

Q. Nearest smallest on left

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Given an array of positive integers

for every index i , find the nearest ele on left side of i which is **smaller** than $A[i]$.

$$A[] = \{ 4, 5, 2, 10, 8, 2 \}$$
$$\quad \quad \quad -1, 4, -1, 2, 2, -1$$

$$A[] = \{ 4, 6, 10, 11, 7, 8, 3, 5 \}$$
$$\quad \quad \quad -1, 4, 6, 10, 6, 7, -1, 3$$

$$A[] = \{ 5, 2, 8, 10, 12, 6, 1 \}$$
$$\quad \quad \quad -1, -1, 2, 8, 10, 2, -1$$

Brute Force :

```
ans[N] = { -1 }
for(i=0; i<N; i++) {
    for(j=i-1; j>=0; j--) {
        if(A[j] < A[i]) {
            ans[i] = A[j]
            break
        }
    }
}
return ans
```

TC: $O(N^2)$
SC: $O(1)$

$$\{ 5, 2, 8, 10, 12, 6, 1 \}$$

-1 -1 2 8 10 2 -1

5	2	8	10	12	6
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Any ele greater than 5 will obviously be greater than 2
hence, need not keep 5 in the box

$$\{ 4, 6, 10, 11, 7, 8, 3, 5 \}$$

-1 4 6 10 6 7 -1 3

4	6	10	11	7	8	3	5
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Pseudocode

stack

($A[i] \leq st.top()$)
 $st.pop()$

($A[i] > st.top()$)
 $ans[i] = st.top()$

```

ans[N] = {-1}
stack<int> s;
for(i=0; i < N; i++) {
    while(s.size() > 0 && A[i] <= st.top()) {
        st.pop()
    }
    if(s.size() > 0) { ans[i] = st.top() }
    s.push(A[i])
}
return ans

```

TC: $O(N)$

SC: $O(N)$

Q. Find the index of nearest smaller on left side

-1
→ NO answer present

Code

ans[N] = {-1}

stack<int> s;

for(i=0; i < N; i++) {

 while(s.size() > 0 && A[i] <= A[s.top()]) {

 s.pop();

 if(s.size() > 0) {ans[i] = s.top();}

 s.push(i);

}

return ans;

{ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9
 4, 7, -9, 5, -6, 9, 7, 5, 2, 10 }
-1 0 -1 2 2 4 4 4 4 8 }

Storing the indices will also work for negative elements.

