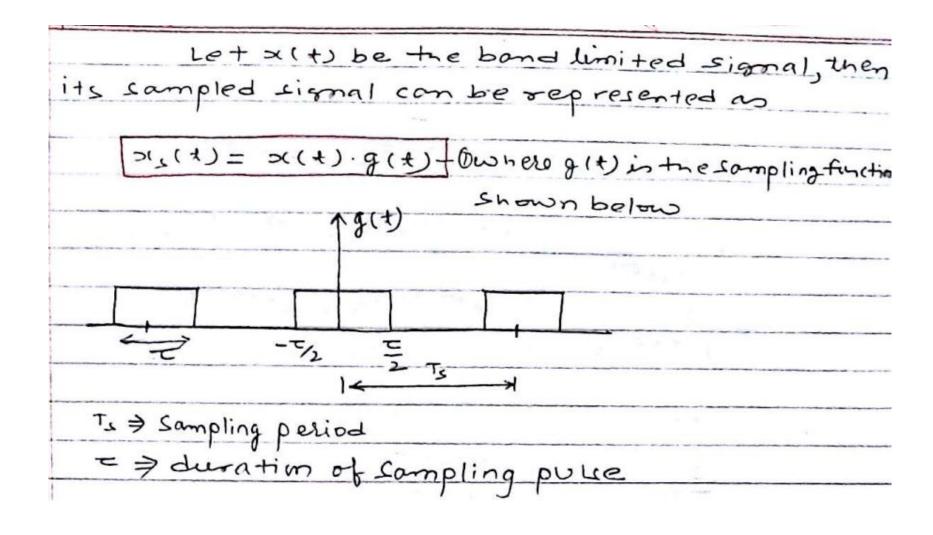
Chapter -2

- Process of converting analog or continuous signal into discrete signal is called sampling.
- Sampling Theorem/Nquist Criteria
- For band limited signal which do not have maximum frequency greater than f_s
- Sampling Rate or Sampling frequency
- For Transmitting and Receiving end
- $f_{s \ge 2} f_x$



The sampling function
$$g(t)$$
 is given by

$$g(t) = C_0 + 2 \sum C_n \quad \text{(os } 2\pi n f_s t - 2)$$

As

$$x_1(t) = x(t) \quad g(t)$$

$$x_2(t) = x(t) \quad \left[c_0 + 2 \sum c_n \cos 2\pi n f_s t \right]$$

$$x_2(t) = c_0 x(t) + 2 c_1 x(t) \cos 2\pi n f_s t$$

$$x_3(t) = c_0 x(t) + 2 c_1 x(t) \cos 2\pi n f_s t$$

$$x_4(t) = c_0 x(t) + 2 c_1 x(t) \cos 2\pi n f_s t$$

$$x_5(t) = c_0 x(t) + 2 c_1 x(t) \cos 2\pi n f_s t$$

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$$x_5(t) = c_0 x(t) + 2 c_1 x(t) \cos 2\pi n f_s t$$

$$x_5(t) = c_0 x(t) + 2 c_1 x(t) \cos 2$$

$$= \frac{1}{T_1} \frac{e^{-j\pi i \pi f_1 t}}{e^{-j\pi i \pi f_1 t}} \Big|_{-\frac{1}{2}}$$

$$= -\frac{1}{j\pi i \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= -\frac{1}{j\pi i \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

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$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

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$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

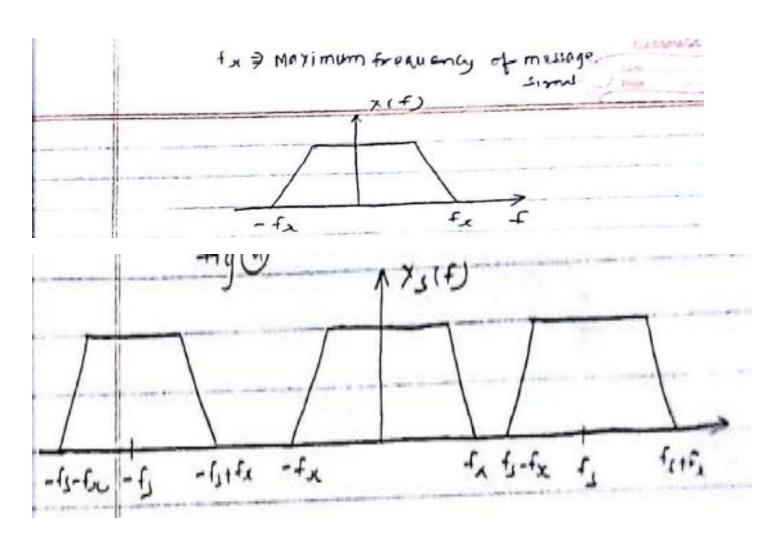
$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1 t} e_{j_2} \right]$$

$$= \frac{1}{j\pi \pi f_1 T_1} \left[e^{-j\pi i \pi f_1 t} e_{j_2} - e^{-j\pi i \pi f_1$$

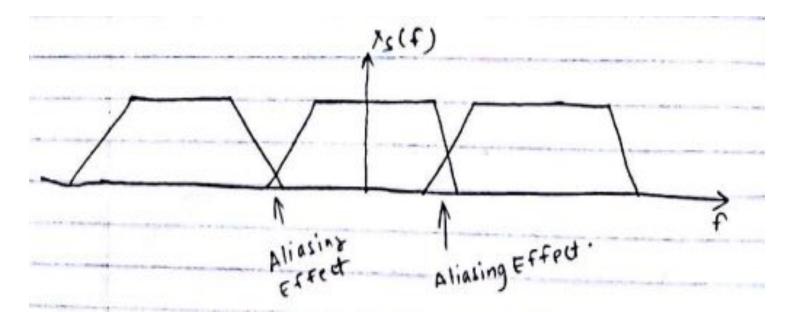
```
Taking Fordies Transform (F.T) of ean ()
we get
 (01 mot = +1) = + [2(+-to) + 2(++to)]
7(+)(01100+ -11 = = [ X (t-to) + X (t+to)]
x1(f)= (0x(f)+(1x(f-fs)+(1x(f+fs)
```

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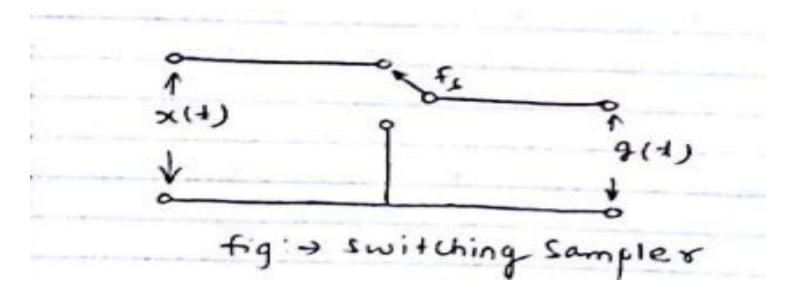
- Fig a represents the fourier transform of original message signal x(t).
- Fig b represents the fourier transform of the output of the sampler.
- For error less recovery of the message signal from the spectrum of the sampled signal mus t obey the nyquist sampling theorem as
- $f_s \ge 2 f_x$

- Similarly for sampling frequency $f_s < 2 f_x$
- Distortion will occur at the receiving side.
- Samples get overlapped while recovering.
- This phenomena is known as Aliasing.



