A General Scheme for NMR Supersequences Combining High- and Low-Sensitivity Experiments

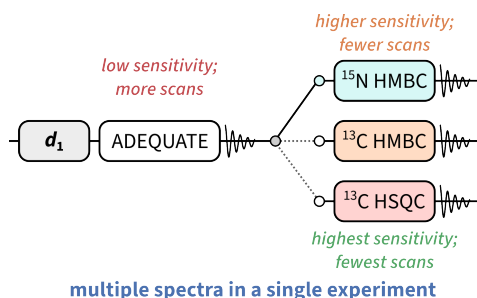Jonathan R. J. Yong,[1] Ēriks Kupče,[2] Tim D. W. Claridge[1,*]

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The concept of NMR supersequences is generalised to allow 2D experiments with vastly different sensitivities to be combined, including 1,1-ADEQUATE, ^{15}N HMBC, and other heteronuclear experiments.

Abstract

NOAH supersequences are a way of collecting multiple 2D NMR experiments in a single measurement. So far, this approach has been limited to experiments with comparable sensitivity. Here, we propose a scheme which overcomes this limitation, combining experiments with very different sensitivities such as 1,1-ADEQUATE, ^{15}N HMBC, and ^{13}C HSQC.

1   Introduction

Nuclear magnetic resonance (NMR) spectroscopy plays a key role in the structural elucidation of natural products; in particular, two-dimensional (2D) NMR experiments provide vast amounts of information on through-bond and through-space molecular connectivity.[1,2] However, these experiments are often time-consuming as they require the incrementation of indirect-dimension evolution periods in order

to construct the requisite 2D data matrices. One particularly flexible method for accelerating 2D data acquisition is the NOAH (NMR by Ordered Acquisition using ^{1}H detection) technique,[3,4] in which multiple 2D experiments ('modules') are combined into a single experiment using only a single recovery delay. These nested 'supersequences', which rely on the tailored excitation of magnetisation from different isotopologues, provide an array of 2D spectra (up to 10 so far[5]) in greatly reduced experiment times.

Virtually all common 2D experiments, such as HSQC, HMQC, COSY, TOCSY, and NOESY, have been exploited in NOAH supersequences, allowing for the (manual or computer-assisted) structural elucidation of a wide range of molecules.[5–8] However, such experiments tend to fall short in proton-sparse molecules[9–11] as they do not yield sufficient correlations. In such cases, additional information may be obtained through the HMBC[12–14] and HSQMBC[15,16] experiments which detect long-range X–^{1}H couplings ($^nJ_{XH}$, X = ^{13}C or ^{15}N). Although these tend to yield vastly more correlations, there may remain ambiguity in interpreting the resulting data as these techniques do not reveal the exact number of bonds over which a coupling is mediated. In contrast, one-bond ^{13}C–^{13}C correlations ($^1J_{CC}$), obtained through the INADEQUATE[17]—or more practically, ADEQUATE[18,19]—experiments, allow chemists to directly trace out carbon backbones with much greater certainty. The main limitation of such experiments is their low sensitivity, as they rely on pairs of heteronuclei with low natural abundances; nonetheless, with the introduction of cryogenically cooled probes and concomitant advances in achievable signal-to-noise ratios (SNRs), such experiments can nowadays be feasibly run even on relatively dilute samples.

To date, insensitive experiments such as ^{15}N HMBC and ADEQUATE have not been the main focus of NOAH supersequences.[20] This is because in a traditional 'linear' supersequence, each constituent module is recorded with the same number of transients. For dilute samples, the total experiment duration is therefore dictated by the module with the lowest sensitivity, and higher-sensitivity modules (e.g. HSQC or COSY) would be recorded with more transients than strictly necessary. Although the more sensitive modules would still be obtained 'for free', the *effective* time savings thus realised are smaller than for a supersequence constructed from modules with balanced sensitivities.

