

UNIT V

ANNOTATING LINGUISTIC STRUCTURE

By

Dr. S. S. Gharde

Dept. of Information Technology/ AIML

Government Polytechnic Nagpur

Contents

- Context-Free Grammars and Constituency Parsing

Introduction to CFG

- Context-free grammars are the backbone of many formal models of the syntax of natural language
- Syntactic parsing is the task of assigning a syntactic structure to a sentence.
- Parse trees can be used in applications such as grammar checking

Context-Free Grammars

- Context-free grammars are also called phrase-structure grammars, and the formalism is equivalent to Backus-Naur form, or BNF.
- A context-free grammar consists of a set of rules or productions and a lexicon of words and symbols.
- Context-free rules can be hierarchically embedded, so we can combine the previous rules with others
- For example, an NP (or noun phrase) can be composed of either a ProperNoun or a determiner (Det) followed by a Nominal; a Nominal in turn can consist of one or more Nouns.

NP \rightarrow Det Nominal

NP \rightarrow ProperNoun

Nominal \rightarrow Noun | Nominal Noun

Det \rightarrow a

Det \rightarrow the

Noun \rightarrow flight

Context-Free Grammars

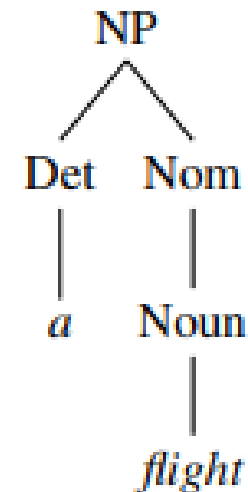
- The symbols that are used in a CFG are divided into two classes: Terminals and Nonterminals
- The symbols that correspond to words in the language are called **terminal symbols**
- The symbols that express abstractions over these terminals are called **non-terminals**.

Context-Free Grammars

- a CFG can be used to generate a set of strings. This sequence of rule expansions is called a derivation of the string of words.
- It is common to represent a derivation by **a parse tree**.

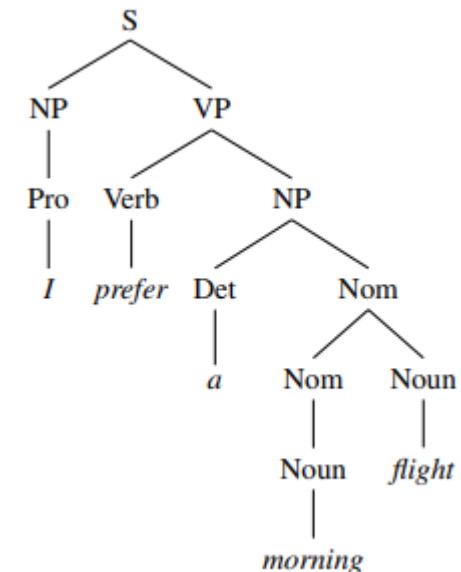
$NP \rightarrow Det\ Nominal$
 $NP \rightarrow ProperNoun$
 $Nominal \rightarrow Noun \mid Nominal\ Noun$

$Det \rightarrow a$
 $Det \rightarrow the$
 $Noun \rightarrow flight$



Noun \rightarrow *flights* | *flight* | *breeze* | *trip* | *morning*
Verb \rightarrow *is* | *prefer* | *like* | *need* | *want* | *fly* | *do*
Adjective \rightarrow *cheapest* | *non-stop* | *first* | *latest*
 | *other* | *direct*
Pronoun \rightarrow *me* | *I* | *you* | *it*
Proper-Noun \rightarrow *Alaska* | *Baltimore* | *Los Angeles*
 | *Chicago* | *United* | *American*
Determiner \rightarrow *the* | *a* | *an* | *this* | *these* | *that*
Preposition \rightarrow *from* | *to* | *on* | *near* | *in*
Conjunction \rightarrow *and* | *or* | *but*

Figure 17.2 The lexicon for \mathcal{L}_0 .



The parse tree for
 “I prefer a morning flight”
 according to grammar \mathcal{L}_0 .

Grammar Rules		Examples
$S \rightarrow NP VP$		I + want a morning flight
$NP \rightarrow$	<i>Pronoun</i>	I
	<i>Proper-Noun</i>	Los Angeles
	<i>Det Nominal</i>	a + flight
<i>Nominal</i> \rightarrow	<i>Nominal Noun</i>	morning + flight
	<i>Noun</i>	flights
$VP \rightarrow$	<i>Verb</i>	do
	<i>Verb NP</i>	want + a flight
	<i>Verb NP PP</i>	leave + Boston + in the morning
	<i>Verb PP</i>	leaving + on Thursday
$PP \rightarrow$	<i>Preposition NP</i>	from + Los Angeles

Figure 17.3 The grammar for \mathcal{L}_0 , with example phrases for each rule.

