

- 18 Cooperative behavior can reduce an individual's fitness and increase the fitness of its conspecifics or competitors (Axelrod and Hamilton, 1981). Nevertheless, cooperative behavior appears to occur in
- 20 many non-human animals (Dugatkin, 1997), including primates (Jaeggi and Gurven, 2013), rats (Rice and Gainer, 1962), birds (Stacey and Koenig, 1990; Krams et al., 2008), and lizards (Sinervo et al.,
- 22 2006). Evolution of cooperative behavior remains an important conundrum in evolutionary biology. Since the work of Hamilton (1964) and Axelrod and Hamilton (1981), theories for the evolution of
- 24 cooperative and altruistic behaviors have been intertwined often under the rubric of kin selection.
- Kin selection theory posits that natural selection is more likely to favor cooperation between more closely related individuals. The importance of relatedness to the evolution of cooperation and altruism was demonstrated by Hamilton (1964), who showed that an allele that determines cooperative behavior
- 28 will increase in frequency if the reproductive cost to the actor that cooperates, c, is less than the benefit to the recipient, b, times the relatedness, r, between the recipient and the actor. This relatedness
- 30 coefficient *r* measures a probability that an allele sampled from the cooperator is identical by descent to one at the same locus in the recipient. This condition is known as *Hamilton's rule*:

$$c < b \cdot r. \tag{1}$$

Eshel and Cavalli-Sforza (1982) studied a related model for the evolution of cooperative behavior.

- Their model included *assortative meeting*, or non-random encounters, where a fraction m of individuals in the population each interact with an individual of the same phenotype, and a fraction 1-m interacts
- with a randomly chosen individual. Such assortative meeting may be due, for example, to population structure or active partner choice. In their model, cooperative behavior can evolve if<sup>1</sup> (Eshel and
- 38 Cavalli-Sforza, 1982, eq. 3.2)

$$c < b \cdot m, \tag{2}$$

- 40 where b and c are the benefit and cost of cooperation. Here m in inequality 2 takes the role of the relatedness r in inequality 1.
- 42 The role of assortment in the evolution of altruism was studied by Fletcher and Doebeli (2009) in a *public goods* game. They found that for altruism to evolve, cooperative individuals must experience
- 44 more cooperation, on average, than defecting individuals, and "thus, the evolution of altruism requires (positive) assortment between focal *cooperative* players and cooperative acts in their interaction
- 46 environment." This condition can be summarized by (Fletcher and Doebeli, 2009, eq. 2.3)

$$c < b \cdot (e_C - e_D), \tag{3}$$

- 48 where  $e_C$  is the probability that a cooperator receives help, and  $e_D$  is the probability that a defector receives help.<sup>2</sup>
- 50 In this paper we study the evolution of a cooperative behavior that is subject to *cultural transmission*, which allows an individual to acquire attitudes or behavioral traits from other individuals in its social
- 52 group through imitation, learning, or other modes of communication (Cavalli-Sforza and Feldman, 1981; Richerson and Boyd, 2008). Feldman et al. (1985) introduced the first model for the evolution
- of altruism by cultural transmission. They demonstrated that if the fidelity of cultural transmission of altruism is  $\varphi$ , then the condition for evolution of altruism in the case of sib-to-sib altruism is (Feldman
- 56 et al., 1985, Eq. 16)

$$c < b \cdot \varphi - \frac{1 - \varphi}{\varphi} \,. \tag{4}$$

<sup>&</sup>lt;sup>1</sup>In an extended model, which allows an individual to encounter N individuals before choosing a partner, the righthand side is multiplied by E[N], the expected number of encounters (Eshel and Cavalli-Sforza, 1982, eq. 4.6).

<sup>&</sup>lt;sup>2</sup>inequality 3 generalizes inequality 1 and inequality 2 by substituting  $e_C = r + p$ ,  $e_D = p$  and  $e_C = m + (1 - m)p$ ,  $e_D = (1 - m)p$ , respectively, where p is the frequency of cooperators.

In inequality 4,  $\varphi$  takes the role of 'relatedness' (r in Eq. 1) or 'assortment' (m in Eq. 2), but the effective benefit  $b \cdot \varphi$  is further reduced by  $(1 - \varphi)/\varphi$ . This shows that under a combination of genetic and vertical (parent-to-offspring) cultural transmission, the condition for the evolutionary success of altruism entails a modification of Hamilton's rule (Eq. 1).

Cultural transmission may be either viewed as vertical, horizontal or oblique: vertical transmission occurs between parents and offspring, horizontal transmission occurs between individuals from the same generation, and oblique transmission occurs to offspring from the generation to which their parents belong (i.e. from non-parental adults). Evolution under either of these transmission models can be be more rapid than under pure vertical transmission (Cavalli-Sforza and Feldman, 1981; Lycett and Gowlett, 2008; Ram et al., 2018). Both Woodcock (2006) and Lewin-Epstein et al. (2017) demonstrated that non-vertical transmission can help explain the evolution of cooperative behavior (the former using simulations with cultural transmission, the latter using a model where cooperation is mediated by microbes that manipulate their host's behavior.) Some of the analyses by Lewin-Epstein et al. (2017) can be applied to cultural transmission, because models of cultural transmission are mathematically similar to those for transmission of infectious diseases (Cavalli-Sforza and Feldman, 1981).

Here, we study cultural-evolution models of cooperation that include both vertical and non-vertical transmission. We investigate these models using mathematical analysis and simulations. In our models behavioral changes are mediated by cultural transmission that can occur specifically during social interactions. For instance, when there is an association between the choice of partner for social interaction and the choice of partner for cultural transmission. As another example, when an individual interacts with an individual of a different phenotype, this exposure to a different phenotype may lead it to learn or convert its phenotype. Our results demonstrate that cultural transmission can enhance the evolution of cooperation even when genetic transmission cannot (partly because it facilitates the generation of assortment in the sense of Fletcher and Doebeli (2009)). This further emphasizes that treatment of cooperation as a cultural trait, rather than a genetic one, can lead to a better understanding of its evolutionary dynamics.

#### **Models**

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Consider a very large population whose members are characterized by their phenotype φ, which can be of two types, φ = A for cooperators or φ = B for defectors. An offspring inherits its phenotype
from its parent via vertical transmission with probability v or from a random individual in the parental population via oblique transmission with probability (1 - v). Following Ram et al. (2018), given that
the parent phenotype is φ and assuming uni-parental inheritance, the conditional probability that the phenotype φ' of the offspring is A is

$$P(\phi' = A \mid \phi) = \begin{cases} v + (1 - v)p, & \text{if } \phi = A \\ (1 - v)p, & \text{if } \phi = B \end{cases}$$
 (5)

where  $p = P(\phi = A)$  is the frequency of A among all adults in the parental generation.