Instantaneous / Ideal Sampling

- Instantaneous sampling gives train of impulse equal to the instantaneous value of input signal at sampling instant.
- Ideal sampling simply consist of switch Circuit.



Instantaneous/Ideal Sampling

- For time t, the output g(t) contains the instantaneous value of input signal x(t).
- Sampling function is represented as train of impulse

ST₃(+) =
$$\sum_{n=-\infty}^{\infty} S(t-n\tau_3) - 0$$

output 3(t) in expressed as

$$g(t) = x(t) ST3(t)$$

$$g(t) = x(t) \sum_{n=-\infty}^{\infty} S(t-n\tau_3) \qquad ST3(t) = ST3(t) =$$

- Process of Reconstructing original Signal x(t) from sampled signal is called Reconstruction.
- Signal x(t) band limited to f_m Hz can be reconstructed by passing the sampled signal through the Ideal Low Pass Filter at cut off frequency f_m
- The expression of sample signal is $g(t) = x(t) \delta T_s(t)$ ----(1)

•
$$g(t) = 1/T_s$$

 $g(t) = \sum_{n=-\alpha}^{\alpha} x(nts)\delta(t - nT_s)$ ----(3)

To recover the original Signal , the sampled signal is passed through the Ideal Low pass filter of bandwidth f_m Hz. The transform function of LPF is

$$H(w) = T_s rect(w/2\pi f_m) --- (4)$$

The impulse response of the filter is

$$h(t) = 2 f_m T_s Sinc(2\pi f_m t)----(5)$$

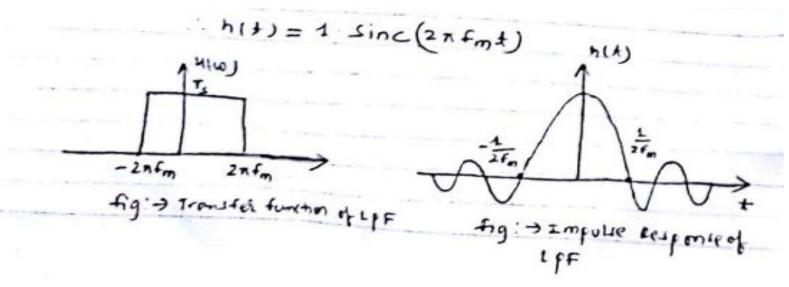
As the sampling is done at Nyquist rate

$$T_s = 1/2 f_m, 2f_m T_s = 1$$

 $h(t) = 1 * T_s Sinc(2\pi f_m t)$
 $h(t) = T_s Sinc(2\pi f_m t)$

Output of the filter is

- $x(t)=\sum x(nT_s) h(t-nT_s)$
- $x(t)=\Sigma x(nT_s) Sinc [2\pi f_m(t-nT_s)]$
- $x(t)=\sum x(nT_s) Sinc [2\pi f_m t-2\pi f_m nT_s)]$
- $x(t)=\Sigma x(nT_s)$ Sinc $[2\pi f_m t-n\pi)]$ is known as Interpolation formula
- Message or original signal can be recovered from the weighted sum of all sample value.

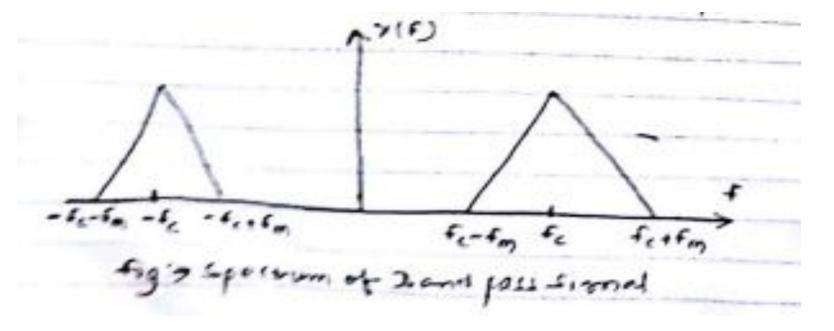


Effect of Under Sampling: Aliasing

- Continuous time band limited signal sampled at rate lower than the Nyquist rate($f_s < 2 f_m$)
- Aliasing effects occurs by overlapping of successive cycle of spectrum.
- Higher frequency overlaps or undertakes over lower frequency component.
- Low Pass Filter called prealias filter to limit band of frequency of the signal to f_m .
- Select sampling frequency $f_{s} \ge 2 f_{m}$.

Sampling of Band Pass Signal

- Also Known as Sub Sampling Theorem.
- Sampling Theorem of band pass signal x(t) can be recovered from its sample if it is sampled with minimum rate of twice of bandwidth.



Sampling of Band Pass Signal

- For bandwidth of spectrum of band pass signal of $2 f_m$.
- Sampling rate of band pass signal must be 4 f_m
 Signal x(t) can be expressed in terms of
 Inphase and Quadrature are expressed as

• $X(t)=x_{l}(t) \cos(2\pi f_{c}t) - x_{Q}(t) \sin(2\pi f_{c}t) - --(1)$

Sampling of Band Pass Signal

By solving
$$\infty$$

we get $x(t) = \sum x(\sqrt[n]{f_m}) \operatorname{Sinc}(2 \operatorname{fm} t - \frac{n}{2}) \operatorname{los}[2\pi f_c(t - \frac{n}{4f_m})]$

Compairing this lectors truction formula with low pass signals

 $x(t) = \sum x(n\tau_t) \operatorname{Sinc}[2\pi f_m t - n\pi]$
 $x(\frac{n}{4f_m}) = x(n\tau_s) = \operatorname{Sompleauelsim} of bandpass signal$
 $T_s = \frac{1}{4f_m}$

. Minimum Sampling rate = Twice of bandwidth = $4 \operatorname{fm}$

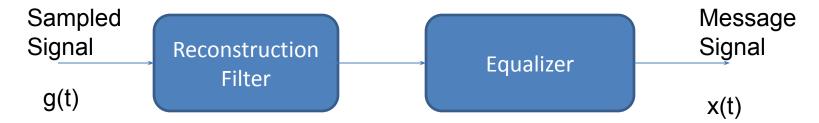
Aperture Effect

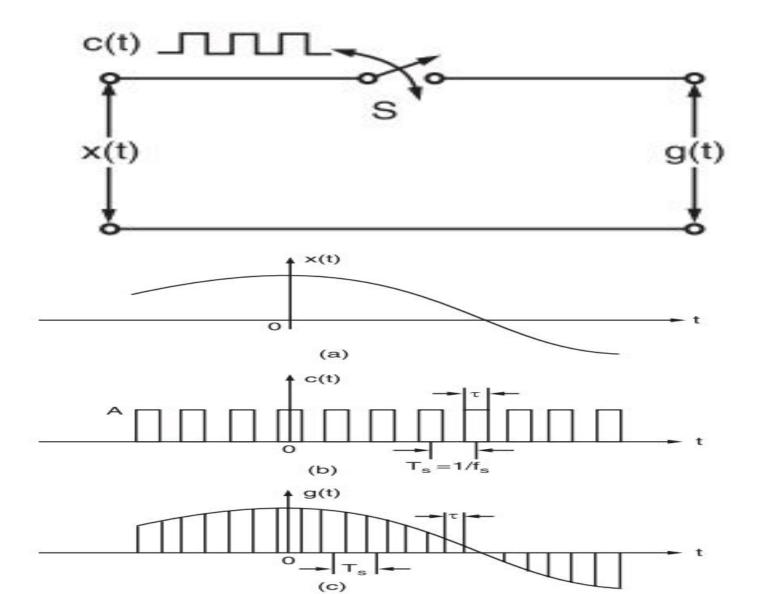
- Attenuation of upper portion of message signal spectrum is called Aperture Effect.
- It effects the high frequency component introducing Amplitude Distortion.
- It is depended upon the duration or pulse width of each sample (T).
- Large or greater value of pulse width 'T' introduces Aperture Effect.

