

# Non-Vertical Cultural Transmission, Assortment, and the Evolution of Cooperation

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## Abstract

Cultural evolution of cooperation under vertical and non-vertical cultural transmission is studied, and conditions are found for fixation and coexistence of cooperation and defection. The evolution of cooperation is facilitated by horizontal transmission and by an association between social interactions and horizontal transmission. The effect of oblique transmission depends on the horizontal transmission bias. Stable polymorphism of cooperation and defection can occur, and when it does, reduced association between social interactions and horizontal transmission evolves, which leads to a decreased frequency of cooperation and lower population mean fitness. The deterministic conditions are compared to outcomes of stochastic simulations of structured populations. Parallels are drawn with Hamilton's rule incorporating assortment and effective relatedness.

## 22 Introduction

Cooperative behavior can reduce an individual's fitness and increase the fitness of its conspecifics or competitors [2]. Nevertheless, cooperative behavior appears to occur in many animals [5], including humans, primates [13], rats [24], birds [15, 27], and lizards [26]. Evolution of cooperative behavior has been an important focus of research in evolutionary theory since at least the 1930s [11, Appendix].

Since the work of Hamilton [12] and Axelrod & Hamilton [2], theories for the evolution of cooperative and altruistic behaviors have been intertwined often under the rubric of *kin selection*. Kin selection theory posits that natural selection is more likely to favor cooperation between more closely related individuals. The importance of *relatedness* to the evolution of cooperation and altruism was demonstrated by Hamilton [12], who showed that an allele that determines cooperative behavior will increase in frequency if the reproductive cost to the actor that cooperates,  $c$ , is less than the benefit to the recipient,  $b$ , times the relatedness,  $r$ , between the recipient and the actor. This condition is known as *Hamilton's rule*:

$$c < b \cdot r, \quad (1)$$

where the relatedness coefficient  $r$  measures the probability that an allele sampled from the cooperator is identical by descent to one at the same locus in the recipient.

Eshel & Cavalli-Sforza [6] studied a related model for the evolution of cooperative behavior. Their model included *assortative meeting*, or non-random encounters, where a fraction  $m$  of individuals in the population each interact specifically with an individual of the same phenotype, and a fraction  $1 - m$  interacts with a randomly chosen individual. Such assortative meeting may be due, for example, to population structure or active partner choice. In their model, cooperative behavior can evolve if [6, eq. 3.2]

$$c < b \cdot m, \quad (2)$$

where  $b$  and  $c$  are the benefit and cost of cooperation<sup>1</sup>.

The role of assortment in the evolution of altruism was emphasized by Fletcher & Doebeli [9]. They found that in a *public-goods* game, altruism will evolve if cooperative individuals experience more cooperation, on average, than defecting individuals, and “thus, the evolution of altruism requires (positive) assortment between focal *cooperative* players and cooperative acts in their interaction environment.” With some change in parameters, this condition is summarized by [9, eq. 2.3]

$$c < b \cdot (p_C - p_D), \quad (3)$$

where  $p_C$  is the probability that a cooperator receives help, and  $p_D$  is the probability that a defector receives help.<sup>2</sup> Bijma & Aanen [3] obtained a result related to inequality 3 for other types of games.

Cooperative behavior can be subject to *cultural transmission*, which allows an individual to acquire attitudes or behavioral traits from other individuals in its social group through imitation, learning, or other modes of communication [4, 25]. Feldman *et al.* [8] introduced the first model for the evolution of altruism by cultural transmission with kin selection and demonstrated that if the fidelity of cultural transmission of altruism is  $\varphi$ , then the condition for evolution of altruism in the case of sib-to-sib altruism is [8, Eq. 16]

$$c < b \cdot \varphi - \frac{1 - \varphi}{\varphi}. \quad (4)$$

<sup>1</sup>In an extended model, which allows an individual to encounter  $N$  individuals before choosing a partner, the right hand side is multiplied by  $E[N]$ , the expected number of encounters [6, eq. 4.6].

<sup>2</sup>Inequality 3 generalizes inequalities 1 and 2 by substituting  $p_C = r + p$ ,  $p_D = p$  and  $p_C = m + (1 - m)p$ ,  $p_D = (1 - m)p$ , respectively, where  $p$  is the frequency of cooperators.

In inequality 4,  $\varphi$  takes the role of relatedness ( $r$  in inequality 1) or assortment ( $m$  in inequality 2), but the effective benefit  $b \cdot \varphi$  is reduced by  $(1 - \varphi)/\varphi$ . This shows that under a cultural transmission, the condition for the evolutionary success of altruism entails a modification of Hamilton's rule (inequality 1).

Cultural transmission may be modeled as vertical, horizontal, or oblique: vertical transmission occurs between parents and offspring, horizontal transmission occurs between individuals from the same generation, and oblique transmission occurs to offspring from the generation to which their parents belong (i.e. from non-parental adults). Evolution under either of these transmission models can be more rapid than under pure vertical transmission [4, 21, 23]. Both Woodcock [28] and Lewin-Epstein *et al.* [16] demonstrated that non-vertical transmission can help explain the evolution of cooperative behavior, the former using simulations with cultural transmission, the latter using a model where cooperation is mediated by host-associated microbes. Indeed, models in which microbes affect their host's behavior [10, 16, 17] are mathematically similar to models of cultural transmission, and they also emphasize the role of non-vertical transmission [4].

Here, we study models for the cultural evolution of cooperation that include both vertical and non-vertical transmission. In our models behavioral changes are mediated by cultural transmission that can occur specifically during social interactions. For instance, there may be an association between the choice of partner for social interaction and the choice of partner for cultural transmission, or when an individual interacts with an individual of a different phenotype, exposure to the latter may lead the former to convert its phenotype. Our results demonstrate that cultural transmission, when associated with social interactions, can enhance the evolution of cooperation even when genetic transmission cannot, partly because it can facilitate the generation of assortment [9], and partly because it can diminish the effect of natural selection [23]. This further emphasizes that treatment of cooperation as a cultural trait, rather than a genetic one, can lead to a broader understanding of its evolutionary dynamics.

## Models

Consider a large population whose members can be one of two phenotypes:  $\phi = A$  for cooperators or  $\phi = B$  for defectors. An offspring inherits its phenotype from its parent via vertical transmission with probability  $v$  or from a random individual in the parental population via oblique transmission with probability  $(1 - v)$ . Following Ram *et al.* [23], given that the parent's phenotype is  $\phi$  and assuming uni-parental inheritance [29], the conditional probability that the phenotype  $\phi'$  of the offspring is  $A$  is

$$P(\phi' = A \mid \phi) = \begin{cases} v + (1 - v)p, & \text{if } \phi = A \\ (1 - v)p, & \text{if } \phi = B \end{cases}, \quad (5)$$

where  $p = P(\phi = A)$  is the frequency of  $A$  among all adults in the parental generation.

Not all adults become parents, and we denote the frequency of phenotype  $A$  among parents by  $\tilde{p}$ . Therefore, the frequency  $\hat{p}$  of phenotype  $A$  among juveniles (after selection and vertical and oblique transmission) is

$$\hat{p} = \tilde{p}[v + (1 - v)p] + (1 - \tilde{p})[(1 - v)p] = v\tilde{p} + (1 - v)p. \quad (6)$$

Individuals are assumed to interact according to a *prisoner's dilemma*. Specifically, individuals interact in pairs; a cooperator suffers a fitness cost  $0 < c < 1$ , and its partner gains a fitness benefit

102  $b$ , where we assume  $c < b$ . Table 1 shows the payoff matrix, i.e. the fitness of an individual with phenotype  $\phi_1$  when interacting with a partner of phenotype  $\phi_2$ .

104 Social interactions occur randomly: two juvenile individuals with phenotype  $A$  interact with probability  $\hat{p}^2$ , two juveniles with phenotype  $B$  interact with probability  $(1 - \hat{p})^2$ , and two juveniles with  
 106 different phenotypes interact with probability  $2\hat{p}(1 - \hat{p})$ . Horizontal cultural transmission occurs between pairs of individuals from the same generation. It occurs between socially interacting partners  
 108 with probability  $\alpha$ , or between a random pair with probability  $1 - \alpha$  (see Figure 1). However, horizontal transmission is not always successful, as one partner may reject the other's phenotype. The  
 110 probability of successful horizontal transmission of phenotypes  $A$  and  $B$  are  $T_A$  and  $T_B$ , respectively (Table 2). Then, the frequency  $p'$  of phenotype  $A$  among adults in the next generation, after horizontal  
 112 transmission, is

$$\begin{aligned} p' = & \hat{p}^2 [\alpha + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & \hat{p}(1 - \hat{p}) [\alpha(1 - T_B) + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & (1 - \hat{p})\hat{p} [\alpha T_A + (1 - \alpha)\hat{p} T_A] + \\ & (1 - \hat{p})^2 [(1 - \alpha)\hat{p} T_A] , \end{aligned} \quad (7)$$

114 which simplifies to

$$p' = \hat{p}^2(T_B - T_A) + \hat{p}(1 + T_A - T_B) . \quad (8)$$

116 The frequency of  $A$  among parents (i.e. after selection) follows a similar dynamic, but also includes the effect of natural selection, and is therefore

$$\begin{aligned} \bar{w}\tilde{p}' = & \hat{p}^2(1 + b - c) [\alpha + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & \hat{p}(1 - \hat{p})(1 - c) [\alpha(1 - T_B) + (1 - \alpha)(\hat{p} + (1 - \hat{p})(1 - T_B))] + \\ & (1 - \hat{p})\hat{p}(1 + b) [\alpha T_A + (1 - \alpha)\hat{p} T_A] + \\ & (1 - \hat{p})^2 [(1 - \alpha)\hat{p} T_A] , \end{aligned} \quad (9)$$

where fitness values are taken from Table 1 and Table 2, and the population mean fitness is  $\bar{w} = 1 + \hat{p}(b - c)$ . Eq. 9 can be simplified to

$$\begin{aligned} \bar{w}\tilde{p}' = & \hat{p}^2(1 + b - c) [1 - (1 - \hat{p})(1 - \alpha)T_B] + \\ & \hat{p}(1 - \hat{p})(1 - c) [\hat{p}(1 - \alpha)T_B + 1 - T_B] + \\ & (1 - \hat{p})\hat{p}(1 + b) [\hat{p}(1 - \alpha) + \alpha] T_A + \\ & (1 - \hat{p})^2 \hat{p}(1 - \alpha) T_A . \end{aligned} \quad (10)$$

122 Starting from Eq. 6 with  $\hat{p}' = v\tilde{p}' + (1 - v)p'$ , we substitute  $p'$  from Eq. 8 and  $\tilde{p}'$  from Eq. 10 and obtain

$$\begin{aligned} \hat{p}' = & \frac{v}{\bar{w}} \left[ \hat{p}^2(1 + b - c) (1 - (1 - \hat{p})(1 - \alpha)T_B) \right] + \\ & \frac{v}{\bar{w}} \left[ \hat{p}(1 - \hat{p})(1 - c) (\hat{p}(1 - \alpha)T_B + 1 - T_B) \right] + \\ & \frac{v}{\bar{w}} \left[ \hat{p}(1 - \hat{p})(1 + b) (\hat{p}(1 - \alpha) + \alpha) T_A \right] + \\ & \frac{v}{\bar{w}} (1 - \hat{p})^2 \hat{p}(1 - \alpha) T_A + \\ & (1 - v) \hat{p}^2 (T_B - T_A) + \\ & (1 - v) \hat{p} (1 + T_A - T_B) . \end{aligned} \quad (11)$$

Table 3 lists the model variables and parameters.