For this reason, the low-sensitivity ADEQUATE and ^{15}N HMBC modules (respectively abbreviated as 'A' and 'B_N') form a 'natural' pairing in the NOAH-2 AB_N supersequence introduced here (Figure 1b). However, in this work, we also go beyond the traditional 'linear' or 'horizontal' model of a supersequence in adding more modules through 'vertical' interleaving, in a similar fashion to the parallel supersequences recently described.[5] We show that, following an initial ADEQUATE module, up to four modules (^{15}N HMBC, ^{13}C HMBC, ^{15}N sensitivity-enhanced HSQC (seHSQC), and ^{13}C HSQC) may be interleaved in this 'vertical' fashion (Figures 1d and 1e), yielding five modules with balanced intensities and high-quality data. By tailoring the number of times each module is acquired, this technique provides a powerful and flexible way to balance modules with different sensitivities, and fully generalises our previous work on parallel supersequences, which only 'vertically' interleaved two modules at a time.
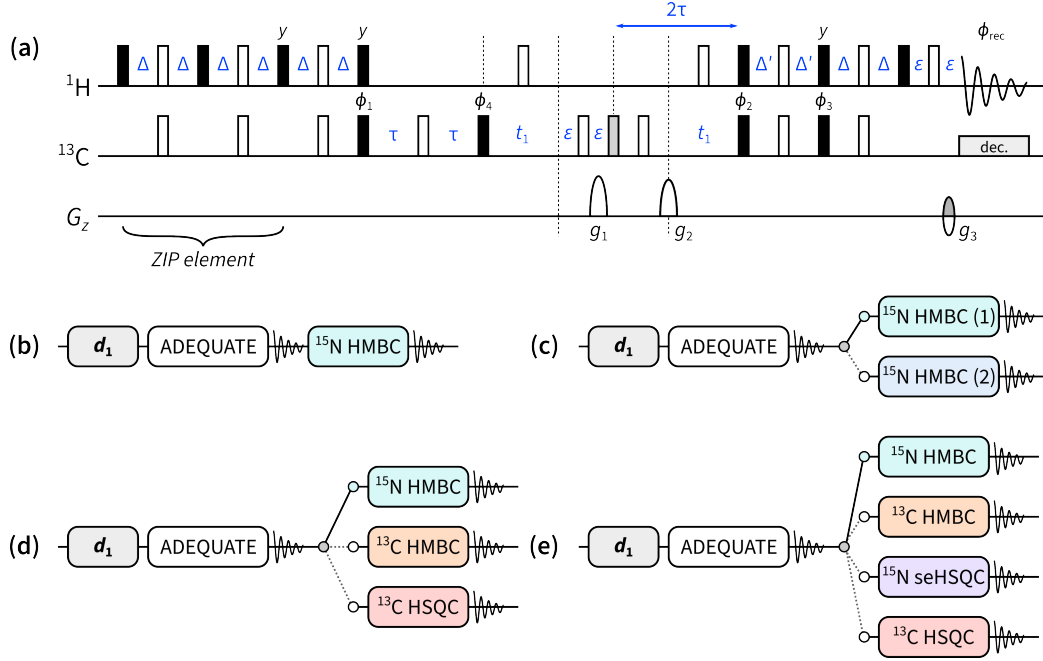
Figure 1: Pulse sequences described in this work. **(a)** ZIP-1,1-ADEQUATE module. Filled and empty bars refer to 90° and 180° pulses respectively; the grey filled bar is a 120° pulse for ^{13}C double-quantum to single-quantum coherence transfer.[21] Pulse and receiver phases are: $\phi_1 = x, -x$; $\phi_2 = 2(x), 2(-x)$; $\phi_3 = 2(y), 2(-y)$; $\phi_4 = 4(x), 4(-x)$; $\phi_{rec} = x, -x, -x, x, -x, x, x, -x$. Delays are set as follows: $\Delta = 1/(4 \cdot {}^1J_{CH})$, $\Delta' = 1/(8 \cdot {}^1J_{CH})$, and $\tau = 1/(4 \cdot {}^1J_{CC})$. ε is the minimum time required for a pulsed field gradient and the following recovery delay. Gradient amplitudes as a percentage of the maximum amplitude are: $g_1 = 78.5\%$, $g_2 = 77.6\%$, and $g_3 = -59\%$. Echo–antiecho selection is achieved by inverting the sign of g_3 as well as the pulse phase ϕ_3. **(b)** NOAH-2 AB_N supersequence. **(c)** NOAH-3 $A(B_N/B_N)$, where the two ^{15}N HMBC experiments are optimised for two different values of $^nJ_{NH}$. **(d)** NOAH-4 $A(B_N/B/S)$. **(e)** NOAH-5 $A(B_N/B/S_N^+/S)$.

2 NOAH-2 AB_N

When designing NMR supersequences, it is generally a good rule of thumb to place the module with the lowest sensitivity first: this is because any incomplete preservation of magnetisation by earlier modules will lead to decreased sensitivity in later modules. The 1,1-ADEQUATE module, which relies on neighbouring pairs of ^{13}C nuclei—occurring only in roughly 1 out of 8130 molecules—is therefore placed at the beginning of all the supersequences described here.

The ADEQUATE module (Figure 1a) is designed to only use the magnetisation of protons directly bonded to ^{13}C, which we denote here as $^1H^C$.[22,23] In order to maintain the sensitivity of later modules, it must return the magnetisation of all other protons (denoted as $^1H^{!C}$) to the equilibrium $+z$ state. This is accomplished by replacing the initial 90° excitation pulse by the zz isotope-selective pulse element (ZIP),[23,24] which effects 90°_{-x} and 90°_{-y} rotations on $^1H^C$ and $^1H^{!C}$ magnetisation respectively. (Other isotope-specific elements such as BANGO[25–27] may also be used here, with similar results generally being obtained.[23]) The ^{15}N HMBC module of choice is a simple magnitude-mode version, with an optional first-order low-pass J-filter. In the NOAH-2 AB_N supersequence (Figure 1b), this module simply consumes the remaining