Ques. Get distance of nearest smaller ele on left side

Ques. Find nearest greater on left side

2 9 7 1 4 7 2 6 5
-1 -1 9 7 7 9 7 7 6

2 9 7 1 4 7 2 6 5

$A[i] < st.top()$
 $ans[i] = st.top()$

$A[i] \geq st.top()$
 $st.pop()$

Q. Find nearest smaller on right

2 9 7 1 4 7 2 6 5
1 7 1 -1 2 2 -1 5 -1

// Iterate from right

Q. Find nearest greater on right

2 9 7 1 4 7 2 6 5
9 -1 -1 4 7 -1 6 -1 -1

// Iterate from the right

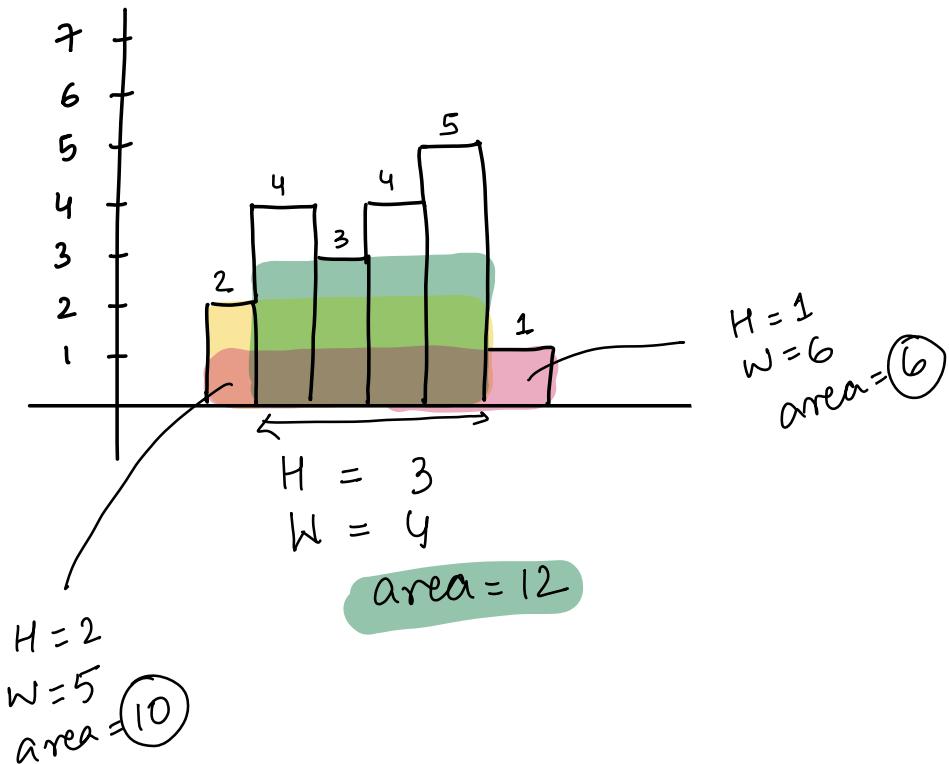
Break \rightarrow 10 : 40

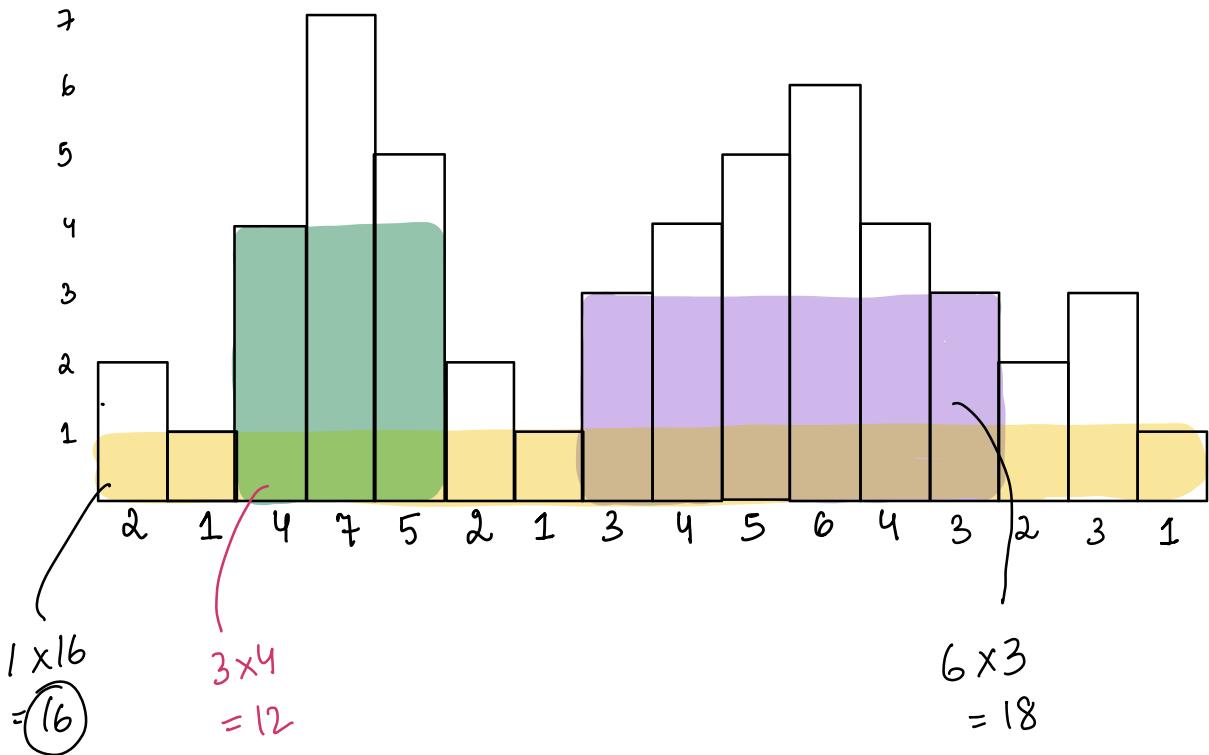
10 : 33
Black Out
↓

Adobe

Ques. Given continuous blocks of histogram, find max

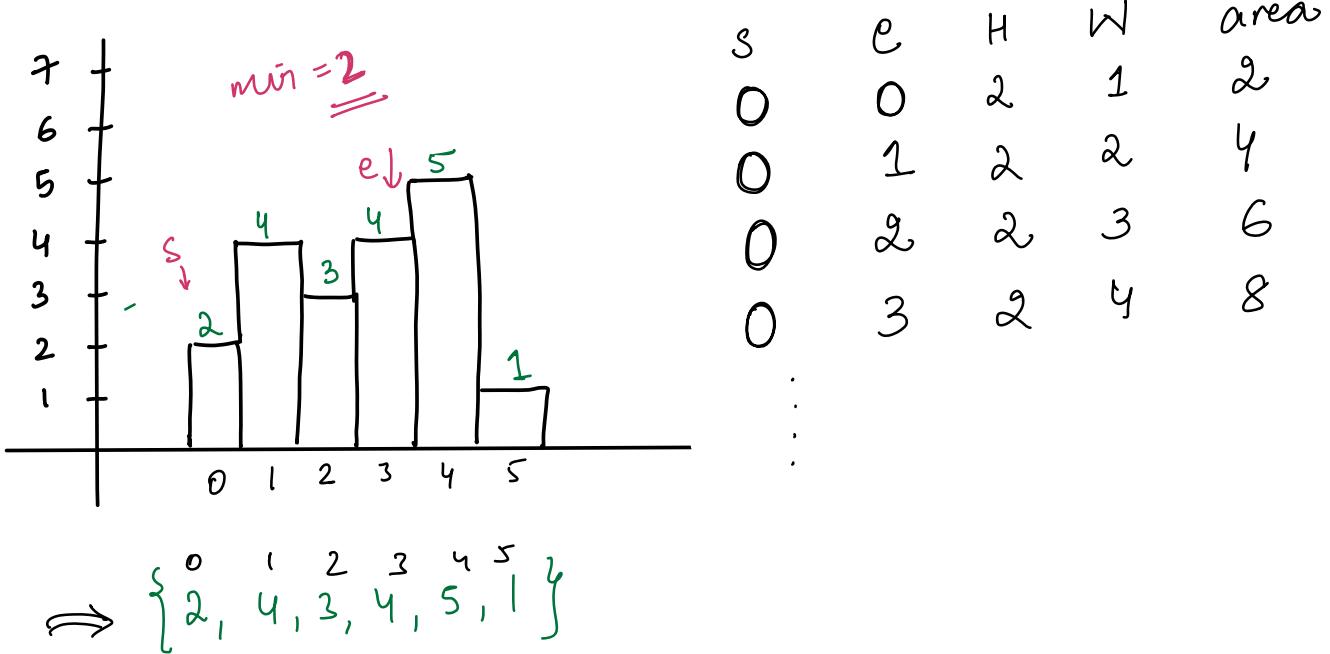
rectangular area
not exceeding histogram





Brute Force

Given any two bars, can we find area b/w them?



```

for( s=0 ; s<N ; s++ ) {
    m_e = A[s]
    for( e=s ; e<N ; e++ ) {
        m_e = min( m_e, A[e] )