## 126 Results

128 In the following sections, we determine the equilibria of the model in Eq. 11, namely, solutions of  $\hat{p}' = \hat{p}$ , and analyze their local stability. We then analyze the evolution of a modifier of social association. Finally, we compare derived conditions to outcomes of stochastic simulations with a structured population.

### Evolution of cooperation

132 The fixed points (equilibria) of the recursion (Eq. 11) are  $\hat{p} = 0$ ,  $\hat{p} = 1$ , and (see Eq. B5)

$$\hat{p}^* = \frac{\alpha b v T_A - c v (1 - T_B) + (T_A - T_B)}{[c(1 - v) - b(1 - \alpha v)](T_A - T_B)}. \quad (12)$$

134 Define the following cost thresholds,  $\gamma_1$  and  $\gamma_2$ , and the vertical transmission threshold,  $\hat{v}$ ,

$$\gamma_1 = \frac{b v \alpha T_A + (T_A - T_B)}{v(1 - T_B)}, \quad \gamma_2 = \frac{b v \alpha T_B + (1 + b)(T_A - T_B)}{v(1 - T_B) + (1 - v)(T_A - T_B)}, \quad \hat{v} = \frac{T_B - T_A}{1 - T_A}. \quad (13)$$

136 Then we have the following result.

138 **Result 1** (Equilibria and stability). *With vertical, horizontal, and oblique transmission, the cultural evolution of a cooperation follows one of the following scenarios in terms of the cost thresholds  $\gamma_1$  and  $\gamma_2$  and the vertical transmission threshold  $\hat{v}$  (Eq. 13):*

1. Fixation of cooperation: if (i)  $T_A \geq T_B$  and  $c < \gamma_1$ ; or if (ii)  $T_A < T_B$  and  $v > \hat{v}$  and  $c < \gamma_2$ .
- 142 2. Fixation of defection: if (iii)  $T_A \geq T_B$  and  $\gamma_2 < c$ ; or if (iv)  $T_A < T_B$  and  $\gamma_1 < c$ .
3. Stable polymorphism: if (v)  $T_A < T_B$  and  $v < \hat{v}$  and  $c < \gamma_1$ ; or if (vi)  $T_A < T_B$  and  $v > \hat{v}$  and  $\gamma_2 < c < \gamma_1$ .
- 144 4. Unstable polymorphism: if (vii)  $T_A > T_B$  and  $\gamma_1 < c < \gamma_2$ .

146 These conditions are illustrated in Figures 2a, 2b, 3a, and 3b, and the full analysis is in Appendix B.

148 Much of the literature on evolution of cooperation focuses on conditions for an initially rare cooperative phenotype to invade a population of defectors. The following remarks address this condition.

150

**Remark 1** (Condition on  $c$  for cooperation to increase when rare, i.e.,  $\hat{p}' > p$  near  $p = 0$ ). *If the initial frequency of cooperation is very close to zero, then its frequency will increase if the cost of cooperation is low enough,*

$$154 \quad c < \gamma_1 = \frac{b v \alpha T_A + (T_A - T_B)}{v(1 - T_B)}. \quad (14)$$

This unites the conditions for fixation of cooperation and for stable polymorphism, both of which entail instability of the state where defection is fixed,  $\hat{p} = 0$ .

Importantly, increasing social association  $\alpha$  increases the cost threshold ( $\partial \gamma_1 / \partial \alpha > 0$ ), making it easier for cooperation to increase from rarity. Similarly, increasing the horizontal transmission of cooperation,  $T_A$ , increases the threshold ( $\partial \gamma_1 / \partial T_A > 0$ ), facilitating the evolution of cooperation ((Figure 3a and 3b). However, increasing the horizontal transmission of defection,  $T_B$ , can increase or

decrease the cost threshold, but it increases the cost threshold when the threshold is already above one  
 162 ( $c < 1 < \gamma_1$ ):  $\partial\gamma_1/\partial T_B$  is positive when  $T_A > \frac{1}{1+\alpha bv}$ , which gives  $\gamma_1 > 1/v$ . Therefore, increasing  $T_B$   
 decreases the cost threshold and limits the evolution of cooperation, but only if  $T_A < \frac{1}{1+\alpha bv}$ .

164 Increasing the vertical transmission rate,  $v$ , can either increase or decrease the cost threshold, depending  
 on the horizontal transmission bias,  $T_A - T_B$ , because  $\text{sign}(\partial\gamma_1/\partial v) = -\text{sign}(T_A - T_B)$ . When  $T_A < T_B$   
 166 we have  $\partial\gamma_1/\partial v > 0$ , and as the vertical transmission rate increases, the cost threshold increases,  
 making it easier for cooperation to increase when rare (Figure 2b). In contrast, when  $T_A > T_B$  we get  
 168  $\partial\gamma_1/\partial v < 0$ , and therefore as the vertical transmission rate increases, the cost threshold decreases,  
 making it harder for cooperation to increase when rare (Figure 2a).

170 In general, this condition cannot be formulated in the form of Hamilton's rule due to the bias in  
 horizontal transmission, represented by  $T_A - T_B$ . When there is no horizontal transmission bias,  
 172  $T_A = T_B$ , the following applies.

From Result 1 and inequality 14, if horizontal transmission is unbiased,  $T = T_A = T_B$ , then cooperation  
 174 will take over the population from any initial frequency if the cost is low enough,

$$c < b \cdot \frac{\alpha T}{1 - T}, \quad (15)$$

176 and regardless of the vertical transmission rate,  $v$ . This condition can be interpreted as a version of  
 Hamilton's rule ( $c < b \cdot r$ , inequality 1) or as a version of inequality 3, where  $\alpha T/(1 - T)$  can be  
 178 regarded as the *effective relatedness* or *effective assortment*, respectively. Figure S2a illustrates this  
 condition. Note that the right-hand side of inequality 15 equals  $\gamma_1$  when  $T = T_A = T_B$ .

180 From inequality 14, without social association ( $\alpha = 0$ ), cooperation will increase when it is rare if  
 there is horizontal transmission bias for cooperation,  $T_A > T_B$ , and

$$182 \quad c < \frac{T_A - T_B}{v(1 - T_B)}. \quad (16)$$

Figure 3a illustrates this condition (for  $v = 1$ ), which is obtained by setting  $\alpha = 0$  in inequality 14.  
 184 Importantly, the benefit of cooperation,  $b$ , does not affect the evolution of cooperation in the absence of  
 social association, and the outcome is determined only by cultural transmission. Further, inequality 14  
 186 shows that with perfect social association ( $\alpha = 1$ ), cooperation will increase when rare if

$$c < \frac{bvT_A + (T_A - T_B)}{v(1 - T_B)}. \quad (17)$$

188 In the absence of oblique transmission,  $v = 1$ , the only equilibria are the fixation states,  $\tilde{p} = 0$  and  
 $\tilde{p} = 1$ , and cooperation will evolve from any initial frequency (i.e.,  $\tilde{p}' > \tilde{p}$ ) if inequality 17 applies  
 190 (Figure 3). This is similar to case of microbe-induced cooperation studied by Lewin-Epstein *et al.*  
 [16]; therefore when  $v = 1$ , this remark is equivalent to their eq. 1.

192 It is interesting to examine the general effect of social association  $\alpha$  on the evolution of cooperation.  
 Define the social association thresholds,  $a_1$  and  $a_2$ , as

$$194 \quad a_1 = \frac{c \cdot v(1 - T_A) - (T_A - T_B)(1 + b - c)}{b \cdot v \cdot T_B}, \quad a_2 = \frac{c \cdot v(1 - T_B) - (T_A - T_B)}{b \cdot v \cdot T_A}. \quad (18)$$

**Remark 2** (Condition on social association  $\alpha$  for cooperation to increase when it is rare). Cooperation  
 196 will increase when rare if social association is high enough, specifically if  $a_2 < \alpha$ .

Figures 2c and 2d illustrate this condition. With horizontal transmission bias for cooperation,  $T_A > T_B$ , cooperation can fix from any initial frequency if  $a_2 < \alpha$  (green area in the figures). With horizontal bias favoring defection,  $T_A < T_B$ , cooperation can fix from any frequency if social association is high,  $a_1 < \alpha$  (green area with  $T_A < T_B$ ), and can also increase when rare and reach stable polymorphism if social association is intermediate,  $a_2 < \alpha < a_1$  (yellow area). Without horizontal bias,  $T_A = T_B$ , fixation of cooperation occurs if social association is high enough,  $\frac{c}{b-v} \cdot \frac{1-T}{T} < \alpha$  (inequality 15; in this case  $a_1 = a_2$ ).