Formal Definition of Context-Free Grammar

- A context-free grammar G is defined by four tuples as

$$G = (N, \Sigma, R, S)$$

$$\text{OR } G = (V, T, P, S)$$

Where

- N is a set of non-terminal symbols (or variables V)
- Σ is a set of terminal symbols (T)
- R is a set of rules or productions (P)
 - each of the form $A \rightarrow \beta$
 - where A is a non-terminal, β is a string of symbols from the infinite set of strings $(\Sigma \cup N)^*$
- S is a designated start symbol and a member of N

Formal Definition of Context-Free Grammar

- General conventions for CFG
- Non-terminals - Capital letters like A, B, and S
- The start symbol - S
- Strings drawn from $(\Sigma \cup N)^*$ - Lower-case Greek letters like α , β , and γ
- Strings of terminals - Lower-case Roman letters like u, v, and w

Formal Definition of Context-Free Grammar

- **Derivation**
- A language is defined through the concept of derivation.
- One string derives another one if it can be rewritten as the second one by some series of rule applications.
- if $A \rightarrow \beta$ is a production of R and α and γ are any strings in the set $(\Sigma \cup N)^*$, then $\alpha A \gamma$ directly derives $\alpha \beta \gamma$, or $\alpha A \gamma \Rightarrow \alpha \beta \gamma$.
- Derivation is then a generalization of direct derivation.
- Let $\alpha_1, \alpha_2, \dots, \alpha_m$ be strings in $(\Sigma \cup N)^*$, $m \geq 1$, such that

$$\alpha_1 \Rightarrow \alpha_2, \quad \alpha_2 \Rightarrow \alpha_3, \quad \dots, \quad \alpha_{m-1} \Rightarrow \alpha_m$$
- We say that α_1 derives α_m , or α_1 derives $\Rightarrow \alpha_m$.

Formal Definition of Context-Free Grammar

- Language LG generated by a grammar G can be formally define as the set of strings composed of terminal symbols that can be derived from the designated start symbol S.

$$\mathcal{L}_G = \{w | w \text{ is in } \Sigma^* \text{ and } S \Rightarrow^* w\}$$

- The problem of mapping from a string of words to its **parse tree** is called syntactic parsing.

Treebanks

- A corpus in which every sentence is annotated with a parse tree is called a treebank.
- Treebanks play an important role in parsing as well as in linguistic investigations of syntactic phenomena.
- Treebanks are generally made by parsing each sentence with a parse that is then hand-corrected by human linguists.
- The sentences in a treebank implicitly constitute a grammar of the language.

Examples

- 1. Show that $S \rightarrow aabbaa$ and construct a derivation tree whose yield is $aabbaa$. Consider the G whose productions are

$$S \rightarrow aAS \mid a$$

$$A \rightarrow SbA \mid SS \mid ba$$

- Solution:
- $S \Rightarrow aAS$
- $\Rightarrow aSbAS$
- $\Rightarrow aabAS$
- $\Rightarrow aabbaS$
- $\Rightarrow aabbaa$

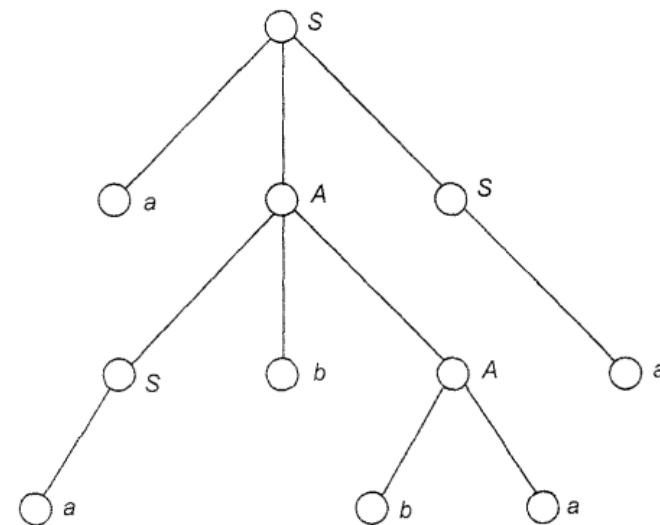


fig. 6.8 The derivation tree with yield $aabbaa$ for Example 6.2.

Examples

- 1. Let G be the grammar $S \rightarrow 0B \mid 1A$, $A \rightarrow 0 \mid 0S \mid 1AA$, $B \rightarrow 1 \mid 1S \mid 0BB$. For the string 00110101, find (a) the leftmost derivation, (b) the rightmost derivation, and (c) the derivation tree.

Solution

- (a) $S \Rightarrow 0B \Rightarrow 00BB \Rightarrow 001B \Rightarrow 0011S$
 $\Rightarrow 0^21^20B \Rightarrow 0^21^201S \Rightarrow 0^21^2010B \Rightarrow 0^21^20101$
- (b) $S \Rightarrow 0B \Rightarrow 00BB \Rightarrow 00B1S \Rightarrow 00B10B$
 $\Rightarrow 0^2B101S \Rightarrow 0^2B1010B \Rightarrow 0^2B10101 \Rightarrow 0^2110101$.
- (c) The derivation tree is given in Fig. 6.9.

