

AGENDA

- Stacks Basics
- Remove duplicates
- Sort stack
- Infix to Postfix
- Postfix Evaluation

Stacks

LIFO :

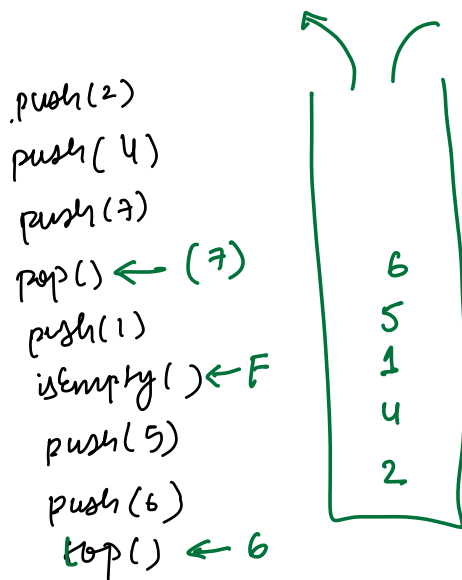
A data structure in which element inserted at last .
is the first one to come out

Applications

- 1) UNDO / REDO
- 2) Browser Tabs
- 3) Recursion
- 4) Expression Evaluation
- 5) Balanced Parenthesis

Functionalities

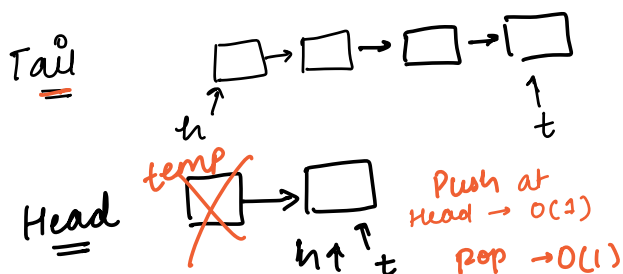
- 1) $\text{push}(x)$: pushes an ele on top of stack
- 2) $\text{pop}()$: deletes the ele from top of stack
- 3) $\text{peek}()/\text{top}()$: returns the ele present on top of stack.
- 4) $\text{isEmpty}()$: returns T/F depending on stack is empty / full.



Implementation → Arrays.

→ Linked List

$\text{push}(x) \quad // O(1)$
 $\text{pop}() \quad // O(1)$



push $\rightarrow O(1)$
pop $\rightarrow O(N)$

Node newNode = new Node(x)
 newNode.next = head
 head = newNode

Q.

Walmart | Google | BiKayi

Given a string, remove every pair of consecutive duplicates until there are no consecutive duplicates.

s: acbbck
ack
[ak] ans

s: aaab
[ab]

s: abckkc b a m
abcc b a m
abb a m
aa m
m.

s: ababab
↓
ababab ≡

s: acrbck
acrcK

Palindrome

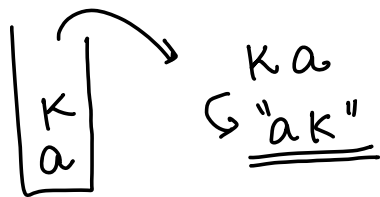
aa r bbxx r aca

Try to implement

↓ ↓ ↓ ↓ ↓ ↓
a c b b c k

TC: $O(N)$

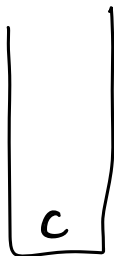
SC: $O(N)$



Follow up questions

Remove all duplicated characters.

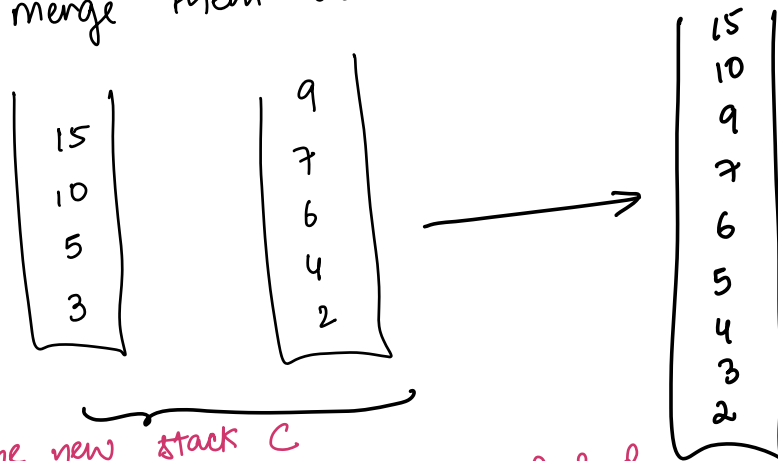
b a a a b b c
↑ ↑ ↑ ↑ ↑ ↑ ↑



flag = ~~F~~ ~~F~~ ~~F~~ F F

a a x x x b b x x x a c a
↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

Que. Given 2 sorted stacks.
merge them into one sorted stack



Take the new stack C
Compare top ele on both stacks A & B
Push the bigger ele on top of stack.