Aperture Effect

Mitigation of Aperture Effect

- We use the pulse width 'T' or duration as low / small/narrow as possible.
- By use of Equalizer while Reconstruction, which will compensate attenuation caused by Low Pass Reconstruction Filter.
- Introducing Guard band between frequency.





- Natural Sampler is a practical method whose periodic pulse of sampling function c(t) is of width 'T'.
- Continuous Input signal x(t) is sampled at the rate of Sampling frequency satisfying Nyquist Criterion.
- Sampled Signal
- g(t)=x(t).C(t)----(1)

We know that the exponential Fourier series for any periodic waveform is

expressed as
$$\mathbf{c(t)} = \sum_{\mathbf{n} = -\infty}^{\infty} \mathbf{C_n} e^{j2\pi n t/T_0}$$

$$\mathbf{c(t)} = \sum_{\mathbf{n} = -\infty}^{\infty} \mathbf{C_n} e^{j2\pi f_s n t} \text{ with } \frac{1}{T_0} = f_s$$

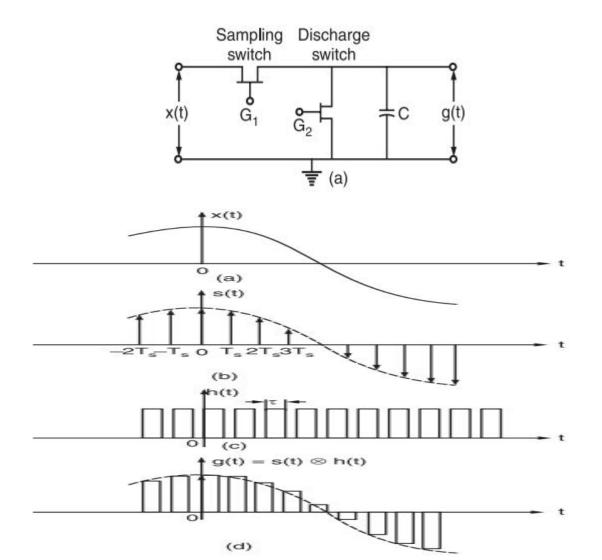
Since C(t) is rectangular pulse train

$$\begin{aligned} \mathbf{C_n} &= \frac{\tau.\mathbf{A}}{T_s} \cdot \sin \mathbf{c}(\mathbf{f_{n.}}\tau) \\ c(t) &= \sum_{n=-\infty}^{\infty} \frac{\tau.\mathbf{A}}{T_s} \cdot \sin \mathbf{c}(\mathbf{f_{n.}}\tau) e^{j2\pi f_s \cdot nt} \\ g(t) &= \frac{\tau \mathbf{A}}{T_s} \cdot \sum_{n=-\infty}^{\infty} \sin \mathbf{c}(\mathbf{f_{n.}}\tau) \cdot e^{j2\pi f_s nt}.\mathbf{x}(t) \end{aligned}$$

Taking Fourier Transform the spectrum of Natural Sampled signal

$$G(f) = \frac{\tau A}{T_s} \cdot \sum_{n = -\infty}^{\infty} \sin c(nf_{s.} \tau) X(f - nf_{s})$$

- The output sample has varying top in accordance with continuous time analog signal.
- Difficult to determine the shape of top of pulse.
- Amplitude detection at Reconstruction may not be exact.
- More susceptible of contamination of Noise.



$$\begin{split} g(t) &= s(t) \otimes h(t) \\ s(t) &= x(t) \cdot \delta_{T_s}(t) \\ \delta_{T_s}(t) &= \sum_{n = -\infty}^{\infty} \delta(t - nT_s) \\ s(t) &= \sum_{n = -\infty}^{\infty} \delta(t - nT_s) = \sum_{n = -\infty}^{\infty} x(nT_s) \cdot \delta(t - nT_s) \\ g(t) &= s(t) \otimes h(t) \\ g(t) &= \int_{-\infty}^{\infty} s(\tau)h(t - \tau) d\tau \\ g(t) &= \int_{-\infty}^{\infty} \sum_{n = -\infty}^{\infty} x(nT_s) \delta(\tau - nT_s)h(t - \tau) d\tau \\ g(t) &= \sum_{n = -\infty}^{\infty} x(nT_s) \int_{-\infty}^{\infty} \delta(\tau - nT_s)h(t - \tau) d\tau \end{split}$$

$$g(t) = \sum_{n=-\infty}^{\infty} x(nT_s) h(t - nT_s)$$

$$g(t) = s(t) \otimes h(t)$$

Taking Fourier transform of both sides of above equation, we get

$$G(f) = S(f) H(f)$$

We know that S(f) is given as

$$S(f) = f_s \sum_{n = -\infty}^{\infty} X(f - nf_s)$$

Therefore,

$$G(f) = f_s \sum_{n=-\infty}^{\infty} X(f - nf_s) \cdot H(f)$$

Thus, spectrum of flat top sampled signal:

$$G(f) = f_s \sum_{n = -\infty}^{\infty} X(f - nf_s) H(f)$$

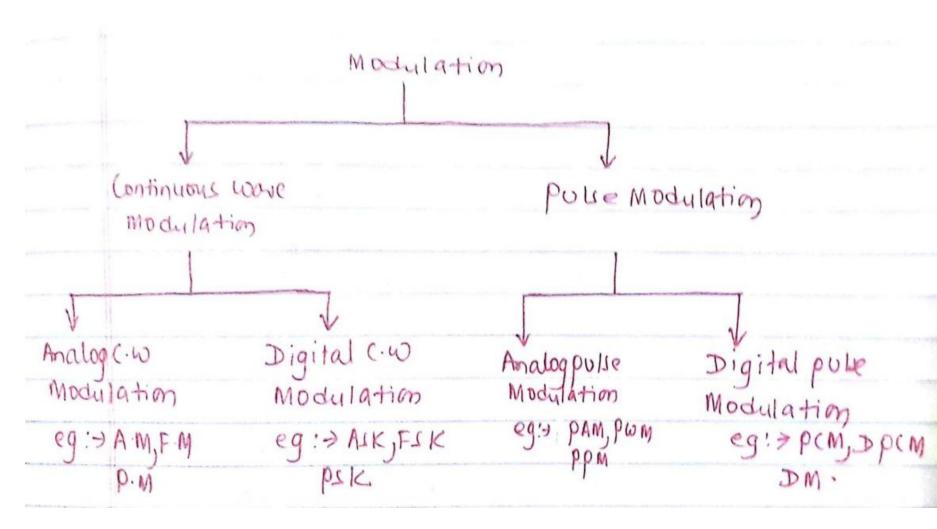
- The output sample has constant top in accordance with continuous time analog signal.
- Easy to determine the shape of top of pulse.
- More immune to Noise.
- Sample and Hold Circuit is used to get Flat Top Sampled.
- It consist of Two FET Switches and a Capacitor.

