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# Solution For School Geometry Problems

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Abstract—This document includes different problems and solution on geometry from trigonometry and linear algebra.It also provides the imformation about the python and latex codes of figures.

Download all python codes from

svn co https://github.com/yogi13995/ yogesh\_training/tree/master/Geometry/ line\_alg/codes

and latex-tikz codes from

svn co https://github.com/yogi13995/ yogesh\_training/tree/master/Geometry/ line\_alg/figures

#### 1 Triangle

#### 1.0.1 Problem:

1. The vertices of  $\triangle PQR$  are  $\mathbf{P} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} 4 \\ 5 \end{pmatrix}$ . Find the equation of the median through the vertex  $\mathbf{R}$ .

#### 1.1 Solution

1. We have a triangle as given bellow .First of all we will find out the midpoint of the  $\mathbf{A}B$  because each median devide the side in two equal part.

Finding out the point S as given in fig (1.1)...

 ${\bf S}$  is the midpoint of the  ${\bf P}$  and  ${\bf Q}$ 

$$\mathbf{S} = \frac{\mathbf{P} + \mathbf{Q}}{2} \tag{1.1.1.1}$$

Direction vector in the direction of RS

$$\mathbf{RS} = \mathbf{S} - \mathbf{R} \tag{1.1.1.2}$$

equation of the line going through points  ${\bf S}$  and  ${\bf R}$  can be given as

$$\mathbf{x} = \mathbf{R} + \lambda (\mathbf{S} - \mathbf{R}) \tag{1.1.1.3}$$

$$\mathbf{x} = \begin{pmatrix} 4 \\ 5 \end{pmatrix} + \lambda \begin{pmatrix} 0 \\ 2 \end{pmatrix} - \begin{pmatrix} 4 \\ 5 \end{pmatrix}$$
 (1.1.1.4)

$$\mathbf{x} = \begin{pmatrix} 4 \\ 5 \end{pmatrix} + \lambda \begin{pmatrix} -4 \\ -3 \end{pmatrix}$$
 (1.1.1.5)

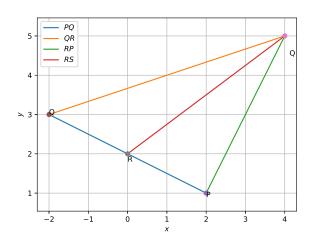


Fig. 1.1.1: triange for median

codes/triangle.py

#### 2 Quadrilateral

#### 2.1 Problem

1. Find the area of a rhombus if its vertices are  $\binom{3}{0}$ ,  $\binom{4}{5}$ ,  $\binom{-1}{4}$  and  $\binom{-2}{-1}$  taken in order.

## 2.2 Solution

1. let assume that the vertices of the rhombus are **P**, **Q**, **R** and **S** respectively as shown in fig(2.2.1).

finding out the SP and QP...

$$\mathbf{SP} = \mathbf{P} - \mathbf{S} = \begin{pmatrix} 3+2\\0+1 \end{pmatrix} \tag{2.2.1.1}$$

$$= \begin{pmatrix} 5 \\ 1 \end{pmatrix} \tag{2.2.1.2}$$

$$\mathbf{PQ} = \mathbf{Q} - \mathbf{P} = \begin{pmatrix} 4 - 3 \\ 5 - 0 \end{pmatrix} \tag{2.2.1.3}$$

$$= \begin{pmatrix} 1 \\ 5 \end{pmatrix} \tag{2.2.1.4}$$

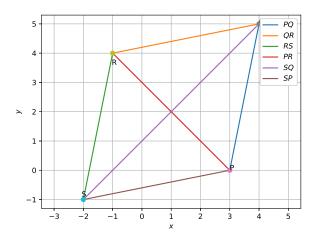


Fig. 2.2.1: quadrilateral

#### codes/quad.py

**S** Area of the rhombus can be calculated as follows

$$||\Delta|| = abs \, ||\mathbf{SP} \times \mathbf{PQ}|| \qquad (2.2.1.5)$$

$$\|\Delta\| = abs \left\| \begin{pmatrix} 5\\1 \end{pmatrix} \times \begin{pmatrix} 1\\5 \end{pmatrix} \right\|$$
 (2.2.1.6)

