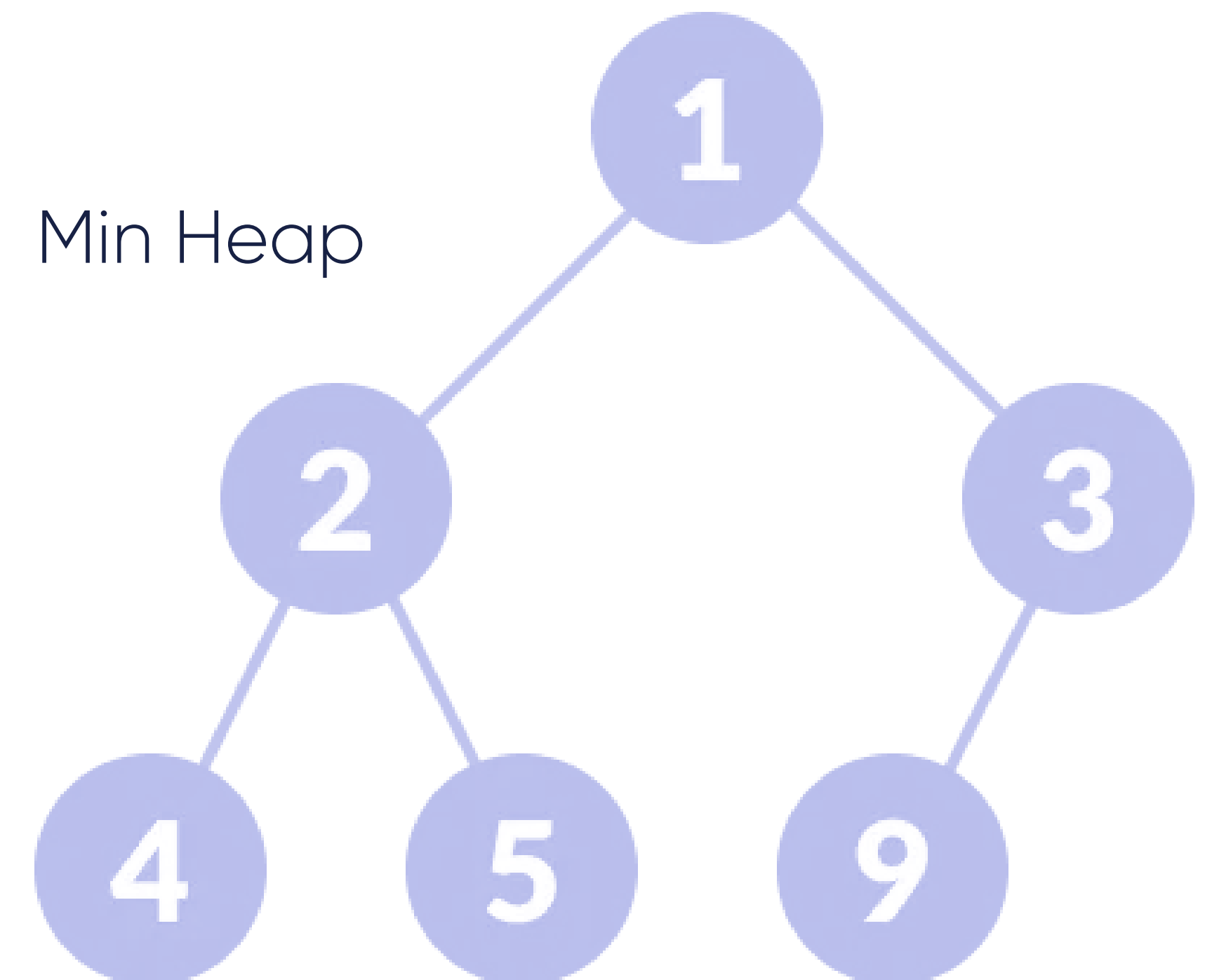
