

Simulating the 21 cm forest detectable with LOFAR and SKA in the spectra of high- z GRBs

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ABSTRACT

We investigate the feasibility of detecting 21 cm absorption features in the afterglow spectra of high redshift long Gamma Ray Bursts (GRBs). This is done employing simulations of cosmic reionization, together with the instrumental characteristics of the LOw Frequency ARray (LOFAR). We find that absorption features could be marginally (with a S/N larger than a few) detected by LOFAR at $z \gtrsim 7$ if the GRB originated from Pop III stars, while the detection would be easier if the noise were reduced by one order of magnitude, i.e. similar to what is expected for the first phase of the Square Kilometer Array (SKA1-low). On the other hand, more standard GRBs are too dim to be detected even with ten times the sensitivity of SKA1-low, and only in the most optimistic case can a S/N larger than a few be reached at $z \gtrsim 9$.

Key words: Cosmology - IGM - reionization - 21cm line - GRBs

1 INTRODUCTION

Present and planned radio facilities such as LOFAR¹ (van Haarlem et al. 2013), MWA², PAPER³ and SKA⁴, aim

¹ <http://lofar.org>

² <http://www.mwatelescope.org>

³ <http://eor.berkeley.edu>

⁴ <http://www.skatelescope.org>

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at detecting the 21 cm signal from the Epoch of Reionization (EoR) in terms of observations such as tomography (e.g. Tozzi et al. 2000; Ciardi & Madau 2003; Furlanetto et al. 2004; Mellema et al. 2006; Santos et al. 2008; Geil & Wyithe 2009; Zaroubi et al. 2012; Malloy & Lidz 2013), fluctuations and power spectrum (e.g. Madau et al. 1997; Shaver et al. 1999; Tozzi et al. 2000; Ciardi & Madau 2003; Furlanetto et al. 2004; Mellema et al. 2006; Pritchard & Loeb 2008; Baek et al. 2009; Patil et al. 2014), or absorption features in the spectra of high- z radio-loud sources (e.g. Carilli et al. 2002; Furlanetto 2006; Xu et al. 2009; Mack & Wyithe 2012; Meiksin 2011; Xu et al. 2011; Vasiliev & Shchekinov 2012; Ciardi et al. 2013; Ewall-Wice et al. 2014). These observations would offer unique information on the statistical properties of the EoR (such as e.g. its duration), the amount of H I present in the intergalactic medium (IGM), and, ultimately, the history of cosmic reionization and the properties of its sources.

In particular, the detection of absorption features in 21 cm could be used to gain information on the cold, neutral hydrogen present along the line of sight (LOS) towards e.g. high- z quasars, similarly to what is presently done at lower redshift with the Ly α forest (for a review see Meiksin 2009). While the detection and analysis of the 21 cm forest is in principle an easier task compared to imaging or even statistical measurements and could probe larger k -modes, these absorption like experiments are rendered less likely to happen due to the apparent lack of high- z radio-loud sources (e.g. Carilli et al. 2002; Xu et al. 2009), the most distant being TN0924-2201 at $z=5.19$ (van Breugel et al. 1999).

Gamma Ray Bursts (GRBs) have been suggested as alternative background sources (e.g. Ioka & Mészáros 2005; Inoue et al. 2007; Toma et al. 2011), as they have been observed up to $z \sim 8 - 9$ (Salvaterra et al. 2009; Tanvir et al. 2009; Cucchiara et al. 2011), they are expected to occur up to the epoch of the first stars (Bromm & Loeb 2002; Natarajan et al. 2005; Komissarov & Barkov 2010a; Mészáros & Rees 2010; Campisi et al. 2011; Suwa & Ioka 2011; Toma et al. 2011) and to be visible in the IR and radio up to very high- z due to cosmic time dilation effects (Ciardi & Loeb 2000; Lamb & Reichart 2000). Because of the latter, if a GRB afterglow were observed in the IR by e.g. ALMA⁵ at a post-burst observer time of a few hours, this would offer a few days to plan for an observation in the radio accordingly (e.g. Inoue et al. 2007).