$$||\Delta|| = 5 * 5 - 1 * 1$$
 (2.2.1.7)

$$||\Delta|| = 24 \qquad (2.2.1.8)$$

3 Line

### 3.1 Point and Vector

#### 3.1.1 Problem:

1. Name the type of Quadriletral formed ,if any,by the following points, and give reaons for your answer.

(a) 
$$\begin{pmatrix} -1 \\ -2 \end{pmatrix}$$
,  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ ,  $\begin{pmatrix} -1 \\ 2 \end{pmatrix}$ ,  $\begin{pmatrix} -3 \\ 0 \end{pmatrix}$ 

(b) 
$$\begin{pmatrix} -3 \\ 5 \end{pmatrix}$$
,  $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$ ,  $\begin{pmatrix} 0 \\ 3 \end{pmatrix}$ ,  $\begin{pmatrix} -1 \\ -4 \end{pmatrix}$   
(c)  $\begin{pmatrix} 4 \\ 5 \end{pmatrix}$ ,  $\begin{pmatrix} 7 \\ 6 \end{pmatrix}$ ,  $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ ,  $\begin{pmatrix} 1 \\ 2 \end{pmatrix}$   
3.1.2 Solution:

1. here

$$\mathbf{d1} = \mathbf{R} - \mathbf{P} = \begin{pmatrix} 0 \\ 4 \end{pmatrix}$$

$$(3.1.1.1)$$

$$\mathbf{d2} = \mathbf{S} - \mathbf{Q} = \begin{pmatrix} -4 \\ 0 \end{pmatrix}$$

$$(3.1.1.2)$$

$$\mathbf{SP} = \mathbf{P} - \mathbf{S} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$

$$(3.1.1.3)$$

$$\mathbf{PQ} = \mathbf{Q} - \mathbf{P} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$

$$(3.1.1.4)$$

$$abs \|\mathbf{d1} \times \mathbf{d2}\| = abs \left\| \begin{pmatrix} 5 \\ 1 \end{pmatrix} \times \begin{pmatrix} 1 \\ 5 \end{pmatrix} \right\| = 16$$

$$(3.1.1.5)$$

$$abs \|\mathbf{SP} \times \mathbf{PQ}\| = abs \left\| \begin{pmatrix} 2 \\ 2 \end{pmatrix} \times \begin{pmatrix} 2 \\ 2 \end{pmatrix} \right\| = 8$$

$$(3.1.1.6)$$

$$\frac{1}{2}abs \|\mathbf{d1} \times d2\| = abs \|\mathbf{SP} \times PQ\| = 8$$

$$(3.1.1.7)$$

from above we can say that the area of the quadrileteral is equal to the half of the multiplication of its diogonals.thus this is a rhombus.

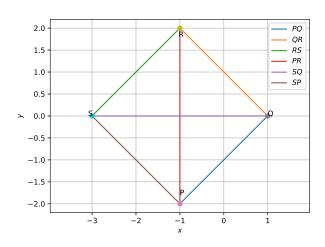


Fig. 3.1.1: quadrilateral1

codes/quad1.py

2.

$$\mathbf{PQ} = \mathbf{Q} - \mathbf{P} = \begin{pmatrix} 6 \\ -4 \end{pmatrix} \tag{3.1.2.1}$$

$$\mathbf{PR} = \mathbf{R} - \mathbf{P} = \begin{pmatrix} 3 \\ -2 \end{pmatrix} \tag{3.1.2.2}$$

$$\mathbf{RQ} = \mathbf{Q} - \mathbf{R} = \begin{pmatrix} 3 \\ -2 \end{pmatrix} \tag{3.1.2.3}$$

$$\mathbf{PQ} = \mathbf{PR} + \mathbf{RQ} = \begin{pmatrix} 6 \\ -4 \end{pmatrix} \tag{3.1.2.4}$$

so from above we can say that P, Q and R are linear so it can not be a quadrilateral.