Interestingly, because  $\text{sign}(\partial a_2 / \partial v) = \text{sign}(T_A - T_B)$ , the effect of the vertical transmission rate  $v$  on  $a_1$  and  $a_2$  depends on the horizontal transmission bias. That is, with horizontal bias for cooperation,  $T_A > T_B$ , evolution of cooperation is facilitated by oblique transmission, whereas with horizontal bias for defection,  $T_A < T_B$ , evolution of cooperation is facilitated by vertical transmission. This is demonstrated in Figures 2c and 2d.

Next, we look at the roles of vertical and oblique transmission in the evolution of cooperation. Fixation of cooperation is possible only if the vertical transmission rate is high enough,

$$v > \hat{v} = \frac{T_B - T_A}{1 - T_A} . \quad (19)$$

This condition is necessary for fixation of cooperation, but it is not sufficient. If horizontal transmission is biased for cooperation,  $T_A > T_B$ , cooperation can fix with any vertical transmission rate (because  $\hat{v} < 0$ ). In contrast, if horizontal transmission is biased for defection,  $T_A < T_B$ , cooperation can fix only if the vertical transmission rate is high enough: in this case oblique transmission can prevent fixation of cooperation (see Figures 2b and 2d).

With only vertical transmission ( $v = 1$ ), inequality 14 entails that cooperation will increase when rare if

$$c < \frac{b\alpha T_A + (T_A - T_B)}{1 - T_B} , \quad (20)$$

which can also be written as

$$\frac{c(1 - T_B) - (T_A - T_B)}{bT_A} < \alpha . \quad (21)$$

In the absence of vertical transmission ( $v = 0$ ), from recursion 11 we see that the frequency of the cooperator phenotype among adults increases every generation, i.e.  $p' > p$ , if there is a horizontal transmission bias in favor of cooperation, namely  $T_A > T_B$ . That is, in the absence of vertical transmission, selection plays no role in the evolution of cooperation (i.e.,  $b$  and  $c$  do not affect  $\hat{p}'$ ). The dynamics are determined solely by differential horizontal transmission of the two phenotypes, namely, the relative tendency of each phenotype to be horizontally transmitted to peers. With no bias in horizontal transmission,  $T_A = T_B$ , phenotype frequencies do not change,  $\hat{p}' = \hat{p}$ .

Cooperation and defection can coexist at frequencies  $\hat{p}^*$  and  $1 - \hat{p}^*$  (Eq. 12). When it is feasible, this equilibrium is stable or unstable under the conditions of Result 1, parts 3 and 4, respectively. The yellow and blue areas in Figures 3 and 2 show cases of stable and unstable polymorphism, respectively. When  $\hat{p}^*$  is unstable, cooperation will fix if its initial frequency is  $\hat{p} > \hat{p}^*$ , and defection will fix if  $\hat{p} < \hat{p}^*$ ; this occurs when there is horizontal transmission bias for cooperation,  $T_A > T_B$ , and the cost is intermediate,  $\gamma_1 < c < \gamma_2$ . Figure S1 shows the mapping  $\hat{p} \rightarrow \hat{p}' - \hat{p}$ .

## Evolution of social association

We now focus on the evolution of social association under perfect vertical transmission,  $v = 1$ , assuming that the population is initially at a stable polymorphism of the two phenotypes, cooperation

240  $A$  and defection  $B$ , where the frequency of  $A$  among juveniles is  $\hat{p}^*$  (Eq. 12). Note that for a stable  
 polymorphism, there must be horizontal bias for defection,  $T_A < T_B$ , and an intermediate cost of  
 242 cooperation,  $\gamma_2 < c < \gamma_1$  (Eq. 13), see Figure 3b. The equilibrium population mean fitness is  
 $\bar{w}^* = 1 + \hat{p}^*(b - c)$ , which is increasing in  $\hat{p}^*$ , and  $\hat{p}^*$  is increasing in  $\alpha$  (Appendix C). Therefore, if  
 social association increases, the population mean fitness also increases. But can an allele that increases  
 244 social association evolve?

To answer this question, we extend our model to include a “modifier locus” [7, 18, 19, 20] that de-  
 246 termines social association, but has no direct effect on fitness. The modifier locus has two alleles,  
 $M$  and  $m$ , which induce social associations  $\alpha_1$  and  $\alpha_2$ , respectively. Suppose that the population has  
 248 evolved to a stable equilibrium  $\hat{p}^*$  when only allele  $M$  is present. We study the local stability of this  
 equilibrium to invasion by the modifier allele  $m$ ; this is called “external stability” [1, 20] and obtain  
 250 the following result.

252 **Result 2** (Reduction principle for social association). *From a stable polymorphism between coopera-*  
*tion and defection, a modifier allele can successfully invade the population if it decreases the social*  
 254 *association  $\alpha$ .*

The full analysis is in Appendix D. Note that this reduction principle entails that successful invasions  
 256 will reduce the frequency of cooperation, as well as the population mean fitness (Figure 4). Fur-  
 thermore, if we assume that modifier alleles with decreased social association appear and invade the  
 258 population from time to time, then social association will continue to decrease, further reducing the  
 frequency of cooperation and the population mean fitness. This evolution will proceed as long as  
 260 there is a stable polymorphism, that is, as long as  $a_2 < \alpha < a_1$  (Remark 2, Figure 3c). Thus, we can  
 expect social association to eventually approach  $a_2$ , the frequency of cooperation to fall to zero, and  
 262 the population mean fitness to decrease to one (Figure 4).

## Population structure

264 Social association may also emerge from population structure. Consider a population colonizing a  
 two-dimensional grid of size 100-by-100, where each site is inhabited by one individual, similarly to  
 266 the model of Lewin-Epstein & Hadany [17]. Each individual is characterized by its phenotype: either  
 cooperator,  $A$ , or defector,  $B$ . Initially, each site in the grid is randomly colonized by either a cooperator  
 268 or a defector, with equal probability. In each generation, half of the individuals are randomly chosen  
 to “initiate” interactions, and these initiators interact with a random neighbor (i.e. individual in a  
 270 neighboring site) in a prisoners’ dilemma game (Table 1) and a random neighbor (with replacement)  
 for horizontal cultural transmission (Figure 1). The expected number of each of these interactions per  
 272 individual per generation is one. The effective social association  $\alpha$  in this model is the probability that  
 the same neighbor is picked for both interactions, or  $\alpha = 1/m$ , where  $m$  is the number of neighbors.  
 274 On an infinite grid,  $m = 8$ , but on a finite grid  $m$  can be lower in edge neighborhoods close to the grid  
 border. As before,  $T_A$  and  $T_B$  are the probabilities of successful horizontal transmission of phenotypes  
 276  $A$  and  $B$ , respectively.

The order of the interactions across the grid at each generation is random. After all interactions take  
 278 place, an individual’s fitness is determined by  $w = 1 + b \cdot n_b - c \cdot n_c$ , where  $n_b$  is the number of interactions  
 that individual had with cooperative neighbors, and  $n_c$  is the number of interactions in which that  
 280 individual cooperated (note that the phenotype may change between consecutive interactions due to  
 horizontal transmission). Then, a new generation is produced, and the sites can be settled by offspring  
 282 of any parent, not just the neighboring parents. Selection is global, rather than local, in accordance  
 with our deterministic model: The parent is randomly drawn with probability proportional to its



284 fitness, divided by the sum of the fitness values of all potential parents. Offspring are assumed to have the same phenotype as their parents (i.e.  $v = 1$ ).

286 The outcomes of stochastic simulations with such a structured population are shown in Figure 5, which demonstrates that the highest cost of cooperation  $c$  that permits the evolution of cooperation agrees

288 with the conditions derived above for our model without population structure or stochasticity. An example of stochastic stable polymorphism is shown in Figure 5c. Changing the simulation so that

290 selection is local (i.e., sites can only be settled by offspring of neighboring parents) had only a minor effect on the agreement with the derived conditions (Figure S3).

292 These comparisons between the deterministic unstructured model and the stochastic structured model show that the conditions derived for the deterministic model can be useful for predicting the dynamics

294 under complex scenarios. Moreover, this structured population model demonstrates that our parameter for social association ( $\alpha$ ) can represent local interactions between individuals.

## 296 Discussion

Under a combination of vertical, oblique, and horizontal transmission with payoffs in the form

298 of a prisoner's dilemma game, cooperation or defection can either fix or coexist, depending on the relationship between the cost and benefit of cooperation, the horizontal transmission bias, and

300 the association between social interaction and horizontal transmission (Result 1, Figures 2 and 3). Importantly, cooperation can increase when initially rare (i.e. invade a population of defectors) if and

302 only if, rewriting inequality 14,

$$c \cdot v(1 - T_B) < b \cdot v\alpha T_A + (T_A - T_B), \quad (22)$$

304 namely, the effective cost of cooperation (left-hand side) is smaller than the effective benefit plus the horizontal transmission bias (right-hand side). This condition cannot be formulated in the form of

306 Hamilton's rule,  $c < b \cdot r$ , due to the effect of biased horizontal transmission, represented by  $(T_A - T_B)$ . Remarkably, a polymorphism of cooperation and defection can be stable if horizontal transmission

308 is biased in favor of defection ( $T_A < T_B$ ) and both the cost of cooperation and social association are intermediate (yellow areas in Figures 2 and 3).

310 We find that stronger social association  $\alpha$  leads to evolution of higher frequency of cooperation and increased population mean fitness. Nevertheless, when cooperation and defection coexist, social

312 association is expected to be reduced by natural selection, leading to extinction of cooperation and decreased population mean fitness (Result 2, Figure 4). Without social association, the benefit of

314 cooperation cannot facilitate its evolution, and cooperation can only succeed if horizontal transmission is biased in its favor.

316 Indeed, in our model, horizontal transmission plays a major role in the evolution of cooperation: increasing the transmission of cooperation,  $T_A$ , or decreasing the transmission of defection,  $T_B$ , facilitates

318 the evolution of cooperation. However, the effect of oblique transmission is more complicated. When there is horizontal transmission bias in favor of cooperation,  $T_A > T_B$ , increasing the rate of oblique

320 transmission,  $1 - v$ , will facilitate the evolution of cooperation. In contrast, when the bias is in favor of defection,  $T_A < T_B$ , higher rates of vertical transmission,  $v$ , are advantageous for cooperation, and the

322 rate of vertical transmission must be high enough ( $v > \hat{v}$ ) for cooperation to fix in the population.

