

Definitions

$$P = \text{Positive outcomes} = FN + TP$$

$$N = \text{Negative outcomes} = FP + TN$$

$$PP = \text{Predicted Positive outcomes} = FP + TP$$

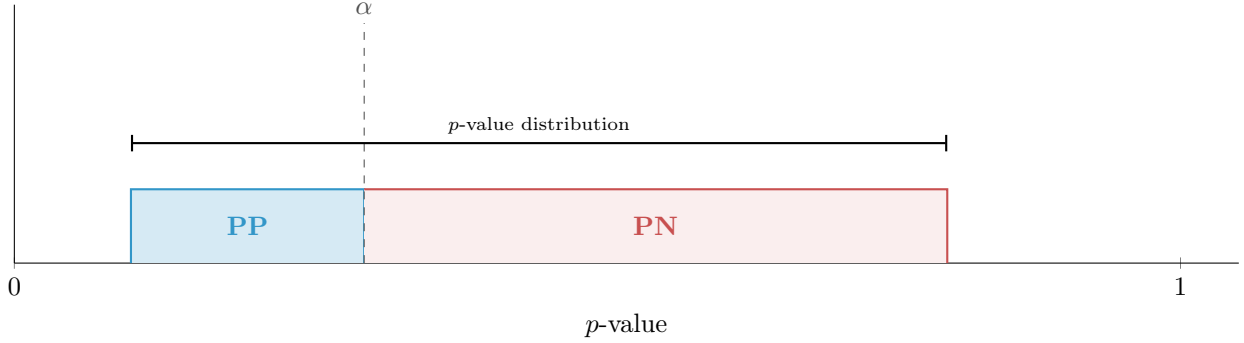
$$PN = \text{Predicted Negative outcomes} = FN + TN$$

Positive Prediction Rate (PPR):

$$PPR = \frac{PP}{PP + PN} = \frac{TP + FP}{TP + FN + FP + TN} = \frac{TP + FP}{P + N}$$

Sampled p -value distribution

p -value distribution classified as “Predicted Positive” (PP) when below α and “Predicted Negative” (PN) otherwise. Standard deviation (σ_p) is sampled from the distribution.

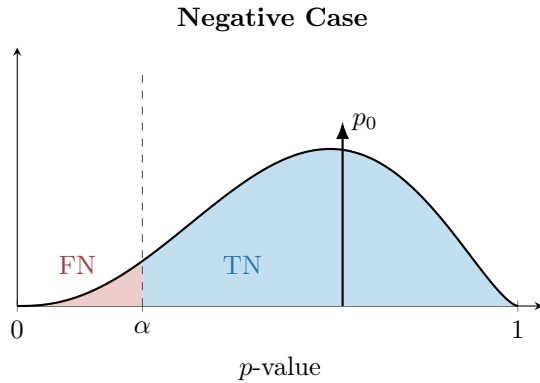


Simulated p -value using Beta distributions

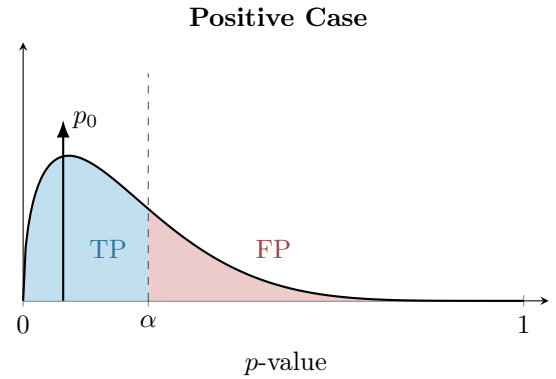
Standard deviation σ_p is simulated using uncertainty formulae from Table 1. Uncertainty on p -value is modeled using Beta distributions. With $\mathbb{E}[\beta] = p_0$ and $\text{Var}[\beta] = \sigma_p^2$, we solve for parameters a, b :

$$\begin{cases} p_0 = \frac{a}{a+b} \\ \sigma_p^2 = \frac{ab}{(a+b)^2(a+b+1)} \end{cases} \implies \begin{cases} a = p_0 \left(\frac{p_0(1-p_0)}{\sigma_p^2} - 1 \right) \\ b = (1-p_0) \left(\frac{p_0(1-p_0)}{\sigma_p^2} - 1 \right) \end{cases}$$

Then, we have two cases depending on p_0 significance:



$$\begin{aligned} \mathbb{P}[FN] &= \int_0^\alpha \beta(x; a, b) dx \\ \mathbb{P}[TN] &= 1 - \mathbb{P}[FN] \end{aligned}$$



$$\begin{aligned} \mathbb{P}[TP] &= \int_0^\alpha \beta(x; a, b) dx \\ \mathbb{P}[FP] &= 1 - \mathbb{P}[TP] \end{aligned}$$

Statistic	Numerical standard deviation	Numerical p-value uncertainty
Cohen's d	$\sigma_d \approx \nu_{\text{npv}} \frac{2}{\sqrt{n}}$	-
Two-sample t	$\sigma_t \approx \nu_{\text{npv}}$	$\sigma_p \approx 2f_{t,df}(t)\nu_{\text{npv}}$
Partial correlation	$\sigma_r \geq \nu_{\text{npv}} \sqrt{\frac{(1-r^2)^3}{n-1}}$	$\sigma_p \geq 2f_{t,df}(t) \sqrt{\frac{df}{n-1}} \nu_{\text{npv}}$
ANCOVA	$\sigma_F \approx 2\sqrt{F}\nu_{\text{npv}}$	$\sigma_p \approx 2\sqrt{F}f_{\mathcal{F}}(F; 1, df_2)\nu_{\text{npv}}$

Table 1: First-order numerical uncertainty of common statistical tests under Monte Carlo Arithmetic perturbations. Cohen's d formula assumes large and equal group sizes. $f_{t,df}$ and $f_{\mathcal{F}}(F; 1, df_2)$ denote the probability density functions of the Student's t -distribution with df degrees of freedom and the \mathcal{F} -distribution with $(1, df_2)$ degrees of freedom, respectively. The p -value approximation for the partial correlation uses $t = r(df/(1 - r^2))^{1/2}$.