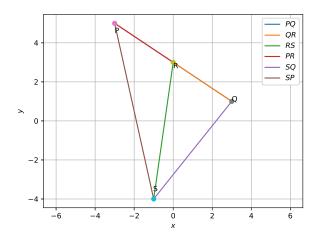


Fig. 3.1.2: quadrilateral2

codes/quad1.py

#### 3.2 Point on a line

#### 3.2.1 Problem:

- 1. Find the ratio in wich the line segment joining is devided by the x-axis. Also find the coardinates of the point of division.
- 3.2.2 Solution:
- 1. Let assume that we have a point C which devide the linesegment AB in k:1 ratio.

$$\begin{pmatrix} x \\ 0 \end{pmatrix} = k \begin{pmatrix} 1 \\ -5 \end{pmatrix} + \begin{pmatrix} -4 \\ 5 \end{pmatrix}$$
 (3.2.1.1)

$$0 = -5k + 5 \tag{3.2.1.2}$$

$$k = 1$$
 (3.2.1.3)

$$\mathbf{C} = \frac{\binom{-3}{0}}{2} = \binom{-1.5}{0} \tag{3.2.1.4}$$

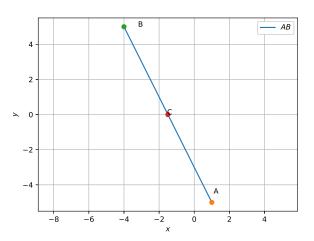


Fig. 3.2.1: line

codes/points on line.py

#### 3.3 Lines and Planes

#### 3.3.1 Problem:

- 1. Sketch the lines
  - a)  $(2 \ 3) \mathbf{x} = 9.35$ ,
  - b)  $(1 \frac{1}{5}) \mathbf{x} = 10$

  - e)  $(2 5) \mathbf{x} = 0$ , f)  $(3 0) \mathbf{x} = -2$
- 3.3.2 Solution:
- 1. All the lines can be drawn as follow

a) put 
$$\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$$
 in equation

$$(2 \ 3)\begin{pmatrix} x \\ 0 \end{pmatrix} = 9.35$$
 (3.3.1.1)

$$x = 4.67$$
 (3.3.1.2)

put  $\mathbf{x} \begin{pmatrix} 0 \\ y \end{pmatrix}$  in equation

$$(2 \ 3)\binom{0}{y} = 9.35$$
 (3.3.1.3)

$$y = 3.116$$
 (3.3.1.4)

$$(2 \quad 3) \begin{pmatrix} 0 \\ y \end{pmatrix} = 9.35$$
 (3.3.1.3)  
 
$$y = 3.116$$
 (3.3.1.4)  
 
$$\mathbf{P} = \begin{pmatrix} 4.67 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 0 \\ 3.116 \end{pmatrix}$$
 (3.3.1.5)

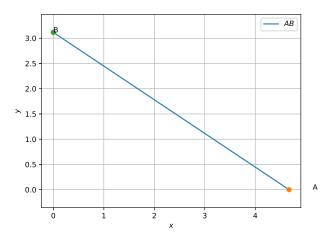


Fig. 3.3.1: line1

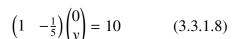
codes/plane\_and\_line1.py

b) put  $\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$  in equation

$$(1 - \frac{1}{5})\begin{pmatrix} x \\ 0 \end{pmatrix} = 10$$
 (3.3.1.6)

$$x = 10 (3.3.1.7)$$

put  $\mathbf{x} \begin{pmatrix} 0 \\ y \end{pmatrix}$  in equation



$$y = -50 (3.3.1.9)$$

$$\begin{pmatrix}
1 & -\frac{1}{5} \end{pmatrix} \begin{pmatrix} 0 \\ y \end{pmatrix} = 10 \qquad (3.3.1.8)$$

$$y = -50 \qquad (3.3.1.9)$$

$$\mathbf{P} = \begin{pmatrix} 10 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 0 \\ -50 \end{pmatrix} \qquad (3.3.1.10)$$

