Assignment 3 - Jupyter Notebook

Yogesh Agarwala
EE19B130

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[ ]:
```
"""
Before running this notebook:
1. Generate fitting.dat file by running generate_data.py␣
↪code
2. Make sure fitting.dat and this notebook are in the␣
↪same folder
"""
```

[2]:
```
import numpy as np
import matplotlib.pyplot as plt
import scipy.special as sp
```

0.0.1 Q2. Reading data from files and parsing them

[3]:
```
filedata = np.loadtxt('fitting.dat')
time = filedata[:,0]
data = filedata[:,1:]
```

0.0.2 Q3. Plotting the data

[4]:
```
# Plotting
x=time
y=data
plt.grid()
plt.plot(x,y)
plt.xlabel(r't$\rightarrow$',fontsize=12)
plt.ylabel(r'f(t)+noise$\rightarrow$',fontsize=12)
plt.show()
```

output_7_0.png

0.0.3 Q4. Fitting a Function to this data

[5]:
```
def g(t,A,B):
return A*sp.jn(2,t) + B*t
```

[6]:
```
# Plot of the Fitting Function
A=1.05
B=-0.105
plt.grid()
plt.plot( time , g(time,A,B),'-k',label='True curve')
plt.xlabel(r't$\rightarrow$',fontsize=12)
plt.ylabel(r'f(t)$\rightarrow$',fontsize=12)
plt.show()
```

output_10_0.png

[7]:
```
plt.figure(figsize=(8,6))
sigma = np.logspace(-1,-3,9)

#Different Noise Levels
for i in range(9):
plt.plot(x,y[:,i],label=f'$\sigma_{i+1}$ = %.3f'%sigma[i])

# Plot of the Fitting Function
A=1.05
B=-0.105
plt.grid()
plt.plot( x , g(x,A,B),'-k',label='True curve')
plt.title(r'Plot of Different Noise Levels and Fitting Function')

plt.xlabel(r't$\rightarrow$',fontsize=15)
plt.ylabel(r'f(t)+noise$\rightarrow$',fontsize=15)
plt.legend(loc='upper right')
plt.show()
```

output_11_0.png

0.0.4 Q5. The Errorbar plot

[8]:
```
data = y[:,0]
plt.grid()
plt.plot(time,g(time,1.05,-0.105),'b',label='f(t)')
plt.errorbar(time[::5],data[::5],sigma[0],fmt='ro',label='Errorbar')
plt.legend(loc='upper right')
plt.title('Data points for $\sigma$ = ' + str(sigma[0]) + ' along with exact function')
plt.xlabel(r't$\rightarrow$',fontsize=15)
plt.show()
```

output_13_0.png

0.0.5 Q6. The Matrix Equation

[9]:
```
# construct M matrix
fn_column = sp.jn(2,time)
M = np.c_[fn_column,time]

# parameter matrix
A = 1.05; B = -0.105
p = np.array([A,B])

# column vector obtained by multiplication of matrix M and p

G1 = np.matmul(M,p)
```

[10]:
```
# column vector obtained directly from the function g(t,A,B)
```

```
G2 = np.array(g(time,A,B))
```

[11]:
```
# testing equality
if np.array_equal(G1,G2):
print('Yes, the above two column vectors are equal.')
else:
print('No, the above two column vectors are not equal.')
```

```
Yes, the above two column vectors are equal.
```

0.0.6 Q7. Mean Squared Error

[12]:
```
y_data = G1 #first column of data
y_actual = G2 #actual model

error = (np.square(y_data - y_actual)).mean()
print("Mean square error in calcutaion of M = ",error)
```

```
Mean square error in calcutaion of M =  0.0
```

0.0.7 Q8. Contour Plot of Error

[13]:
```
#initialization
e = np.zeros((21,21,9))
A = np.linspace(0,2,21)

B = np.linspace(-0.2,0,21)

for k in range(9):
f = y[:,k]
for i in range(21):
for j in range(21):
e[i][j][k] = np.sum((f -np.array(g(time,A[i],B[j])))**2)/
↪101
```