In this letter we investigate the feasibility of detecting the 21 cm forest with LOFAR and SKA in the radio afterglow of high- z GRBs. In Section 2 we present the method used to calculate the forest; in Section 3 we discuss the properties of the GRBs; in Section 4 we present our results; and in Section 5 we give our conclusions.

2 THE 21 CM FOREST

In this work we make use of the pipeline developed in Ciardi et al. (2013, hereafter C2013) to assess the feasibility of detecting the 21 cm forest in the spectra of high- z GRBs. For this reason, here we only give a brief overview of this pipeline, while we refer the reader to the original paper for more details.

If a radio-loud source is located at redshift z_s , the photons emitted at a frequency $\nu > \nu_{21\text{cm}} = 1.42$ GHz can be absorbed by the neutral hydrogen encountered along their LOS at $z =$

$(\nu_{21\text{cm}}/\nu)(1 + z_s) - 1$, with a probability $(1 - e^{-\tau_{21\text{cm}}})$. The optical depth in the low-frequency limit, as appropriate for the 21 cm line, can be written as (e.g. Madau et al. 1997):

$$\tau_{21\text{cm}} = \frac{3}{32\pi} \frac{h_p c^3 A_{21\text{cm}}}{k_B \nu_{21\text{cm}}^2} \frac{x_{\text{HI}} n_{\text{H}}}{T_s (1 + z) (dv_{\parallel}/dr_{\parallel})}, \quad (1)$$

where n_{H} is the hydrogen number density, x_{HI} is the mean neutral hydrogen fraction, T_s is the gas spin temperature, $A_{21\text{cm}} = 2.85 \times 10^{-15} \text{ s}^{-1}$ is the Einstein coefficient of the transition, and $dv_{\parallel}/dr_{\parallel}$ is the gradient of the proper velocity along the LOS. The other symbols have the usual meaning.

The optical depth has been calculated using the simulation of reionization called $\mathcal{L}4.39$ in C2013. This has been obtained by post-processing a GADGET-3 (an updated version of the publicly available code GADGET-2; see Springel 2005) hydrodynamic simulation with the 3D Monte Carlo radiative transfer code CRASH (Ciardi et al. 2001; Maselli et al. 2003, 2009; Pierleoni et al. 2009; Partl et al. 2011; Graziani et al. 2013), which follows the propagation of UV photons and evaluates self-consistently the evolution of H I, He I, He II and gas temperature. The hydrodynamic simulations were run in a box of size $4.39 h^{-1}$ Mpc comoving, with 2×256^3 gas and dark matter particles, and cosmological parameters $\Omega_{\Lambda} = 0.74$, $\Omega_m = 0.26$, $\Omega_b = 0.024 h^2$, $h = 0.72$, $n_s = 0.95$ and $\sigma_8 = 0.85$, where the symbols have the usual meaning. The gas density, temperature, peculiar velocity and halo masses, were gridded onto a uniform 128^3 grid to be processed with CRASH. The sources are assumed to have a power-law spectrum with index 3. For more details on the choice of the parameters and the results of the reionization histories we refer the reader to Ciardi et al. (2012) and C2013. Here we further note that the simulations were designed to match WMAP observations of the Thomson scattering optical depth (Komatsu et al. 2011), while more recent Planck measurements (Planck Collaboration et al. 2015) favor a lower value, i.e. a delayed reionization process. This does not change our conclusions, and it actually makes them conservative, as more H I would be expected at each redshift compared to the one estimated here.

Random LOS are cast through the simulation boxes and the corresponding 21 cm absorption is calculated. It should be noted that here we consider a case in which the temperature of the IGM is determined only by the effect of UV photons, i.e. gas which is not reached by ionizing photons remains cold, while the effect of Ly α and x-ray photons on the 21 cm forest is extensively discussed in C2013.