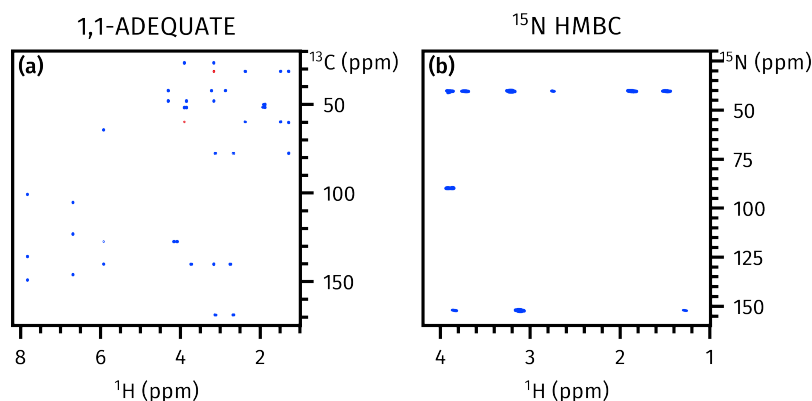$^1H^{!C}$ magnetisation which was preserved by the ZIP-ADEQUATE module.

Figure 2: Spectra obtained from the NOAH-2 AB$_N$ supersequence. **(a)** 1,1-ADEQUATE. **(b)** ^{15}N HMBC. Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM brucine in CDCl$_3$ (see Figure S2 for structure).

3   NOAH-3 AB$_N$B$_N$

Although this NOAH-2 AB$_N$ sequence performs well on its own (Figure 2), it suffers from the drawback that the ^{15}N HMBC is optimised for one specific value of $^nJ_{NH}$. In practice, $^nJ_{NH}$ values range from 2–16 Hz; in a single HMBC experiment, some correlations may therefore be lost due to J-coupling mismatch.

To circumvent this issue, a variety of accordion-type experiments[28–30] have been designed which decrement the J-evolution period in step with t_1, allowing a wider range of couplings to be sampled. Alternatively, and perhaps more commonly, two (or more) separate HMBC experiments, optimised for different $^nJ_{NH}$ values, can be recorded; the resulting spectra may be co-added to mimic an accordion-type HMBC if desired. These separate HMBC modules cannot be recorded *sequentially*, as they both draw on the same $^1H^{!C}$ magnetisation. However, they can easily be executed in an *interleaved* or parallel manner where, after the ADEQUATE module, the two HMBC experiments are alternately acquired.[5] In Figure 1c, this is illustrated by a 'vertical' stacking of the two modules. Thus, after each odd-numbered increment of the ADEQUATE, the first HMBC is acquired; and after each even-numbered increment, the second HMBC is acquired. This means that both HMBC spectra have half the usual number of t_1 increments compared to the ADEQUATE, which is acceptable since the ^{15}N dimension is typically sparse and a high resolution is not required; furthermore, since the ^{15}N HMBC is more sensitive than the ADEQUATE, the reduced number of FIDs recorded per HMBC is practically inconsequential. As can be seen in Figure 3, the two HMBC spectra reveal different sets of correlations, allowing for more confident structural determination.

4   NOAH-4 AB$_N$BS

In the above NOAH-3 A(B$_N$/B$_N$) experiment and in previous work,[5] we have shown how two alternating modules can be used to construct parallel supersequences. This concept can naturally be further
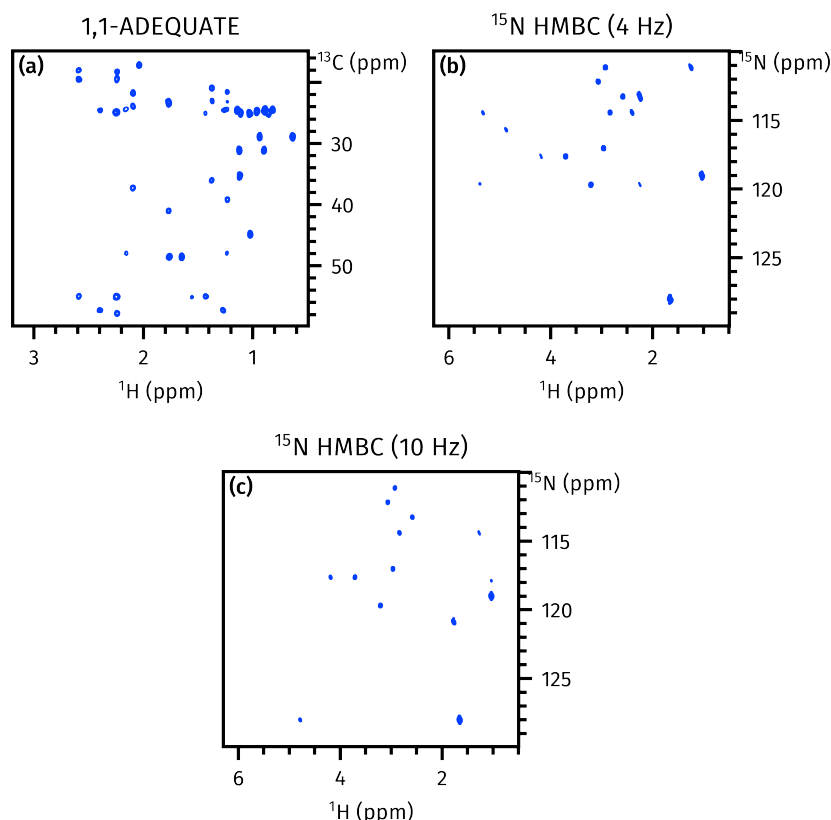
Figure 3: Spectra obtained from the NOAH-3 $A(B_N/B_N)$ supersequence. **(a)** 1,1-ADEQUATE (256 t_1 increments). **(b)** ^{15}N HMBC optimised for $^nJ_{NH} = 4$ Hz (128 t_1 increments). **(c)** ^{15}N HMBC optimised for $^nJ_{NH} = 10$ Hz (128 t_1 increments). Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM cyclosporin A in C_6D_6 (see Figure S5 for structure).