Not all adults become parents due to natural selection, and we denote the frequency of phenotype A among parents by  $\tilde{p}$ . Therefore, the frequency  $\hat{p}$  of phenotype A among juveniles (after selection and vertical and oblique transmission) is

$$\hat{p} = \tilde{p}[v + (1 - v)p] + (1 - \tilde{p})[(1 - v)p] = v\tilde{p} + (1 - v)p.$$
(6)

Individuals are assumed to interact according to a *prisoner's dilemma*. Specifically, individuals interact in pairs; a cooperator suffers a fitness cost 0 < c < 1, and its partner gains a fitness benefit</li>
b, where we assume c < b. Table 1 shows the payoff matrix, i.e. the fitness of an individual with phenotype φ₁ when interacting with a partner of phenotype φ₂.</li>

	$\phi_2 = A$	$\phi_2 = B$
$\phi_1 = A$	1 + b - c	1-c
$\phi_1 = B$	1 + b	1

**Table 1: Payoff matrix for prisoner's dilemma.** The fitness of phenotype  $\phi_1$  when interacting with phenotype  $\phi_2$ . A is a cooperative phenotype, B is a defector phenotype, b is the benefit gained by an individual interacting with a cooperator, and c is the cost of cooperation. b > c > 0.

Social interactions occur randomly: two juvenile individuals with phenotype A interact with probability  $\hat{p}^2$ , two juveniles with phenotype B interact with probability  $(1 - \hat{p})^2$ , and two juveniles with different phenotypes interact with probability  $2\hat{p}(1 - \hat{p})$ .

Horizontal cultural transmission occurs between pairs of individuals from the same generation. It occurs between social partners with probability  $\alpha$ , or between a random pair with probability  $1 - \alpha$  (see Figure 1). The social association  $\alpha$  is therefore the fraction of population that receives (horizontal transmission) from the social interaction partner, and  $1-\alpha$  receives randomly. Horizontal transmission is not always successful, as one partner may reject the other's phenotype. The probability for successful horizontal transmission of phenotypes A and B are  $T_A$  and  $T_B$ , respectively (Table 2).

Therefore, the frequency p' of phenotype A among adults in the next generation, after horizontal transmission, is

$$p' = \hat{p}^{2} [\alpha + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_{B}))] + \hat{p}(1 - \hat{p})[\alpha(1 - T_{B}) + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_{B}))] + (1 - \hat{p})\hat{p}[\alpha T_{A} + (1 - \alpha)\hat{p}T_{A}] + (1 - \hat{p})^{2}[(1 - \alpha)\hat{p}T_{A}],$$
(7)

114 which simplifies to

$$p' = \hat{p}^2 (T_B - T_A) + \hat{p} (1 + T_A - T_B).$$
(8)

The frequency of A among parents (i.e. after selection) follows a similar dynamic, but also includes

Phenotype $\phi_1$	Phenotype $\phi_2$	Frequency	Fitness of $\phi_1$	$P(\phi_1 = A)$ via horizontal transmission:	
Thenotype $\phi_1$				from partner, $\alpha$	from population, $(1 - \alpha)$
$\overline{A}$	A	$\hat{p}^2$	1+b-c	1	$\hat{p} + (1 - \hat{p})(1 - T_B)$
A	B	$\hat{p}(1-\hat{p})$	1 <i>- c</i>	$1-T_B$	$\hat{p} + (1 - \hat{p})(1 - T_B)$
B	A	$\hat{p}(1-\hat{p})$	1 + b	$T_A$	$\hat{p}T_A$
В	В	$(1-\hat{p})^2$	1	0	$\hat{p}T_A$

Table 2: Interaction frequency, fitness, and transmission probabilities.

the effect of natural selection, and is therefore

$$\bar{w}\tilde{p}' = \hat{p}^{2}(1+b-c)[\alpha+(1-\alpha)(\hat{p}+(1-\hat{p})(1-T_{B}))] + \hat{p}(1-\hat{p})(1-c)[\alpha(1-T_{B})+(1-\alpha)(\hat{p}+(1-\hat{p})(1-T_{B}))] + (1-\hat{p})\hat{p}(1+b)[\alpha T_{A}+(1-\alpha)\hat{p}T_{A}] + (1-\hat{p})^{2}[(1-\alpha)\hat{p}T_{A}],$$
(9)

where fitness values are taken from Table 1 and Table 2, and the population mean fitness is

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$$\bar{w} = 1 + \hat{p}(b - c)$$
. (10)

Eq. 9 can be simplified to

$$\bar{w}\,\tilde{p}' = \hat{p}^2 (1 + b - c) \left( 1 - (1 - \hat{p})(1 - \alpha)T_B \right)$$

$$+ \hat{p}(1 - \hat{p})(1 - c) \left( \hat{p}(1 - \alpha)T_B + 1 - T_B \right)$$

$$+ (1 - \hat{p})\hat{p}(1 + b) \left( \hat{p}(1 - \alpha) + \alpha \right)T_A$$

$$+ (1 - \hat{p})^2 \hat{p}(1 - \alpha)T_A .$$
(11)

where  $\hat{p} = v\tilde{p} + (1 - v)p$ .

#### 124 Results

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#### **Oblique and Horizontal Transmission**

126 With only oblique and horizontal transmission, i.e. v = 0, Eq. 6 becomes  $\hat{p} = p$  and Eq. 8 becomes

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$$p' = p^{2}(T_{B} - T_{A}) + p(1 + T_{A} - T_{B}), \tag{12}$$

which gives the following result.

**Result 1** (Oblique and horizontal transmission of cooperation). Without vertical transmission (v = 0), if there is a horizontal transmission bias in favor of cooperation, namely

$$T_A > T_B, \tag{13}$$

134 then p' > p, and the frequency of the cooperator phenotype among adults increases every generation.

If  $T_A = T_B$ , then p' = p and the population is static. Therefore, in the absence of vertical transmission, selection plays no role in the evolution of cooperation. Hence, cooperation will evolve if the cooperator phenotype has a horizontal transmission bias (see Figure 6c).