Once the theoretical spectra are evaluated, instrumental effects and noise need to be included to calculate mock spectra. To do this we assume to have a radio source at redshift z_s , with a power-law spectrum with spectral index α , and a flux density $S_{\text{in}}(z_s)$. We then simulate spectra as they would be seen by LOFAR. While we refer the reader to C2013 for more details, here we just mention that the noise n is given by:

$$n = \frac{1}{\eta} \frac{SEFD}{\sqrt{2t_{\text{int}}\Delta\nu}}, \quad (2)$$

where $\eta = 0.5$ is the system efficiency, $\Delta\nu$ is the bandwidth, t_{int} is the integration time, and $SEFD$ is the system equivalent density calculated assuming to have 48 stations, 24 tiles per station with 16 dipoles each, a dipole efficiency of 1, and a system noise $T_{\text{sys}} = [140 + 60(\nu/300 \text{ MHz})^{-2.55}] \text{ K}$.

⁵ <http://www.almaobservatory.org/>

3 RADIO AFTERGLOWS OF HIGH-Z GRBS

Here we discuss aspects of the radio afterglow emission from GRBs (see e.g. van Eerten 2013; Granot & van der Horst 2014, for recent reviews) that are most relevant for studies of the 21 cm forest at high redshift. GRB afterglows consist primarily of broadband synchrotron emission from nonthermal electrons accelerated in the forward shock of relativistic blastwaves, which are driven into the ambient medium by transient, collimated jets triggered by the GRB central engine. The low-frequency radio flux is typically suppressed in the beginning due to synchrotron self-absorption and rises gradually as the blastwave expands. The light curve at a given frequency ν peaks when the emission becomes optically thin to self-absorption, after which it decays, according to the overall behavior of the decelerating blastwave. As background sources for observing the 21 cm forest, the emission near this peak flux time is naturally the most interesting.

The expected observer peak time, $t_{pk}(\nu)$, and the corresponding peak flux, $S_{in}(\nu)$, can be evaluated using the formulation outlined in the Appendix of Inoue (2004), which is based on standard discussions in the literature (e.g. Sari et al. 1998, 1999; Panaitescu & Kumar 2000) and is sufficient for our purposes of estimating the radio afterglow emission at relatively late times after the burst. We consider cases for which the peak time occurs after the crossing time of the minimum frequency, ν_m , as well as the jet break time, valid for the range of parameters chosen here⁶. For concreteness, the spectral index of the accelerated electron distribution is taken to be $p = 2.2$, implying a radio spectral index of $\alpha = 0.6$ for the optically thin, slow cooling regime. We also choose $\epsilon_e = 0.1$ and $\epsilon_B = 0.01$ for the fractions of post-shock energy imparted to accelerated electrons and magnetic fields, respectively, consistent with observationally inferred values (Panaitescu & Kumar 2001). This gives:

$$t_{pk}(\nu) \simeq 540 \text{ days } E_{53}^{0.44} n_0^{0.2} \theta_{-1}^{0.88} \times \left(\frac{1+z}{11} \right)^{0.03} \left(\frac{\nu}{10^8 \text{ Hz}} \right)^{-0.97} \quad (3)$$

and

$$S_{in}(\nu) \simeq 1.1 \times 10^{-3} \text{ mJy } E_{53}^{0.77} n_0^{-0.38} \theta_{-1}^{1.54} \times \left(\frac{D_L(z)}{3.3 \times 10^{29} \text{ cm}} \right)^{-2} \left(\frac{1+z}{11} \right)^{2.53} \left(\frac{\nu}{10^8 \text{ Hz}} \right)^{-1.53} \quad (4)$$

where $E = 10^{53} E_{53}$ erg is the isotropic-equivalent blastwave kinetic energy, $\theta = 0.1 \theta_{-1}$ rad is the jet collimation half-angle, $n_{medium} = n_0 \text{ cm}^{-3}$ is the ambient medium number density, and $D_L(z)$ is the luminosity distance.

The known population of GRBs (referred to as GRBII, as they are expected to originate from standard Pop II/I stars) has been observationally inferred to possess values of these quantities up to $E \sim 10^{54}$ erg, $\theta \sim 0.3$ rad and/or down to $n_{medium} \sim 10^{-4} \text{ cm}^{-3}$ (Panaitescu & Kumar 2001; Ghirlanda et al. 2013a). Thus, they may provide fluxes up to $S_{in} \sim 0.1$ mJy at $\nu \sim 100$ MHz and $t_{pk} \sim 3000$ days (i.e. as sources virtually steady over several years) for events at $z \sim 10$ under favorable conditions (see also Ioka & Mészáros 2005; Inoue et al. 2007).

