

Roll No. ...62111...

Total No. of Questions : 9]
(2042)

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**BCA (CBCS) RUSA IInd Semester
Examination**

3743

MATHEMATICS-II

Paper : BCA-0201

Time : 3 Hours]

[Maximum Marks : 70

Note :- Attempt one question from each Unit. Q. No. 9 is compulsory.

Unit-I

Q.1.

- (a) Verify Lagrange's mean value theorem for the function $f(x) = (x - 2)(x - 3)(x - 4)$ in the interval $[0, 4]$. Also find the value of 'C'.

- (b) If $y = (ax + b)^m$ and $y_n = \frac{d^n y}{dx^n}$, show that :

$$y_n = m(m - 1)(m - 2) \dots (m - n + 1)$$

$$(ax + b)^{m-n} a^n \quad 5,5$$

CH-710

(1)

Turn Over

2. (a) By using mean value theorem find the approximate value of $\sqrt{66}$.

(b) Apply Leibnitz theorem to find the third order derivative of :

$$f(x) = (x^2 + 1)e^{2x} \text{ at } x = 0 \quad 5.5$$

Unit-II

3. (a) Find the greatest common divisor of 275 and 200 and express it in the form $m.275 + n.200$.

(b) Show that the relation of divisibility in the set of integer is reflexive, transitive but not symmetric. 5.5

4. (a) Prove that if a and b be two integers, then $a \equiv b \pmod{m}$ if and only if a and b has the same remainder when divided by m .

(b) For positive integer a and b show that :
 $\text{GCD}(a, b) \times \text{LCM}(a, b) = (a \times b) = ab \quad 5.5$

Unit-III

5. (a) Show that the set of all 2×2 non-singular matrices from an infinite non-abelian group under the composition of matrix multiplication.

CH-710 (2)

(b) Show that the set $G = \{1, \omega, \omega^2\}$ of cube roots of unity from a finite abelian group of order 3 under multiplication of complex number. 5.5

6. (a) Let $M_g(I) = \left\{ \begin{bmatrix} a, b \\ c, d \end{bmatrix} \right\}$ where $a, b, c, d \in I$, show that $M_g(I)$ from a monoid under the operation of matrix multiplication.

(b) Define a cyclic group and prove that every cyclic group is abelian but converse is not true. 5.5

Unit-IV

7. (a) Prove that the set of integer is a ring with respect to usual addition and multiplication.

(b) Prove that $\langle R, +, \cdot \rangle$ where R is set of all reals, is a commutative ring with unity. 5.5

8. (a) Let R be a ring. Then show that the following conditions are equivalent :

- (i) R has no zero divisor
- (ii) R satisfies left cancellation law
- (iii) R satisfies right cancellation law

CH-710 (3)

Turn Over

- (b) Show that the set of rationals 'Q' is a field under composition of addition \oplus and multiplication \odot , given as :

$$a \oplus b = a + b - 1 \quad \text{and} \quad a \odot b = a + b - ab$$

5,5

Unit-V

(Compulsory Question)

- 9 (i) Discuss applicability of Rolle's theorem for the function $f(x) = |x|$ in $[-3, 3]$.
- (ii) If $f(x) = x^2 \sin 2x$, find the value of $f'''(0)$.
- (iii) If a/b and a/c , then show that $a/(bx + cy) \forall x, y \in \mathbb{Z}$.
- (iv) Solve the following congruence $3x \equiv 4 \pmod{5}$.
- (v) Find the LCM of (272, 1479).
- (vi) Define a group.
- (vii) Show that the set $G = \{1, 2, 3, \dots, n-1\}$ does not form a group under multiplication modulo n , where 'n' is a composite number.
- (viii) Let R bearing such that $x^2 = x \forall x \in R$, show that R is a commutative ring.
- (ix) Define a ring and a ring with unity.
- (x) Prove that every field is an integral domain.

3×10=30