- Sampling Switch G1 is closed for short duration.
- Capacitor gets quickly charged up to voltage equal to the instantaneous sample value of the incoming signal x(t).
- Sampling switch G1 is opened. With the applied pulse to gate Discharge switch G2.
- Capacitor then gets discharged producing output of sample and Hold Circuit.

Chapter -3

Pulse Modulation System

Modulation



Pulse Modulation Systems

- In Pulse Modulation the carrier is pulse train instead of sinusoidal carrier.
- Characteristics or parameter of carrier signal is Amplitude, Width and Position which is changed w.r.t instantaneous value of modulating signal.
- PAM, PLM/PWM/PDM and PPM.
- Benefits of Pulse modulation: It Permits simultaneous transmission of several signals on time sharing basis. Time Division Multiplexing.

Pulse Amplitude Modulation(PAM)

- Amplitude of carrier of periodic train of rectangular pulse is changed in proportion to sample value of message signal.
- Flattop sampling is used over Natural Sampling.
- Flattop Sampling has better noise immunity over Natural Sampling.

Transmission Bandwidth of PAM

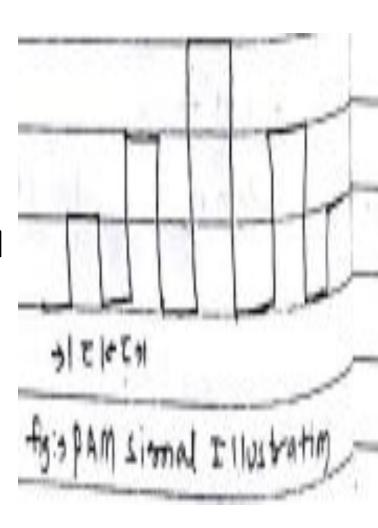
 Pulse duration is "T" is very small in comparision to sampling period "T_s" between two sample.

•
$$T << T_s ----(1)$$

- According to Sampling Theorem
- $f_{s} \ge 2 f_{m}$ ----(2)
- $1/T_{S \ge 2} f_{m}$ ----(3)
- $1/2 f_{m} \ge \ge T_{s} ----(4)$

Transmission Bandwidth of PAM

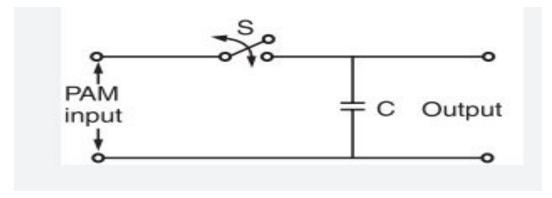
- From equation (1 & 3)
- $T << T_S \le 1/2 f_m$
- For both ON and OFF Time
- Maximum frequency of PAM
- $f_{max} = 1/T + T = 1/2T$
- Transmission bandwidth
- BW>> $f_{max} \ge 1/2T$



Demodulation(Reconstruction)



Block Diagram of PAM Demodulator



Holding Circuit (Zero-Order Holding Circuit)

Demodulation(Reconstruction)

- Recovering of the message signal from the modulated signal is called Reconstruction.
- Demodulation is done by Holding Circuit.
- Switch S is closed after arrival of pulse.
- Capacitor is charged to the pulse amplitude value and passed through LPF to recover the

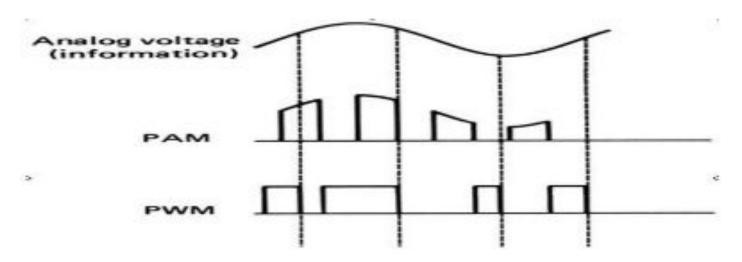
Holding circuit output

LPF output

modulating signal.

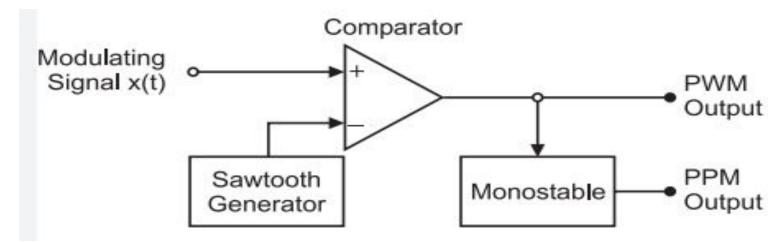
PLM/PWM/PDM

• In Pulse Length/Width/Duration Modulation the pulse width or length or duration is changed in proportion to the amplitude of the modulating signal.



PLM/PWM/PDM

- Saw tooth Generator generates saw tooth signal of frequency f_s sampling frequency
- Message/Modulating signal x(t) is applied to Non Inverting Terminal of comparator.
- Output of Comparator is PLM/PWM/PDM.



PLM/PWM/PDM

Advantages:-

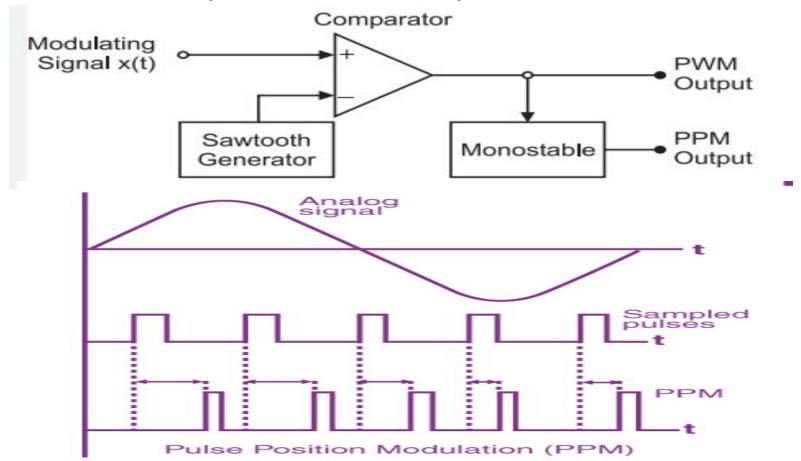
- Better Noise Immunity.
- Synchronization between Tx and Rx is not required.
- Possible to reconstruct the signal from Noise.