On the other hand, although not yet confirmed by observations, an intriguing possibility for high- z detections is the existence of GRBs arising from Population III stars (GRBIII), with

⁶ Although the time evolution after the jet break is not explicitly described in Inoue (2004), it is taken into account following Sari et al. (1999).

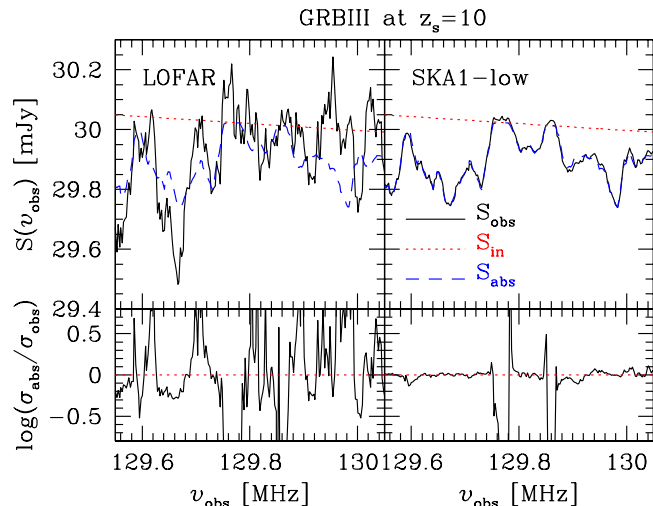


Figure 1. Upper panels: Spectrum of a GRBIII positioned at $z_s = 10$ (i.e. $\nu \sim 129$ MHz), with a flux density $S_{in}(z_s) = 30$ mJy. The red dotted lines refer to the intrinsic spectrum of the source, S_{in} ; the blue dashed lines to the simulated spectrum for 21 cm absorption, S_{abs} ; and the black solid lines to the spectrum for 21 cm absorption as it would be seen with a bandwidth $\Delta\nu = 10$ kHz, after an integration time $t_{int} = 1000$ h. The left and right panels refer to a case with the noise n given in eq. 2 (LOFAR telescope) and with $0.1n$ (expected for SKA1-low), respectively. Lower panels: $\sigma_{abs}/\sigma_{obs}$ corresponding to the upper panels. See text for further details.

significantly larger blastwave energies, up to values as high as $E \sim 10^{57}$ erg, by virtue of their prolonged energy release fueled by accretion of the extensive envelopes of their progenitor stars (Mészáros & Rees 2010; Komissarov & Barkov 2010b; Suwa & Ioka 2011). Compared to known GRBs, their blastwaves can expand to much larger radii and consequently with much brighter low-frequency radio emission, potentially exceeding $S_{in} \sim 10$ mJy at $\nu \sim 100$ MHz and $t_{pk} \sim 3 \times 10^4$ days for events at $z \sim 20$ (Toma et al. 2011; Ghirlanda et al. 2013b).

Note that although more recent and detailed theoretical studies of afterglow emission relying on hydrodynamical simulations have revealed non-trivial deviations from the simple description presented above (van Eerten 2013; Ghirlanda et al. 2013b), the latter should still be sufficient for our aim of discussing expectations for observations of 21 cm forest.

Finally, as reference numbers, Campisi et al. (2011) find that ~ 1 (< 0.06) $\text{yr}^{-1} \text{ sr}^{-1}$ GRBII (GRBIII) are predicted to lie at $z > 6$. This translates into $\sim 7.5 \times 10^{-3}$ GRBII ($\sim 4.5 \times 10^{-4}$ GRBIII) per year in a 25 deg^2 (LOFAR) field of view, and ~ 3 (~ 0.2) per year in a 10^4 deg^2 (SKA) field of view.

4 RESULTS

For an easier comparison to a case in which the background source is a radio-loud QSO, here we show results for the same LOS and at the same redshift of C2013 (see their Figs. 11, 12 and 13).

