

Selection Sort

Code

```
1 function selectionSort(A: number[]) {
2   for (let i = 0; i < A.length; i++) {
3     // find index of minimum element
4     let min = i;
5     for (let j = i; j < A.length; j++) {
6       if (A[j] < A[min]) min = j;
7     }
8     // swap with front of sorted subarray
9     if (min !== i) {
10      const tmp = A[i];
11      A[i] = A[min];
12      A[min] = tmp;
13    }
14  }
15  return A;
16 }
```

Design

- the algorithm maintains 2 subarrays in a given array
- in every iteration, the minimum element from the unsorted subarray is added to the end of the sorted subarray

Runtime Analysis

The first iteration will run $n - 1$ times, the second will run $n - 2$, and so on until 1.

$$\begin{aligned}(n - 1) + (n - 2) + \dots + 1 &= \sum_{i=1}^{n-1} (n - i) \\ &= \frac{(n - 1)((n - 1) + 1)}{2} \\ &= \Theta(n^2)\end{aligned}$$

- note that you can use the sum of an arithmetic series formula to show this
- also notice that the runtime analysis is *always* $\theta(n^2)$ for best, worst, and average cases