Disadvantages:-

- Requires large Bandwidth compared to PAM Signal.
- Tx must handle the power content of pulse with maximum width.

Pulse Position Modulation(PPM)

- Amplitude and Width is Kept Constant.
- Position of each pulse is changed with respect to the amplitude of sampled Value.



Pulse Position Modulation(PPM)

- Pulse Width Modulated signal:
- Output of Comparator is fed to monostable multivibrator.
- Multistable Vibrator is negative edge triggered.
- Pulse position modulated signal is obtained at the falling edge of triggering clock Pulse.

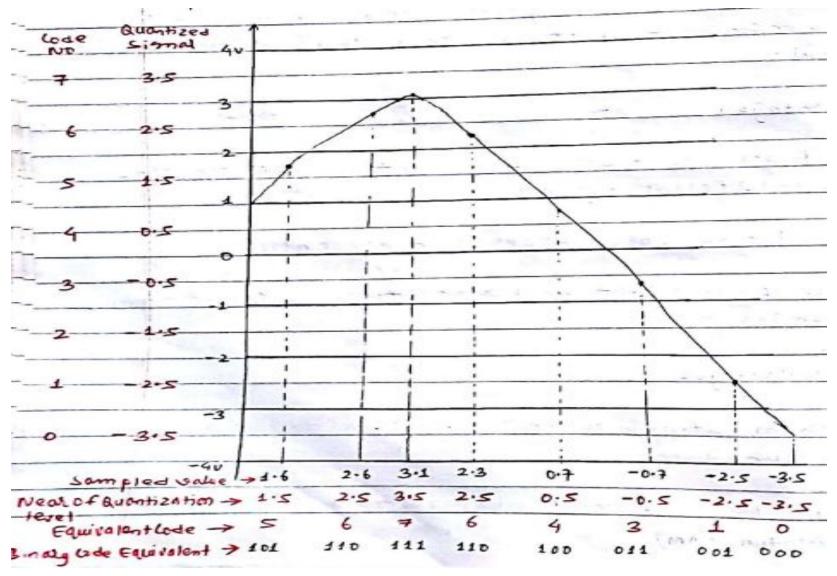
Pulse Position Modulation(PPM)

Advantages:-

- PPM has less interference of noise.
- Separation of Signal and Noise is easy.
- Pulse length/Pulse amplitude is constant:
 Requirement of transmission power is same.

Disadvantages:-

- Synchronization between Tx and Rx is required.
- Large / More bandwidth is required as compared to PAM.



- Digital Pulse modulation Technique.
- Analog signal is sampled and converted into digital encoded signal.
- Encoded signal is represented with n-bit binary code.
- Three basic operation in PCM
- Sampling
- Quantization
- Encoding

- Quantization:- Process of representing analog sampled values to a finite set of level.
- Finite set of level is a discrete amplitude value from 0 to maximum level.
- Two types of Quantization:-
- Uniform Quantization.
- Non Uniform Quantization.

Uniform Quantization:-

- Quantization level are uniformly spaced.
- Same step size.
- Input is divided into interval of equal size.
- Two types of Uniform Quantization
- Mid Rise type Quantizer Mid Tread Quantizer

Mid Rise Quantizer:

- Origin lies in the middle of a raising part of the stair-case like graph.
- The quantization levels are even in number.

Mid Tread Quantizer:-

- Origin lies in the middle of a tread of the stair-case.
- Quantization levels are odd in number.

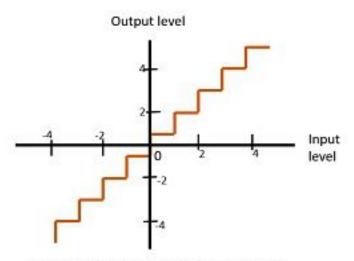


Fig 1: Mid-Rise type Uniform Quantization

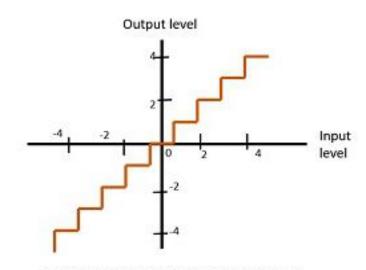


Fig 2 : Mid-Tread type Uniform Quantization

Non Uniform Quantization:-

- Step size is not same and fixed.
- Step size is small or reduced for small amplitude or weak signal.
- Step size is increased or big for large amplitude or strong signal.
- Non Uniform Quantization is achieved practically by Companding. (Improves SQNR).

Companding

- Process of compressing signal at the Transmitter (Tx) side.
- Expansion on the Receiver(Rx) Side.
- Improves the SQNR.
- Two types of Companding Technique:-
- μ Law Companding.
- A Law Companding.

μ Law Companding

- Compressor Characteristics is Continuous.
- Approximately linear for small Value of input level.
- Approximately logarithmic for high input level.
- Compressed Output is given as

$$|v| = \log(1 + \mu |x| / x_{max}) / \log(1 + \mu)$$

V= Normalized Compressed Output voltage.

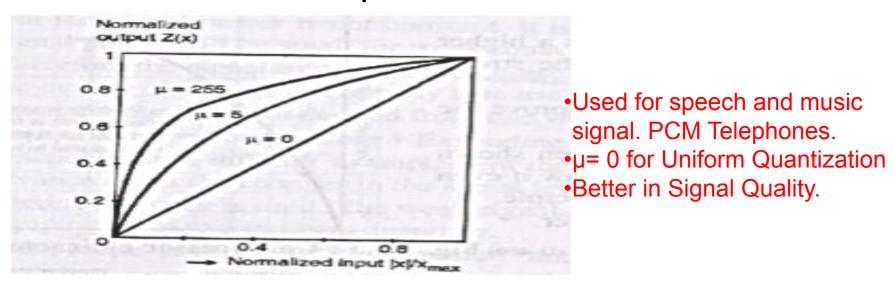
 μ = Parameter to define amount of compression

x_{max} = Maximum Value

 IxI/x_{max} = Normalized value of Input W.r.t maximum Value.

μ Law Companding

- American Standard. U.S, Canada and Japan.
- Compressor Characteristics neither strictly Linear nor strictly Logarithmic.
- Practical value of μ =255.



Compressor Characteristics of a µ Law Compressor

A Law Companding

- Compressor Characteristics is Piecewise.
- Linear segment for low level input.
- Logarithmic curve for high level input.

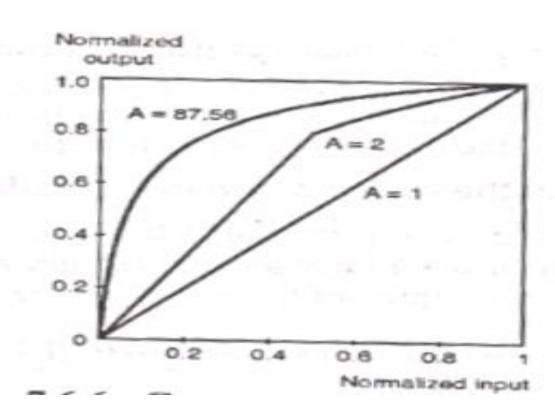
```
IVI = \log(1 + A |x|/x_{max}) / 1 + \log A for 1/A \le |x|/x_{max} \le 1
IVI = A |x|/x_{max}) / 1 + \log A for 0 \le |x| \le 1/A
V= Normalized Compressed Output voltage.
```

A = Parameter to define amount of compression

```
x<sub>max</sub> = Maximum Value
```

 IxI/x_{max} = Normalized value of Input W.r.t maximum Value.