        // [s e]
        W = e - s + 1
        H = get min from [s e] m_e
        area = W * H
        ans = max( ans, area )
    }
}
return ans

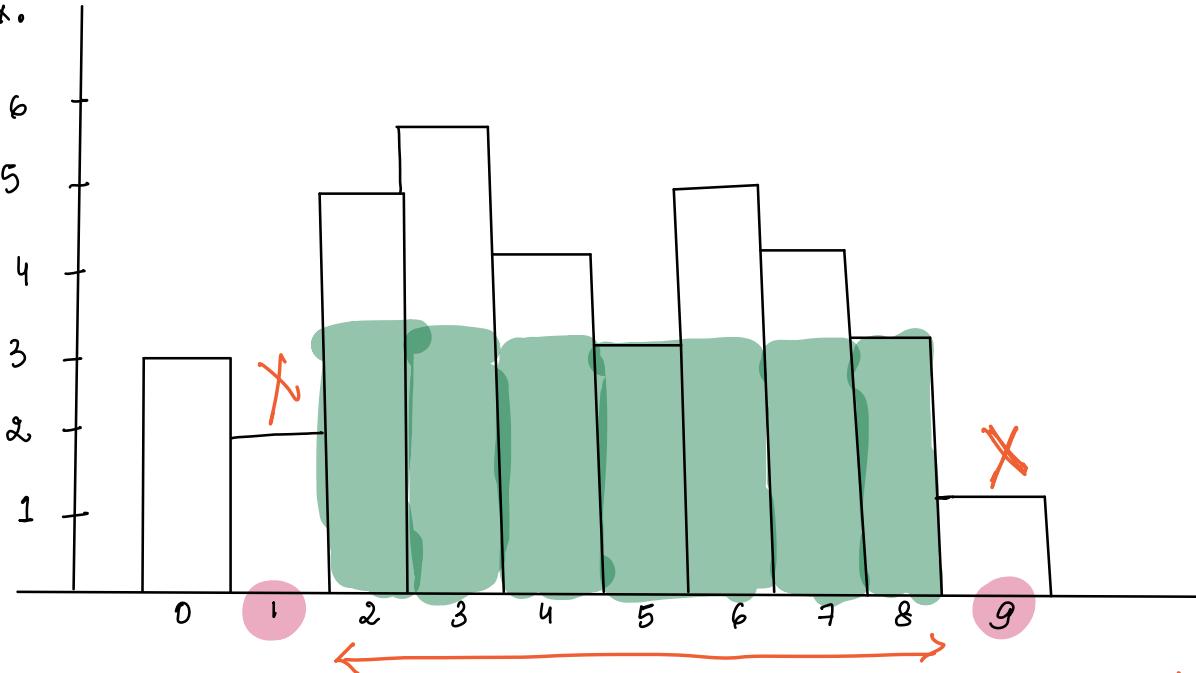
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Carry Forward

$$\begin{aligned}
 n &= \min[i \ j] \\
 \min[i \ j+1] &= \min(x, j+1) \\
 TC: O(N^2) \\
 SC: O(1)
 \end{aligned}$$

$$\begin{aligned}
 TC: O(N^3) \\
 SC: O(1)
 \end{aligned}$$

Ex.



Code