#### 138 Vertical and Horizontal Transmission

With only vertical and horizontal transmission, i.e. v=1, Eq. 6 becomes  $\hat{p}=\tilde{p}$ , and Eq. 11 for the frequency of the cooperative phenotype among parents in the next generation  $\tilde{p}'$  can be written as

$$\bar{w}\tilde{p}' = \tilde{p}^{2}(1+b-c)[1-(1-\tilde{p})(1-\alpha)T_{B}] + \tilde{p}(1-\tilde{p})(1-c)[\tilde{p}(1-\alpha)T_{B}+1-T_{B}] + \tilde{p}(1-\tilde{p})(1+b)[\tilde{p}(1-\alpha)+\alpha]T_{A} + (1-\tilde{p})^{2}\tilde{p}(1-\alpha)T_{A}.$$
(14)

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Fixation of either cooperation,  $\tilde{p} = 1$ , or defection,  $\tilde{p} = 0$ , are equilibria of Eq. 14, that is, they solve  $\tilde{p}' = \tilde{p}$ . We therefore assume for the remainder of the analysis that  $0 < \tilde{p} < 1$ .

If  $\alpha = 1$ , then  $\tilde{p}' = \tilde{p}$  is reduced to

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$$\tilde{p}(1-\tilde{p})[(1+b)T_A + (1-c)(1-T_B) - 1] = 0, \tag{15}$$

and there are no additional equilibria. For cooperation to take over the population (for  $\tilde{p}=1$  to be globally stable) we require  $\tilde{p}' > \tilde{p}$ ; that is,

$$\tilde{p}^{2}(1+b-c) + \tilde{p}(1-\tilde{p})[(1-c)(1-T_{B}) + (1+b)T_{A}] > \bar{w}\tilde{p}.$$
(16)

150 Factoring out  $\tilde{p}(1-\tilde{p})$  and setting  $\bar{w}=1+\tilde{p}(b-c)$ , we find that  $\hat{p}'>\hat{p}$  if

$$(1-c)(1-T_B) + (1+b)T_A > 1 (17)$$

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154 If  $\alpha < 1$ , divide both sides of Eq. 14 by  $\tilde{p}$  and set  $\bar{w} = 1 + \tilde{p}(b - c)$ . Then  $\tilde{p}' > \tilde{p}$  if

$$1 + \tilde{p}(b-c) < \tilde{p}(1+b-c)(1-(1-\tilde{p})(1-\alpha)T_B)$$

$$+ (1-\tilde{p})(1-c)(\tilde{p}(1-\alpha)T_B + 1 - T_B)$$

$$+ (1-\tilde{p})(1+b)(\tilde{p}(1-\alpha) + \alpha)T_A$$

$$+ (1-\tilde{p})^2(1-\alpha)T_A.$$
(18)

156 Simplifying, we find that  $\tilde{p}' > \tilde{p}$  if and only if

$$c(1-T_B) - b\alpha T_A - (T_A - T_B) < \tilde{p} \cdot b(1-\alpha)(T_A - T_B). \tag{19}$$

Besides the fixation states  $\tilde{p} = 0$  and  $\tilde{p} = 1$ , there may be an actual polymorphic equilibrium of  $\tilde{p}' = \tilde{p}$  in Eq. 14, namely

which is legitimate if  $0 < \tilde{p}^* < 1$ .

 $\tilde{p}^* = \frac{c(1 - T_B) - b\alpha T_A - (T_A - T_B)}{b(1 - \alpha)(T_A - T_B)},\tag{20}$ 

Since all parameters are positive, we can apply inequality 19 and see that for  $\tilde{p}' > \tilde{p}$  we require that either

$$T_A > T_B$$
 and  $\tilde{p} > \tilde{p}^*$ , or (21)

$$T_A < T_B$$
 and  $\tilde{p} < \tilde{p}^*$ . (22)

We define the initial frequency of the cooperator phenotype among parents,  $\tilde{p}_0$ , and the *cost boundaries*,

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$$\gamma_1 = \frac{b\alpha T_A + (T_A - T_B)}{1 - T_B}, \quad \gamma_2 = \frac{b\alpha T_B + (1 + b)(T_A - T_B)}{1 - T_B}.$$
 (23)

Then, applying Eqs. 20, 21, and 22, we summarize the possible outcomes in following result and corollaries.

168 **Result 2** (Vertical and horizontal transmission of cooperation). With vertical and horizontal but without oblique transmission (v = 1), the cultural evolution of a cooperator phenotype will follow one 170 of the following scenarios, depending on the cost boundaries  $\gamma_1$  and  $\gamma_2$  (Eq. 23):

- 1. Fixation of cooperation: if (i)  $T = T_A = T_B$  and  $c < b \cdot \alpha \frac{T}{1-T}$ ; or if (ii)  $T_A > T_B$  and  $c < \gamma_1$ ; or if (iii)  $T_A < T_B$  and  $c < \gamma_2$ .
- 2. Fixation of defection: if (iv)  $T = T_A = T_B$  and  $c > b \cdot \alpha \frac{T}{1-T}$ ; or if (v)  $T_A > T_B$  and  $\gamma_2 < c$ ; or if (vi)  $T_A < T_B$  and  $\gamma_1 < c$ .
  - 3. Stable coexistence of both phenotypes at  $\tilde{p}^*$ : if (vii)  $T_A < T_B$  and  $\gamma_2 < c < \gamma_1$ .
- 176 4. Unstable coexistence and fixation of either phenotype depending on initial frequency: if (viii)  $T_A > T_B$  and  $\gamma_1 < c < \gamma_2$ .
- 178 These conditions are illustrated in Figure 3. Note that cooperation and defection can coexist stably if there is horizontal bias for defection and the cost of cooperation is large but not too large. The recursion dynamic for this case is illustrated in Figure 2.
- Much of the literature on evolution of cooperation focuses on conditions for an initially rare cooperative phenotype to invade a population of defectors. The next corollary deals with such a condition, followed by a corollary that deals with symmetric horizontal transmission, i.e.  $T_A = T_B$ .