generalised in order to allow two or more different experiments to be acquired alternately as the second module in the supersequence. These interleaved experiments can be arranged such that they each have lower resolution compared to the first module (as was done here), or such that they each have a fewer number of transients. In principle, such an arrangement can be used for *all* modules in a supersequence, not just the second module as is done here. However, it is important to remember that earlier modules affect the amount of magnetisation passed on to the later modules; thus, interleaving later modules in a sequence usually leads to more robust supersequences with minimal discrepancies in data intensity or spectral quality.

In the NOAH-4 $A(B_N/B/S)$ supersequence (Figure 1d), the ADEQUATE module is followed by one of three choices: a ^{15}N HMBC, a ^{13}C HMBC (denoted B), or a ^{13}C HSQC (denoted S). Because these three latter modules do not have the same intrinsic sensitivity, we balance this by allocating a different number of transients to each module. In this specific example, each t_1 increment of the ADEQUATE collects a total of $8n$ transients (where n is some positive integer); the ^{15}N HMBC $6n$ transients; and the ^{13}C HMBC and HSQC n transients each. The value of n is chosen to ensure that all spectra have sufficient sensitivity; the spectra in Figure 4 were acquired with $n = 2$. Using the pulse programmes provided in the *Supplementary*

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Information, the exact number of transients for each module can be customised via user-defined constants. The exact implementation of these supersequences is described in detail in Section S1.
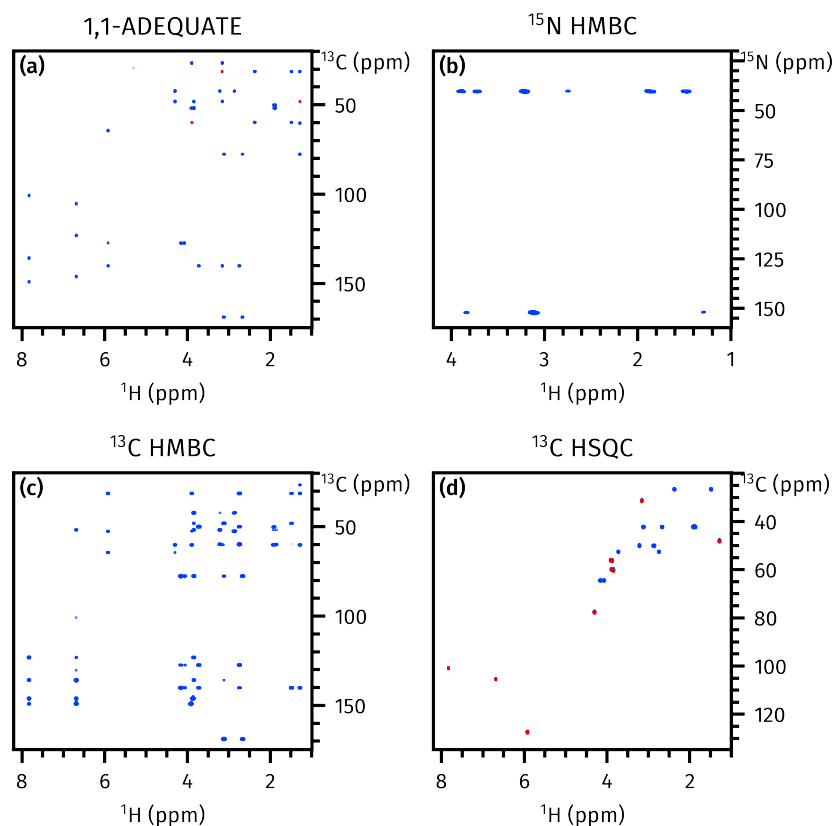

Figure 4: Spectra obtained from the NOAH-4 A(B_N/B/S) supersequence. All modules were recorded with 256 t_1 increments. **(a)** 1,1-ADEQUATE (16 transients). **(b)** ^{15}N HMBC (12 transients). **(c)** ^{13}C HMBC (2 transients). **(d)** ^{13}C HSQC (2 transients). Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM brucine in CDCl$_3$.