The conditions derived from our deterministic model provide a good approximation to outcomes of

324 simulations of a complex stochastic model with population structure in which individuals can only interact with and transmit to their neighbors. In these structured populations social association arises

326 due to both social interactions and horizontal cultural transmission being local (Figure 5).

Feldman *et al.* [8] studied the dynamics of an altruistic phenotype with vertical cultural transmission and a gene that modifies the transmission of the phenotype. Their results are very sensitive to this genetic modification: without it, the conditions for invasion of the altruistic phenotype reduce to Hamilton’s rule. Further work is needed to incorporate such genetic modification of cultural transmission into our model. Woodcock [28] stressed the significance of non-vertical transmission for the evolution of cooperation and carried out simulations with prisoner’s dilemma payoffs but without horizontal transmission or social association ( $\alpha = 0$ ). Nevertheless, his results demonstrated that it is possible to sustain altruistic behavior via cultural transmission for a substantial length of time. Our results provide strong evidence for his hypothesis that horizontal transmission can play an important role in the evolution of cooperation.

To understand the role of horizontal transmission, we first review the role of *assortment*. Eshel & Cavalli-Sforza [6] showed that altruism can evolve when the tendency for *assortative meeting*, i.e., for individuals to interact with others of their own phenotype, is strong enough. Fletcher & Doebeli [9] further argued that a general explanation for the evolution of altruism is given by *assortment*: the correlation between individuals that carry an altruistic trait and the amount of altruistic behavior in their interaction group (see also Bijma & Aanen [3]). They suggested that to explain the evolution of altruism, we should seek mechanisms that generate assortment, such as population structure, repeated interactions, and individual recognition. Our results highlight another mechanism for generating assortment: an association between social interactions and horizontal transmission that creates a correlation between one’s partner for interaction and the partner for transmission. This mechanism does not require repeated interactions, population structure, or individual recognition. We show that high levels of such social association greatly increase the potential for evolution of cooperation. With enough social association, cooperation can increase in frequency when initially rare even when there is horizontal transmission bias against it ( $T_A < T_B$ ).

How does non-vertical transmission generate assortment? Lewin-Epstein *et al.* [16] and Lewin-Epstein & Hadany [17] suggested that microbes that induce their hosts to act altruistically can be favored by selection, which may help to explain the evolution of cooperation. From the kin selection point-of-view, if microbes can be transmitted *horizontally* from one host to another during host interactions, then following horizontal transmission the recipient host will carry microbes that are closely related to those of the donor host, even when the two hosts are (genetically) unrelated. From the assortment point-of-view, infection by behavior-determining microbes during interactions effectively generates assortment because a recipient of help may be infected by a behavior-determining microbe and consequently become a helper. Cultural horizontal transmission can similarly generate assortment between cooperators and enhance the benefit of cooperation if cultural transmission and helping interactions occur between the same individuals, i.e. when there is social association, so that the recipient of help may also be the recipient of the cultural trait for cooperation. Thus, with horizontal transmission, “assortment between focal cooperative players and cooperative acts in their interaction environment” [9] is generated not because the helper is likely to be helped, but rather because the helped is likely to become a helper.

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# Appendices

## 372 Appendix A Local stability criterion

Let  $f(p) = \lambda \cdot (p' - p)$ , where  $\lambda > 0$ , and 0 and 1 are equilibria, that is,  $f(0) = 0$  and  $f(1) = 0$ .

374 Set  $p > p^* = 0$ . Using a linear approximation for  $f(p)$  near 0, we have

$$p' < p \Leftrightarrow f(p)/p < 0 \Leftrightarrow \frac{f'(0) \cdot p + O(p^2)}{p} < 0 \Leftrightarrow f'(0) + O(p) < 0. \quad (\text{A1})$$

376 Therefore, by definition of big-O notation, if  $f'(0) < 0$  then there exists  $\epsilon > 0$  such that for any local perturbation  $0 < p < \epsilon$ , it is guaranteed that  $0 < p' < p$ ; that is,  $p'$  is closer to zero than  $p$ .

378 Set  $p < p^* = 1$  Using a linear approximation for  $f(p)$  near 1, we have

$$1 - p' < 1 - p \Leftrightarrow -\frac{f(p)}{1 - p} < 0 \Leftrightarrow \frac{f'(1)(p - 1) + O((p - 1)^2)}{p - 1} < 0 \Leftrightarrow f'(1) - O(1 - p) < 0. \quad (\text{A2})$$

380 Therefore, if  $f'(1) < 0$  then there exists  $\epsilon > 0$  such that for any  $1 - \epsilon < 1 - p < 1$  we have  $1 - p' < 1 - p$ ; that is,  $p'$  is closer to one than  $p$ .

## 382 Appendix B Equilibria and stability

Let  $f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p})$ . Then, using *SymPy* [22], a Python library for symbolic mathematics, this simplifies to

$$f(\hat{p}) = \bar{w}(\hat{p}' - \hat{p}) = \beta_1 \hat{p}^3 + \beta_2 \hat{p}^2 + \beta_3 \hat{p}, \quad (\text{B1})$$

386 where

$$\begin{aligned} \beta_1 &= [c(1 - v) - b(1 - \alpha v)](T_A - T_B), \\ \beta_2 &= -\beta_1 - \beta_3, \\ \beta_3 &= \alpha b v T_A - c v(1 - T_B) + (T_A - T_B). \end{aligned} \quad (\text{B2})$$

388 If  $T = T_A = T_B$  then  $\beta_1 = 0$  and  $\beta_3 = -\beta_2 = \alpha b v T - c v(1 - T)$ , and  $f(\hat{p})$  becomes a quadratic polynomial,

$$f(\hat{p}) = \hat{p}(1 - \hat{p})[\alpha b v T - c v(1 - T)]. \quad (\text{B3})$$

390 Clearly the only two equilibria are the fixations  $\hat{p} = 0$  and  $\hat{p} = 1$ , which are locally stable if  $f'(\hat{p}) < 0$  near the equilibrium (see Appendix A), where  $f'(\hat{p}) = (1 - 2\hat{p})[\alpha b v T - c v(1 - T)]$ , so that

$$\begin{aligned} f'(0) &= \alpha b v T - c v(1 - T), \\ f'(1) &= -\alpha b v T + c v(1 - T). \end{aligned} \quad (\text{B4})$$

In the general case where  $T_A \neq T_B$ , the coefficient  $\beta_1$  is not necessarily zero, and  $f(\hat{p})$  is a cubic polynomial.

394 Therefore, three equilibria may exist, two of which are  $\hat{p} = 0$  and  $\hat{p} = 1$ , and the third is

$$\hat{p}^* = \frac{\beta_3}{\beta_1} = \frac{\alpha b v T_A - c v(1 - T_B) + (T_A - T_B)}{[c(1 - v) - b(1 - \alpha v)](T_A - T_B)}. \quad (\text{B5})$$

396 Note that the sign of the cubic (Eq. B1) at positive (negative) infinity is equal (opposite) to the sign of  $\beta_1$ . If  $T_A > T_B$ , then

$$\beta_1 < [c(1 - \alpha v) - b(1 - \alpha v)](T_A - T_B) = (1 - \alpha v)(c - b)(T_A - T_B) < 0, \quad (\text{B6})$$

since  $c < b$  and  $\alpha v < 1$ . Hence the signs of the cubic at positive and negative infinity are negative and positive, respectively. First, if  $\beta_3 < \beta_1$  then  $1 < \hat{p}^*$ . Also,  $f'(0) < 0$  and  $f'(1) > 0$ ; that is, fixation of the defector

phenotype  $B$  is the only locally stable feasible equilibrium. Second, if  $\beta_1 < \beta_3 < 0$  then  $0 < \hat{p}^* < 1$  and therefore  $f'(0) < 0$  and  $f'(1) < 0$  so that both fixations are locally stable and  $\hat{p}^*$  separates the domains of attraction. Third, if  $0 < \beta_3$  then  $\hat{p}^* < 0$  and therefore  $f'(0) > 0$  and  $f'(1) < 0$ ; that is, fixation of the cooperator phenotype  $A$  is the only locally stable legitimate equilibrium.

Similarly, if  $T_A < T_B$ , then

$$\beta_1 > [c(1 - \alpha v) - b(1 - \alpha v)](T_A - T_B) = (1 - \alpha v)(c - b)(T_A - T_B) > 0, \quad (\text{B7})$$

since  $c < b$  and  $\alpha v < 1$ , and the signs of the cubic at positive and negative infinity are positive and negative, respectively. First, if  $\beta_3 < 0$  then  $\hat{p}^* < 0$  and therefore  $f'(0) < 0$  and  $f'(1) > 0$ ; that is, fixation of the defector phenotype  $A$  is the only locally stable legitimate equilibrium. Second, if  $0 < \beta_3 < \beta_1$  then  $0 < \hat{p}^* < 1$  and therefore  $f'(0) > 0$  and  $f'(1) > 0$ ; that is, both fixations are locally unstable and  $\hat{p}^*$  is a stable polymorphic equilibrium. Third, if  $\beta_1 < \beta_3$  then  $\hat{p}^* > 1$  and therefore  $f'(0) > 0$  and  $f'(1) < 0$ , and fixation of the cooperator phenotype  $A$  is the only locally stable feasible equilibrium.

This analysis can be summarized as follows:

1. *Fixation of cooperation*: if (i)  $T = T_A = T_B$  and  $c < b \cdot \frac{\alpha T}{1-T}$ ; or if (ii)  $T_A > T_B$  and  $0 < \beta_3$ ; or if (iii)  $T_A < T_B$  and  $\beta_1 < \beta_3$ .
2. *Fixation of the defection*: if (iv)  $T = T_A = T_B$  and  $c > b \cdot \frac{\alpha T}{1-T}$ ; or if (v)  $T_A > T_B$  and  $\beta_3 < \beta_1 < 0$ ; or if (vi)  $T_A < T_B$  and  $\beta_3 < 0$ .
3. *polymorphism of both phenotypes at  $\hat{p}^*$* : if (vii)  $T_A < T_B$  and  $0 < \beta_3 < \beta_1$ .
4. *Fixation of either phenotype depending on initial frequency*: if (viii)  $T_A > T_B$  and  $\beta_1 < \beta_3 < 0$ .