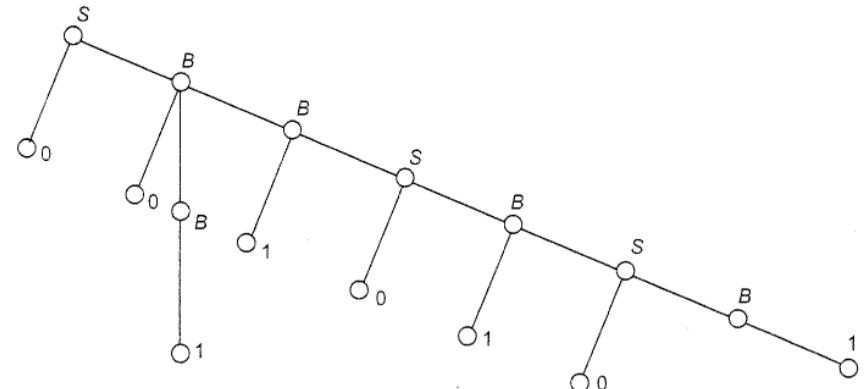


Fig. 6.9 The derivation tree with yield 00110101 for Example 6.3.

Examples

- Find the leftmost derivation for `aaa bba bbba` and construct parse tree for the same string. Consider the G whose productions are

$$S \rightarrow aB \mid bA$$

$$A \rightarrow a \mid aS \mid bAA$$

$$B \rightarrow b \mid bS \mid aBB$$

- 6.1** Find a derivation tree of $a * b + a * b$ given that $a * b + a * b$ is in $L(G)$, where G is given by $S \rightarrow S + S \mid S * S$, $S \rightarrow a \mid b$.

Examples

EXAMPLE 6.4

If G is the grammar $S \rightarrow SbS \mid a$, show that G is ambiguous.

6.5 Consider the following productions:

$$S \rightarrow aB \mid bA$$

$$A \rightarrow aS \mid bAA \mid a$$

$$B \rightarrow bS \mid aBB \mid b$$

For the string $aaabbabbba$, find

- (a) the leftmost derivation,
- (b) the rightmost derivation, and
- (c) the parse tree.

6.6 Show that the grammar $S \rightarrow a \mid abSb \mid aAb$, $A \rightarrow bS \mid aAAb$ is ambiguous.

6.7 Show that the grammar $S \rightarrow aB \mid ab$, $A \rightarrow aAB \mid a$, $B \rightarrow ABb \mid b$ is ambiguous.

Grammar Equivalence and Normal Form

- **Eliminating ϵ -productions**
- A CFG may have a production for $A \rightarrow \epsilon$ where A is a Non terminal.
- In CFG if there is production B and $B \rightarrow \epsilon$ and B derives ϵ in one or more steps then B is called **Nullable Nonterminal**.
- Ex. $A \rightarrow a|\epsilon$ and $B \rightarrow a$
- Here A is Nullable NT and B is not nullable NT.

Grammar Equivalence and Normal Form

- **Eliminating ϵ -productions**
- Procedure
- Step 1: Delete all ϵ -productions.
- Step 2: Identify all Nullable NT
- Step 3: For each Nullable NT, add subset of each nullable NT on RHS of productions.

Ex: Eliminate ϵ -production from Grammar G whose productions are

$$S \rightarrow aSa \mid bSb \mid \epsilon$$

Grammar Equivalence and Normal Form

- **Eliminating ϵ -productions**

Ex 1: Eliminate ϵ -production from Grammar G whose productions are

$$S \rightarrow aSa \mid bSb \mid \epsilon$$

Solution:

Here S is Nullable NT since $S \rightarrow \epsilon$

Eliminate it.

$$S \rightarrow aSa \mid bSb$$

Subset of $S \rightarrow aSa$ are $S \rightarrow aSa|aa$

Subset of $S \rightarrow bSb$ are $S \rightarrow bSb|bb$

By adding these subset, we get resultant Grammar as

$$\mathbf{S \rightarrow aSa \mid bSb \mid aa \mid bb}$$

Grammar Equivalence and Normal Form

- **Eliminating ϵ -productions**

Ex 2: Eliminate ϵ -production from Grammar G whose productions are

$$S \rightarrow Xa$$

$$X \rightarrow aX \mid bX \mid \epsilon$$

Ex 3: Eliminate ϵ -production from Grammar G whose productions are

$$S \rightarrow ABA$$

$$A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bB \mid \epsilon$$

Grammar Equivalence and Normal Form

- It is sometimes useful to have a **normal form** for grammars
- A context-free grammar is in **Chomsky normal form (CNF)** if it is ϵ -free and if in addition each production is either of the form

$$A \rightarrow B C \text{ or } A \rightarrow a.$$
- That is, the right-hand side of each rule either has two non-terminal symbols or one terminal symbol.
- **Chomsky normal form** grammars are binary branching, that is they have binary trees.
- Any context-free grammar can be converted into equivalent Chomsky normal form grammar.
- For example, a rule of the form

$$A \rightarrow B C D$$
- can be converted into the following two CNF rules

$$A \rightarrow B X$$

$$X \rightarrow C D$$

Ambiguity

- Structural ambiguity occurs when the grammar can assign more than one parse to a sentence.
- Two common kinds of ambiguity are **attachment ambiguity** and **coordination ambiguity**.
 - A sentence has an attachment ambiguity if a particular constituent can be attached to the parse tree at more than one place.
 - In coordination ambiguity phrases can be conjoined by a conjunction like *and*.
- Simple: For deriving input string w , if more than one derivation tree are produced, then the grammar is Ambiguous.