The acquisition of the NOAH-4 A(B_N/B/S) spectra in Figure 4 took 124 minutes; in contrast, normal acquisition of all four experiments (with the equivalent number of transients per module) required a total of 223 minutes. As the ADEQUATE is placed first in the supersequence, its sensitivity is almost identical to that of a standalone ADEQUATE; the inclusion of the ZIP element causes only an approximate 5% loss. The ^{15}N and ^{13}C HMBC spectra experience small losses (16–29%) in sensitivity, due to imperfect magnetisation retention by the ADEQUATE module. This is, however, outweighed by the almost twofold time savings provided by concatenation of the modules: if the NOAH supersequence were acquired for as long as the standalone experiments were, the ^{15}N HMBC spectra would have almost the same SNR, and the ^{13}C HMBC from the NOAH would in fact have a 12% improvement in SNR. Due to the reuse of ^{1}H^C magnetisation, the HSQC module only retains 29% of its original sensitivity. However, as the HSQC is still two orders of magnitude more sensitive than the ADEQUATE, this decrease is readily tolerated; if necessary, the sensitivity-enhanced HSQC module[23,24] may also be used in its place.

While this combination of modules proves to be particularly elegant in that it furnishes virtually all

heteronuclear correlations needed for structural assignment of nitrogen-containing organic molecules, it is by no means the only valid one. The principle of interleaved modules can be used to incorporate almost any experiment that may be required: as an example, spectra from a NOAH-4 $A(B_N/N/S)$ experiment (N = NOESY, replacing the ^{13}C HMBC) are shown in Figure S3.

5 NOAH-5 $AB_NBS_N^+S$

As a final example, we add a further ^{15}N seHSQC module to the above sequence. The ^{15}N seHSQC uses only $^1H^N$ magnetisation (i.e. protons directly bonded to ^{15}N), which is separate from all other modules introduced so far. Thus, in principle, it can simply be added *linearly* as a third sequential module to the supersequence: such an arrangement would maximise its sensitivity as the ^{15}N seHSQC data are collected on every scan in the supersequence. Such an arrangement would, however, compromise the performance of the other modules, as they must then be modified to preserve the requisite $^1H^N$ magnetisation: for example, the HMBC modules would need to be modified to include the *zz*-filter,[6,7] which leads to further sensitivity losses. Instead of this, the ^{15}N seHSQC can most efficiently be implemented in a 'vertical', interleaved manner, by simply reducing the number of transients for the ^{15}N HMBC by n and diverting these towards the ^{15}N seHSQC. This means that the second slot in the supersequence now alternates between four different experiments, as shown in Figure 1e. This example especially illustrates how the use of interleaved *and* sequential acquisition leads to much greater flexibility in supersequence design, especially when considering the relative sensitivities of different modules.

The five spectra obtained from this sequence are shown in Figure S6. Collectively, this supersequence provides virtually all heteronuclear correlation data required for structural elucidation or assignment. These can further be processed using covariance techniques[31–33] to yield double-heteronuclear correlation spectra (Section S6). This supersequence is similar in spirit to the PANACEA experiment,[34,35] but yields greater sensitivity as it uses equilibrium ^1H magnetisation rather than the low-magnetogyric ratio ^{13}C and ^{15}N nuclei, and does not require multiple-receiver hardware.[4,36] Of course, the ADEQUATE experiment may not be necessary for every novel compound encountered. However, in cases where it *is* needed, the supersequences described here demonstrate that other valuable heteronuclear spectra can also be acquired together with the ADEQUATE in a manner which yields significant time savings and sensitivity per unit time improvements.

6 Conclusion(ish)

In conclusion, we have demonstrated here how low-sensitivity experiments, such as 1,1-ADEQUATE and ^{15}N HMBC, may be optimally combined in NMR supersequences, leading to substantial reductions in experiment time. Through a generalisation of our previous concept of parallel supersequences, further high-sensitivity modules may be added to the supersequence both 'horizontally' and 'vertically', corresponding respectively to sequential and interleaved/parallel acquisition. The spectra thus obtained provide the chemist with far more powerful tools for the characterisation of complex molecules, especially in cases

where existing (sequential) NOAH supersequences do not provide sufficient information for unambiguous assignment. a notable example of this is proton-sparse nitrogen heterocycles, which are commonly found in pharmaceuticals. The pulse programmes and processing scripts used in this work can be obtained via the Bruker User Library or GitHub; links are provided in Section S2 of the *Supplementary Information*.

Acknowledgements

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Supporting Information

for

A General Scheme for NMR Supersequences Combining High- and Low-Sensitivity Experiments

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Contents

S1 Pulse programme description

This section presents a more detailed description of how the pulse programme works; this information is important to anybody seeking to use the pulse programmes given here (or anybody writing similar 'interleaved' experiments). We use the NOAH-4 A(B_N/B/S) experiment as an example here. In this experiment, the second module alternates between the ^{15}N HMBC (B_N), ^{13}C HMBC (B), and ^{13}C HSQC (S); the pulse programme is set up such that these three modules have fewer transients than the ADEQUATE (A). For every 8 transients of the ADEQUATE, 6, 1, and 1 transient(s) are recorded for the B_N, B, and S modules respectively.