**Corollary 1** (Condition for cooperation to increase when initially rare). *If the initial frequency of the cooperative phenotype is very close to zero,*  $\tilde{p}_0 \approx 0$ , then this frequency will increase if

$$T_A > T_B$$
 and  $c < \gamma_1$ , or  $T_A < T_B$  and  $\gamma_2 < c < \gamma_1$ . (24)

- In general, these conditions cannot be formulated in the form of Hamilton's rule (c < b · r) due to the horizontal transmission bias T<sub>A</sub> T<sub>B</sub>. Without horizontal transmission bias, i.e., with T = T<sub>A</sub> = T<sub>B</sub>, these conditions reduce to a form of Hamilton's rule.
- 192 **Corollary 2** (Symmetric horizontal transmission). If  $T = T_A = T_B$ , then cooperation will take over the population if

$$c < b \cdot \alpha \frac{T}{1 - T}. \tag{25}$$

- Inequality 25 is obtained by setting  $T = T_A = T_B$  in inequality 19 and can be interpreted as a version of Hamilton's rule (inequality 1) or as a version of inequality 3, where  $\alpha T/(1-T)$  can be regarded as the 'effective relatedness' or 'effective assortment', respectively. Figure 6a demonstrates this condition.
- Corollary 3 (No social association of transmission and cooperation). Without association ( $\alpha=0$ ) and with horizontal bias for cooperation ( $T_A>T_B$ ), then (1) if the cost is low compared to the bias ( $c<(T_A-T_B)/(1-T_B)$ ), then cooperation will fix from any positive frequency; (2) if the cost is low compared to the benefit ( $c<(1+b)(T_A-T_B)(1-T_B)$ ), then cooperation will fix if the initial frequency is high enough ( $\tilde{p}_0>\tilde{p}^*$ ).
- 204 Figure 3a illustrates these conditions, where the third equilibrium given by Eq. 20 becomes

$$\tilde{p}^*(\alpha = 0) = \frac{c(1 - T_B) - (T_A - T_B)}{b(T_A - T_B)},\tag{26}$$

206 and the cost boundaries are

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$$\gamma_1(\alpha = 0) = \frac{T_A - T_B}{1 - T_B}, \quad \gamma_2(\alpha = 0) = (1 + b) \frac{T_A - T_B}{1 - T_B}.$$
(27)

208 If  $T_A > T_B$  then  $0 < \gamma_1(\alpha = 0) < \gamma_2(\alpha = 0)$ . So either  $c < \gamma_1(\alpha = 0)$  or  $\gamma_1(\alpha = 0) < c < \gamma_2(\alpha = 0)$  will allow fixation of cooperation, the latter only if the initial frequency is high enough. If  $T_A < T_B$ 

210 then  $\gamma_2(\alpha = 0) < \gamma_1(\alpha = 0) < 0 < c$ , and defection will fix.

Corollary 4 (Perfect social association of transmission and cooperation). With perfect social association ( $\alpha = 1$ ), there are only two equilibria,  $\tilde{p} = 0$  and  $\tilde{p} = 1$ . The condition for evolution of cooperation (i.e. global stability of  $\tilde{p} = 1$ ) is found from inequality 17, namely

$$c < \frac{b \cdot T_A + (T_A - T_B)}{1 - T_B}. (28)$$

- With perfect social association horizontal transmission always co-occurs with the cooperative interaction. The same occurs in Lewin-Epstein et al. (2017), and therefore this corollary is equivalent to their result (see their eq. 1).
- In terms of the cost boundaries, inequality 28 is equivalent to  $c < \gamma_1$ , and if  $T_A > T_B$  then that suffices 220 for fixation of cooperation. If  $T_B > T_A$  then  $\gamma_2(\alpha = 1) < 0$  and again, inequality 28 is sufficient for increase in the frequency of A. Inequality 28 can be written as

$$1 - (1 - c)(1 - T_B) < (1 + b)T_A, \tag{29}$$

- which provides an interesting interpretation for the success of cooperation. In the interaction between a cooperator and a defector,  $(1-c)(1-T_B)$  is the probability that the cooperator remains cooperative and also reproduces. Therefore,  $1-(1-c)(1-T_B)$  is the probability that either the cooperator becomes a defector, or that it fails to reproduce. This is the *effective cost of cooperation* from this interaction, while  $(1+b)T_A$  is the probability that the defector becomes cooperative and reproduces, which is the *effective benefit of cooperation* from this interaction. Thus, inequality 28 entails that cooperation can evolve if the effective cost of cooperation is less than the effective benefit.
- Given the previous two corollaries for no association and perfect association ( $\alpha = 0$  and  $\alpha = 1$ ), it is interesting to examine the general effect of social association on the evolution of cooperation. We denote the social association boundaries by

$$a_1 = \frac{c(1 - T_B) - (1 + b)(T_A - T_B)}{b \cdot T_B}, \quad a_2 = \frac{c(1 - T_B) - (T_A - T_B)}{b \cdot T_A}.$$
 (30)

- 234 Applying Eqs. 20, 21, and 22, we have the following corollary.
- 236 **Corollary 5** (Intermediate assortment of transmission and cooperation). *The cooperative phenotype will increase from rarity if the assortment rate is high enough, or specifically if*

$$T_A > T_B \quad and \quad a_2 < \alpha, \quad or$$

$$T_A < T_B \quad and \quad a_1 < \alpha.$$
(31)

Figure 3c demonstrates these conditions. With horizontal bias for cooperation  $(T_A > T_B)$ ; positive x-axis) cooperation fixes in the population from any initial positive frequency (green) if  $\alpha$  (y-axis) is above the orange line  $(a_1)$ , or if initially present at a high enough frequency (blue) if  $\alpha$  is above the blue line  $(a_2)$ . With horizontal bias for defection  $(T_B > T_A)$ ; negative x-axis) cooperation fixes if  $\alpha$  is above the blue line  $(a_2)$ , but can be maintained in coexistence with defection (yellow) if  $\alpha$  is above the orange line  $(a_1)$ . Without horizontal bias  $(T_A = T_B)$  fixation occurs if the assortment rate is high enough,  $\alpha > \frac{c}{b} \cdot \frac{1-T}{T}$  (inequality 25).

#### 246 With Vertical and Oblique Transmission

With both vertical and oblique transmission, 0 < v < 1, the recursion system is more complex, and we</li>
focus on local rather than on global stability. To proceed, we note that Eq. 6 can give p̂' as a function of both p' and p̂'. Eq. 8 gives p' as a function of p̂, since p̂ is given in Eq. 6 as a function of p̂ and Eq.
11 gives p̂' as a function of p̂. Combining these equations, we find an equation for p̂' as a function of p̂ (shown in Appendix Appendix A). We then determine the equilibria, namely, solutions of p̂' = p̂,
and analyse their local stability.