We now proceed to use the cost thresholds,  $\gamma_1$  and  $\gamma_2$ , and the vertical transmission threshold,  $\hat{v}$  (Eq. 13). First, assume  $T_A < T_B$ .  $\beta_3 < 0$  requires  $\gamma_1 < c$ . For  $\beta_3 < \beta_1$  we need  $c[v(1 - T_B) + (1 - v)(T_A - T_B)] > b\alpha T_B + (1 + b)(T_A - T_B)$ . Note that the expression in the square brackets is positive if and only if  $v > \hat{v}$ . Thus, for  $\beta_3 < \beta_1$  we need  $v > \hat{v}$  and  $\gamma_2 < c$  or  $v < \hat{v}$  and  $c < \gamma_2$ , and for  $0 < \beta_3 < \beta_1$  we need  $v > \hat{v}$  and  $\gamma_2 < c < \gamma_1$ , or  $v < \hat{v}$  and  $c < \min(\gamma_1, \gamma_2)$ . For  $\beta_1 < \beta_3$  we need  $v > \hat{v}$  and  $c < \gamma_2$  or  $v < \hat{v}$  and  $\gamma_2 < c$ . However, some of these conditions cannot be met, since  $v < \hat{v}$  implies  $c < 1 < \gamma_2$ .

Second, assume  $T_A > T_B$ .  $\beta_3 > 0$  requires  $\gamma_1 > c$ . For  $\beta_1 < \beta_3$  we need  $c[v(1 - T_B) + (1 - v)(T_A - T_B)] < b\alpha T_B + (1 + b)(T_A - T_B)$ . Thus for  $\beta_1 < \beta_3$  we need  $v > \hat{v}$  and  $c < \gamma_2$  or  $v < \hat{v}$  and  $c > \gamma_2$ . But  $\hat{v} < 0$  when  $T_A > T_B$ , and therefore we have  $\beta_1 < \beta_3$  if  $c < \gamma_2$ . Similarly, we have  $\beta_3 < \beta_1$  if  $c > \gamma_2$ .

This analysis is summarized in Result 1.

## Appendix C Effect of social association on mean fitness

To determine the effect of increasing  $\alpha$  on the stable population mean fitness,  $\bar{w}^* = 1 + (b - c)\hat{p}^*$ , we must analyze its effect on  $\hat{p}^*$ ,

$$\frac{\partial \hat{p}^*}{\partial \alpha} = \frac{bT_A - c(1 - T_B) + (T_A - T_B)}{b(1 - \alpha)^2(T_B - T_A)}. \quad (\text{C1})$$

Note that stable polymorphism implies  $c < \gamma_1$ , and because  $\alpha < 1$ , we have

$$c < \gamma_1 = \frac{b\alpha T_A + (T_A - T_B)}{1 - T_B} < \frac{bT_A + (T_A - T_B)}{1 - T_B}. \quad (\text{C2})$$

Therefore, the numerator in Eq. C1 is positive. Since  $T_A < T_B$ , the denominator in Eq. C1 is also positive, and hence the derivative  $\partial \hat{p}^* / \partial \alpha$  is positive. Thus, the population mean fitness increases as social association  $\alpha$  increases.

## Appendix D Reduction principle

440 We assume here that  $v = 1$ , i.e. no oblique transmission, and therefore  $\hat{p} = \tilde{p}$ . Denote the frequencies of the  
 442 pheno-genotypes  $AM$ ,  $BM$ ,  $Am$ , and  $Bm$  by  $\tilde{\mathbf{p}} = (\tilde{p}_1, \tilde{p}_2, \tilde{p}_3, \tilde{p}_4)$ . The frequencies of the pheno-genotypes in  
 the next generation are defined by the recursion system,

$$\begin{aligned}
 \bar{w}\tilde{p}'_1 &= \tilde{p}_1x(1+b-c)(1-(1-\alpha_1)(1-x)T_B) + \\
 &\quad \tilde{p}_1(1-x)(1-c)(1-\alpha_1T_Bx - T_B(1-x)) + \\
 &\quad \tilde{p}_2x(1+b)T_A(x+\alpha_1(1-x)) + \\
 &\quad \tilde{p}_2(1-x)x(1-\alpha_1)T_A, \\
 \bar{w}\tilde{p}'_2 &= \tilde{p}_1x(1+b-c)(1-\alpha_1)(1-x)T_B + \\
 &\quad \tilde{p}_1(1-x)(1-c)(\alpha_1T_B + (1-\alpha_1)(1-x)T_B) + \\
 &\quad \tilde{p}_2x(1+b)(1-\alpha_1T_A(1-x) - T_Ax) + \\
 &\quad \tilde{p}_2(1-x)(1-(1-\alpha_1)xT_A), \\
 \bar{w}\tilde{p}'_3 &= \tilde{p}_3x(1+b-c)(1-(1-\alpha_2)(1-x)T_B) + \\
 &\quad \tilde{p}_3(1-x)(1-c)(1-\alpha_2T_Bx - T_B(1-x)) + \\
 &\quad \tilde{p}_4x(1+b)T_A(x+\alpha_2(1-x)) + \\
 &\quad \tilde{p}_4(1-x)x(1-\alpha_2)T_A, \\
 \bar{w}\tilde{p}'_4 &= \tilde{p}_3x(1+b-c)(1-\alpha_2)(1-x)T_B + \\
 &\quad \tilde{p}_3(1-x)(1-c)(\alpha_2T_B + (1-\alpha_2)(1-x)T_B) + \\
 &\quad \tilde{p}_4x(1+b)(1-\alpha_2T_A(1-x) - T_Ax) + \\
 &\quad \tilde{p}_4(1-x)(1-(1-\alpha_2)xT_A),
 \end{aligned} \tag{D1}$$

444 where  $x = \tilde{p}_1 + \tilde{p}_3$  is the total frequency of the cooperative phenotype  $A$ , and  $\bar{w} = 1 + (b-c)x$  is the population  
 mean fitness.

446 The equilibrium where only allele  $M$  is present is  $\tilde{\mathbf{p}}^* = (\tilde{p}^*, 1 - \tilde{p}^*, 0, 0)$ , where

$$\tilde{p}^* = \frac{c(1-T_B) - b\alpha_1T_A - (T_A - T_B)}{b(1-\alpha_1)(T_A - T_B)}, \tag{D2}$$

448 setting  $\alpha = \alpha_1$  and  $v = 1$  in Eq. 12. When  $v = 1$ ,  $\tilde{p}^*$  is a feasible polymorphism ( $0 < \tilde{p}^* < 1$ ) if  $T_A < T_B$  and  
 $\gamma_2 < c < \gamma_1$  (Result 1).

450 The local stability of  $\tilde{\mathbf{p}}^*$  to the introduction of allele  $m$  is determined by the linear approximation  $\mathbf{L}^*$  of the  
 transformation in Eq. D1 near  $\tilde{\mathbf{p}}^*$  (i.e., the Jacobian of the transformation at the equilibrium).  $\mathbf{L}^*$  is known  
 452 to have a block structure, with the diagonal blocks occupied by the matrices  $\mathbf{L}_{in}^*$  and  $\mathbf{L}_{ex}^*$  [1, 20]. The latter  
 is the external stability matrix: the linear approximation to the transformation near  $\tilde{\mathbf{p}}^*$  involving only the  
 454 pheno-genotypes  $Am$  and  $Bm$ , derived from Eq. D1 as

$$\begin{aligned}
 \mathbf{L}_{ex}^* &= \frac{1}{\bar{w}^*} \begin{bmatrix} X & Y \\ Z & Q \end{bmatrix} = \frac{1}{\bar{w}^*} \begin{bmatrix} \frac{\partial \bar{w}\tilde{p}'_3}{\partial \tilde{p}_3}(\tilde{\mathbf{p}}^*) & \frac{\partial \bar{w}\tilde{p}'_4}{\partial \tilde{p}_4}(\tilde{\mathbf{p}}^*) \\ \frac{\partial \bar{w}\tilde{p}'_3}{\partial \tilde{p}_3}(\tilde{\mathbf{p}}^*) & \frac{\partial \bar{w}\tilde{p}'_4}{\partial \tilde{p}_4}(\tilde{\mathbf{p}}^*) \end{bmatrix} = \\
 &\quad \frac{1}{\bar{w}^*} \begin{bmatrix} (1+b\tilde{p}^*-c)(1-T_B(1-\tilde{p}^*)) + b\tilde{p}^*\alpha_2T_B(1-\tilde{p}^*) & (1+b\tilde{p}^*)T_A\tilde{p}^* + b\tilde{p}^*\alpha_2T_A(1-\tilde{p}^*) \\ (1+b\tilde{p}^*-c)T_B(1-\tilde{p}^*) - b\tilde{p}^*\alpha_2T_B(1-\tilde{p}^*) & (1+b\tilde{p}^*)(1-T_A\tilde{p}^*) - b\tilde{p}^*\alpha_2T_A(1-\tilde{p}^*) \end{bmatrix}.
 \end{aligned} \tag{D3}$$

456 Because we assume that  $\tilde{\mathbf{p}}^*$  is internally stable (i.e. locally stable to small perturbations in the frequencies of  
 $AM$  and  $BM$ ), the stability of  $\tilde{\mathbf{p}}^*$  is determined by the eigenvalues of the external stability matrix  $\mathbf{L}_{ex}^*$ . This is  
 458 a positive matrix, and due to the Perron-Frobenius theorem, the leading eigenvalue of  $\mathbf{L}_{ex}^*$  is real and positive.  
 Thus, if the leading eigenvalue is less (greater) than one, then the equilibrium  $\tilde{\mathbf{p}}^*$  is externally stable (unstable)  
 460 and allele  $m$  cannot (can) invade the population of allele  $M$ . The eigenvalues of  $\mathbf{L}_{ex}^*$  are the roots of the  
 characteristic polynomial,

$$R(\lambda) = \lambda^2 - \lambda \frac{(X+Q)}{\bar{w}^*} + \frac{XQ - YZ}{\bar{w}^{*2}}, \tag{D4}$$

where  $X, Y, Z$ , and  $Q$  are defined in Eq. D3. The characteristic polynomial  $R(\lambda)$  is a quadratic with a positive  
 464 leading coefficient. Therefore,  $\lim_{\lambda \rightarrow \pm\infty} R(\lambda) = \infty$ , and the leading eigenvalue is less than one (implying  
 466 stability) if and only if  $R(1) > 0$  and  $R'(1) > 0$ . Thus, a sufficient condition for external instability of  $\tilde{\mathbf{p}}^*$   
 is

$$R(1) < 0 \Leftrightarrow 1 - \frac{(X + Q)}{\bar{w}^*} + \frac{XQ - YZ}{\bar{w}^{*2}} < 0 \Leftrightarrow \bar{w}^{*2} - \bar{w}^*(X + Q) + XQ - YZ < 0. \quad (\text{D5})$$