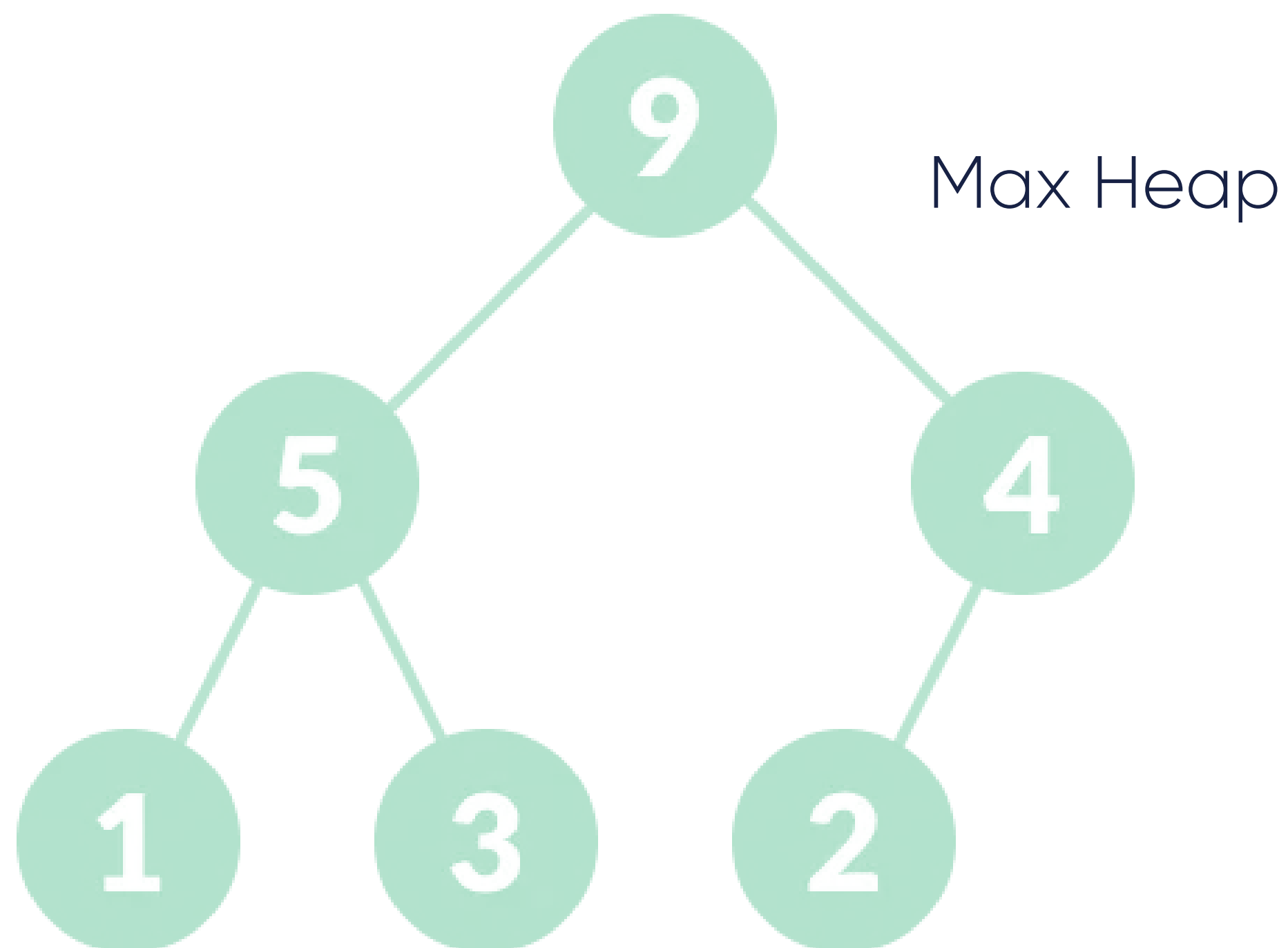


