# ECON 810 Final Project

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# Roadmap

Data

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#### Environment

- Agents live for T periods, without retirement.
- Agents are heterogeneous in human capital h, assets k, and years of schooling S.
- Agents have 1 unit of time endowment each period.
- They spend  $s \le 1$  in school each period.
- Agents are either employed or unemployed (but looking for a job).
- There are two kinds of firms: good firms (high type) and bad firms (low type).

#### **Firms**

- There are 2 firm types  $I \in \{L, H\}$ .
- ullet  $\mu$  fraction of firms are low type.
  - $\bullet$  Alternatively, we could think of this as  $\mu$  proportion of all job vacancies are for the low type firm.
- Firm type I = L hires all workers while firm type I = H hires only workers with  $S \ge \underline{S}$ .

- Workers are either employed ( without on the job search) or unemployed (actively searching for a job).
- Agents take as given these 3 state variables each period:
  - $h \in \mathbb{R}_+$  human capital. Law of motion  $h' = \exp z' H(h, s)$ .
  - $k \in \mathbb{R}_+$  assets.
  - $S \in \mathbb{R}_+$  (accumulated) schooling. Law of motion S' = S + s.
- *S*, i.e. years of schooling, determines the probability that an agents receives an offer from the high type firm.
  - ullet We could think of S as minimum required qualifications for a high paying job.

#### Unemployed Agents

 $\bullet$  Agents divide their time between searching for a job with intensity  $\gamma$  and schooling s:

$$\gamma + s = 1$$

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ullet Given  $\gamma$  and S, their probability of finding a job is

$$\Pi_t(\gamma,S) = \gamma \cdot \frac{S}{t}$$

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ullet Value function depends on whether the agents have a minimum of  $\underline{S}$  years of schooling or not.

### **Value Function if** $S < \underline{S}$

$$\begin{aligned} U_t(h,k,S) &= \max_{k',s} \bigg\{ u(c) + \beta \mathbb{E} \bigg[ \Pi(\gamma,S) \cdot \mu \cdot W_{t+1}^L(h',k',S') \\ &+ (1 - \Pi(\gamma,S) \cdot \mu) U_{t+1}^L(h',k',S') \bigg] \bigg\} \end{aligned}$$

### **Value Function if** $S \ge \underline{S}$

$$U_{t}(h, k, S) = \max_{k', s} \left\{ u(c) + \beta \mathbb{E} \left[ \Pi_{t}(\gamma, S) \left[ \mu W_{t+1}^{L}(h', k', S') + (1 - \mu) W_{t+1}^{H}(h', k', S') \right] + (1 - \Pi_{t}(\gamma, S)) U_{t+1}^{L}(h', k', S') \right] \right\}$$

with the budget constraint

$$c + k' \leq b + k(1+r).$$

#### **Employed Workers**

- Divide their time for s + l = 1.
- No on-the-job search allowed.

### Value function, employed at firm /

$$W_t'(h, k, S) = \max_{k', s} \left\{ u(c) + \beta \mathbb{E} \left[ (1 - \delta) W_{t+1}'(h', k', S') + \delta U_{t+1}(h', k', S') \right] \right\}$$

with the budget constraint

$$c+k'\leq R_t^IhI+k(1+r)$$

#### Timing

- Start each period t with (k, h, S). At t = 1, all agents are unemployed.
- ② Given their employment status at the start of each period, agents choose s and k', and pin down c.
- **1** If employed, l = 1 s. If unemployed,  $\gamma = 1 s$ .
- $\ \, \ \, \ \, \ \, \ \, \ \, \ \,$  If unemployed, given  $\gamma,$  S, agents have a probability of receiving a job offer.
- $\textbf{ If } S>\underline{S} \text{, of the offers they receive, a fraction } 1-\mu \text{ comes from high type firm.}$
- **1** If employed, agents may lose their job with a probability  $\delta$ .