468 Using *SymPy* [22], a Python library for symbolic mathematics, we find that inequality D5 is true if and only  
 if

$$470 \quad \alpha_2(bT_A + (T_A - T_B) - c(1 - T_B)) < \alpha_1(bT_A + (T_A - T_B) - c(1 - T_B)). \quad (\text{D6})$$

We assumed  $c < \gamma_1$ , that is,

$$\begin{aligned} c < \gamma_1 &= \frac{b\alpha_1 T_A + (T_A - T_B)}{1 - T_B} \Leftrightarrow \\ 472 \quad 0 &< b\alpha_1 T_A + (T_A - T_B) - c(1 - T_B) \Rightarrow \\ 0 &< bT_A + (T_A - T_B) - c(1 - T_B), \end{aligned} \quad (\text{D7})$$

since  $0 \leq \alpha_1 \leq 1$ . Therefore, combining inequalities D5, D6, and D7, we find that  $R(1) < 0$  if and only  
 474 if  $\alpha_2 < \alpha_1$ . This is a sufficient condition for external instability. So, if  $\alpha_2$ , the social association of the  
 invading modifier allele  $m$ , is less than  $\alpha_1$ , the social association of the resident allele  $M$ , then invasion will be  
 476 successful.

Determining a necessary and sufficient condition for successful invasion is more complicated, requiring analysis  
 478 of the sign of  $R'(1)$ . However, we numerically validated that the leading eigenvalue is greater than one if and  
 only if  $\alpha_2 < \alpha_1$ .

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**Table 1: Payoff matrix for prisoner's dilemma.**

	$\phi_2 = A$	$\phi_2 = B$
$\phi_1 = A$	$1 + b - c$	$1 - c$
$\phi_1 = B$	$1 + b$	$1$

The fitness of phenotype  $\phi_1$  when interacting with phenotype  $\phi_2$ .  $A$  is a cooperative phenotype,  $B$  is a defector phenotype,  $b$  is the benefit gained by an individual interacting with a cooperator, and  $c$  is the cost of cooperation.  $0 < c < 1$  and  $c < b$ .

**Table 2: Interaction frequency, fitness, and transmission probabilities.**

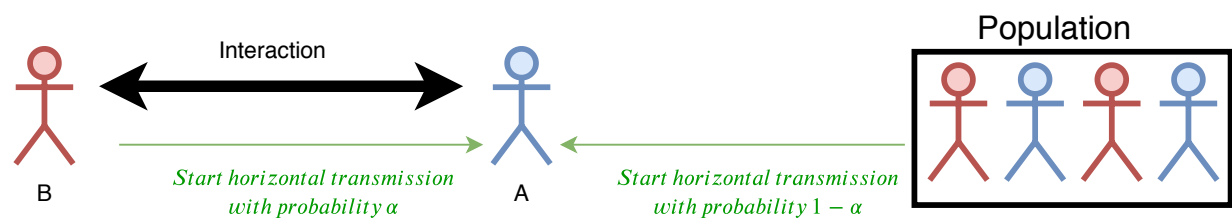
Phenotype $\phi_1$	Phenotype $\phi_2$	Frequency	Fitness of $\phi_1$	$P(\phi_1 = A)$ via horizontal transmission:	
				from partner, $\alpha$	from population, $(1 - \alpha)$
$A$	$A$	$\hat{p}^2$	$1 + b - c$	$1$	$\hat{p} + (1 - \hat{p})(1 - T_B)$
$A$	$B$	$\hat{p}(1 - \hat{p})$	$1 - c$	$1 - T_B$	$\hat{p} + (1 - \hat{p})(1 - T_B)$
$B$	$A$	$\hat{p}(1 - \hat{p})$	$1 + b$	$T_A$	$\hat{p}T_A$
$B$	$B$	$(1 - \hat{p})^2$	$1$	$0$	$\hat{p}T_A$

**Table 3: Model variables and parameters.**

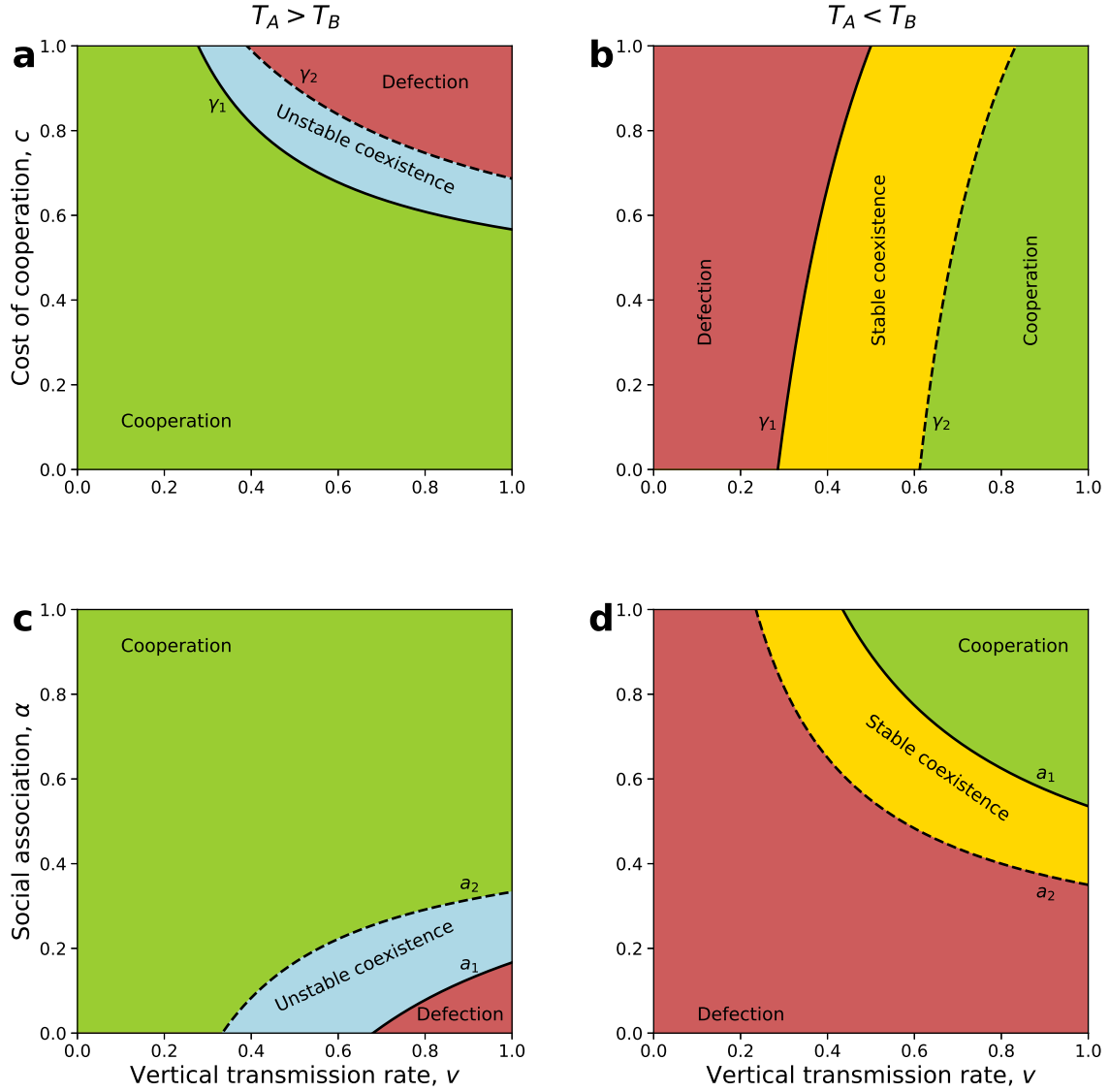
Symbol	Description	Values
$A$	Cooperator phenotype	
$B$	Defector phenotype	
$p$	Frequency of phenotype $A$ among adults	$[0, 1]$
$\tilde{p}$	Frequency of phenotype $A$ among parents	$[0, 1]$
$\hat{p}$	Frequency of phenotype $A$ among juveniles	$[0, 1]$
$v$	Vertical transmission rate	$[0, 1]$
$c$	Cost of cooperation	$(0, 1)$
$b$	Benefit of cooperation	$c < b$
$\alpha$	Probability of social association	$[0, 1]$
$T_A, T_B$	Horizontal transmission rates of phenotype $A$ and $B$	$(0, 1)$