In the upper panels of Figure 1 we plot the spectrum of a GRBIII at $z_s = 10$ (i.e. $\nu \sim 129$ MHz) with a flux density $S_{in}(z_s) = 30$ mJy. The simulated absorption spectrum, S_{abs} , is shown together with the observed spectrum, S_{obs} , calculated assuming an observation time $t_{int} = 1000$ h, a bandwidth $\Delta\nu = 10$ kHz and a noise n (given in eq. 2; left panels) and $0.1n$ (similar to the value expected

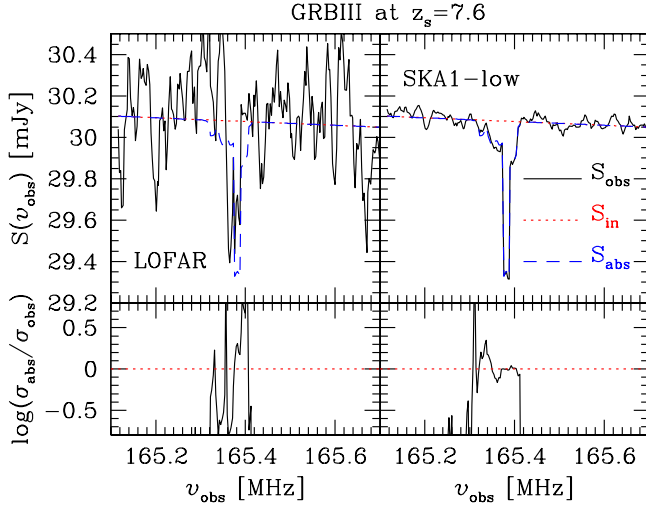


Figure 2. As Figure 1, but the GRBIII is positioned at $z_s = 7.6$ (i.e. $\nu \sim 165$ MHz) and $\Delta\nu = 5$ kHz.

for SKA1-low⁷, which is $\sim 1/8$ th of the LOFAR noise; right panels). In analogy to C2013, in the lower panels of the Figure we also show the quantity $\sigma_{\text{abs}}/\sigma_{\text{obs}}$, where $\sigma_i = S_i - S_{\text{in}}$ and $i = \text{abs, obs}$. If indeed such powerful GRBs exist, then absorption features could be detected by LOFAR with a signal-to-noise $S/N \sim 5$, while if the noise were reduced by a factor of 10 the detection would be much easier.

Figure 2 shows a LOS to the same GRB located at $z = 7.6$, when the IGM is $\sim 80\%$ ionized by volume. The LOS has been chosen to intercept a pocket of gas with $\tau_{21\text{cm}} > 0.1$ to show that strong absorption features could be detected, albeit by LOFAR only marginally with a S/N of a few, also at a redshift when most of the IGM is in a highly ionized state.

On the other hand, a strong average absorption (rather than the absorption features seen in the previous figures) can be easily detected ($S/N > 10$) in the spectra of GRBs located at very high redshift, as shown in Figure 3. If the intrinsic spectrum of the source were known by other means, such detection could be used to infer the global amount of neutral hydrogen present in the IGM.

We have applied the same pipeline also to more standard GRBII, which have a flux density two to three orders of magnitude lower than a GRBIII. In this case we find that, even if we could collect 1000 h of observations with a noise $0.01 n$ (i.e. $1/10$ th of the SKA1-low noise), these would be barely enough to detect absorption features in 21 cm. Also in the most optimistic case, with $S_{\text{in}}(z_s) = 0.1$ mJy, a positive detection would be extremely difficult at any redshift, as shown in Figure 4, and only at $z \gtrsim 9$ a S/N larger than a few could be reached.

5 CONCLUSIONS

In this letter we have discussed the feasibility of detecting 21 cm absorption features in the spectra of high redshift GRBs with LOFAR and SKA. The distribution of H I , gas temperature and ve-

⁷ SKA1-low is the first phase of the SKA covering the lowest frequency band.

