

1. Derive the following asymptotic moments associated with  $m_3(x)$  : mean, variance, first order autocorrelation. Furthermore, compute  $\nabla_b g(b_0)$ . Which moments are informative for estimating  $b$ ?
2. Simulate a series of “true” data of length  $T = 200$  using (i). We will use this to compute  $M_T(x)$ .
3. Set  $H = 10$  and simulate  $H$  vectors of length  $T = 200$  random variables  $e_t$  from  $N(0, 1)$ . We will use this to compute  $M_{TH}(y(b))$ . Store these vectors. You will use the same vector of random variables throughout the entire exercise. Since this exercise requires you to estimate  $\sigma^2$ , you want to change the variance of  $e_t$  during the estimation. You can simply use  $\sigma_{e_t}$  when the variance is  $\sigma^2$ .
- 4.
5. Next we estimating the  $l = 2$  vector  $b$  for the just identified case where  $m_2$  uses the variance and autocorrelation. Given what you found in part (i), do you now think there will be a problem? If not, hopefully the standard error of the estimate of  $b$  as well as the J test will tell us something. Let’s see. For this case, perform steps (a)-(d) above.
6. Next, we will consider the overidentified case where  $m_3$  uses the mean, variance and autocorrelation. Let’s see. For this case, perform steps (a)-(d) above. Furthermore, bootstrap the the finite sample distribution of the estimators using the following algorithm:
  - i. Draw  $\epsilon_t$  and  $e_t^h$  from  $N(0, 1)$  for  $t = 1, 2, \dots, T$  and  $h = 1, 2, \dots, H$ . Compute  $(\hat{b}_{TH}^1), \hat{b}_{TH}^2$  as described.
  - ii. Repeat (e) using another seed.