# Figures

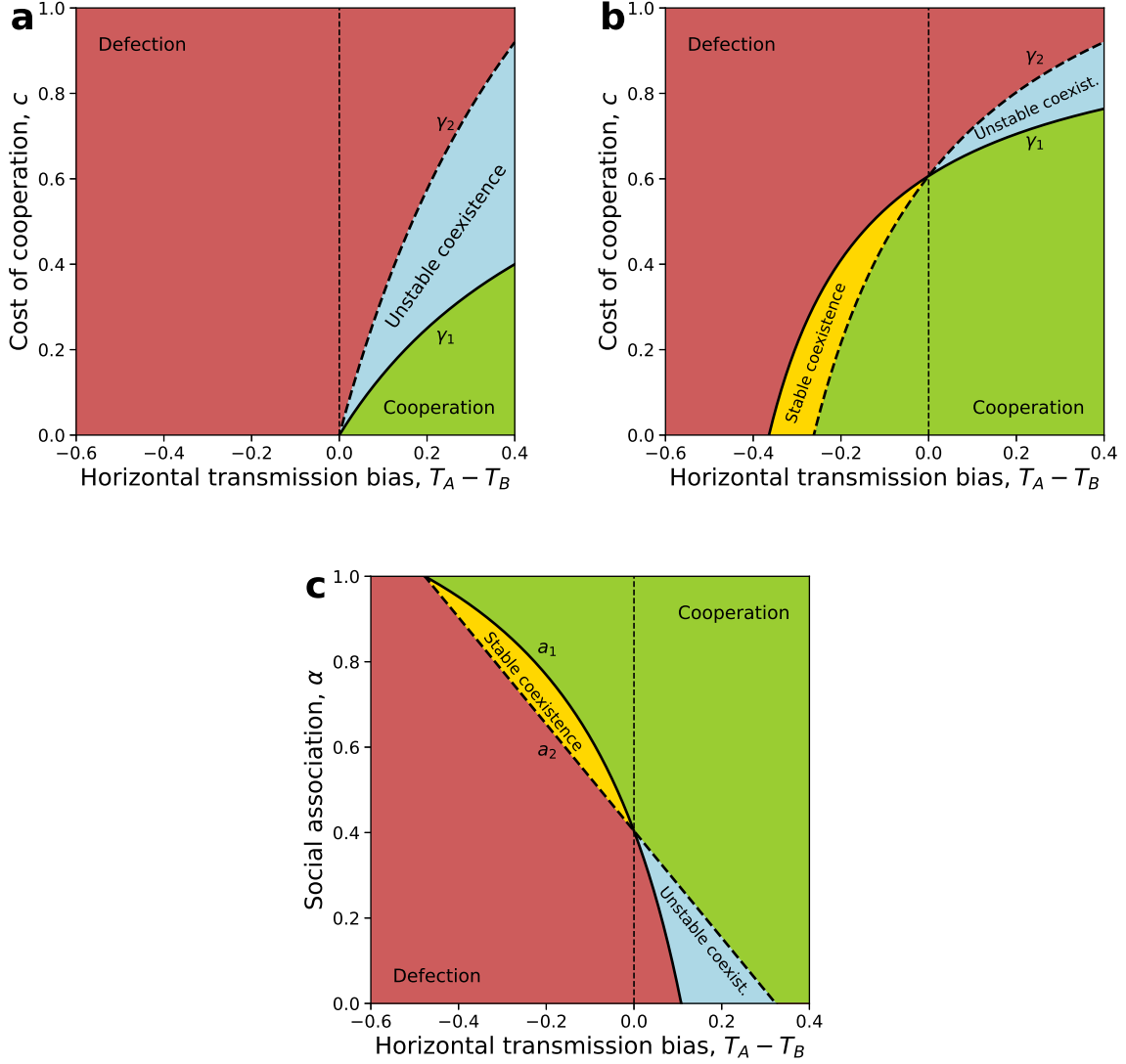


**Figure 1: Cultural horizontal transmission with assortment.** Transmission occurs between interacting partners with probability  $\alpha$  (left) or between two random peers with probability  $1 - \alpha$ , where  $\alpha$  is the *social association* parameter.

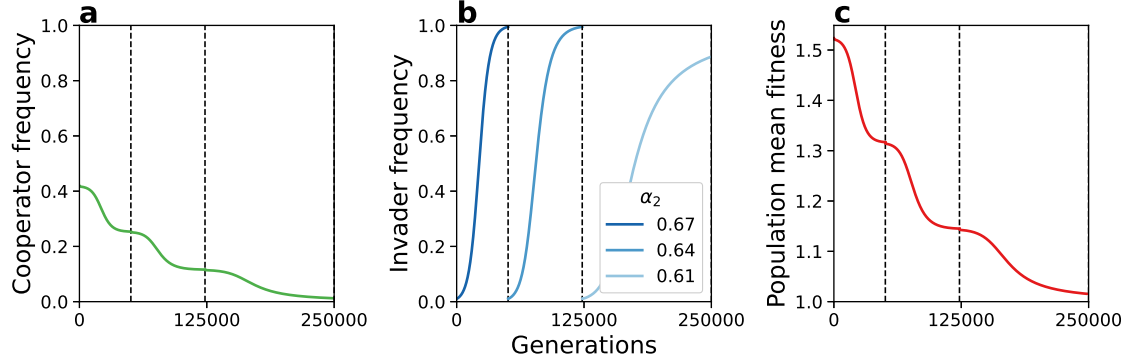


**Figure 2: Evolution of cooperation under vertical, oblique, and horizontal cultural transmission.**

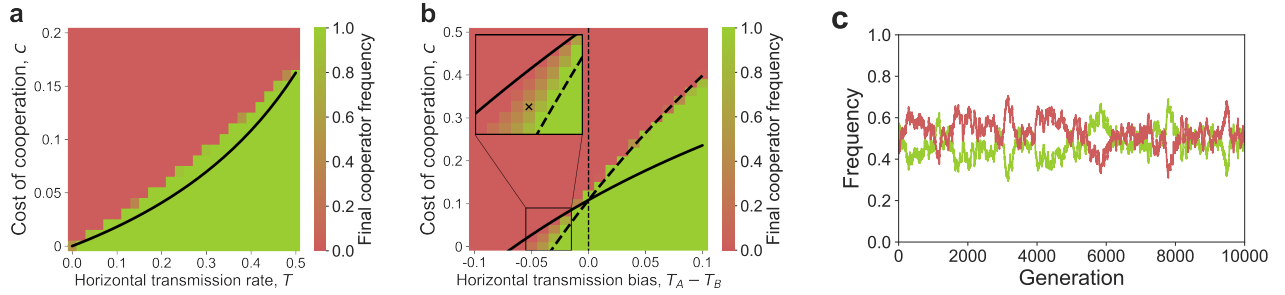
The figure shows the parameter ranges for global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable polymorphism (blue), and stable polymorphism of cooperation and defection (yellow). In all cases the vertical transmission rate  $v$  is on the x-axis. **(a-b)** Cost of cooperation  $c$  is on the y-axis and the cost thresholds  $\gamma_1$  and  $\gamma_2$  (Eq. 13) are represented by the solid and dashed lines, respectively. **(c-d)** Social association  $\alpha$  is on the y-axis and the social association thresholds  $a_1$  and  $a_2$  (Eq. 18) are represented by the solid and dashed lines, respectively. Horizontal transmission is biased in favor of cooperation,  $T_A > T_B$ , in **(a)** and **(c)**, or defection,  $T_A < T_B$ , in **(b)** and **(d)**. Here,  $T_A = 0.5$ , and **(a)**  $b = 1.2$ ,  $T_B = 0.4$ ,  $\alpha = 0.4$ ; **(b)**  $b = 2$ ,  $T_B = 0.7$ ,  $\alpha = 0.7$ ; **(c)**  $b = 1.2$ ,  $T_B = 0.4$ ,  $c = 0.5$ ; **(d)**  $b = 2$ ,  $T_B = 0.7$ ,  $c = 0.5$ .



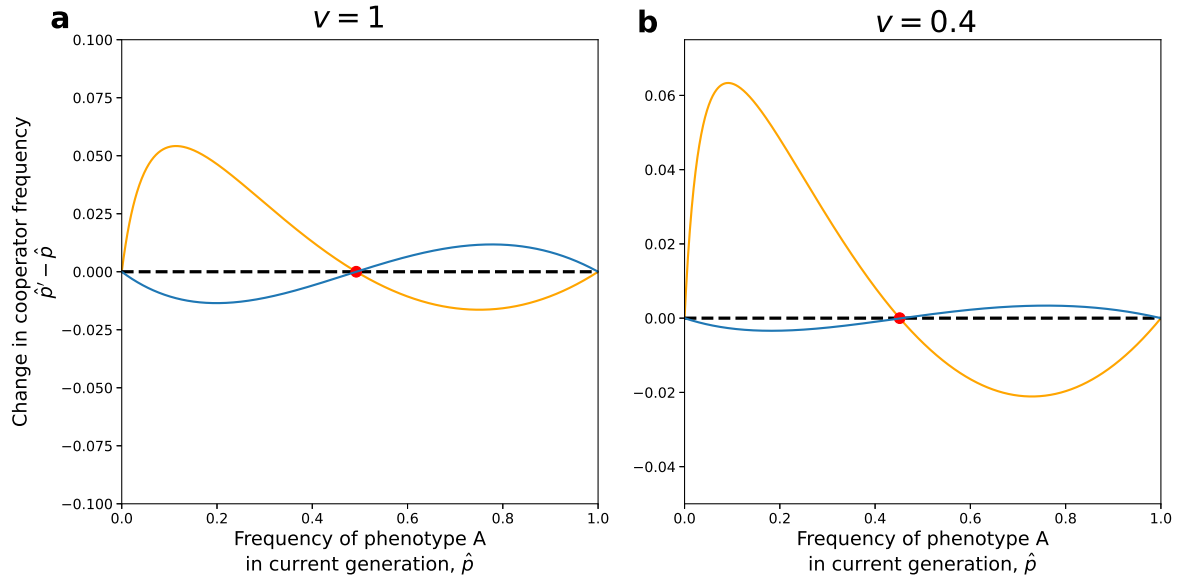
**Figure 3: Evolution of cooperation under vertical and horizontal cultural transmission ( $v=1$ ).** The figure shows the parameter ranges for global fixation of cooperation (green), global fixation of defection (red), fixation of either cooperation or defection depending on the initial conditions, i.e. unstable polymorphism (blue), and stable polymorphism of cooperation and defection (yellow). In all cases the horizontal bias ( $T_A - T_B$ ) is on the x-axis. **(a-b)** Cost of cooperation  $c$  is on the y-axis; the cost thresholds  $\gamma_1$  and  $\gamma_2$  (Eq. 13) are the solid and dashed lines, respectively. **(c)** Social association  $\alpha$  is on the y-axis; the social association thresholds  $a_1$  and  $a_2$  (Eq. 18) are the solid and dashed lines, respectively. Here,  $b = 1.3$ ,  $T_A = 0.4$ , **(a)**  $\alpha = 0$ , **(b)**  $\alpha = 0.7$ , **(c)**  $c = 0.35$ .