[14]:
```
# plotting the contour and locating the minima
plot = plt.contour(A,B,e[:,:,0],20)
plt.title('Contour plot of error')
plt.xlabel(r'A$\rightarrow$',fontsize=12)
plt.ylabel(r'B$\rightarrow$',fontsize=12)
plt.clabel(plot,inline=1,fontsize=10)

# Using np.unravel_index to obtain the location of the␣
↪minima in the original array
a = np.unravel_index(np.argmin(e[:,:,0]),e[:,:,0].shape)
plt.plot(A[a[0]],B[a[1]],'ro',markersize=7)
plt.annotate('(%0.2f,%0.
↪2f)'%(A[a[0]],B[a[1]]),(A[a[0]],B[a[1]]))
```

```
plt.show()
```

output_22_0.png

0.0.8 Q9. Best estimate of A and B (least mean square estimation)

[15]:
```
def estimateAB(M,b):
return np.linalg.lstsq(M,b,rcond=None)

def error_prediction(estimated,actual):
A0,B0 = actual[0], actual[1]
A1,B1 = estimated[0], estimated[1]
return abs(A0-A1), abs(B0-B1)
```

[16]:
```
# construct M matrix
fn_column = sp.jn(2,time)
M = np.c_[fn_column,time]
```

[17]:
```
AB = [1.05, -0.105]
estimatedAB,_,_,_ = estimateAB(M,y[:,1]) #for first␣
↪column data

print("Estimated A,B  = ",list(estimatedAB))

errorA, errorB = error_prediction(estimatedAB,AB)
print("Error in A,B = ", [errorA, errorB])
```

```
Estimated A,B  =  [1.0598311905174036, -0.10454165768706138]
Error in A,B =  [0.009831190517403554, 0.00045834231293861993]
```

0.0.9 Q10. Error vs σ_n plot on *linear* scale

[18]:
```
"""
error in the estimate of A and B for different data␣
↪columns
"""
error_a = []
error_b = []
mean_error = []
for i in range(9):
estimatedAB,error,_,_ = estimateAB(M ,y[:,i])
```

```
        error_a.append(error_prediction(estimatedAB,AB)[0])
        error_b.append(error_prediction(estimatedAB,AB)[1])
        mean_error.append(error)
```

[19]:
```
        plt.grid()
        plt.plot(sigma,error_a,'bo--',label='Aerr')
        plt.plot(sigma,error_b,'ro--',label='Berr')
        plt.title("Variation of Aerr and Berr with Noise")
        plt.xlabel(r'$\sigma_{n}\rightarrow$',fontsize=15)
        plt.ylabel(r'Aerr and Berr$\rightarrow$',fontsize=12)
        plt.legend(loc='upper left')
        plt.show()
```

output_29_0.png

0.0.10 Error returned by lstsq vs Noise on *linear* scale

[20]:
```
        plt.grid()
        plt.plot(sigma,mean_error, 'bo--')
        plt.title("Variation of Error returned by Lstsq with Noise")
        plt.xlabel(r'$\sigma_n\rightarrow$',size=15)
        plt.ylabel(r'MS Error$\rightarrow$',size=12)
        plt.show()
```

output_31_0.png

0.0.11 Q11. Error vs σ_n plot in *loglog* scale

[21]:
```
        plt.grid()
        plt.loglog(sigma,error_a,'ro', label='Aerr in logscale')
        plt.loglog(sigma,error_b,'bo', label='Berr in logscale')
        plt.errorbar(sigma,error_a,yerr=0.1,fmt ='ro')
```

```
                        plt.errorbar(sigma,error_b,yerr=0.1,fmt ='bo')
                        plt.title('Variation of Aerr and Berr with Noise in␣
↪logscale')
                        plt.xlabel(r'$\sigma_{n}\rightarrow$',fontsize=15)
                        plt.ylabel(r'Aerr and Berr$\rightarrow$',fontsize=12)
                        plt.legend(loc='upper right')
                        plt.show()
```

output_33_0.png

0.0.12 Error returned by Lstsq with Noise in *loglog* scale

[22]:
```
                        plt.grid()
                        plt.loglog(sigma,mean_error, 'b--',basex = 10)
                        plt.scatter(sigma,mean_error)
                        plt.title("Variation of Error returned by Lstsq with␣
↪Noise on loglog scale")
                        plt.xlabel(r'$\sigma_n\rightarrow$',size=15)
                        plt.ylabel(r'MS Error$\rightarrow$',size=12)
                        plt.show()
```

output_35_0.png