Ambiguity

- Example 1: Show that G is ambiguous if G is the grammar

$$S \rightarrow S + S \mid S * S \mid a \mid b$$

Consider string : $a + a * b$

The leftmost derivations of $a + a * b$ induced by the two derivation trees are

$$S \Rightarrow S + S \Rightarrow a + S \Rightarrow a + S * S \Rightarrow a + a * S \Rightarrow a + a * b$$

$$S \Rightarrow S * S \Rightarrow S + S * S \Rightarrow a + S * S \Rightarrow a + a * S \Rightarrow a + a * b$$

Therefore, $a + a * b$ is ambiguous.

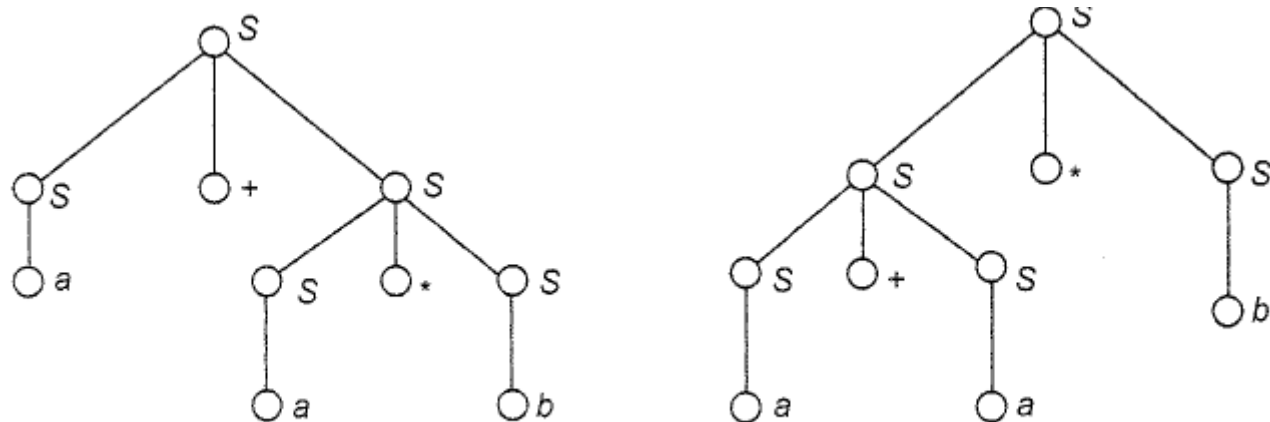


Fig. 6.10 Two derivation trees for $a + a * b$.

Ambiguity

- Example 2: Show that G is ambiguous if G is the grammar

$$S \rightarrow SbS|a$$

- Consider string : *abababa*

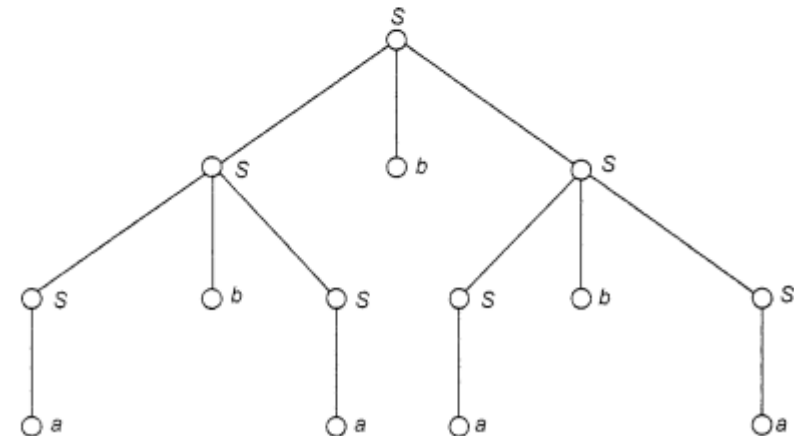
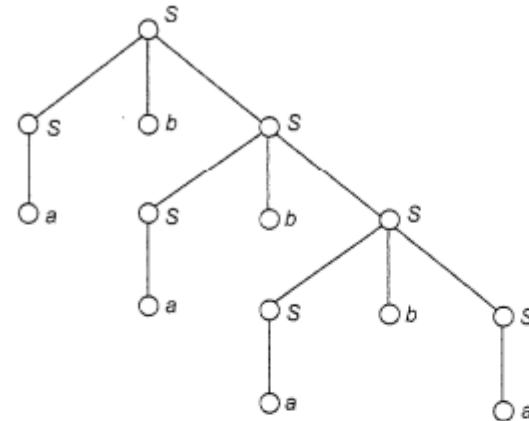


Fig. 6.11 Two derivation trees of *abababa* for Example 6.4.