A Law Companding



- -European Standard used in Europe and rest of the world.
- -Used in PCM Telephone System.

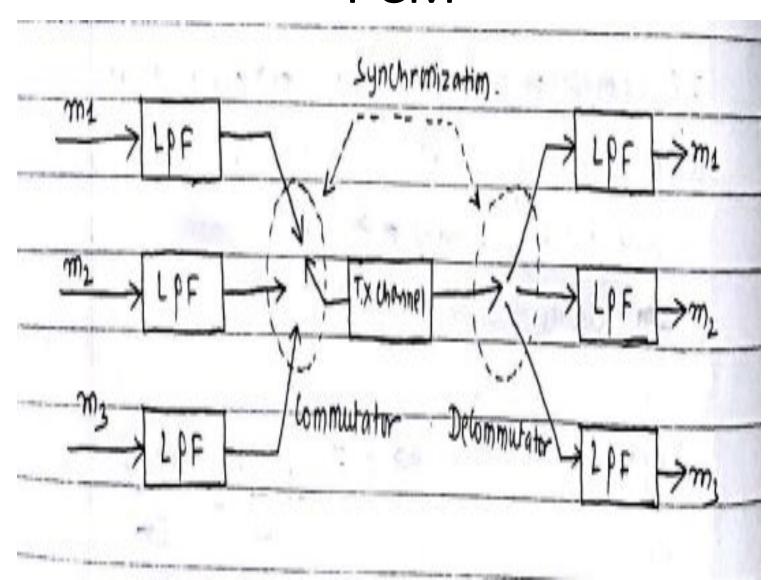
Necessity of Non Uniform Quantization for Speech Signal

- Crest factor = Peak Value of signal/ rms value of signal.
- X(t) is the input to quantizer with its amplitude
 -X_{max} to + X_{max}
- Peak Value of Signal= X_{max}
- rms value of signal= $\sqrt{X^2}$ (t)
- Power is defined as P= X² (t)/R
- For normalized power R=1

Necessity of Non Uniform Quantization for Speech Signal

- $P = X^2(t)$
- Crest factor = $X_{max} / \sqrt{X^2}$ (t)
- For normalized signal x(t) has $X_{max} = 1$
- Crest factor = $1 / \sqrt{X^2}$ (t)
- Crest factor = $1/\sqrt{P}$
- P<<1 will decrease the SQNR.

Time Division Multiplexing with PCM



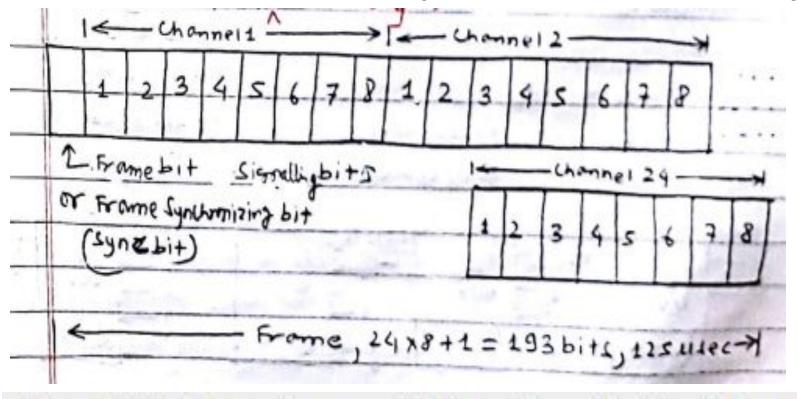
Time Division Multiplexing with PCM

- In Time Division Multiplexing, samples of messages are transmitted at some fixed interval of time.
- Samples of signal are transmitted serially and recovered separately on destination.
- Commutator takes low pass filtered signal sequentially at fixed interval of time over same channel.

Time Division Multiplexing with PCM

- Decommutator at receiving end separates the signal.
- Commutator and Decommutator are synchronized
- Low Pass Filter(LPF) at the receiving end converts the sampled signal into original signal.