TC: $O(N+M)$

SC: $O(N+M)$ [Give good explanation for it]

If LL: $O(1)$

If arrays: $O(N+M)$

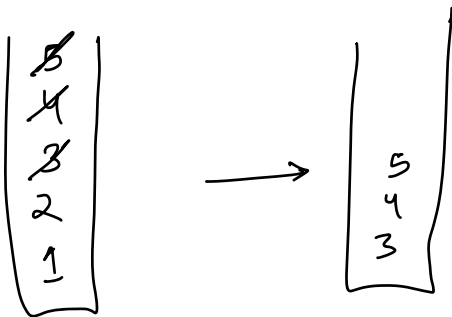
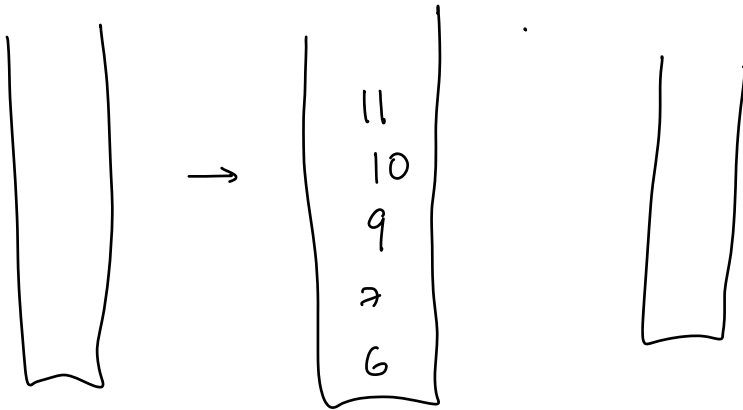
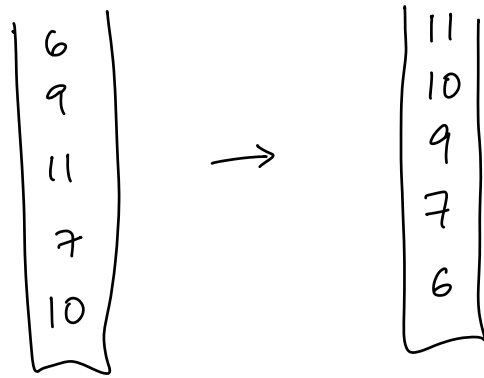
Merge the two stacks into one.

```
stack<int> merge (stack<int> A,  
                  stack<int> B) {
```

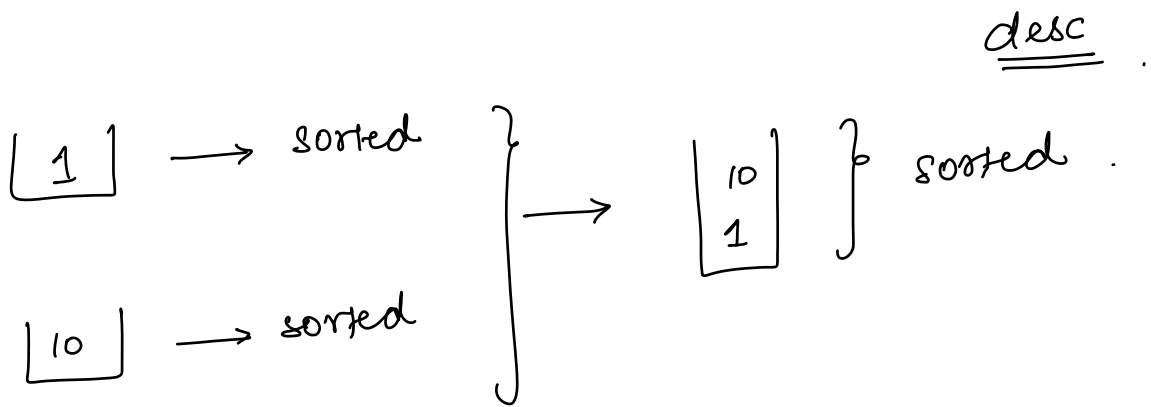
```
    stack<int> C;  
    while (A.size() > 0 && B.size() > 0) {  
        if (A.top() > B.top()) {  
            C.push(A.pop());  
        }  
        else {  
            C.push(B.pop());  
        }  
    }  
    while (A.size() > 0) {  
        C.push(A.pop());  
    }  
    while (B.size() > 0) {  
        C.push(B.pop());  
    }  
    C = reverse(C);  
    return C;
```

```
}
```