Ambiguity

- Elimination of Ambiguity:
- $E \rightarrow E + E$
- $E \rightarrow E * E$
- $E \rightarrow id$

EXAMPLE 6.26

Show that a CFG G with productions $S \rightarrow SS \mid (S) \mid \Lambda$ is ambiguous.

Solution

$$S \Rightarrow SS \Rightarrow S(S) \Rightarrow \Lambda(S) \Rightarrow \Lambda(\Lambda) = (\Lambda)$$

Also,

$$S \Rightarrow SS \Rightarrow (S)S \Rightarrow (\Lambda)S \Rightarrow (\Lambda)\Lambda = (\Lambda)$$

Hence G is ambiguous.

CKY Parsing

- Cocke-Kasami-Younger (CKY) algorithm is the most widely used dynamic-programming based approach to parsing.
- **Conversion to Chomsky Normal Form**
- The CKY algorithm requires grammars to first be in Chomsky Normal Form (CNF)
- Eliminate unit productions
- Eliminate null productions

CKY Parsing

- Conversion to Chomsky Normal Form
- The entire conversion process can be summarized as follows:
 - 1. Copy all conforming rules to the new grammar unchanged.
 - 2. Convert terminals within rules to dummy non-terminals.
 - 3. Convert unit productions.
 - 4. Make all rules binary and add them to new grammar.

Grammar Equivalence and Normal Form

- Convert the given grammar into in CNF

$$S \rightarrow aSa \mid bSb \mid \varepsilon$$

- Convert the given grammar into in CNF

$$S \rightarrow bA \mid aB$$

$$A \rightarrow bAA \mid aS \mid a$$

$$B \rightarrow aBB \mid bS \mid b$$

Grammar Equivalence and Normal Form

Reduce the following grammar G to CNF. G is $S \rightarrow aAD$, $A \rightarrow aB \mid bAB$, $B \rightarrow b$, $D \rightarrow d$.

Solution

As there are no null productions or unit productions, we can proceed to step 2.

Step 2 Let $G_1 = (V'_N, \{a, b, d\}, P_1, S)$, where P_1 and V'_N are constructed as follows:

- (i) $B \rightarrow b$, $D \rightarrow d$ are included in P_1 .
- (ii) $S \rightarrow aAD$ gives rise to $S \rightarrow C_aAD$ and $C_a \rightarrow a$.
 $A \rightarrow aB$ gives rise to $A \rightarrow C_aB$.
 $A \rightarrow bAB$ gives rise to $A \rightarrow C_bAB$ and $C_b \rightarrow b$.
 $V'_N = \{S, A, B, D, C_a, C_b\}$.

Step 3 P_1 consists of $S \rightarrow C_aAD$, $A \rightarrow C_aB \mid C_bAB$, $B \rightarrow b$, $D \rightarrow d$, $C_a \rightarrow a$, $C_b \rightarrow b$.

$A \rightarrow C_aB$, $B \rightarrow b$, $D \rightarrow d$, $C_a \rightarrow a$, $C_b \rightarrow b$ are added to P_2

$S \rightarrow C_aAD$ is replaced by $S \rightarrow C_aC_1$ and $C_1 \rightarrow AD$.

$A \rightarrow C_bAB$ is replaced by $A \rightarrow C_bC_2$ and $C_2 \rightarrow AB$.

Let

$$G_2 = (\{S, A, B, D, C_a, C_b, C_1, C_2\}, \{a, b, d\}, P_2, S)$$

where P_2 consists of $S \rightarrow C_aC_1$, $A \rightarrow C_aB \mid C_bC_2$, $C_1 \rightarrow AD$, $C_2 \rightarrow AB$, $B \rightarrow b$, $D \rightarrow d$, $C_a \rightarrow a$, $C_b \rightarrow b$. G_2 is in CNF and equivalent to G .

Grammar Equivalence and Normal Form

EXAMPLE 6.12

Find a grammar in Chomsky normal form equivalent to $S \rightarrow aAbB$, $A \rightarrow aA \mid a$, $B \rightarrow bB \mid b$.

Solution

As there are no unit productions or null productions, we need not carry out step 1. We proceed to step 2.

Step 2 Let $G_1 = (V'_N \cup \{a, b\}, P_1, S)$, where P_1 and V'_N are constructed as follows:

- (i) $A \rightarrow a$, $B \rightarrow b$ are added to P_1 .
- (ii) $S \rightarrow aAbB$, $A \rightarrow aA$, $B \rightarrow bB$ yield $S \rightarrow C_aAC_bB$, $A \rightarrow C_aA$, $B \rightarrow C_bB$, $C_a \rightarrow a$, $C_b \rightarrow b$.

$$V'_N = \{S, A, B, C_a, C_b\}.$$

Step 3 P_1 consists of $S \rightarrow C_aAC_bB$, $A \rightarrow C_aA$, $B \rightarrow C_bB$, $C_a \rightarrow a$, $C_b \rightarrow b$, $A \rightarrow a$, $B \rightarrow b$.