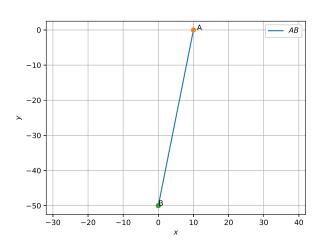


Fig. 3.3.1: line2

codes/plane and line2.py

c) put  $\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$  in equation

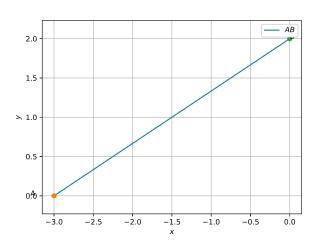


Fig. 3.3.1: line3

codes/plane and line3.py

$$(-2 \ 3) \begin{pmatrix} x \\ 0 \end{pmatrix} = 6$$
 (3.3.1.11)

$$x = -3 \tag{3.3.1.12}$$

put  $\mathbf{x} \begin{pmatrix} 0 \\ y \end{pmatrix}$  in equation

$$(-2 \ 3) \begin{pmatrix} 0 \\ y \end{pmatrix} = 6$$
 (3.3.1.13)  
 $y = 2$  (3.3.1.14)

$$y = 2$$
 (3.3.1.14)

$$\mathbf{P} = \begin{pmatrix} -3\\0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 0\\2 \end{pmatrix} \tag{3.3.1.15}$$

d) there is no constant in the line equation thus it passes through the origin. put  $\mathbf{x} \begin{pmatrix} 3 \\ y \end{pmatrix}$  in equation

$$(1 -3)\binom{3}{y} = 0$$
 (3.3.1.16)

$$y = 1 (3.3.1.17)$$

$$\mathbf{P} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 3 \\ 1 \end{pmatrix}$$
 (3.3.1.17)

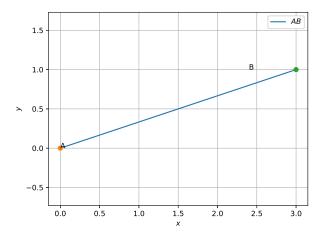


Fig. 3.3.1: line4

codes/plane and line4.py

e) there is no constant in the line equation thus it passes through the origin put  $\mathbf{x} \begin{pmatrix} 1 \\ y \end{pmatrix}$  in equation

$$(2 -1)\begin{pmatrix} 1 \\ v \end{pmatrix} = 0$$
 (3.3.1.19)

$$y = 1 (3.3.1.20)$$

$$\begin{pmatrix} 2 & -1 \end{pmatrix} \begin{pmatrix} 1 \\ y \end{pmatrix} = 0 \qquad (3.3.1.19)$$
$$y = 1 \qquad (3.3.1.20)$$
$$\mathbf{P} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \qquad (3.3.1.21)$$

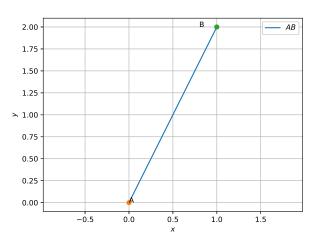


Fig. 3.3.1: line5

codes/plane and line5.py

f) put  $\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$  in equation

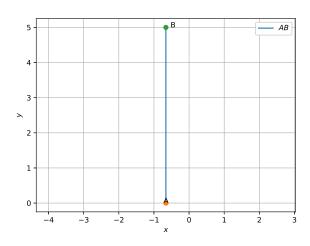


Fig. 3.3.1: line6

codes/plane and line6.py

$$(3 \ 0)\begin{pmatrix} x \\ 0 \end{pmatrix} = -2$$
 (3.3.1.22)

$$x = -\frac{2}{3} \tag{3.3.1.23}$$

we can see in this equation the value of x coordinate does not depend on the y coordinate so we can say that it is parallel to the y-axis.

g) put  $\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$  in equation

$$(0 \quad 1) \binom{0}{y} = 2$$
 (3.3.1.24)

$$y = 2 (3.3.1.25)$$

we can see in this equation the value of y coordinate does not depend on the x coordinate so we can say that it is parallel to the x-axis.