An excerpt of the pulse programme is shown here and explained on the next page:

```
  "l3 = 0"        ; initialise loop counter
  "cnst51 = 8"   ; number of transients for ADEQUATE
  "cnst52 = 6"   ; number of transients for 15N HMBC
  "cnst53 = 1"   ; number of transients for 13C HMBC
  ; HSQC doesn't need a separate counter; it's just cnst51-cnst52-cnst53

2 d1

  ; run ADEQUATE
  goscnp ph30    ; record ADEQUATE FID

  if "l3 % cnst51 < cnst52" {
    ; transients 1 through 6: run 15N HMBC
    go=2 ph31
  }

  else {
  if "l3 % cnst51 < cnst52 + cnst53" {
    ; transient 7: run 13C HMBC
    go=2 ph31
  }

  else {
    ; transient 8: run 13C HSQC
    go=2 ph31   ; 'go' loops back to the label '2' a total of NS times
  }
  }

  1m iu3   ; increment loop counter
  if "l3 % cnst51 == 0" {
      ; increment t1 here
  }
  lo to 2 times x   ; see main text for description of x
```

Generally, interleaving is performed using modular arithmetic. A loop counter (L3) is used in order to keep track of how many transients have been recorded so far, and the value of this counter *modulo* 8 is used in order to determine which module to run in the second slot. Note that this is independent of the NS parameter in TopSpin. So, each t_1 increment of the ADEQUATE module is actually recorded $8 \times$ NS times.

Of course, the values of cnst51, cnst52, and cnst53 are not hardcoded as in the example above. By changing these numbers, the user can control the number of transients allocated to each module. In total, each t_1 increment of the ADEQUATE module is acquired cnst51 $\times$ NS times; the ^{15}N HMBC is acquired cnst52 $\times$ NS times; and so on. (For the final module (HSQC), there is no need to define an analogous cnst54 because it simply 'uses up' all the remaining transients; thus, the HSQC is acquired a total of (cnst51 − cnst52 − cnst53) $\times$ NS times.)

Finally, t_1 is only incremented if we have completed a full cycle of 8 runs through the loop. Again, this is checked using modular arithmetic; every 8 loop iterations, l3 will be a multiple of cnst51. The value of x in the last line corresponds to the total number of loop iterations which need to be made; thus, this value is equal to 8 times the number of desired t_1 increments.
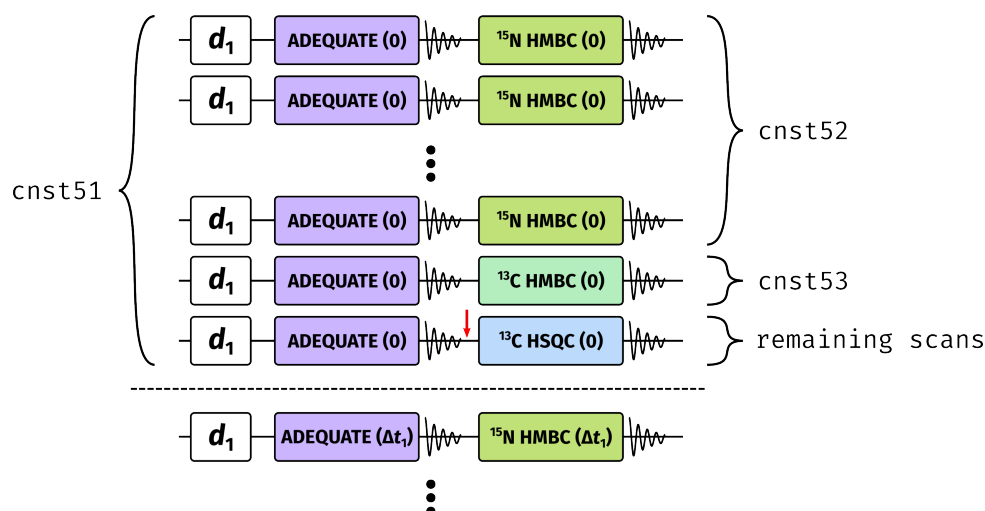

Figure S1: Diagram illustrating the practical implementation of the NOAH-4 A(B_N/B/S) supersequence. Numbers in parentheses refer to the value of t_1; the first increment is recorded with $t_1 = 0$ for all modules. d_1 represents a recovery delay. Each row is repeated NS times, during which phase cycling is performed; however, no phase cycling is performed *between* rows, even those which are identical (e.g. the first two rows). Since each row only consists of two horizontally concatenated modules, the NBL parameter is to be still set to 2. The red arrow indicates where DIPSI-2 mixing is inserted: this is discussed in Section S4.