$S \rightarrow C_aAC_bB$ is replaced by $S \rightarrow C_aC_1$, $C_1 \rightarrow AC_2$, $C_2 \rightarrow C_bB$

The remaining productions in P_1 are added to P_2 . Let

$$G_2 = (\{S, A, B, C_a, C_b, C_1, C_2\}, \{a, b\}, P_2, S),$$

where P_2 consists of $S \rightarrow C_aC_1$, $C_1 \rightarrow AC_2$, $C_2 \rightarrow C_bB$, $A \rightarrow C_aA$, $B \rightarrow C_bB$, $C_a \rightarrow a$, $C_b \rightarrow b$, $A \rightarrow a$, and $B \rightarrow b$.

G_2 is in CNF and equivalent to the given grammar.

Grammar Equivalence and Normal Form

EXAMPLE 6.22

Reduce the following grammar to CNF:

$$S \rightarrow ASA \mid bA, \quad A \rightarrow B \mid S, \quad B \rightarrow c$$

Solution

Step 1 *Elimination of unit productions:*

The unit productions are $A \rightarrow B$, $A \rightarrow S$.

$$W_0(S) = \{S\}, \quad W_1(S) = \{S\} \cup \emptyset = \{S\}$$

$$W_0(A) = \{A\}, \quad W_1(A) = \{A\} \cup \{S, B\} = \{S, A, B\}$$

$$W_2(A) = \{S, A, B\} \cup \emptyset = \{S, A, B\}$$

$$W_0(B) = \{B\}, \quad W_1(B) = \{B\} \cup \emptyset = \{B\}$$

The productions for the equivalent grammar without unit productions are

$$S \rightarrow ASA \mid bA, \quad B \rightarrow c$$

$$A \rightarrow ASA \mid bA, \quad A \rightarrow c$$

So, $G_1 = (\{S, A, B\}, \{b, c\}, P, S)$ where P consists of $S \rightarrow ASA \mid bA$, $B \rightarrow c$, $A \rightarrow ASA \mid bA \mid c$.

Step 2 *Elimination of terminals in R.H.S.:*

$S \rightarrow ASA$, $B \rightarrow c$, $A \rightarrow ASA \mid c$ are in proper form. We have to modify $S \rightarrow bA$ and $A \rightarrow bA$.

Replace $S \rightarrow bA$ by $S \rightarrow C_bA$, $C_b \rightarrow b$ and $A \rightarrow bA$ by $A \rightarrow C_bA$, $C_b \rightarrow b$.

So, $G_2 = (\{S, A, B, C_b\}, \{b, c\}, P_2, S)$ where P_2 consists of

$$S \rightarrow ASA \mid C_bA$$

$$A \rightarrow ASA \mid c \mid C_bA$$

$$B \rightarrow c, \quad C_b \rightarrow b$$

Step 3 *Restricting the number of variables on R.H.S.:*

$$S \rightarrow ASA \text{ is replaced by } S \rightarrow AD, \quad D \rightarrow SA$$

$$A \rightarrow ASA \text{ is replaced by } A \rightarrow AE, \quad E \rightarrow SA$$

So the equivalent grammar in CNF is

$$G_3 = (\{S, A, B, C_b, D, E\}, \{b, c\}, P_3, S)$$

where P_3 consists of

$$S \rightarrow C_bA \mid AD$$

$$A \rightarrow c \mid C_bA \mid AE$$

$$B \rightarrow c, \quad C_b \rightarrow b, \quad D \rightarrow SA, \quad E \rightarrow SA$$

Grammar Equivalence and Normal Form

6.12 Reduce the following grammars to Chomsky normal form:

- (a) $S \rightarrow 1A \mid 0B$, $A \rightarrow 1AA \mid 0S \mid 0$, $B \rightarrow 0BB \mid 1S \mid 1$
 (b) $G = (\{S\}, \{a, b, c\}, \{S \rightarrow a \mid b \mid cSS\}, S)$
 (c) $S \rightarrow abSb \mid a \mid aAb$, $A \rightarrow bS \mid aAAb$.