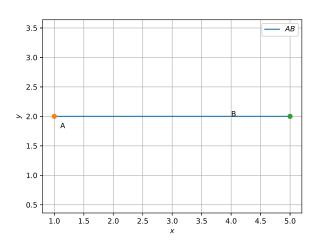


Fig. 3.3.1: line7

codes/plane\_and\_line7.py

h) put  $\mathbf{x} \begin{pmatrix} x \\ 0 \end{pmatrix}$  in equation

$$(2 \ 0)\begin{pmatrix} x \\ 0 \end{pmatrix} = 5$$
 (3.3.1.26)

$$x = -\frac{5}{2} \tag{3.3.1.27}$$

we can see in this equation the value of x coordinate does not depend on the y coordi-

nate so we can say that it is parallel to the y-axis.

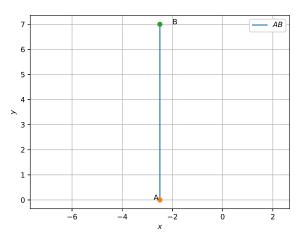


Fig. 3.3.1: line8

codes/plane and line8.py

#### 3.4 Motion

#### 3.4.1 Problem:

1. A hicker stands on the edge of a cliff 490m above the ground and throws a stone horizantally with an initial speed of 15ms<sup>-1</sup>. Neglecting air rsistance, find the time taken by the stone to reach the ground, and the speed with which it hits the ground.

#### 3.4.2 Solution:

1. given  $\Longrightarrow$ 

$$\mathbf{A} = \begin{pmatrix} 0 \\ 490 \end{pmatrix} \tag{3.4.1.1}$$

$$\mathbf{a} = \begin{pmatrix} 0 \\ -9.8 \end{pmatrix} \tag{3.4.1.2}$$

$$\mathbf{v}_A = \begin{pmatrix} 1.5\\0 \end{pmatrix} \tag{3.4.1.3}$$

$$\mathbf{v}_B = \mathbf{v}_A + \mathbf{a}t \tag{3.4.1.4}$$

$$\mathbf{d} = \mathbf{v}_A t + \frac{1}{2} \mathbf{a} t^2 \tag{3.4.1.5}$$

$$\mathbf{B} = \mathbf{A} + \mathbf{d} \tag{3.4.1.6}$$

$$\mathbf{B} = \begin{pmatrix} 0 \\ 490 \end{pmatrix} + \begin{pmatrix} 1.5 \\ 0 \end{pmatrix} t + \frac{1}{2} \begin{pmatrix} 0 \\ -9.8 \end{pmatrix} t^2 \qquad (3.4.1.7)$$

$$\begin{pmatrix} x \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 490 \end{pmatrix} + \begin{pmatrix} 1.5 \\ 0 \end{pmatrix} t + \frac{1}{2} \begin{pmatrix} 0 \\ -9.8 \end{pmatrix} t^2$$
 (3.4.1.8)

$$490 = \frac{1}{2}9.8t^2 \quad (3.4.1.9)$$

$$t = 10 (3.4.1.10)$$

$$\mathbf{v}_B = \begin{pmatrix} 1.5 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 9.8 \end{pmatrix} 10 = \begin{pmatrix} 1.5 \\ 98 \end{pmatrix}$$
 (3.4.1.11)

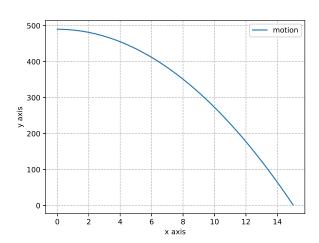


Fig. 3.4.1: motion

codes/motion.py

#### 3.5 Matrix

#### 3.5.1 Problem:

1. Construct a 2 x 2 matrix  $A = [a_i j]$ , whose elements are given by:

a) 
$$a_{ij} = \frac{(i+j)^2}{2}$$

b) 
$$a_{ij} = \frac{i}{j}$$

c) 
$$a_{ij} = \frac{(i+2j)^2}{2}$$

#### 3.5.2 Solution:

1. Formation of matrix can be done as follow a)

$$a_{11} = 2, a_{12} = 4.5$$
 (3.5.1.1)

$$a_{21} = 4.5, a_{22} = 8$$
 (3.5.1.2)

