

202206UECM34630E4a

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Review of preview

Started on	Monday, 5 September 2022, 03:22 PM
Completed on	Monday, 5 September 2022, 03:22 PM
Time taken	7 secs
Grade	0 out of a maximum of 10 (0%)

1

Marks: 0/1

You are given the following claim frequency data:

Number of Claims	0	1	2	3	4	≥ 5
Number of risks	15	10	8	8	7	13

The null hypothesis that the number of claims per risk follows a Poisson distribution with mean θ . Let Q be the value of the chi-square statistic and u be the degrees of freedom. Determine $Q+u$. _____

Answer:

✗

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Incorrect

Correct answer: 35.6017

Marks for this submission: 0/1.

2

Marks: 0/1

You are given the following:

- 121 observed losses have been recorded and are grouped as follows:

Interval	Number of Losses
$[0,1)$	19
$[1,5)$	44
$[5,10)$	23
$[10,15)$	24
$[15,\infty)$	11

- The random variable X underlying the observed losses, is believed to follow the exponential distribution with mean 5.

Determine the value of Pearson's goodness-of-fit statistic. _____

Answer:

✗

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Incorrect

Correct answer: 25.502549

Marks for this submission: 0/1.

3

Marks: 0/1

You are given the following:

- 1148 observed losses have been recorded and are grouped as follows:

Interval	Number of Losses
$[0,1)$	111
$[1,5)$	331
$[5,10)$	339

[10,15]	227
[15, ∞)	140

- The random variable X underlying the observed losses, is believed to follow the gamma distribution with $\alpha = 2$ and $\theta = 5$.

Determine the value of Pearson's goodness-of-fit statistic. _____

Answer:

X

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Incorrect

Correct answer: 457.803573

Marks for this submission: 0/1.

4

Marks: 0/1

A random sample of 8 claims x_1, \dots, x_8 is taken from the probability density function

$$f(x_i) = (\alpha \theta^\alpha) / (x_i^{\alpha+1}), \alpha, \theta > 0, x_i > \theta.$$

In ascending order the observations are:

192, 195, 197, 199, 204, 206, 210, 237

Suppose the parameters are $\alpha = 6$ and $\theta = 192$. Commonly used critical values for this test are

α	0.10	0.05	0.025	0.01
Critical Value	$1.22/\sqrt{n}$	$1.36/\sqrt{n}$	$1.48/\sqrt{n}$	$1.63/\sqrt{n}$

Determine the Kolmogrov-Smirnov statistic for the fitted distribution. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 0.4591

Marks for this submission: 0/1.

5

Marks: 0/1

A random sample of 10 claims x_1, \dots, x_{10} is taken from the probability density function

$$f(x_i) = 1/[\Gamma(\alpha)\theta^\alpha]x_i^{\alpha-1}e^{-x_i/\theta}, x_i > 0.$$

In ascending order the observations are:

35.53, 64.12, 67.22, 75.35, 79.22, 106.82, 134.72, 137.84, 143.04, 265.81

Suppose the parameters are $\alpha = 3$ and $\theta = 35$. Commonly used critical values for this test are

α	0.10	0.05	0.025	0.01
Critical Value	$1.22/\sqrt{n}$	$1.36/\sqrt{n}$	$1.48/\sqrt{n}$	$1.63/\sqrt{n}$

Determine the Kolmogrov-Smirnov statistic for the fitted distribution. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 0.178

Marks for this submission: 0/1.

6

Marks: 0/1

You fit a Pareto distribution to a sample of 250 claim amounts and use the likelihood ratio test to test the hypothesis that $\alpha = 1.5$ and $\theta = 6.5$. You are given:

- The maximum likelihood estimates are $\hat{\alpha} = 1.4$ and $\hat{\theta} = 6.2$.
- $\sum \ln(x_i + 6.5) = 691.05$
- $\sum \ln(x_i + 6.2) = 600.05$

Let Q be the value of the likelihood ratio test statistic and u be the degrees of freedom. Determine Q-u. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 411.84

Marks for this submission: 0/1.

7

Marks: 0/1

You fit a Weibull distribution to a sample of 20 claim amounts. You test $H_0: \tau = 2$ versus $H_1: \tau \neq 2$ using the likelihood ratio statistic. You are given:

- $\sum \ln x_i = 71.8411$
- $\sum x_i^2 = 86760$
- At the maximum likelihood estimate, the loglikelihood is -98.393
- The maximum likelihood estimate of θ when $\tau = 2$ is $\theta^* = 65.8635$

Determine the likelihood ratio statistic. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 6.8126

Marks for this submission: 0/1.

8

Marks: 0/1

Suppose that X_1, \dots, X_8 denotes a random sample from the probability density function given by

$$f(x|\theta_1, \theta_2) = 1/\theta_1 e^{-(x-\theta_2)/\theta_1}, x > \theta_2$$

The following random sample of 8 has been observed:

62, 125, 17, 47, 30, 25, 34, 53

Determine the likelihood ratio test statistic for testing $H_0: \theta_1 = 84.5$ versus $H_1: \theta_1 > 84.5$ with θ_2 _____

Answer:

X

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Incorrect

Correct answer: 5.558019

Marks for this submission: 0/1.

9

Marks: 0/1

Suppose that X_1, \dots, X_{10} denotes a random sample from the probability density function given by

$$f(x|\theta_1, \theta_2) = 1/\theta_1 e^{-(x-\theta_2)/\theta_1}, x > \theta_2$$

The following random sample of 10 has been observed:

65, 19, 84, 65, 63, 50, 36, 98, 47, 43

Determine the likelihood test statistic for testing $H_0: \theta_2 = 16.8$ versus $H_1: \theta_2 > 16.8$ with θ_1 unknown. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 1.125642

Marks for this submission: 0/1.

10

Marks: 0/1

You are given the following observed claim frequency data collected over a period of 365 days:

Number of Claims per Day	Observed Number of Days
0	58
1	123
2	117
3	67
4+	0

Fit a Poisson distribution to the above data, using the method of maximum likelihood. Group the data by number of claims per day into four groups: 0, 1, 2, 3.

Apply the chi square goodness of fit test to evaluate the null hypothesis that the claims follow a Poisson distribution. Let T be the value of the chi-square statistic and v be the degrees of freedom. Determine T-v. _____

Answer:

X

[Make comment or override grade](#)

Incorrect

Correct answer: 10.6045

Marks for this submission: 0/1.