6.13 Reduce the grammars given in Exercises 6.1, 6.2, 6.6, 6.7, 6.9, 6.10 to Chomsky normal form.

1. Consider the grammar G which has the productions

$$A \rightarrow a \mid Aa \mid bAA \mid AAb \mid AbA$$

2. Consider the grammar G which has the following productions

$$S \rightarrow aB \mid bA, A \rightarrow aS \mid bAA \mid a, B \rightarrow bS \mid aBB \mid b.$$

- 6.1** Find a derivation tree of $a * b + a * b$ given that $a * b + a * b$ is in $L(G)$, where G is given by $S \rightarrow S + S \mid S * S$, $S \rightarrow a \mid b$.
6.6 Show that the grammar $S \rightarrow a \mid abSb \mid aAb$, $A \rightarrow bS \mid aAAb$ is ambiguous.
6.7 Show that the grammar $S \rightarrow aB \mid ab$, $A \rightarrow aAB \mid a$, $B \rightarrow ABb \mid b$ is ambiguous.
6.9 Find a reduced grammar equivalent to the grammar $S \rightarrow aAa$, $A \rightarrow bBB$, $B \rightarrow ab$, $C \rightarrow aB$.

Dependency Parsing

- **Dependency Relations**
- The traditional linguistic notion of grammatical relation provides the basis for the binary relations that comprise these dependency structures.
- The arguments to these relations consist of a **head** and a **dependent**.
- The head plays the role of the central organizing word, and the dependent as a kind of modifier.
- The head-dependent relationship is made explicit by directly linking heads to the words that are immediately dependent on them.

Dependency Parsing

- **Dependency Relations**
- Linguists have developed taxonomies of relations that go well beyond the familiar notions of subject and object.
- The **Universal Dependencies** (UD) project, an open community effort to annotate dependencies and other aspects of grammar across more than 100 languages, provides an inventory of 37 dependency relations.
- Fig. 18.2 shows a subset of the UD relations and Fig. 18.3 provides some examples.

Dependency Parsing

- Dependency Relations**

Clausal Argument Relations	Description
NSUBJ	Nominal subject
OBJ	Direct object
IOBJ	Indirect object
CCOMP	Clausal complement
Nominal Modifier Relations	Description
NMOD	Nominal modifier
AMOD	Adjectival modifier
NUMMOD	Numeric modifier
APPOS	Appositional modifier
DET	Determiner
CASE	Prepositions, postpositions and other case markers
Other Notable Relations	Description
CONJ	Conjunct
CC	Coordinating conjunction

Figure 18.2 Some of the Universal Dependency relations (de Marneffe et al., 2021).

Relation	Examples with <i>head</i> and dependent
NSUBJ	United <i>canceled</i> the flight.
OBJ	United <i>diverted</i> the flight to Reno. We <i>booked</i> her the first flight to Miami.
IOBJ	We <i>booked</i> her the flight to Miami.
NMOD	We took the morning flight.
AMOD	Book the cheapest flight.
NUMMOD	Before the storm JetBlue canceled 1000 flights.
APPOS	<i>United</i> , a unit of UAL, matched the fares.
DET	The flight was canceled. Which flight was delayed?
CONJ	We <i>flew</i> to Denver and drove to Steamboat.
CC	We flew to Denver and drove to Steamboat.
CASE	Book the flight through Houston.

Figure 18.3 Examples of some Universal Dependency relations.

Dependency Formalisms

- A dependency structure can be represented as a directed graph
 $G = (V, A)$
- consisting of a set of vertices V ,
- and a set of ordered pairs of vertices A , which we'll call *arcs*.
- The set of arcs, A , captures the head dependent and grammatical function relationships between the elements in V .
- A **dependency tree** is a directed graph that satisfies the following constraints:
 - 1. There is a single designated root node that has no incoming arcs.
 - 2. With the exception of the root node, each vertex has exactly one incoming arc.
 - 3. There is a unique path from the root node to each vertex in V

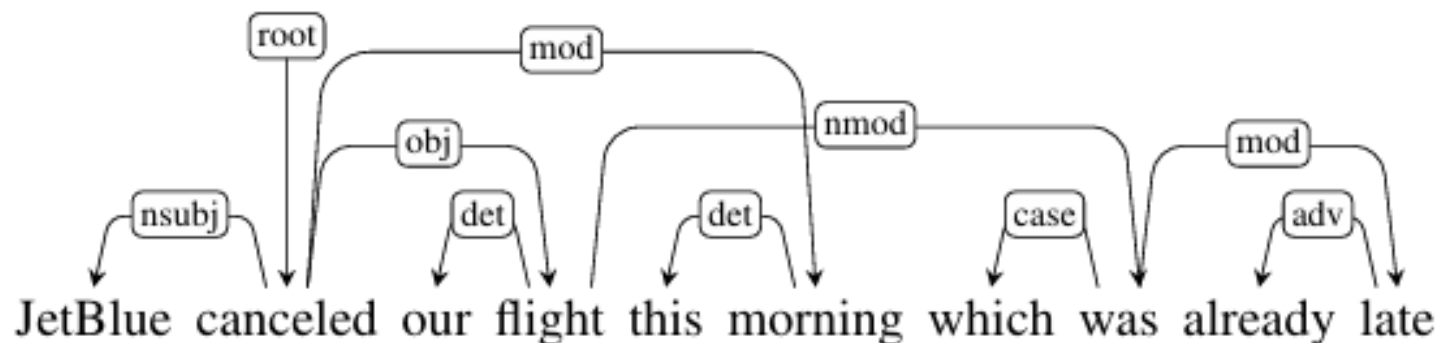
Projectivity

- The notion of projectivity imposes an additional constraint that is derived from the order of the words in the input.
- An **arc** from a head to a dependent **is said to be projective** if there is a path from the head to every word that lies between the head and the dependent in the sentence.
- A **dependency tree is then said to be projective** if all the arcs that make it up are projective.