$$\mathbf{A} = \begin{pmatrix} 2 & 4.5 \\ 4.5 & 8 \end{pmatrix} \tag{3.5.1.3}$$

$$a_{11} = 1, a_{12} = 0.5$$
 (3.5.1.4)

$$a_{21} = 2, a_{22} = 1$$
 (3.5.1.5)

$$\mathbf{A} = \begin{pmatrix} 1 & 0.5 \\ 2 & 1 \end{pmatrix} \tag{3.5.1.6}$$

c)

$$a_{11} = 4.5, a_{12} = 12.5$$
 (3.5.1.7)

$$a_{21} = 8, a_{22} = 18$$
 (3.5.1.8)

$$\mathbf{A} = \begin{pmatrix} 4.5 & 12.5 \\ 2 & 18 \end{pmatrix} \tag{3.5.1.9}$$

#### 3.6 Determinents

3.6.1 Problem:

2. If 
$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 4 \end{bmatrix}$$
 then show that  $|3A| = 27|A|$ 

3.6.2 Solution.

1.

$$\begin{vmatrix} 3A \end{vmatrix} = 3 \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 4 \end{bmatrix} = \begin{bmatrix} 3 & 0 & 3 \\ 0 & 3 & 6 \\ 0 & 0 & 12 \end{bmatrix}$$
 (3.6.1.1)

$$|3A| = 108$$
 (3.6.1.2)

$$|A| = 4$$
 (3.6.1.3)

$$\begin{vmatrix} 3A \end{vmatrix} = 108 \quad (3.6.1.2)$$
  
 $\begin{vmatrix} A \end{vmatrix} = 4 \quad (3.6.1.3)$   
 $\begin{vmatrix} 3A \end{vmatrix} = 27 \begin{vmatrix} A \end{vmatrix} \quad (3.6.1.4)$ 

hence proved

#### 3.7 Linear inequalities

#### 3.7.1 Problem:

1. the marks obtained by the student of class XI in first and second terminal examination are 62 and 48, respectively. Find the minimum marks in annual examination to have an average of at least 60 marks.

#### 3.7.2 Solution:

1. let assume that the student get x marks in the annual examination so now...

$$60 = \frac{62 + 48 + \mathbf{x}}{3} \tag{3.7.1.1}$$

$$\mathbf{x} = 180 - 62 - 48 \tag{3.7.1.2}$$

$$\mathbf{x} = 70 \tag{3.7.1.3}$$

#### 4 CIRCLE

#### 4.1 Problem

1. find the area enclosed by the circle (x) = a area

#### 4.2 Solution

1.

$$||\Delta|| = 2\pi r^2 \tag{4.2.1.1}$$

$$||\Delta|| = 2\pi a^2 \tag{4.2.1.2}$$

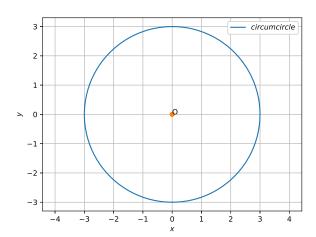


Fig. 4.2.1: circle

codes/circle.py

#### 5 Conics

#### 5.1 Problem

1. Find the zeroes of the following Quadratic polynomials and verify the relationship between the zeroes and the coefficients.

a) 
$$x^2 - 2x - 8$$

- b)  $4u^2 + 8u$
- c)  $4s^2 4s + 1$
- d)  $t^2 15$
- e)  $6x^2 3 7x$ f)  $3x^2 2x 8$

#### 5.2 Solution

1.

$$\begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} A & \frac{B}{2} \\ \frac{B}{2} & C \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} D & E \end{bmatrix} \begin{bmatrix} x & y \end{bmatrix} + F$$
(5.2.1.1)

2.