Heap Animation

Heap

Heap data structure is a complete binary tree that satisfies the heap property, where any given node is:

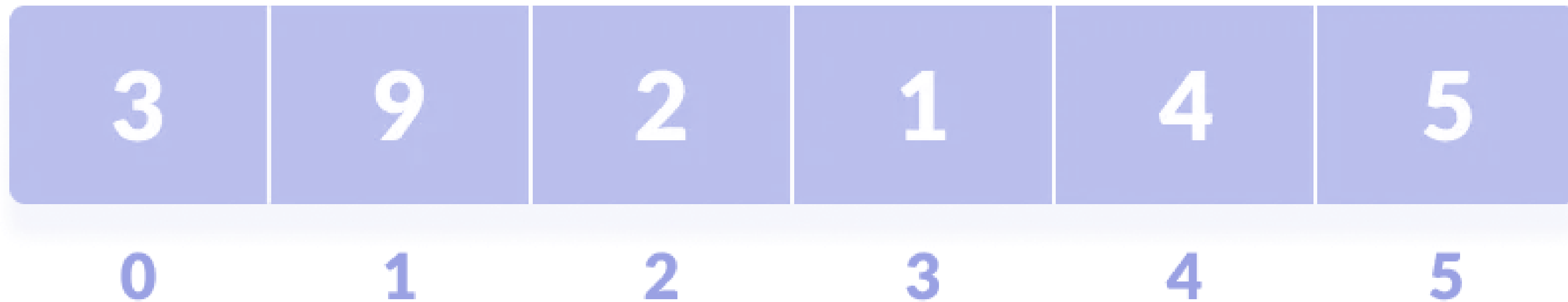
- always greater than its child node/s and the key of the root node is the largest among all other nodes. This property is also called max heap property.
- always smaller than the child node/s and the key of the root node is the smallest among all other nodes. This property is also called min heap property.



Heap Operations

Heapify

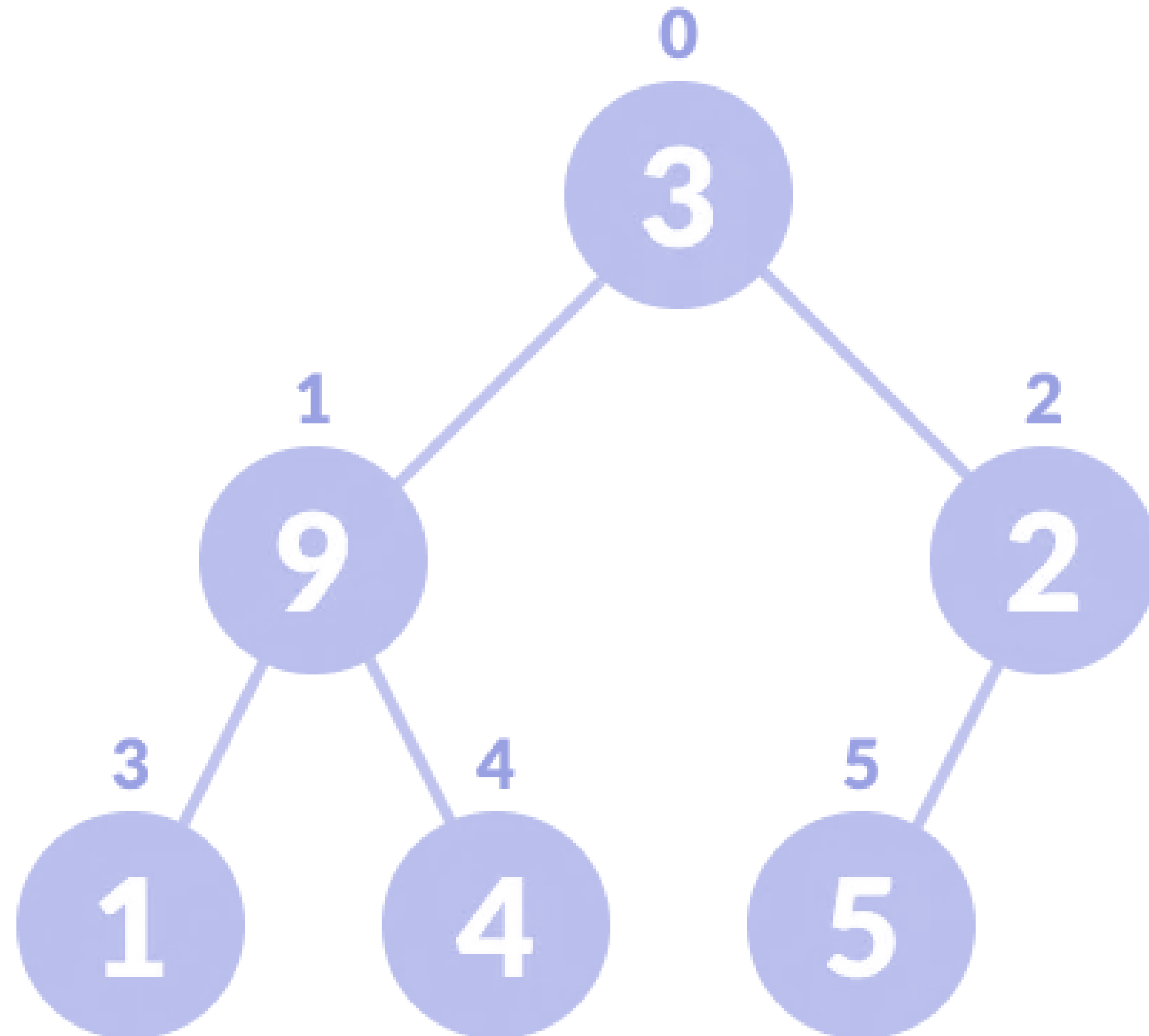
1- Heapify is the process of creating a heap data structure from a binary tree. It is used to create a Min-Heap or a Max-Heap.