We apply Eqs. 6, 8, and 11 to obtain the function  $f(\hat{p})$  (see Appendix Appendix A):

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$$f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p}) = \beta_1 \hat{p}^3 + \beta_2 \hat{p}^2 + \beta_3 \hat{p}, \tag{32}$$

where

$$\beta_{1} = [c(1-v) - b(1-\alpha v)](T_{A} - T_{B}),$$

$$\beta_{2} = -\beta_{1} - \beta_{3},$$

$$\beta_{3} = \alpha b v T_{A} - c v (1 - T_{B}) + (T_{A} - T_{B}).$$
(33)

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If  $T = T_A = T_B$  then  $\beta_1 = 0$  and  $\beta_3 = -\beta_2 = \alpha b v T - c v (1 - T)$ , and  $f(\hat{p})$  becomes a quadratic polynomial:

$$f(\hat{p}) = \hat{p}(1-\hat{p})[\alpha b \nu T - c \nu (1-T)]. \tag{34}$$

Clearly the only two equilibria are the fixations  $\hat{p} = 0$  and  $\hat{p} = 1$ . These equilibria are locally stable if  $f'(\hat{p}) < 0$  near the equilibrium (Appendix Appendix B), and

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$$f'(\hat{p}) = (1 - 2\hat{p}) \left[ \alpha b \nu T - c \nu (1 - T) \right], \tag{35}$$

with

$$f'(0) = \alpha b v T - c v (1 - T),$$
  

$$f'(1) = -\alpha b v T + c v (1 - T).$$
(36)

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Therefore with symmetric horizontal transmission, fixation of the cooperative phenotype ( $\hat{p} = 1$ ) occurs under the same condition as Corollary 1.1, namely Eq. 25.

In the general case where  $T_A \neq T_B$ , the coefficient  $\beta_1$  is not necessarily zero, and  $f(\hat{p})$  is a cubic polynomial. Therefore, three equilibria may exist, two of which are  $\hat{p} = 0$  and  $\hat{p} = 1$ , and the third is

$$\hat{p}^* = \frac{\beta_3}{\beta_1}.$$
 (37)

Note that the sign of the cubic (Eq. 32) at positive (negative) infinity is equal (opposite) to the sign of  $\beta_1$ . If  $T_A > T_B$ , then

$$\beta_1 < [c(1 - \alpha v) - b(1 - \alpha v)](T_A - T_B) = (1 - \alpha v)(c - b)(T_A - T_B) < 0, \tag{38}$$

since c < b and  $1 > \alpha v$ . Hence the signs of the cubic at positive and negative infinity are negative and positive, respectively. First, if  $\beta_3 < \beta_1$  then  $1 < \hat{p}^*$  and therefore f'(0) < 0 and f'(1) > 0; that

is, fixation of the defector phenotype B is the only locally stable legitimate (i.e. between 0 and 1) equilibrium. Second, if  $\beta_1 < \beta_3 < 0$  then  $0 < \hat{p}^* < 1$  and therefore f'(0) < 0 and f'(1) < 0, that

278 is, both fixations are locally stable and  $\hat{p}^*$  separates the domains of attraction. Third, if  $0 < \beta_3$  then  $\hat{p}^* < 0$  and therefore f'(0) > 0 and f'(1) < 0; that is, fixation of the cooperator phenotype A is the

280 only locally stable legitimate equilibrium.

Similarly, if  $T_B > T_A$ , then

282 
$$\beta_1 > [c(1-\alpha v) - b(1-\alpha v)](T_A - T_B) = (1-\alpha v)(c-b)(T_A - T_B) > 0, \tag{39}$$

since c < b and  $1 > \alpha v$ , and the signs of the cubic at positive and negative infinity are positive and negative, respectively. First, if  $\beta_3 < 0$  then  $\hat{p}^* < 0$  and therefore f'(0) < 0 and f'(1) > 0; that is, fixation of the defector phenotype A = B is the only locally stable legitimate equilibrium. Second, 286 if  $0 < \beta_3 < \beta_1$  then  $0 < \hat{p}^* < 1$  and therefore f'(0) > 0 and f'(1) > 0; that is, both fixations are locally unstable and  $\hat{p}^*$  is a stable polymorphic equilibrium. Third, if  $\beta_1 < \beta_3$  then  $\hat{p}^* > 1$  and 288 therefore f'(0) > 0 and f'(1) < 0, and fixation of the cooperator phenotype A is the only locally stable legitimate equilibrium.

290 We define new cost boundaries,  $\hat{\gamma}_1$  and  $\hat{\gamma}_2$ ,

$$\hat{\gamma}_1 = \frac{bv\alpha T_A + (T_A - T_B)}{v(1 - T_B)}, \quad \hat{\gamma}_2 = \frac{bv\alpha T_B + (1 + b)(T_A - T_B)}{v(1 - T_B) + (1 - v)(T_A - T_B)},\tag{40}$$

292 and define a vertical transmission threshold,

$$\hat{v} = \frac{T_B - T_A}{1 - T_A} \,. \tag{41}$$

294 The following result summarizes the possible outcomes.

- Result 3 (Vertical, oblique, and horizontal transmission of cooperation). With vertical, horizontal, and oblique transmission, the cultural evolution of a cooperator phenotype will follow one of the following scenarios depending on the cost boundaries \(\hat{\gamma}\_1\) and \(\hat{\gamma}\_2\) (Eq. 40) and the vertical threshold \(\hat{\gamma}\) (Eq. 41):
- 300 *I.* Fixation of cooperation: if (i)  $T = T_A = T_B$  and  $c < b \cdot \alpha \frac{T}{1-T}$ ; or if (ii)  $T_A > T_B$  and  $c < \hat{\gamma}_1$ ; or if (iii.a)  $T_A < T_B$  and  $v > \hat{v}$  and  $c < \hat{\gamma}_2$ ; or if (iii.b)  $T_A < T_B$  and  $v < \hat{v}$  and  $\hat{\gamma}_2 < c$ .
- 2. Fixation of defection: if (iv)  $T = T_A = T_B$  and  $c > b \cdot \alpha \frac{T}{1-T}$ ; or if (v)  $T_A > T_B$  and  $\hat{\gamma}_2 < c$ ; or if (vi)  $T_A < T_B$  and  $\hat{\gamma}_1 < c$ .
- 3. Stable Coexistence of both phenotypes at  $\hat{p}^*$ : if (vii.a)  $T_A < T_B$  and  $v < \hat{v}$  and  $c < \hat{\gamma}_2$  and  $c < \hat{\gamma}_1$ ; or if (vii.b)  $T_A < T_B$  and  $v > \hat{v}$  and  $\hat{\gamma}_2 < c < \hat{\gamma}_1$ .
- 4. Unstable coexistence and fixation of either phenotype depending on initial frequency: if (viii)  $T_A > T_B$  and  $\hat{\gamma}_1 < c < \hat{\gamma}_2$ .
- 308 These conditions are illustrated in Figure 4.