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^T \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} -2 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} - 8 \qquad (5.2.2.1)$$

$$x^2 - 2x - 8 = 0 (5.2.2.2)$$

$$(x-4)(x+2) = 0$$
 (5.2.2.3)

$$\mathbf{s}_1 = 4, \mathbf{s}_2 = -2 \quad (5.2.2.4)$$

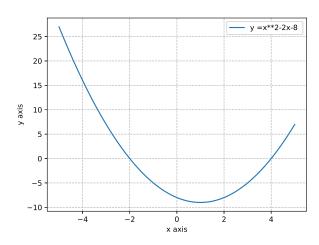


Fig. 5.2.2: equation 1

codes/perabola2.py

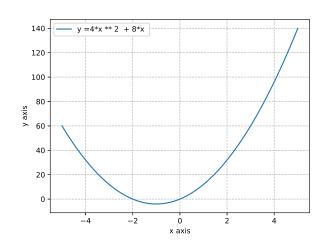


Fig. 5.2.3: equation 2

codes/perabola2.py

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^T \begin{bmatrix} 4 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} 8 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix}$$
 (5.2.3.1)

$$4u^2 + 8u = 0 (5.2.3.2)$$

$$(4u)(u+2) = 0 (5.2.3.3)$$

$$(4u)(u+2) = 0$$
 (5.2.3.3)  
 $\mathbf{u}_1 = 0, \mathbf{u}_2 = -2$  (5.2.3.4)

4.

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^T \begin{bmatrix} 4 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} -4 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + 1 \quad (5.2.4.1)$$

$$4s^2 - 4s + 1 = 0 (5.2.4.2)$$

$$(2s-1)(2s+1) = 0$$
 (5.2.4.3)

$$\mathbf{s}_1 = \frac{1}{2}, \mathbf{s}_2 = -\frac{1}{2}$$
 (5.2.4.4)

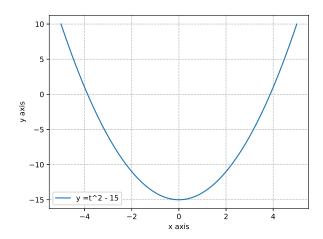


Fig. 5.2.5: equation 4

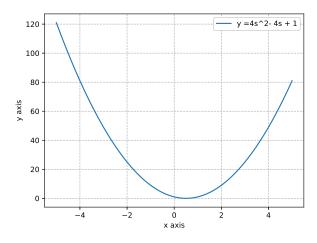


Fig. 5.2.4: equation 3

6.

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^T \begin{bmatrix} 6 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} -7 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} - 3 \quad (5.2.6.1)$$

$$6x^2 - 3 - 7x = 0 (5.2.6.2)$$

$$(2x-3)(3x + 1) = 0$$
 (5.2.6.3)

$$\mathbf{x}_1 = \frac{3}{2}, \mathbf{x}_2 = -\frac{1}{3}$$
 (5.2.6.4)

codes/perabola3.py

5.

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^T \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} - 15 \qquad (5.2.5.1)$$

$$t^2 - 15 = 0 \qquad (5.2.5.2)$$

$$\mathbf{t}_1 = \sqrt{15}, \mathbf{t}_2 = -\sqrt{15}$$
 (5.2.5.3)

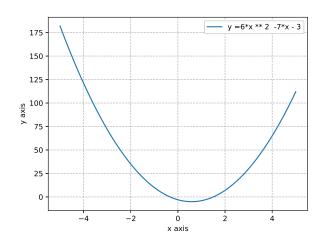


Fig. 5.2.6: equation 5

codes/perabola4.py

codes/perabola5.py

$$\begin{bmatrix} \mathbf{x} \end{bmatrix}^{T} \begin{bmatrix} 3 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} + \begin{bmatrix} -1 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{x} \end{bmatrix} - 4 \qquad (5.2.7.1)$$
$$3x^{2} - 2x - 8 = 0 \qquad (5.2.7.2)$$
$$(3x44)(x+1) = 0 \qquad (5.2.7.3)$$
$$\mathbf{x}_{1} = -1, \mathbf{x}_{2} = -\frac{4}{3} \qquad (5.2.7.4)$$

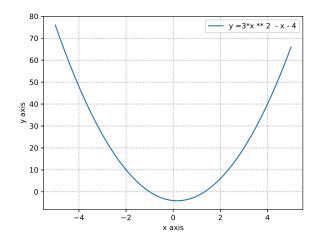


Fig. 5.2.7: equation 6

codes/perabola6.py