Projectivity

- In this example, the arc from flight to its modifier was is non-projective since there is no path from flight to the intervening words this and morning.
- As we can see from this diagram, projectivity (and non-projectivity) can be detected in the way we've been drawing our trees.

Consider the following example.



Dependency Treebanks

- Treebanks play a critical role in the development and evaluation of dependency parsers.
- They are used for training parsers, they act as the gold labels for evaluating parsers, and they also provide useful information for corpus linguistics studies.
- **Dependency treebanks** are created by having human annotators directly generate dependency structures for a given corpus, or by hand-correcting the output of an automatic parser.
- The largest open community project for building dependency trees is the Universal Dependencies project, which currently has almost 200 dependency treebanks in more than 100 languages.

Transition-Based Dependency Parsing

- First approach to dependency parsing is called transition-based parsing.
- This architecture draws on shift-reduce parsing, a paradigm originally developed for analyzing programming languages.
- In transition-based parsing we'll have a stack on which we build the parse, a buffer of tokens to be parsed, and a parser which takes actions on the parse via a predictor called an oracle, as illustrated in Fig. 18.4.

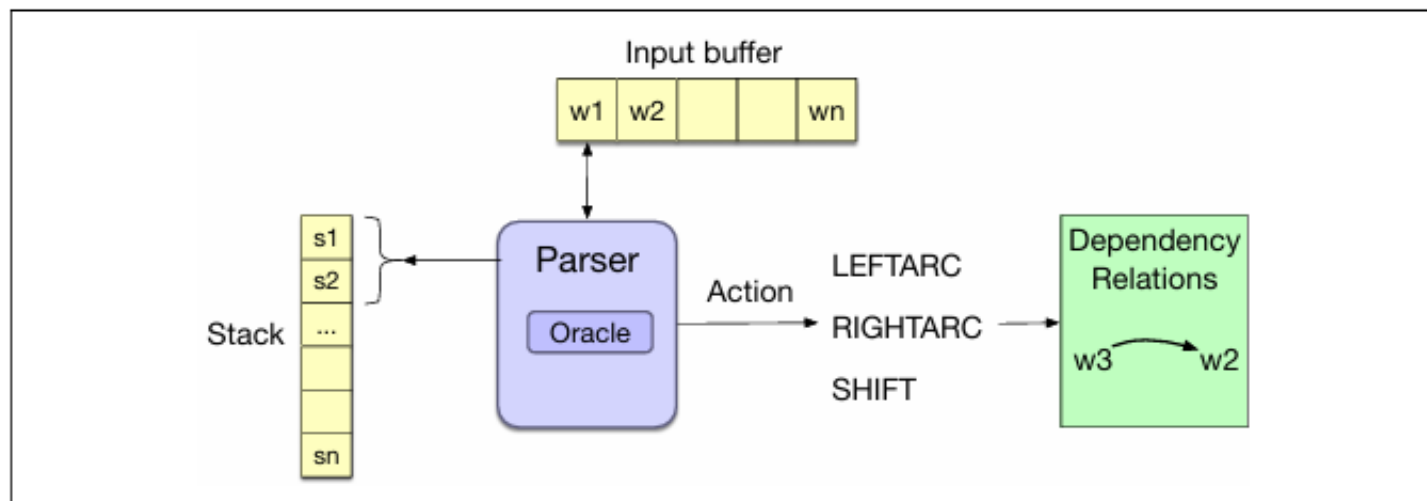


Figure 18.4 Basic transition-based parser. The parser examines the top two elements of the stack and selects an action by consulting an oracle that examines the current configuration.

Transition-Based Dependency Parsing

- The parser walks through the sentence left-to-right, successively shifting items from the buffer onto the stack.
- At each time point we examine the top two elements on the stack, and the oracle makes a decision about what transition to apply to build the parse.
- The specification of a transition-based parser is quite simple, based on representing the current state of the parse as a configuration:
 - the stack,
 - an input buffer of words or tokens, and
 - a set of relations representing a dependency tree.
- We start with an initial configuration in which the stack contains the ROOT node, the buffer has the tokens in the sentence, and an empty set of relations represents the parse.
- In the final goal state, the stack and the word list should be empty, and the set of relations will represent the final parse.

Transition-Based Dependency Parsing

- Fig. 18.5 gives the algorithm.

```
function DEPENDENCYPARSE(words) returns dependency tree  
  
state ← { [root], [words], [] } ; initial configuration  
while state not final  
    t ← ORACLE(state) ; choose a transition operator to apply  
    state ← APPLY(t, state) ; apply it, creating a new state  
return state
```

Figure 18.5 A generic transition-based dependency parser

End of UNIT V