Heap Operations

Complete Binary Tree

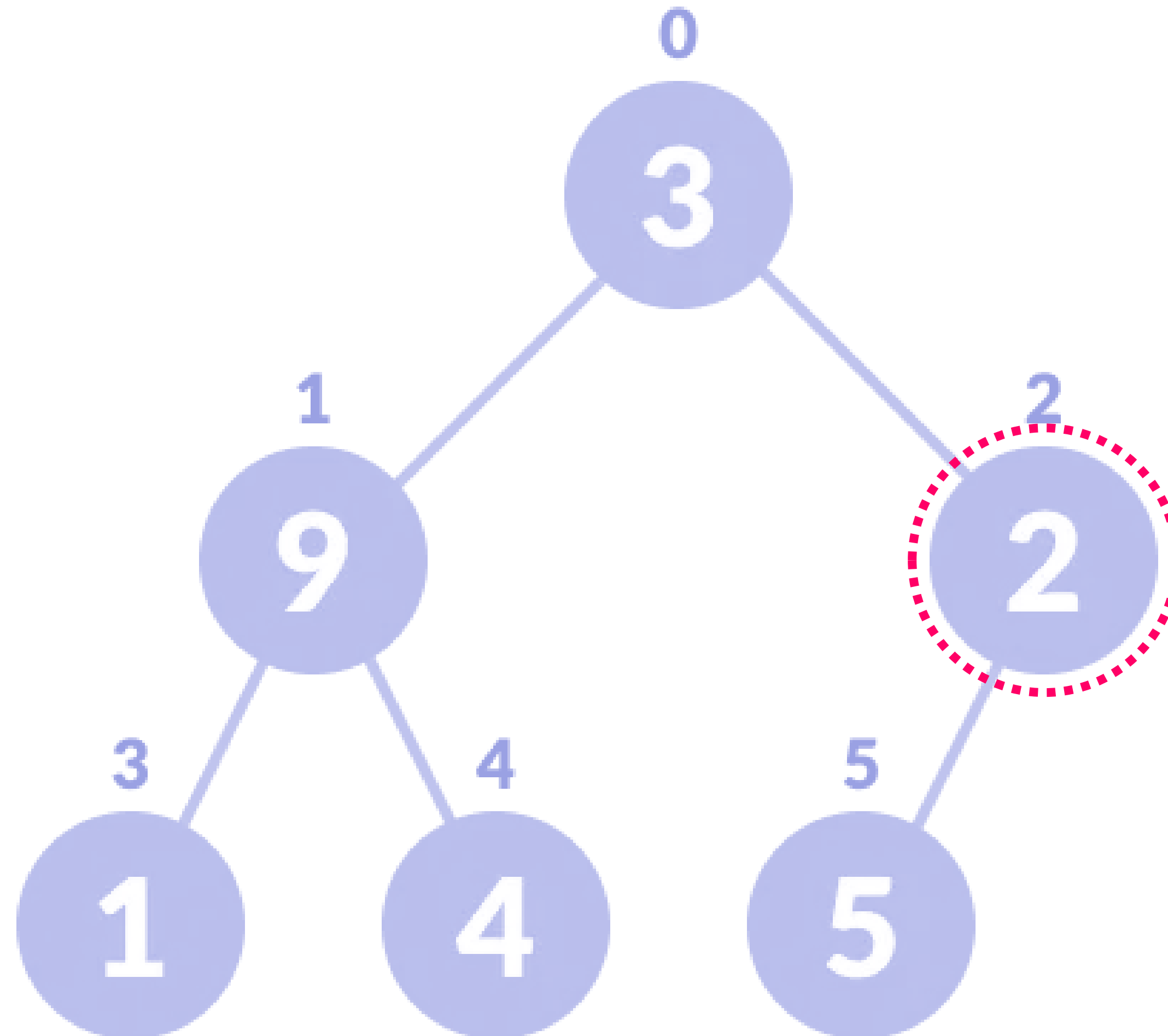
2- Create a complete binary tree from the array