```
for (i=0; i<N; i++) {
```

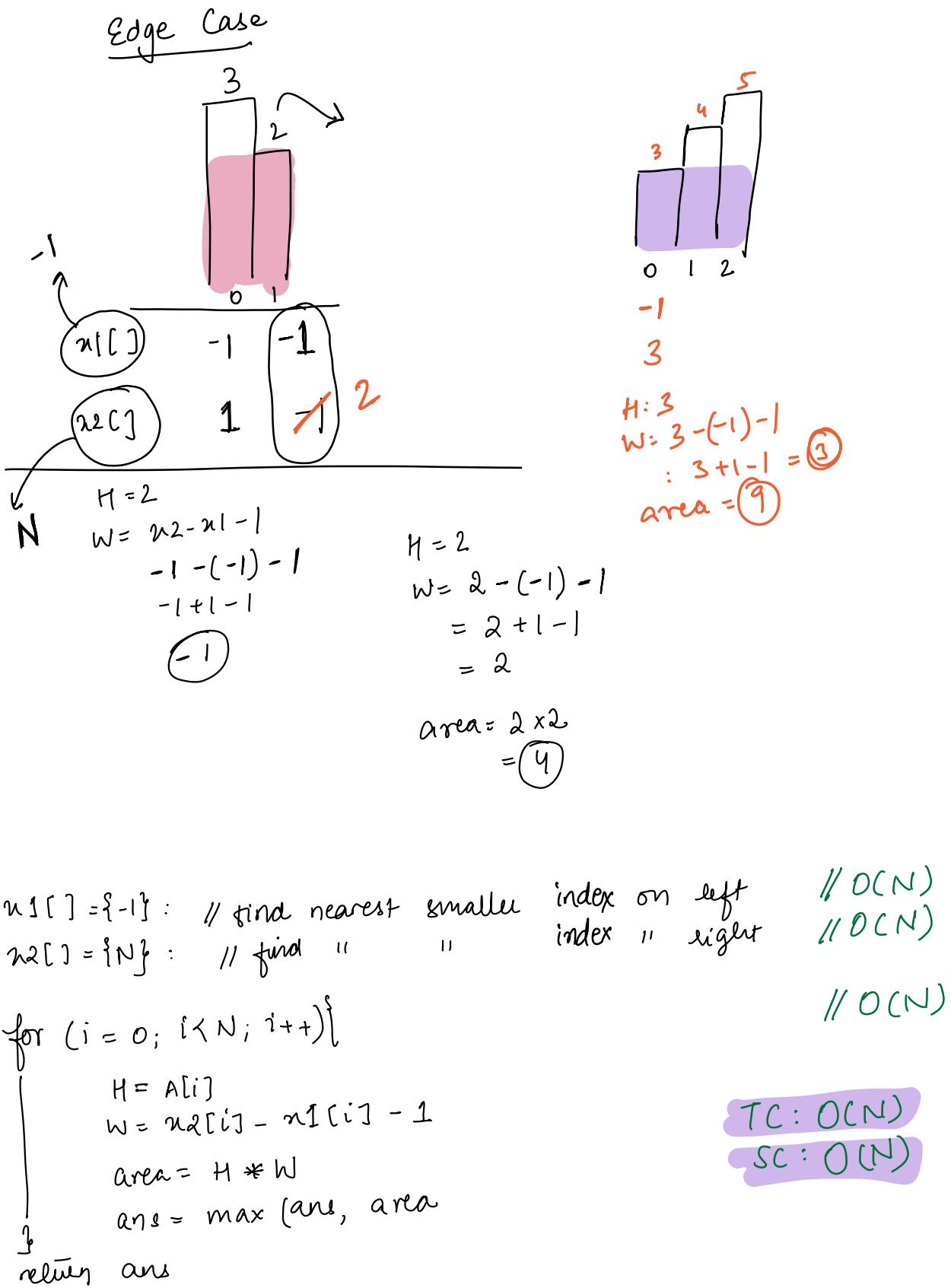
H = A[i]

x_1 = get the nearest smaller to $A[i]$ on
left

x_2 = get the nearest smaller to $A[i]$ on
right

$W = x_2 - x_1 - 1$

ans = max (ans, H * W)





$$n1[] \quad -1 \quad -1$$

$$n2[] \quad 1 \quad 2$$

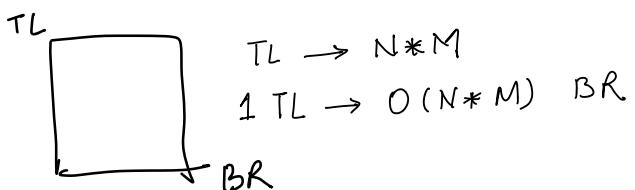
$$\begin{array}{c} \overbrace{\begin{array}{c} 1 - (-1) - 1 \\ = 1 \end{array}}^{\textcircled{1}} \quad \left| \begin{array}{c} \overbrace{\begin{array}{c} 2 - (-1) - 1 \\ = 2 \end{array}}^{\textcircled{2}} \\ 2 \times 1 = 2 \end{array} \right. \\ 1 \times 100 \\ 100 \end{array}$$

Ques: Given a matrix which contains 1 & 0, find max rectangular area which contains all 1s.

	0	1	2	3	4	5
0	1	1	0	1	0	1
1	0	1	1	1	1	1
2	1	1	1	1	1	0
3	1	0	1	0	0	1
4	1	1	0	0	1	1

Brute Force

consider all the submatrices



$$TL \rightarrow N * M$$

$$1 TL \rightarrow O(N * M) \quad BR$$

Total submatrices

$$\overbrace{\quad\quad\quad}^{=} N^2 M^2$$

\uparrow TL \rightarrow $N \times M$ BR

$N \times M$ TL $\underline{\underline{\underline{=}}} \rightarrow N^2 \times M^2$ submatrices.

If size == sum for a submatrix
then could be a possible answer.

$\uparrow \rightarrow \underline{\underline{\underline{O(1)}}}$

TC: $O(\underline{\underline{\underline{N^2M^2}}})$



	0	1	2	3	4	5
0	1	1	0	1	0	1
1	0	1	1	1	1	1
2	1	1	1	1	1	0
3	1	0	1	0	0	1
4	1	1	0	0	1	1

1

1	1	0	1	0	1
0	2	1	2	1	2
1	3	2	3	2	0
2	0	3	0	0	1
3	1	0	0	1	2

TC: $O(N \times M) + O(N \times M)$

SC: $O(M \times N) + O(M)$

if 1D array SC: $\underline{\underline{\underline{O(M)}}} + O(M)$

Problem Solving
↳ Double character extended trouble's version

$\text{mat}[N][M] = \{0\}$

$\text{for}(i=0; i < M; i++) \{$
| $\text{mat}[0][i] = A[0][i]$
| } }

$\text{for}(i=1; i < N; i++) \{$
| $\text{for}(j=0; j < M; j++) \{$
| | if($A[i][j] \neq 0$) $\text{mat}[i][j] += \text{mat}[i-1][j]$
| | else $\text{mat}[i][j] = 0$
| | } }

$\text{for}(i=0; i < N; i++) \{$
| $\text{maxRectangleArea}(\text{mat}[i])$
| } }

TC: $O(N \times M)$
SC: $O(N \times M)$

$ar[M] = \{0\}$

for($i=0$; $i < M$; $i++$) {

| $ar[i] = A[0][i]$

}

$ans = \max(ans, \text{maxRectangleArea}(ar))$

for($i=1$; $i < N$; $i++$) {

| for($j=0$; $j < M$; $j++$) {

| | if ($A[i][j] \neq 0$) $ar[j] += A[i][j]$

| | else { $ar[j] = 0$ }

| }

} $ans = \max(ans, \text{maxRectangleArea}(ar))$

return ans

TC: $O(N * M)$

SC: $O(M)$