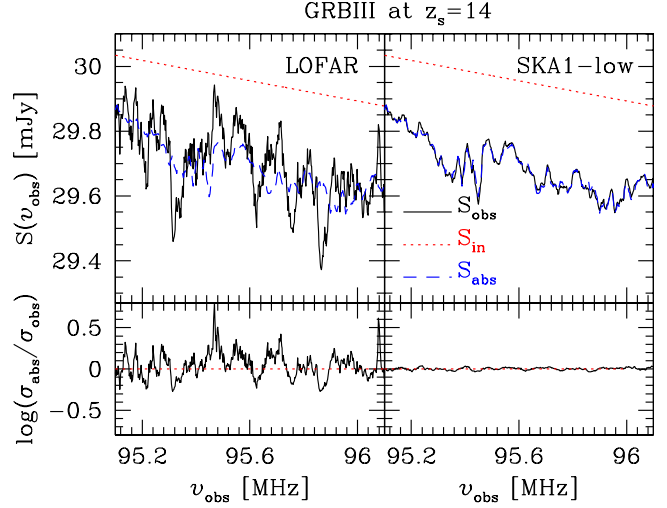


Figure 3. As Figure 1, but the GRBIII is positioned at $z_s = 14$ (i.e. $\nu \sim 95$ MHz) and $\Delta\nu = 20$ kHz.

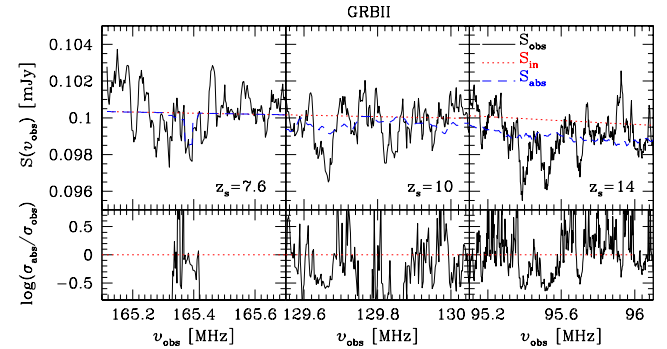


Figure 4. Upper panels: Spectrum of a GRBII with a flux density $S_{\text{in}}(z_s) = 0.1$ mJy. The red dotted lines refer to the intrinsic spectrum of the source, S_{in} ; the blue dashed lines to the simulated spectrum for 21 cm absorption, S_{abs} ; and the black solid lines to the spectrum for 21 cm absorption as it would be seen after an integration time $t_{\text{int}} = 1000$ h with a noise $0.01 n$ (i.e. $1/10$ th of the SKA1-low noise). The panels refer to a case with $z_s = 7.6$ and $\Delta\nu = 5$ kHz (left), $z_s = 10$ and $\Delta\nu = 10$ kHz (middle), $z_s = 14$ and $\Delta\nu = 20$ kHz (right). Lower panels: $\sigma_{\text{abs}}/\sigma_{\text{obs}}$ corresponding to the upper panels. See text for further details.

locity field used to calculate the optical depth to the 21 cm line have been obtained from the simulations of reionization presented in Ciardi et al. (2012) and C2013. We find that:

- absorption features in the spectra of a GRB from Pop III stars could be marginally (with a S/N larger than a few, depending on redshift) detected by LOFAR at $z \gtrsim 7$;
- the same features could be easily detected if the noise were reduced by one order of magnitude (similar to what is expected for SKA1-low);
- the flux density of a more standard GRB is too low to be detected even with ten times the sensitivity of SKA1-low. Only in the most optimistic case with a flux density of 0.1 mJy, can a S/N larger than a few be reached at $z \gtrsim 9$.

The problem of a small flux could be alleviated in case of a lensed GRB. Lensing of high- z sources has been already discussed in the literature both from a theoretical (e.g. Wyithe et al. 2011), and an observational (e.g. with the Frontier Fields as in Oesch et al. 2014) perspective. Alternatively, a statistical detection of the 21 cm forest could be attempted, as already suggested by several authors (e.g. Meiksin 2011; Mack & Wyithe 2012; Ewall-Wice et al. 2014).

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