It is worth pointing out at this point that, because of the way TopSpin increments pulse phase pointers, *phase cycling* (as defined by the phase tables in the pulse programme) is only carried out NS times. That is, although the ADEQUATE module is recorded cnst51 $\times$ NS times, only a NS-step phase cycle is being used. With modern gradient-based coherence selection techniques,

this does not have a substantial impact on the data quality. (For example, the data in Figure 4 were recorded with NS=2 and are perfectly serviceable.) Nevertheless, it is always a good idea to make NS as large as possible, and always at least 2 to ensure suppression of axial peaks. As a concrete illustration, the two parameter sets below yield the same signal-to-noise for all modules, but parameter set 2 will have a longer (and presumably better) 4-step phase cycle.

	Parameter set 1, NS=2	Parameter set 2, NS=4
cnst51	12	6
cnst52	8	4
cnst53	2	1
cnst51 − cnst52 − cnst53	2	1

The parameter NBL should still be set to 2 for all of the supersequences shown in this work. The NBL parameter corresponds to the number of *sequentially* concatenated modules, which in all cases is only 2; the parallel modules play no role here. The value of TD1 should then be set to $\text{cnst51} \times \text{NBL} \times N_1$, where N_1 is the desired number of t_1 increments (i.e. TD1 in a 'traditional' 2D experiment).

Finally, it should be noted that the if/else conditionals are evaluated only at runtime by the spectrometer. TopSpin does not calculate ahead of time when each interleaved module is run. This means that the TopSpin expt command (which shows the expected experimental duration) can yield (very slightly) inaccurate results.

S2 Pulse programme and processing script availability

The pulse programmes used in this work, along with all requisite processing scripts, can be downloaded from the Bruker User Library at https://www.bruker.com/protected/en/services/bruker-user-library.html, or equivalently, from GitHub at https://github.com/yongrenjie/abbs-paper/releases/tag/data. The zip archive contains further instructions on setting up the pulse programmes.

S3 NOAH-4 A(B_N/N/S) experiment

Since the ^{1}H–^{1}H NOESY uses the same ^{1}H$^{!C}$ magnetisation as ^{13}C HMBC so can be directly substituted in its place, leading to a NOAH-4 A(B_N/N/S) supersequence (Figure S3). This not only provides a wealth of through-bond correlations which aid in eludicating molecular constitution, but also furnishes through-space correlations for the determination of configuration or conformation. Depending on the molecular size and spectrometer frequency, the NOESY module may easily be replaced with a ROESY.
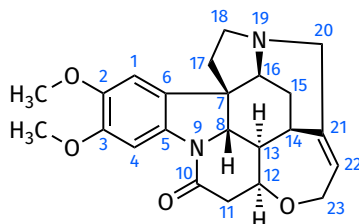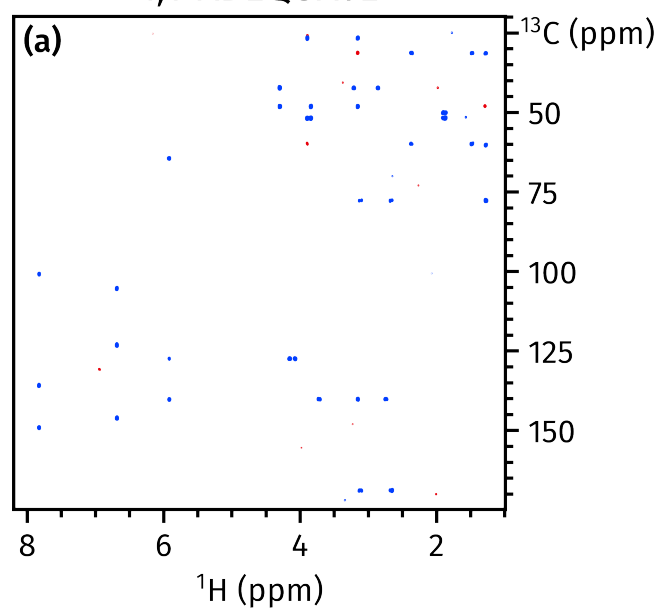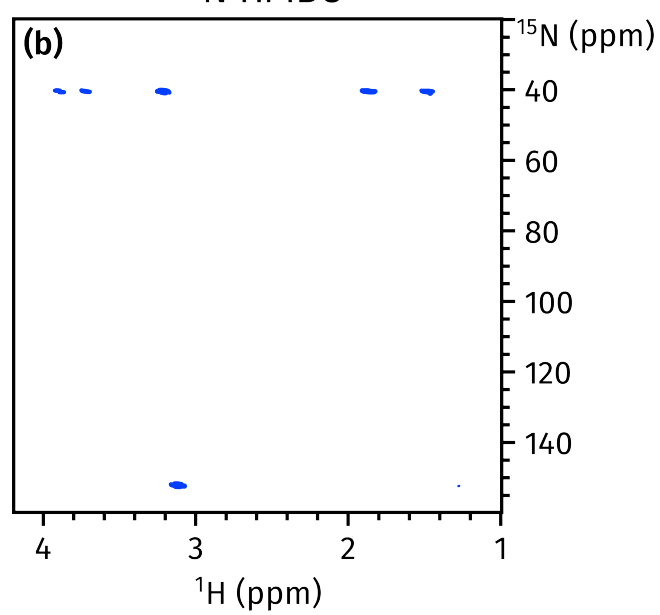

Figure S2: Structure of brucine.