Q. Given an unsorted stack, sort it.



TC: $O(N^2)$



Merge Sort

```

mergeSort ( data ) {
    d1 = first half
    d2 = second half
    mergeSort ( d1 )
    mergeSort ( d2 )
    return merge ( d1 , d2 )
}
  
```

```

stack<int> mergeSort ( stack<int> A ) {
    if ( A.size() <= 1 ) return A
    stack<int> B
    S = A.size()
    for ( i = 0; i < ( S / 2 ); i++ ) {
        B.push ( A.pop() );
    }
    A = mergeSort ( A )
    B = mergeSort ( B )
    return merge ( A, B )
}
  
```

	A.size() / 2		
0	8/2	4	(1)
1	/2	3	(2)
2	/2	3	(3)
3	/2	2	

TC:

$$T(N) = 2T(N/2) + N$$

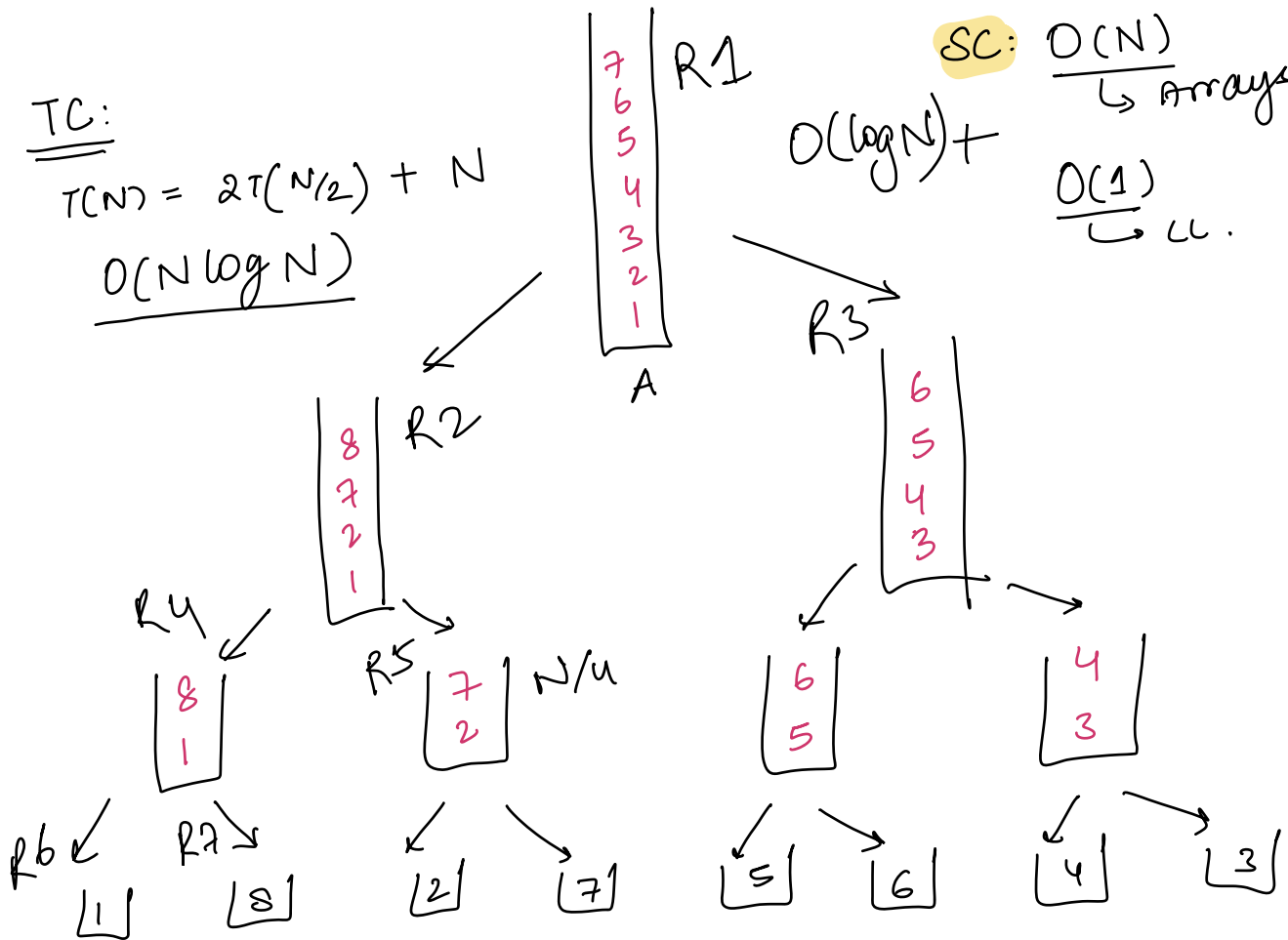
$$\underline{O(N \log N)}$$

SC: $\underline{O(N)}$
↳ Arrays

$$O(\log N) +$$

$$\underline{O(1)}$$

↳ LL.



Break

11:00 PM

Expression Evaluation

$$7 \times 1 + 2 - 8 \times 3 + 10 / 5$$

$$7 + 2 - 24 + 2$$

$$9 - 24 + 2$$

$$-15 + 2$$

$$-13$$

$$\begin{array}{c} \uparrow / * \int \text{L to R} \\ \downarrow + - \int \text{L to R} \end{array}$$

Infix Expressions

$$A + B$$

$$A - B$$

$$A / B$$

$$A * B$$

Post Fix Expression

$$A B +$$

$$A B -$$

$$A B /$$

$$A B *$$

$$\begin{array}{l} A + B \times C \\ \underline{A} + \underline{BC * } \\ A B C * + \end{array}$$

Infix \rightarrow Postfix