T1 TDM-PCM Telephone Hierarchy



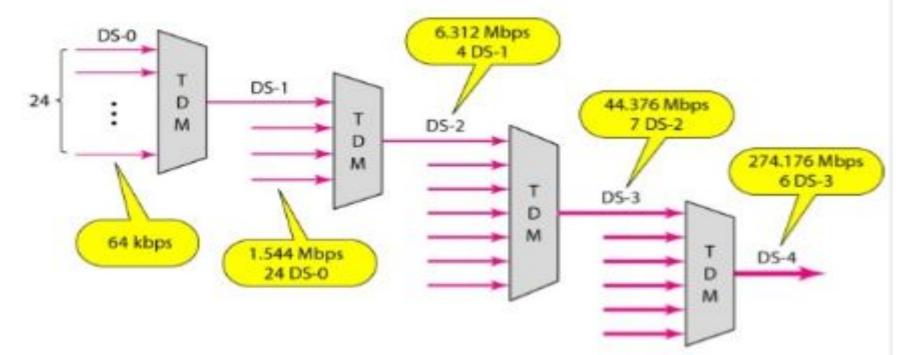
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T1 = 8000 frames/sec x ((24 x 8) + 1) bits/frame
= 1544000 bits/sec
= 1.544 Mbps
```

T1 TDM-PCM Telephone Hierarchy

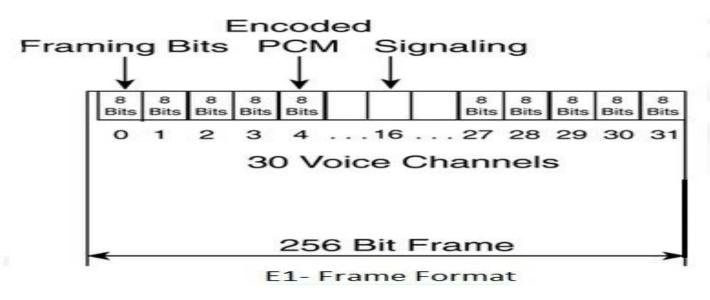
- T1 System is North American digital multiplexing standard recognized by ITU-T.
- 24 voice channel band limited to 300-3400 MHz.
- Sampling frequency of 8 KHz.
- Each Sample converted to 7 bit word and 1 bit is reserved for synchronization.
- Similarly there are other standard of T1 as:-

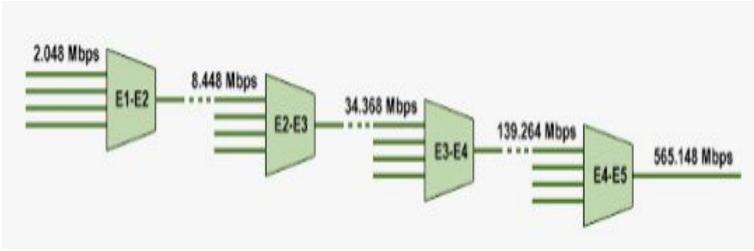
T1 TDM-PCM Telephone Hierarchy

Standard	Channel	Signaling Rate
T2 = 4*T1	96 Channel	6.312 Mbps
T3 = 7 * T2	672 Channel	44.736 Mbps
T4 = 6 * T3	4032 Channel	274.176 Mbps
T5 = 2 * T4	8064 Channel	560.16 Mbps



E1 TDM-PCM Telephone Hierarchy





E1 TDM-PCM Telephone Hierarchy

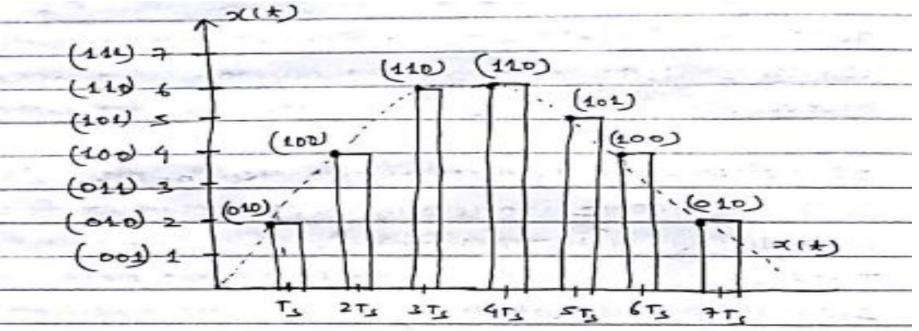
- E1 System is European digital multiplexing standard recognized by ITU-T.
- 32 voice channel band limited to 300-3400 MHz.
- Sampling frequency of 8 KHz.
- Each frame is divided into 32 equal time slot.
- Two time slot is reserved for Signaling & Controlling.

E1 TDM-PCM Telephone Hierarchy

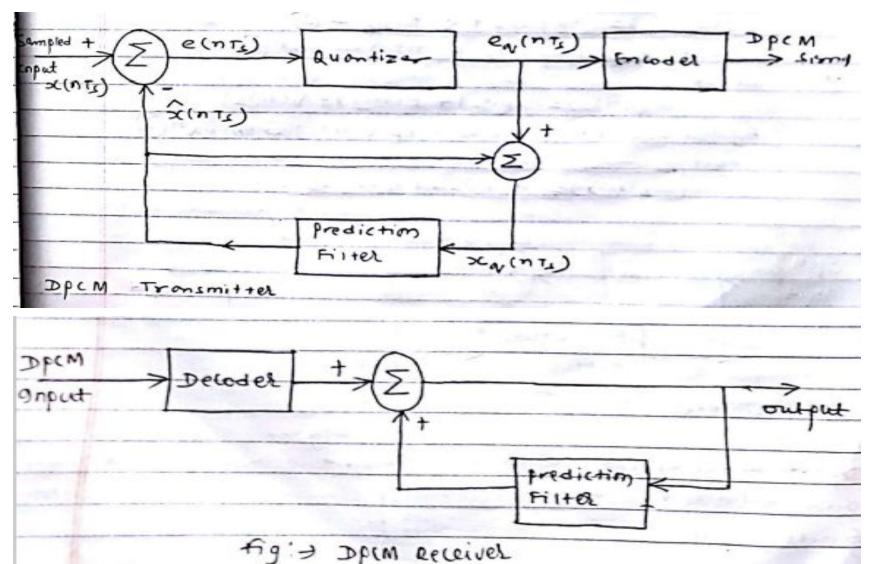
- Bit rate = 32*8 bits/frame * 8000 sample/sec
- Bit Rate = 2.048 Mbps.
- Other standards

Standard	Channel	Signaling Rate
E2 = 4*E1	120	8.448 Mbps
E3 = 4*E2	480	34.368 Mbps
E4 = 4*E3	1920	139.264 Mbps

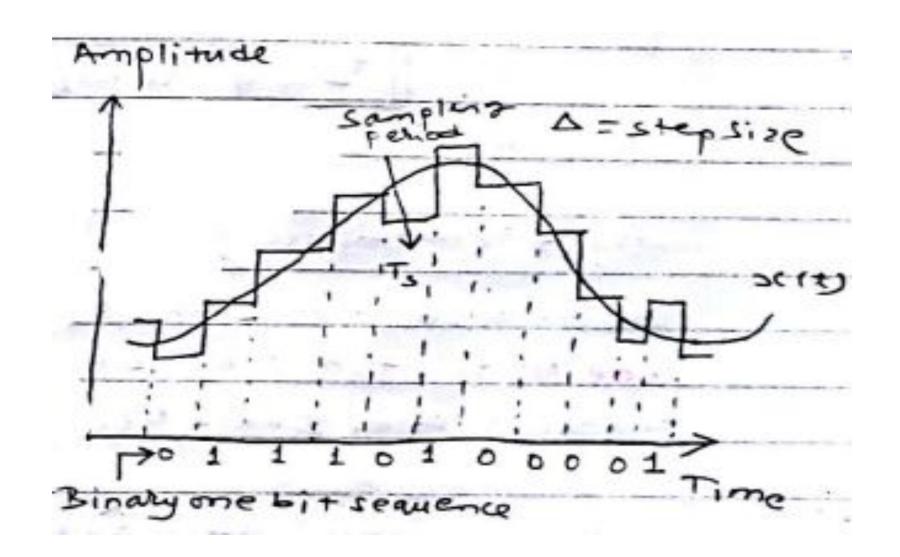
- Each sample is quantized in independent manner in PCM.
- Previous sample value has no effect on quantization of new sample.



- Samples taken at 3Ts and 4Ts are encode with same value (110).
- Single sample can be send in DPCM.
- Samples at 5Ts and 6Ts @ Difference between sample is last bit only.
- Two repeated bit(Redundant bit) can be removed and only the difference third bit can be send to represent the whole sample value.

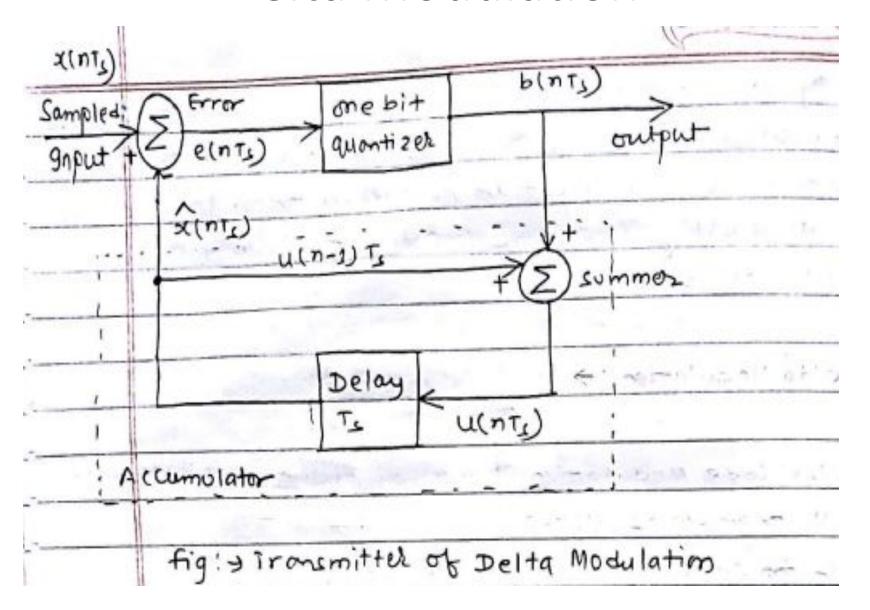


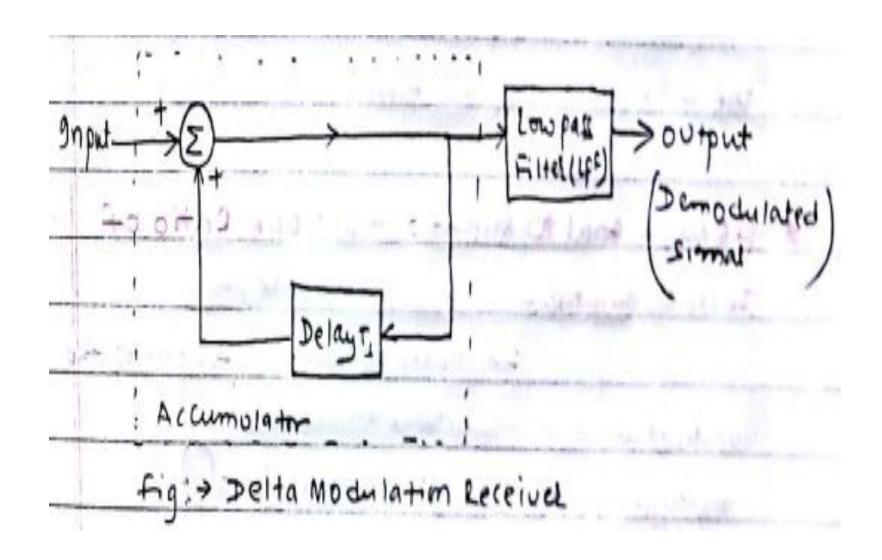
