

Today's Content:

- Currency exchange ✓
- Fractional knapsack ✓
- Greedy Properties ✓
- Activity Selection
- Job Scheduling
- Min Chocolates
- Rats { if time permits }

Indian Currency : 1 \rightarrow 2 \rightarrow 5 \rightarrow 10 \rightarrow 20 \rightarrow 50 \rightarrow 100 \rightarrow 200 \rightarrow 500 \rightarrow 2000

Cash: 5548 \rightarrow min number of coins/notes to get required cash?

	Notes/Coins	leftout	Why <u>Indian Greedy</u> ? <u>works</u>
2000 \rightarrow	2	1548	[Any denomination atleast ≥ 2 more previous denomination]
500 \rightarrow	3	48	
20 \rightarrow	2	8	
5 \rightarrow	1	3	
3 \rightarrow	1	1	
1 \rightarrow	1	0	
	<u>10</u>		

Currency : 1 10 18 : Greedy is not working

\rightarrow Money : 20 \rightarrow Min coins required to get target money

As per greedy : Min Coins

$\left. \begin{array}{l} 18 \\ 1 \\ 1 \end{array} \right\} 3$
 $\left. \begin{array}{l} 10 \\ 10 \end{array} \right\} 2 \text{ coins}$

Super Market : If needed we can eat a single kg from each item

Eating Complete Item		We can eat 70kg	
protein gained		man protein we can get	
Vegetables :		Eat based on total Protein	Eat based on protein/kg
Tomato 20 kg	200p	$200p \rightarrow 20kg$	$10p/kg - 20kg - 200$
Apples 15 kg	180p		$12p/kg - 15kg - 180$
onion 50 kg	250p	$250p \rightarrow 50kg$	$5p/kg -$
chicken 10 kg	150p	$450p \rightarrow 70kg$	$15p/kg - 10kg - 150$
potato 25 kg	200p		$8p/kg - 8kg - 64$
Mango 12 kg	132p		$11p/kg - 12kg - 132$
Seafood 5 kg	100p		$20p/kg - 5kg - 100$
		Man protein: 826	

For every kg we are taking man protein, we can get

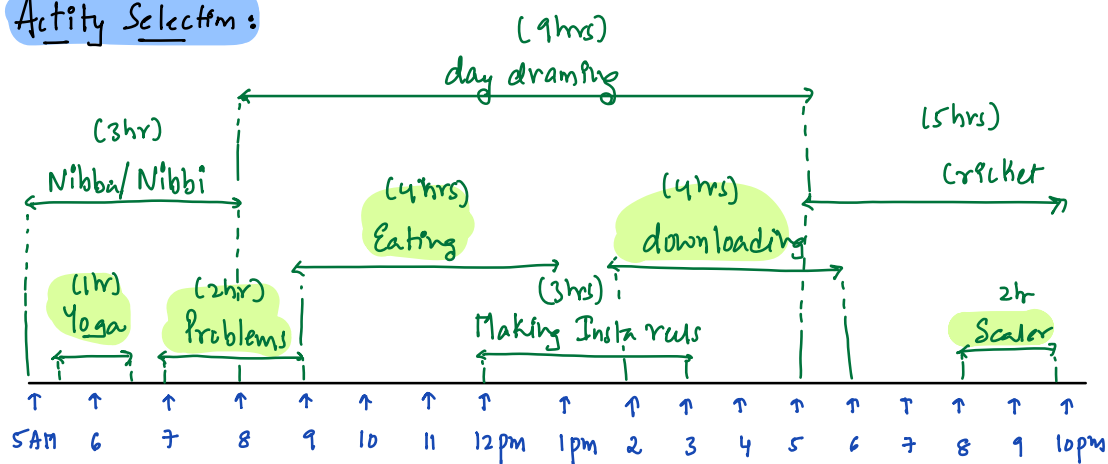
Greedy Properties :

- ✓ a) For optimization related problems
- ✓ b) Based on what parameter we want to apply greedy
- ✓ c) By coming up with counter examples

Real time algorithms :

- a) Prims / kruskals algorithms →
- b) Dijkstra's →
- c) Huffman's coding

Activity Selection:



- Start a task we need to complete
- At any given point single task
- **Main tasks** which we can do

Tasks:

Yoga
Problems
Eating
downloading
Scaler

grades:

1) Min duration *

Yoga
Problems
Scaler
Making Insta reels

3) Pick task which ends earlier: ✓

Yoga
Problems
Eating
downloading
Scaler

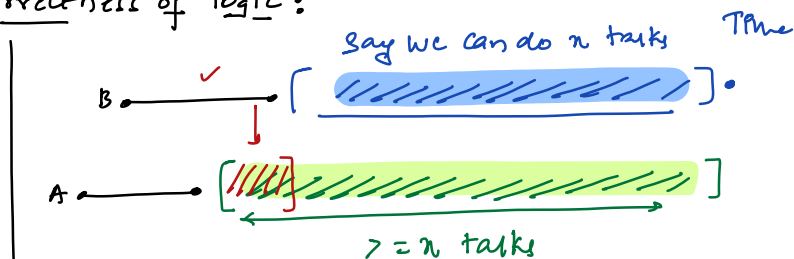
→ Sort all tasks based on end times & iterate & get non-overlapping tasks

2) Pick with min start time

Nibba/Nibbi
day dreaming
cricketer

TC: $N \log N + N$ SC: N

Correctness of logic:



Job Scheduling :

Given N Tasks to complete,

- Deadline assigned for each task, day on or before we can do task
- Payment assigned to Each task
- On any given day we can perform only 1 task & Each task take 1 day finish
- Find max payment we can get

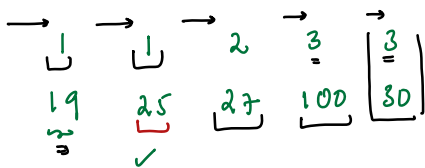
Ex1: deadline 1 → finish task on or before day 1

Job	deadline day	Payment
a	3	100
b	1	19
c	2	27
d	1	25
e	3	30

ans:

c e a → 157 : ans = 157
 d c a → 152
 day1 day2 day3
 a e d →
 ✓ ✓ ✗

→ Greedy Deadline



$$\boxed{\begin{matrix} \cancel{19}, \cancel{25}, 27, 100 \\ 30 \end{matrix}} = 100 + 27 + 30 = 157$$

Ex2: Task Deadline Reward

Task	Deadline	Reward
a	3	5
b	1	1
c	3	6
d	2	3
e	3	9

Sort based on deadline :

1 2 3 3 3
 1 3 6 5 9
 x ✓ ✓ ✓ ✓

$$\boxed{\begin{matrix} \cancel{1}, \cancel{3}, 6 \\ 5, 9 \end{matrix}} \rightarrow \text{ans: } 20$$

last example:

Tasks: 1 2 3 4 5 6 7 8 9 10

dead1: 2 1 1 1 4 5 4 5 5 2

Money: 200 250 200 350 300 100 250 600 400 150

Sort based on deadline:

1	1	1	2	2	4	4	5	5	5
250	200	350	150	200	250	300	600	100	400
✓	✗	✓	✗	✓	✓	✓	✓	✓	✓

250	350	200
150	200	400
300	600	

ans = 1900

100 < min value in deque

we won't insert

400 > min value in deque

operations

→ sifc()
→ insert()
→ getMin()
→ deleteMin()

minHeap

1	1	1	2	2	4
250	200	350	150	200	250
✓	✗	✓	✓	✓	✓

250
350
200
250

// int maxCost (list<pair<int, int>> data) {

int n = data.size();

// data.sort (based on deadline)

TC: $(N \log N + N \log N)$

Minheap<int> mh;

SC: $O(N)$

for (int i = 0; i < n; i++) {

11:06 → 11:15pm

pair<int, int> x = data[i]

int day = x.first

int pay = x.second

if (day > mh.size()) {

// Empty slot is there
mh.insert(pay)

}

else if (pay > mh.getMax()) // No empty slots

mh.deleteMin()
mh.insert(pay)

}

}

int ans = 0

while (mh.size() > 0) {

ans = ans + mh.getMax()

mh.deleteMin()

}

return ans;

}

Chocolate distribution : $\rightarrow \{ \text{tlw} \}$

Given N student marks, assign chocolate to all N students in such a way that

\rightarrow Each student should atleast get 1 chocolate

\rightarrow If $ar[i] > ar[i-1]$,
chocolates assigned to i^{th} student should be more $i-1^{\text{th}}$ student's chocolate

If $ar[i] < ar[i+1]$
chocolates assigned to i^{th} student should be more $i+1^{\text{th}}$ student's chocolate