Postfix \rightarrow Ans.

Quiz 1

$$4 + 8 * 7$$

$$4 + 87 *$$

$$487 * +$$

QUIZ 2

$$10 + 3 * 4 - 7$$

$$10 + 34 * - 7$$

$$10 \ 3 \ 4 \ * \ + \ - \ 7$$

$$10 \ 3 \ 4 \ * \ + \ 7 \ -$$

QUIZ 3

$$10 / (4 - 2) * 6 + 9$$

$$10 / 42 - * 6 + 9$$

$$10 \ 4 \ 2 \ - \ / \ * \ 6 \ + \ 9$$

$$10 \ 4 \ 2 \ - \ / \ 6 \ * \ 9 \ +$$

QUIZ 4 :

$$(10 + 3) * 2 - (7 - 6) * (4 + 8)$$

$$10 \ 3 \ + \ * \ 2 \ - \ 7 \ 6 \ - \ * \ 4 \ 8 \ +$$

$$10 \ 3 \ + \ 2 \ * \ - \ 7 \ 6 \ - \ 4 \ 8 \ + \ *$$

$$10 \ 3 \ + \ 2 \ * \ 7 \ 6 \ - \ 4 \ 8 \ + \ * \ -$$

$$10 + 3 \Rightarrow 10 \ 3 \ +$$

$$10 + 3 \times 4 \Rightarrow 10 \ 3 \ 4 \ \times \ +$$

* Relative ordering of operands is maintained.

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 10 & + & 3 & \times & 4 \end{array}$$

$$10 \ 3 \ 4 \ \times$$

$$\boxed{+ \ \times}$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 10 & \times & 3 & + & 4 \end{array}$$

$$10 \ 3 \ 4$$

$$\boxed{\times \ +}$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 10 & \times & 3 & + & 4 \end{array}$$

$$\boxed{\cancel{\times} \ \cancel{+}}$$

$$10 \ 3 \ \times \ 4 \ +$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 10 & + & 3 & \times & 4 \end{array}$$