#### With population structure

We constructed an additional model in which partner association emerges from the population structure. We model a non-overlapping population colonizing a 2D grid of size 100-by-100, where each site is inhabited by one individual, similarly to Lewin-Epstein and Hadany (2020). Each individual is characterized by its phenotype which is either a cooperator, A, or a defector B. In each generation individuals interact with their neighbors, i.e. individuals that inhabit adjacent sites, in a prisoner's dilemma game (Table 1) and in horizontal cultural transmission. As before, T<sub>A</sub> and T<sub>B</sub> are the probabilities to transmit the phenotypes A and B during horizontal transmission. At each generation, each individual is chosen to "initiate" interactions with probability 1/2. Initiators then interact with a random neighbor for a prisoners' dilemma game and a random neighbor (with replacement) for horizontal cultural transmission (as both the game and the transmission are symmetrical, the expected number of each of these interactions per individual per generation is 1). Therefore, the effective partner association α in this model is the probability that the same neighbor is picked for both interactions, or

- 322  $\alpha = 1/m$ , where m is the number of neighbors. On an infinite grid, m = 8, but on a finite grid m can be lower in edge neighborhoods close to the grid border.
- The order of the interactions across the lattice on each generation is random. After all interactions take place, individual's fitness is determined by  $w = 1 + b \cdot n_b c \cdot n_c$ , where  $n_b$  is the number interactions of
- that individual with cooperative neighbors, and  $n_c$  is the total number of interactions of that individual  $(n_b \le n_c)$ . Then a new generation is generated. Each site is colonized by an offspring of one of
- the individuals that inhabit either this site or one of the neighboring sites. The parent is randomly drawn with probability proportional to its fitness, divided by the average fitness in his neighborhood.
- 330 Offspring then have the same phenotype as their parents.
- Figure 7 shows that the highest cooperation cost to benefit ratio (c/b) that permits the evolution of cooperation in simulations of the spatial model is roughly  $\alpha \cdot T/(1-T)$ , where  $T = T_A = T_B$  is the horizontal transmission rate. This agrees with the condition we derived in Corollary 2 for a population without population structure. This demonstrates that the partner association parameter  $\alpha$  can emerge

#### from local interactions between individuals in a structured population.

## 336 Discussion

- We studied the evolution of cooperation under non-vertical transmission using deterministic discrete-338 time evolutionary models with fitnesses in the form of payoffs from a prisoner's dilemma game. Under oblique and horizontal cultural transmission, a horizontal transmission bias for the cooperative
- 340 phenotype was found to be sufficient and necessary for evolution of cooperation (Result 1). Under a combination of vertical, oblique, and horizontal transmission, cooperation or defection can either fix
- or coexist at a stable polymorphism, depending on the relationship between the cost and benefit of cooperation, the horizontal bias, and the association between cooperation and transmission (Results 2
- and 3). Remarkably, stable coexistence between cooperation and defection can be maintained if horizontal transmission is biased for defection ( $T_B > T_A$ ) and both the cost of cooperation and social
- 346 association are intermediate (yellow areas in Figure 3).
  - We tested the applicability of our analytic results to a complex spatial stochastic model (Figure 7).
- Indeed, our derived condition provide a good approximation to simulation results, demonstrating that association between cooperation and transmission can arise in a structured population simply because
- 350 the choice of individuals for social interactions is small.
- Feldman et al. (1985) studied the dynamics of an altruistic phenotype with vertical cultural transmission and a gene that modifies the transmission of the phenotype. Their results are very sensitive to this genetic modification: without it, the conditions for invasion of the altruistic phenotype reduce to
- Hamilton's rule. Further work is needed to include such genetic modification of cultural transmission to our model.
- Woodcock (2006) has previously argued the significance of non-vertical transmission for the evolution of cooperation. He executed simulations with prisoner's dilemma payoffs but without horizontal
- transmission or social association ( $\alpha = 0$ ). Nevertheless, his results demonstrated that it is possible to sustain altruistic behavior via cultural transmission for a significant duration of time. Our results
- provide strong evidence for his hypothesis that horizontal transmission could have an important role in the evolution of cooperation.
- To understand the role of horizontal transmission, we first discuss the role of *assortment*. Eshel and Cavalli-Sforza (1982) showed that altruism can evolve when there is enough *assortative meeting*,
- namely, a tendency for individuals to interact within their phenotypic group. Fletcher and Doebeli (2009) have further argued that a general explanation for the evolution of altruism is given by *assort*-
- 366 *ment*: the correlation between individuals that carry an altruistic trait and the amount of altruistic

behavior in their interaction group. They therefore suggested that to explain the evolution of altruism,
we should seek mechanisms that generate such assortment, like population structure, repeated interactions, and individual recognition. Our results highlight another mechanism for generating assortment:
an association between social interactions and horizontal transmission that creates a correlation between one's partner for interaction and partner for transmission. This mechanism does not require
population structure, repeated interactions, or individual recognition. We show that high levels of such social association greatly increase the potential for evolution of cooperation (Figure 3). With enough
social association (α > (c(1 - T<sub>B</sub>) + (T<sub>B</sub> - T<sub>A</sub>))/bT<sub>A</sub>), cooperation can increase in frequency when initially rare even when there is horizontal transmission bias against it (T<sub>B</sub> > T<sub>A</sub>, see Result 2).

How does non-vertical transmission generate assortment? Lewin-Epstein et al. (2017) and Lewin-Epstein and Hadany (2020), who suggested that microbes that manipulate their hosts to act altruistically can be favored by selection, and may help explain the evolution of cooperation. From the kin selection point-of-view, if microbes can be transmitted *horizontally* from one host to another during host interactions, then following horizontal transmission the recipient host will carry microbes that are closely related to the microbes of the donor host, even when the two hosts are (genetically) unrelated.
However, we are more interested in the assortment point-of-view: infection by behavior-determining microbes during interactions effectively generates assortment because receipient of help may be infected by the behavior-determining microbe and therefore become a helper. Cultural horizontal transmission can similarly generate assortment between the cooperative phenotype and the benefit of cooperation if cultural transmission and helping interactions occur between the same individuals, which in our model occurs with probability α.

Thus, with horizontal transmission, "assortment between focal cooperative players and cooperative acts in their interaction environment" (Fletcher and Doebeli, 2009) is generated not because *the helper* is likely to be helped, but rather because the helped is likely to become a helper. These conclusions highlight the importance of non-vertical cultural transmission for explaining complex evolutionary phenomena, and furthers our understating of the cultural evolution of cooperation.