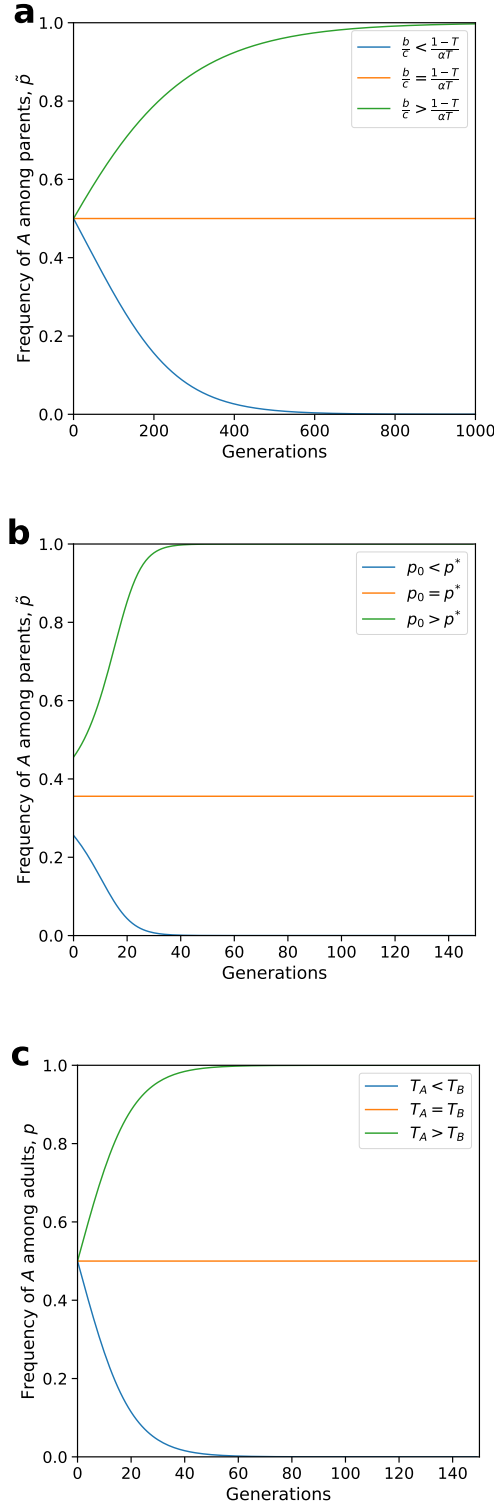
**Figure 4: Reduction principle for social association.** Consecutive fixation of modifier alleles that reduce social association in numerical simulations of evolution with two modifier alleles (Eq. D1). When an invading modifier allele is established in the population (frequency  $> 99.95\%$ ), a new modifier allele that reduces social association by 5% is introduced (at initial frequency 0.5%). **(a)** The frequency of the cooperative phenotype  $A$  over time. **(b)** The frequency of the invading modifier allele  $m$  over time. **(c)** The population mean fitness ( $\bar{w}$ ) over time. Here,  $c = 0.05$ ,  $b = 1.3$ ,  $T_A = 0.4 < T_B = 0.7$ , initial social association  $\alpha_1 = 0.7$ , lower social association threshold  $a_2 = 0.605$ .



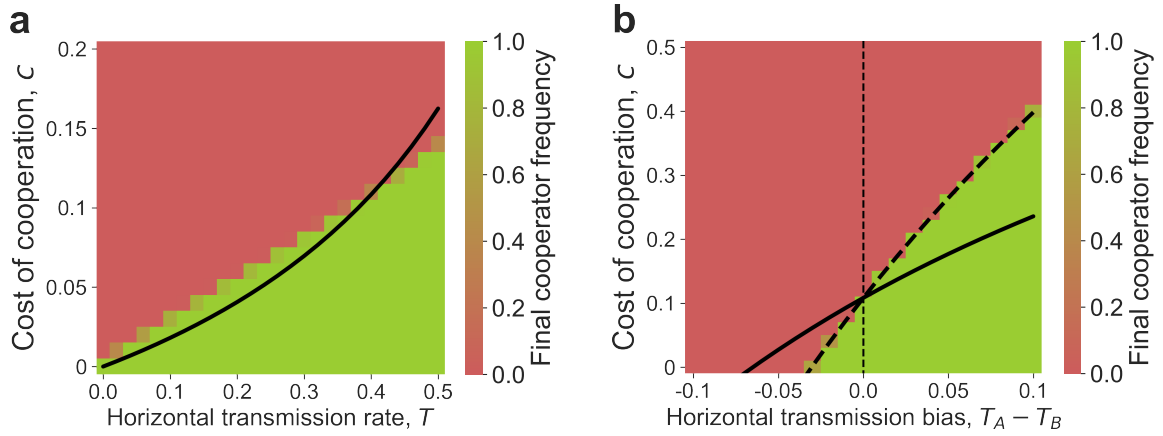
**Figure 5: Evolution of cooperation in a structured population.** **(a-b)** The expected frequency of cooperators in a structured population after 10,000 generations is shown (red for 0%, green for 100%) as a function of both the cost of cooperation,  $c$ , on the y-axis, and either the symmetric horizontal transmission rate,  $T = T_A = T_B$ , on the x-axis of panel (a), or the transmission bias,  $T_A - T_B$ , on the x-axis of panel (b). Black curves represent the cost thresholds for the evolution of cooperation in a well-mixed population with social association, where  $\alpha = 1/8$  in Eq. 15 for panel (a) and in Eq. 13 for (b). The inset in panel (b) focuses on an area of the parameter range in which neither phenotype is fixed throughout the simulation, maintaining a stochastic locally stable polymorphism [14]. This stochastic polymorphism is illustrated in panel (c), which shows the frequency of cooperators (green) and defectors (red) over time for the parameter set marked by an  $x$  in panel (b). In all cases, the population evolves on a 100-by-100 grid. Cooperation and horizontal transmission are both local between neighboring sites, and each site has 8 neighbors. Selection operates globally (see Figure S3 for results from a model with local selection). Simulations were stopped at generation 10,000 or if one of the phenotypes fixed. 50 simulations were executed for each parameter set. Benefit of cooperation,  $b = 1.3$ ; perfect vertical transmission  $v = 1$ ; **(a)** Symmetric horizontal transmission,  $T = T_A = T_B$ ; **(b)** Horizontal transmission rates  $T_A = 0.4$ ,  $0.3 < T_B < 0.5$ ; **(c)** Horizontal transmission rates  $T_A = 0.4 < T_B = 0.435$  and cost of cooperation  $c = 0.02$ .



**Figure S1: Stable and unstable polymorphism of cooperation and defection.** The curves show the change in cooperators frequency,  $\hat{p}' - \hat{p}$ , as a function of the current frequency of cooperators among juveniles,  $\hat{p}$  (Eq. 11). The dashed black line is  $\hat{p}' - \hat{p} = 0$ . The curves and the dashed line intersect at the polymorphic equilibrium  $\hat{p}^*$  (red circle). **(a)** Without oblique transmission,  $v = 1$ . A stable polymorphism (orange curve) is given by  $T_A = 0.4$ ,  $T_B = 0.9$ ,  $b = 12$ ,  $c = 0.35$ , and  $\alpha = 0.45$ . An unstable polymorphism (blue curve) is given by  $T_A = 0.5$ ,  $T_B = 0.1$ ,  $b = 1.3$ ,  $c = 0.904$ , and  $\alpha = 0.4$ . **(b)** With oblique transmission. A stable polymorphism (orange curve) is given by  $T_A = 0.4$ ,  $T_B = 0.9$ ,  $b = 20$ ,  $c = 0.1$ ,  $\alpha = 1$ , and  $v = 0.4$ . An unstable polymorphism (blue curve) is given by  $T_A = 0.5$ ,  $T_B = 0.4$ ,  $b = 1.2$ ,  $c = 0.487$ ,  $\alpha = 0.09$  and  $v = 0.6$ .



**Figure S2: Dynamics of the frequency of cooperation.** The frequency  $\tilde{p}$  of cooperator parents in (a-b) and the frequency  $p$  of adults cooperators in (c). The different lines correspond to parameter values that lead to fixation of cooperation (green), extinction of cooperation (red), or stable polymorphism of cooperators and defectors (yellow). (a)  $v = 1$ ,  $T_A = T_B = T = 0.2$ ,  $\alpha = 0.5 \neq 0$ ,  $\tilde{p}_0 = 0.5$  and  $c = 0.1$ ; (b)  $v = 1$ ,  $\alpha = 0$ ,  $\tilde{p}^* \approx 0.35$ ,  $T_A = 0.65$ ,  $T_B = 0.1$ ,  $b = 1.3$  and  $c = 0.65$ ; (c)  $v = 0$ ,  $\alpha = 0.5$ ,  $p_0 = 0.5$ ,  $T_A = 0.5$ ,  $b = 1.3$  and  $c = 0.5$ .



**Figure S3: Evolution of cooperation in a structured population with local selection.** The expected frequency of cooperators in a structured population after 10,000 generations is shown (red for 0%, green for 100%) as function of both the cost of cooperation ( $c$ ) on the y-axis, and the symmetric horizontal transmission rate ( $T = T_A = T_B$ ) on the x-axis of panel (a), or the transmission bias  $T_A - T_B$  on the x-axis of panel (b). The population evolves on a 100-by-100 grid. Cooperation and horizontal transmission are both local between neighboring sites, and each site had 8 neighbors. Selection operates locally (see Figure 5 for results from a model with global selection). The black curves represent the cost thresholds for the evolution of cooperation in a well-mixed population with social association, where  $\alpha = 1/8$  in Eq. 15 for panel (a) and in Eq. 13 for panel (b). The population evolves on a 100-by-100 grid. Simulations were stopped at generation 10,000 or if one of the phenotypes fixed. 50 simulations were executed for each parameter set. Here, benefit of cooperation,  $b = 1.3$ ; perfect vertical transmission  $\nu = 1$ ; **(a)** Symmetric horizontal transmission,  $T = T_A = T_B$ ; **(b)** Horizontal transmission rates  $T_A = 0.4$ ,  $0.3 < T_B < 0.5$ ;