- DPCM works on the principle of prediction.
- Present Sample is predicted on the basis of past sample.
- Prediction may not be exact.
- Very Close to actual sample value.



- Delta modulation transmits one bit per sample.
- DPCM works on the principle of Comparison.
- Present Sample is compared with the previous sample value.
- Present sample value is smaller than previous sample value : defined by $-\Delta$ level and "0" is transmitted.

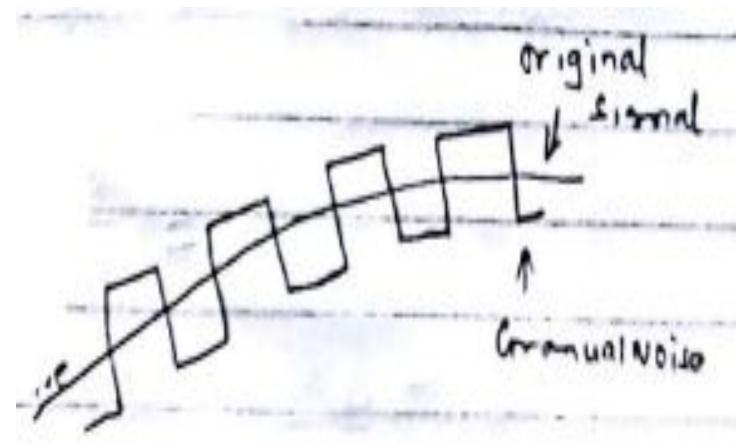
- Present sample value is smaller than previous sample value : defined by $+\Delta$ level and "1" is transmitted.
- It is staircase approximation of the input waveform.
- Each Step is represented by 1 for the rise of step.
- Each Step is represented by 0 for the fall of step.





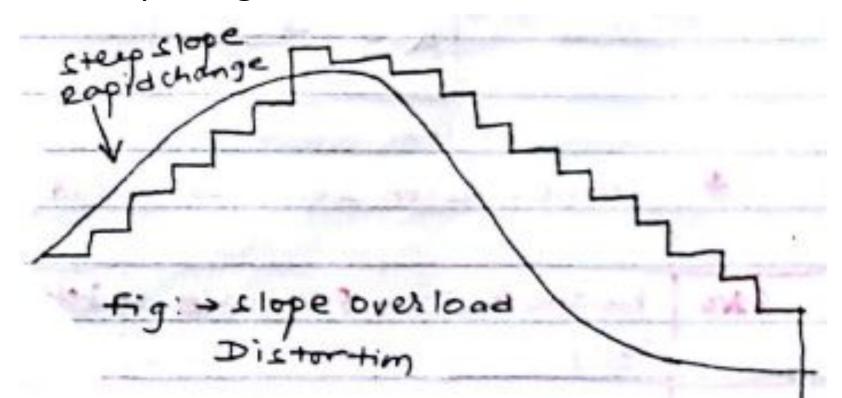
Quantization Noise in Delta Modulation

 Granual noise is introduced if the step size is very large compared to the input signal.



Quantization Noise in Delta Modulation

 Slope Overload Distortion is introduced if the input signal slope is very large compared to the input signal.



Parametric Speech Coding Vocoders, Linear Prediction Coding

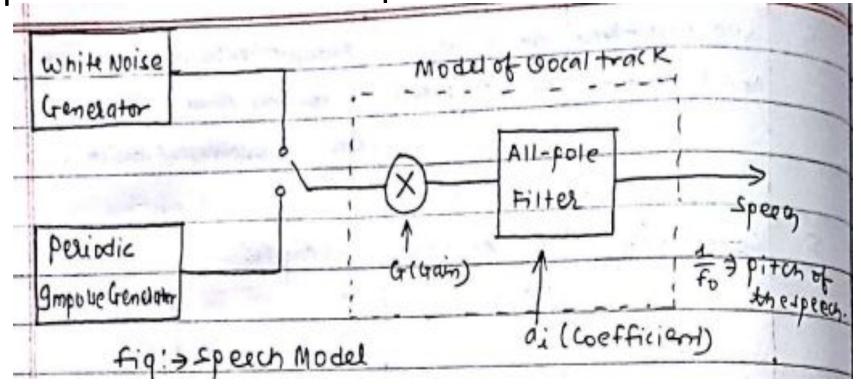
- Digital Speech coders classified into two categories:-
- Waveform Coder: Uses Algorithm to encode and decode.
- Output is the approximation of the input.
- Provides high quality of signal but requires relatively high bandwidth / bit rate.

Parametric Speech Coding Vocoders, Linear Prediction Coding

- VoCoder:-
- Encode the speech signal by modeling the signal extracting set of parameters.
- Original voice is predicted using these parameters extracted at the transmitter.
- This technique of coding of speech is Linear Prediction Coding (LPC).
- It requires relatively less bandwidth / bit rate.

Parametric Speech Coding Vocoders, Linear Prediction Coding

 VoCoder: Speech signal is modeled with parameter like repetition frequency "Fo", all pole filter "Ao" Gain parameter "G".



Unit-3

Thank you