Heap Operations

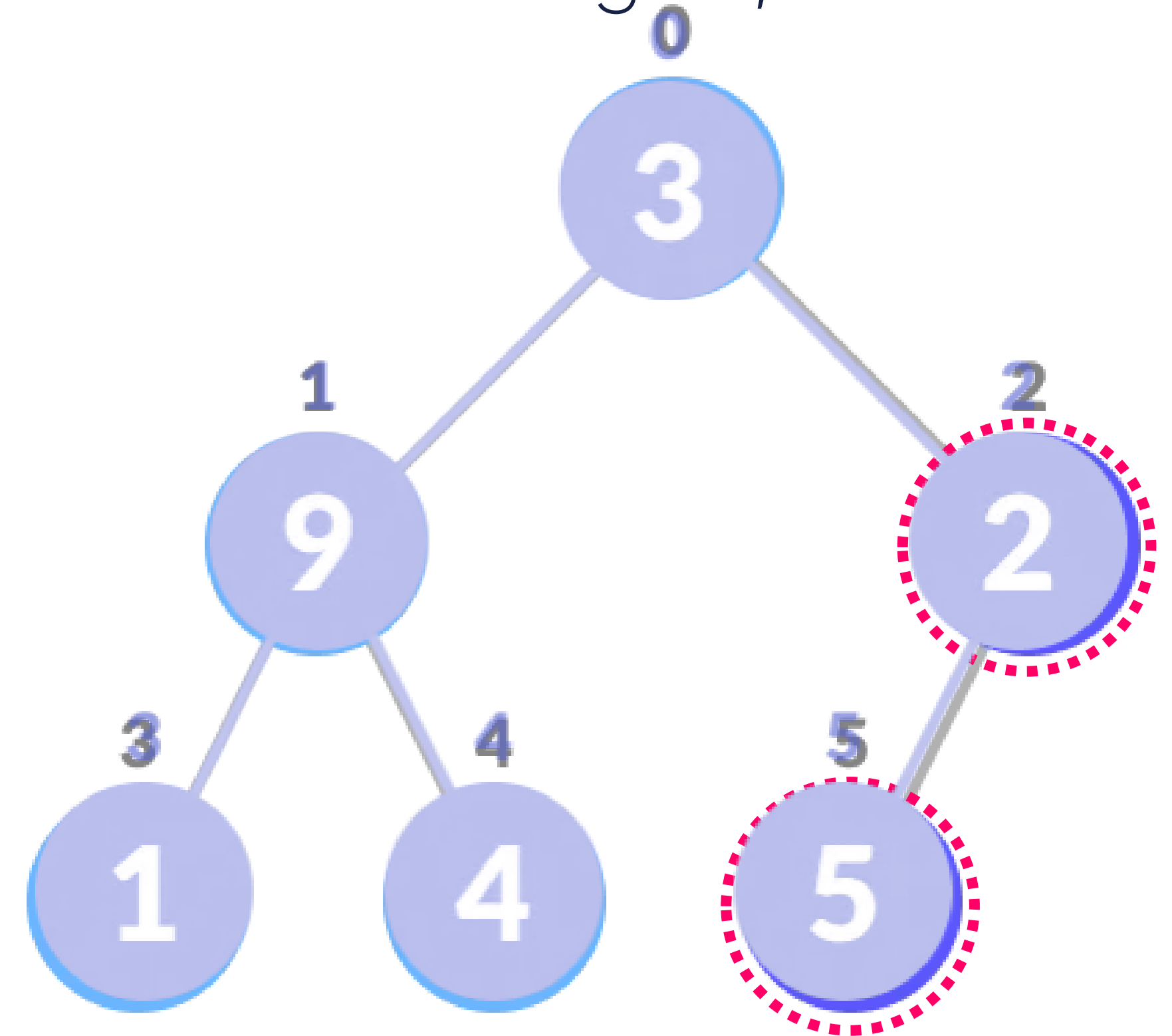
Complete Binary Tree

3- Start from the first index of non-leaf node whose index is given by $n/2 - 1$



Heap Operations

- 4- Set current element i as largest.
- 5- The index of left child is given by $2i + 1$ and the right child is given by $2i + 2$.
If leftChild is greater than currentElement (i.e. element at i th index), set leftChildIndex as largest. If rightChild is greater than element in largest, set rightChildIndex as largest.
- 6- Swap largest with currentElement
- 7- Repeat steps 3-7 until the subtrees are also heapified.