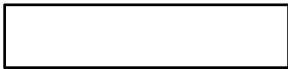
$$10 \ 3 \ 4 \ \times \ +$$

$$\boxed{+ \ \times}$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 10 & + & 3 & \times & 4 & - & 7 \end{array}$$

$$10 \quad 3 \quad 4 \quad * \quad + \quad 7 \quad -$$

$$10 \quad 3 \quad 4 \quad \times \quad + \quad 7 \quad -$$



$$10 \times (3 + 4)$$



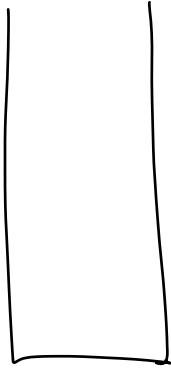
$$\underbrace{10 \quad 3 \quad 4 \quad + \quad \times}$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ (10 + 8) \times 5 \end{array}$$



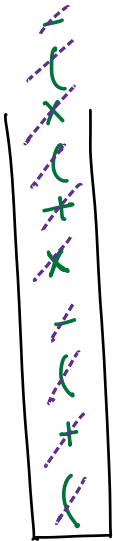
$$\underbrace{10 \quad 8 \quad + \quad 5 \quad \times}$$

$$3 + 10 \times (3 - 4/2) + 3$$



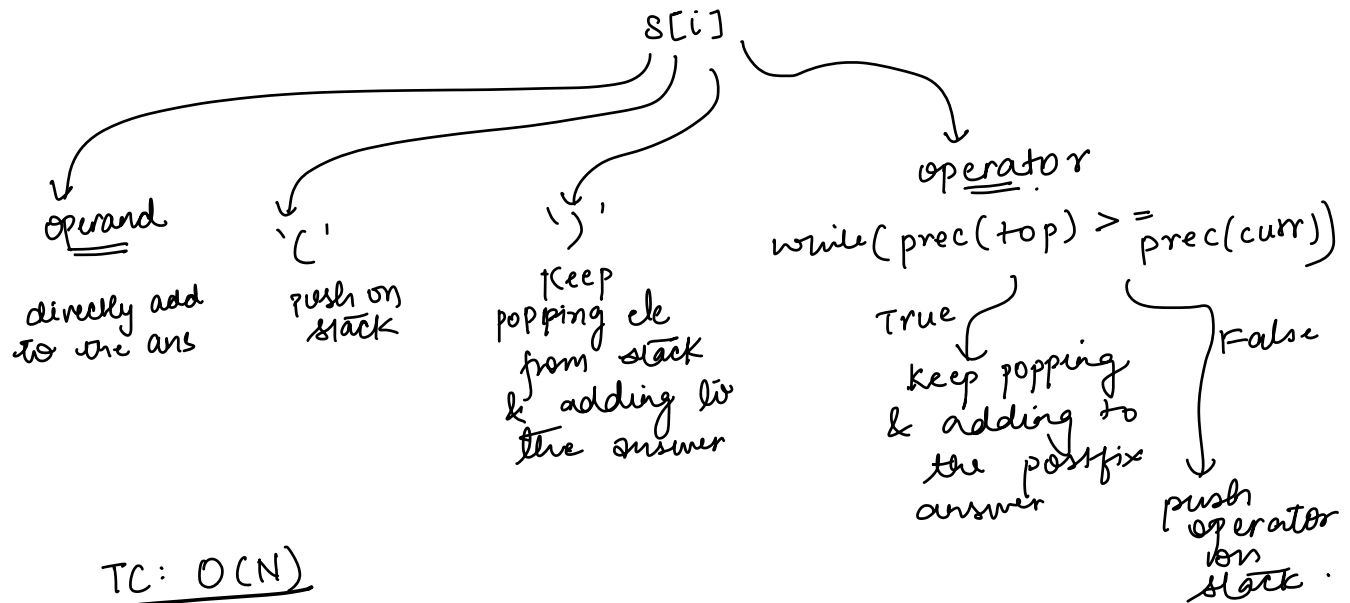
$$\underbrace{3 \ 10 \ 3 \ 4 \ 2 \ / \ - \times \ + \ 3 \ +}$$

$$(2 + (4 - 1) \times 5) + (6 \times (5 - 1))$$



$$\underbrace{2 \ 4 \ 1 \ - \ 5 \ * \ + \ 6 \ 5 \ 1 \ - \times \ +}$$

Traversing the string

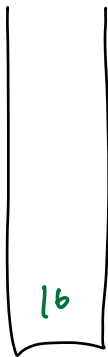


TC: $O(N)$

SC: $O(N)$

Evaluation

3 10 3 4 2 / - x + 3 +
 ↑ ↑ ↑ ↑ ↑ ↑



$(16) =$