## Acknowledgements

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# 6 Appendices

# Appendix A

We want to find the frequency of juveniles with phenotype A in next generation  $\hat{p}'$  as a function of frequency of juveniles with phenotype A in the current generation  $\hat{p}$ . Starting from Eq. 6,

$$\hat{p}' = v\tilde{p}' + (1 - v)p', \tag{A1}$$

we substitute p' using Eq. 8 and  $\tilde{p}'$  using Eq. 11, we have

 $\hat{p}' = \frac{v}{\bar{w}} \left\{ \hat{p}^2 (1 + b - c) \left[ 1 - (1 - \hat{p})(1 - \alpha)T_B \right) \right] \right\}$  $+ \frac{v}{\bar{w}} \left\{ \hat{p} (1 - \hat{p})(1 - c) \left[ \hat{p} (1 - \alpha)T_B + 1 - T_B \right] \right\}$  $+ \frac{v}{\bar{w}} \left\{ \hat{p} (1 - \hat{p})(1 + b) \left[ \hat{p} (1 - \alpha) + \alpha \right] T_A \right\}$  $+ \frac{v}{\bar{w}} (1 - \hat{p})^2 \hat{p} (1 - \alpha)T_A$  $+ (1 - v) \hat{p}^2 (T_B - T_A) + (1 - v) \hat{p} (1 + T_A - T_B),$ (A2)

402

where  $\bar{w} = 1 + \hat{p}(b - c)$ . We define  $f(\hat{p})$  as

 $f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p}) \tag{A3}$ 

Using *SymPy* (Meurer et al., 2017), a Python library for symbolic mathematics, we simplify Eq. A3 to eqs. 32-33.

# Appendix B

Denote  $f(p) = \lambda(p' - p)$ , where  $\lambda > 0$ , and assume  $f(p^*) = 0$ ; i.e.,  $p^*$  is an equilibrium. We want a condition for  $|p' - p^*| < |p - p^*|$ .

410 If  $p > p^* = 0$ , we want a condition for p' < p, or  $\frac{p'}{p} < 1$ , or  $\lambda \frac{p'-p}{p} < 0$ , or  $\frac{f(p)}{p} < 0$ . Using a linear approximation for f(p) near 0, we have

 $\frac{p' 
<math display="block">f'(0) + O(p) < 0.$ (B1)

412

Therefore, by definition of big-O notation, if f'(0) < 0 then there exists  $\epsilon > 0$  such that for any 0 , it is guaranteed that <math>0 < p' < p, that is, p' is closer than p to zero.

If  $p < p^* = 1$ , we want a condition for 1 - p' < 1 - p, or  $\frac{1-p'}{1-p} < 1$ , or  $\lambda \frac{-(p'-p)}{1-p} < 0$ , or  $-\frac{f(p)}{1-p} < 0$ .

416 Using a linear approximation for f(p) near 1, we have

$$\frac{1 - p' < 1 - p \Leftrightarrow}{f'(1)(p - 1) + O((p - 1)^2)} < 0 \Leftrightarrow f'(1) - O(1 - p) < 0.$$
(B2)

Therefore, if f'(1) < 0 then there exists  $\epsilon > 0$  such that for any  $1 - \epsilon < 1 - p < 1$  it is guaranteed that 1 - p' < 1 - p, that is, p' is closer than p to one.

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# **Figures**

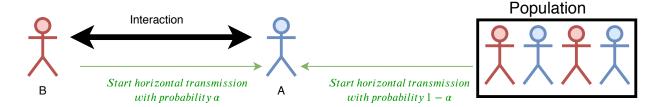


Figure 1: Cultural horizontal transmission with assortment. Transmission occurs between interacting partners with probability  $\alpha$  (left) or between two random peers with probability  $1 - \alpha$ .

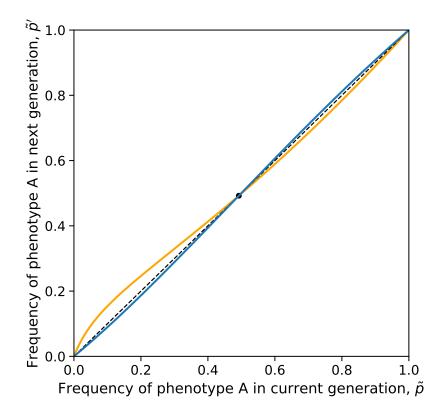
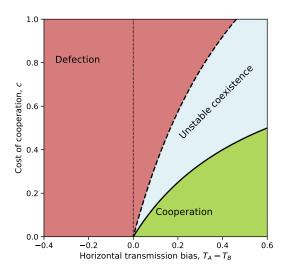
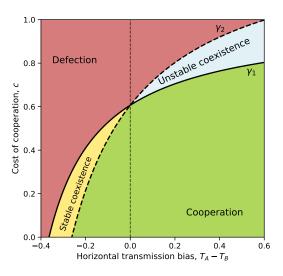


Figure 2: Stable and unstable coexistence between cooperation and defection without oblique transmission. The curves show the frequency of the cooperative phenotype A among parents in the next generation  $\tilde{p}'$  vs. the current generation  $\tilde{p}$  (Eq. 14). The dashed black line is  $\tilde{p}' = \tilde{p}$ . The curves and the dashed line intersect at the polymorphic equilibrium  $\tilde{p}^*$  (black circle). When the curves are above the dashed line,  $\tilde{p} > \tilde{p}$ , then  $\tilde{p}$  increase. When the curves are below the dashed line,  $\tilde{p} < \tilde{p}$ , then  $\tilde{p}$  decreases. The orange curve, for which the polymorphic equilibrium is stable, is given by  $T_A = 0.4$ ,  $T_B = 0.9$ , and  $t_B = 0.9$ ,  $t_B = 0.9$ ,  $t_B = 0.9$ ,  $t_B = 0.9$ , and  $t_B = 0.9$ , which give  $t_B = 0.9$ . In both cases there is no oblique transmission,  $t_B = 0.9$ , see Figure 5 for  $t_B = 0.9$ .





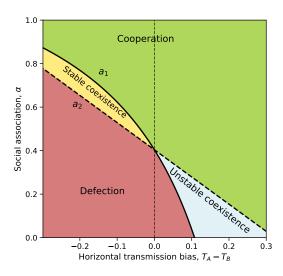


Figure 3: Evolution of cooperation under vertical and horizontal cultural transmission. The figure shows the global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable coexistence (blue), and stable coexistence of cooperation and defection (yellow). In all cases the horizontal bias  $(T_A - T_B)$  is on the x-axis. (a-b) the cost of cooperation c is on the y-axis; the cost boundaries  $\gamma_1$  and  $\gamma_2$  (Eq. 23) are the solid and dashed lines. (c) the social association  $\alpha$  is on the y-axis; the social association boundaries  $a_1$  and  $a_2$  (Eq. 30) are the folid and dashed lines. Here, b = 1.3,  $T_A = 0.4$ . (a)  $\alpha = 0.(b)$   $\alpha = 0.7$ . (c) c = 0.35.