Heap in C

```
#include <stdio.h>
int size = 0;
```

```
void swap(int *a, int *b)
{
    int temp = *b;
    *b = *a;
    *a = temp;
}
```

```
void heapify(int array[], int size, int i)
{
    if (size == 1)
    {
        printf("Single element in the heap");
    }
    else
    {
        int largest = i;
        int l = 2 * i + 1;
        int r = 2 * i + 2;
        if (l < size && array[l] > array[largest])
            largest = l;
        if (r < size && array[r] > array[largest])
            largest = r;
        if (largest != i)
        {
            swap(&array[i], &array[largest]);
            heapify(array, size, largest);
        }
    }
}
```

```
void insert(int array[], int newNum)
{
    if (size == 0)
    {
        array[0] = newNum;
        size += 1;
    }
    else
    {
        array[size] = newNum;
        size += 1;
        for (int i = size / 2 - 1; i >= 0; i--)
        {
            heapify(array, size, i);
        }
    }
}
```

```
void deleteRoot(int array[], int num)
{
    int i;
    for (i = 0; i < size; i++)
    {
        if (num == array[i])
            break;
    }

    swap(&array[i], &array[size - 1]);
    size -= 1;
    for (int i = size / 2 - 1; i >= 0; i--)
    {
        heapify(array, size, i);
    }
}

void printArray(int array[], int size)
{
    for (int i = 0; i < size; ++i)
        printf("%d ", array[i]);
    printf("\n");
}
```

```
int main()
```

```
{
    int array[10];
```

```
    insert(array, 3);
    insert(array, 4);
    insert(array, 9);
    insert(array, 5);
    insert(array, 2);
```

```
    printf("Max-Heap array: ");
    printArray(array, size);
```

```
    deleteRoot(array, 4);
```

```
    printf("After deleting an element: ");
```

```
    printArray(array, size);
}
```

Heap in Java

Heap Sort Algorithm Animation

Heap Sort Algorithm Complexity

Time Complexity

Best $O(n \log n)$

Worst $O(n \log n)$

Average $O(n \log n)$

Space Complexity $O(1)$

Stability No

Heap Sort Algorithm in C

```
#include <stdio.h>
```

```
// Function to swap the position of two elements
```

```
void swap(int *a, int *b) {  
    int temp = *a;  
    *a = *b;  
    *b = temp;  
}
```

```
void heapify(int arr[], int n, int i) {
```

```
    // Find largest among root, left child and right child  
    int largest = i;  
    int left = 2 * i + 1;  
    int right = 2 * i + 2;
```

```
    if (left < n && arr[left] > arr[largest])  
        largest = left;
```

```
    if (right < n && arr[right] > arr[largest])  
        largest = right;
```

```
    // Swap and continue heapifying if root is not largest  
    if (largest != i) {  
        swap(&arr[i], &arr[largest]);  
        heapify(arr, n, largest);  
    }  
}
```

```
// Main function to do heap sort
```

```
void heapSort(int arr[], int n) {  
    // Build max heap  
    for (int i = n / 2 - 1; i >= 0; i--)  
        heapify(arr, n, i);
```

```
    // Heap sort  
    for (int i = n - 1; i >= 0; i--) {  
        swap(&arr[0], &arr[i]);
```

```
        // Heapify root element to get highest  
        // element at root again  
        heapify(arr, i, 0);  
    }  
}
```

```
// Print an array
```

```
void printArray(int arr[], int n) {  
    for (int i = 0; i < n; ++i)  
        printf("%d ", arr[i]);  
    printf("\n");  
}
```

```
// Driver code
```

```
int main() {  
    int arr[] = {1, 12, 9, 5, 6, 10};  
    int n = sizeof(arr) / sizeof(arr[0]);  
  
    heapSort(arr, n);  
  
    printf("Sorted array is \n");  
    printArray(arr, n);  
}
```

Heap Sort Algorithm in Java