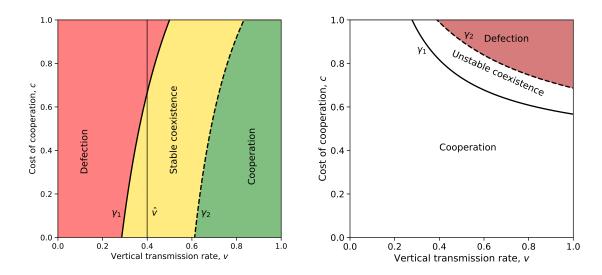


Figure 4: Evolution of cooperation under vertical, oblique and horizontal cultural transmission. The figure shows the global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable coexistence (blue), and stable coexistence of cooperation and defection (yellow). In (a) the horizontal bias  $T_A - T_B$  is negative, in (b) the horizontal bias is positive. The vertical transmission rate v is on the x-axis; the cost boundaries  $\hat{\gamma}_1$  and  $\hat{\gamma}_2$  (Eq. 40) are the solid and dashed lines. In (a), b = 2,  $T_A = 0.5$ ,  $T_B = 0.7$ ,  $\alpha = 0.7$  and (b) b = 1.2,  $T_A = 0.5$ ,  $T_B = 0.4$ .

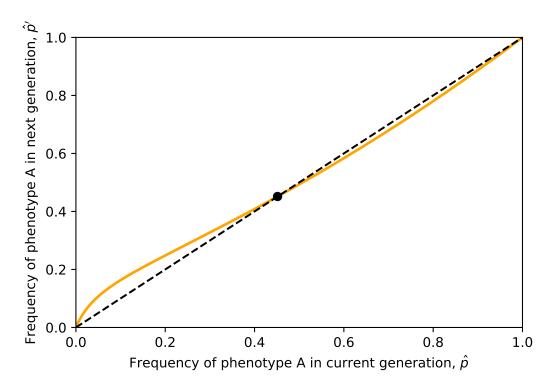
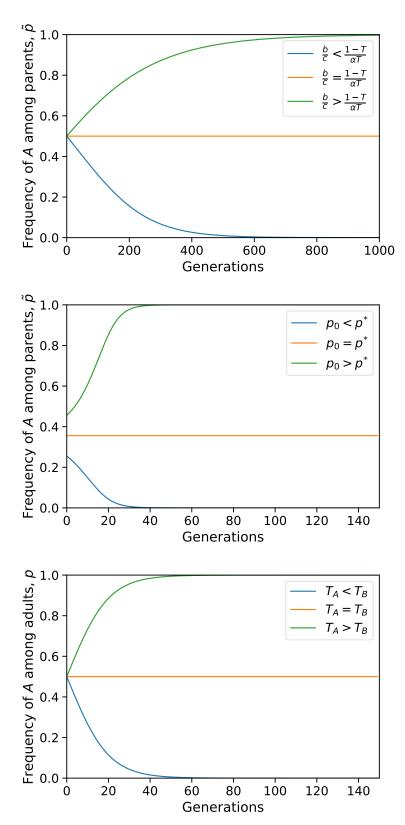
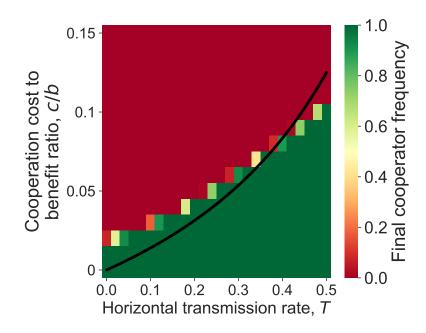


Figure 5: Stable coexistence between cooperation and defection with oblique transmission. The curve shows the frequency of the cooperative phenotype A among juveniles in the next generation  $\hat{p}'$  vs. the current generation  $\hat{p}$  (Eq. 6). The dashed black line is  $\hat{p}' = \hat{p}$ . The curve and the dashed line intersect at the stable equilibrium  $\hat{p}^*$  (black circle). When  $\hat{p} < \hat{p}^*$  then the curve is above the dashed line,  $\hat{p}' > \hat{p}$ , and  $\hat{p}$  increases towards  $\hat{p}^*$ . When  $\hat{p} > \hat{p}^*$  then the curve is below the dashed line,  $\hat{p}' < \hat{p}$ , and  $\hat{p}$  decreases towards  $\hat{p}^*$ . Here,  $T_A = 0.4$ ,  $T_B = 0.9$ , b = 20, c = 0.1,  $\alpha = 1$ , and v = 0.4, which give  $0 < \beta_3 < \beta_1$  (Eq. 33).



**Figure 6: Dynamics of the frequency of cooperation.** The frequency  $\tilde{p}$  of parents with cooperative phenotype A in (**a-b**) and the frequency p of adults with cooperative phenotype A in (**c**). The different lines correspond to parameter values that lead to fixation of cooperation (green), extinction of cooperation (red), or stable coexistence of cooperators and defectors (yellow). (**a**) v = 1,  $T_A = T_B = T = 0.2$ ,  $\alpha = 0.5 \neq 0$ ,  $\tilde{p}_0 = 0.5$  and c = 0.1; (**b**) v = 1,  $\alpha = 0$ ,  $\tilde{p}^* \approx 0.35$ ,  $T_A = 0.65$ ,  $T_B = 0.1$ , t = 0.1, and t = 0.65; (**c**) t = 0.1, t = 0



**Figure 7: Evolution of cooperation in a spatial model.** The expected frequency of cooperators in a structured population after 10,000 generations is shown (red for 0%, green for 100%) as function of both the ratio between the cost and benefit of cooperation (c/b) on the y-axis, and the horizontal transmission rate (without transmission bias,  $T = T_A = T_B$ ) on the x-axis. The population evolves on a 100-by-100 grid. Selection, cooperation, and horizontal cultural transmission are all local between adjacent sites. The black curve represents the condition for the evolution of cooperation in a well-mixed population with partner association,  $c/b < \alpha T/(1-T)$ , where  $\alpha = 1/8$ ; see Eq. 25. Note that in the structured population, selection is local, whereas in the unstructured population, selection is global. This can explain the small difference in the results. Here, population size is 10,000 (100-by-100 grid); cost of cooperation, c = 0.05. 50 simulations were executed per parameter set. Simulations were stopped at generation 10,000 or if one of the phenotypes fixed.