1,1-ADEQUATE

(a)

^{13}C (ppm)

^{15}N HMBC

(b)

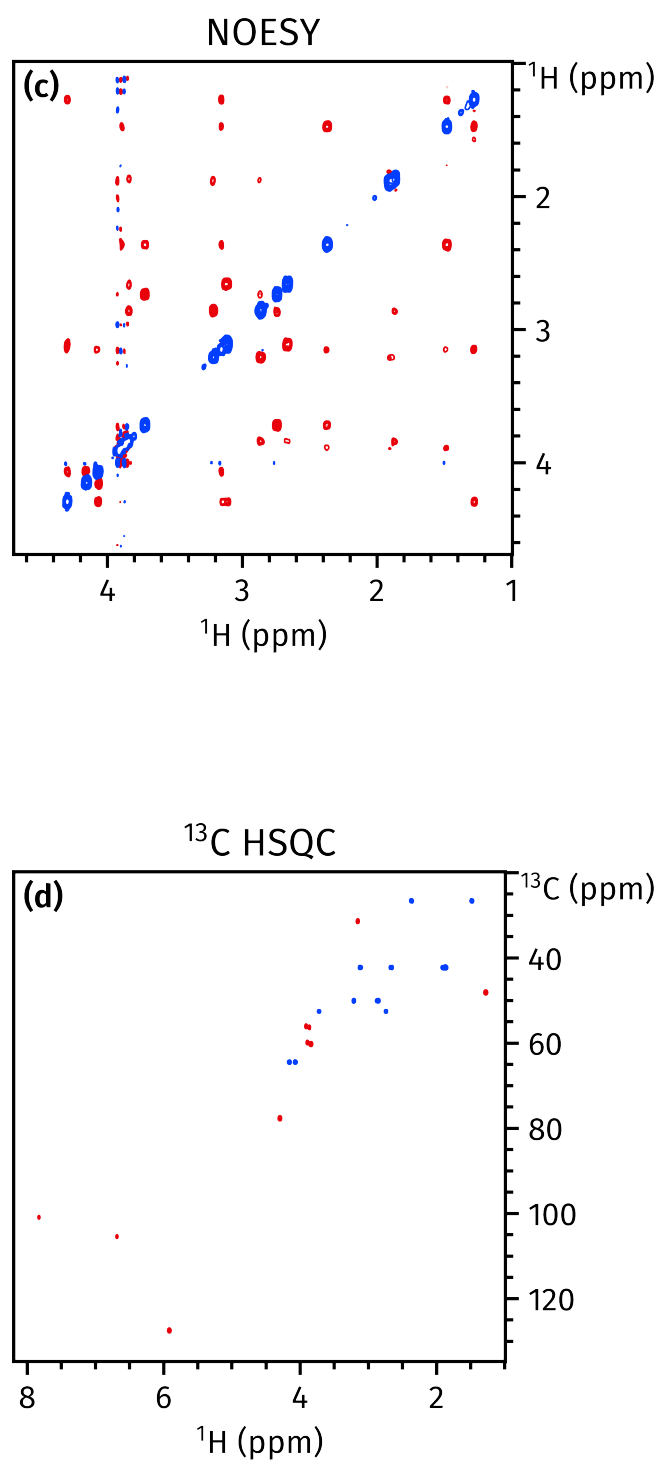^{15}N (ppm)

NOESY

(c)

^{13}C HSQC

(d)

Figure S3: Spectra obtained from the NOAH-4 A(B_N/N/S) supersequence. **(a)** 1,1-ADEQUATE (16 transients). **(b)** ^{15}N HMBC (12 transients). **(c)** NOESY (2 transients, 800 ms mixing time). **(d)** ^{13}C HSQC (2 transients). Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM brucine in CDCl$_3$.

S4 NOAH-4 A(B_N/B/S) comparison with and without DIPSI

One additional feature of the NOAH-4 A(B_N/N/S), not described in the main text, concerns the fact that the ^{13}C HSQC module is placed immediately after the ADEQUATE (the second-last row in Figure S1). Both of these modules draw on the same ^{1}H^{C} magnetisation pool, and this generally causes the latter module (here HSQC) to suffer from sensitivity losses. Since the HSQC has a much greater intrinsic sensitivity compared to the ADEQUATE, this loss would in fact be tolerable.

In this experiment, we chose to also add a 35 ms period of isotropic DIPSI-2 mixing[1] immediately before the HSQC module (at the point marked with the red arrow in Figure S1). This effects ^{1}H$^{!C}$ → ^{1}H^{C} magnetisation transfer, and has previously been demonstrated in ASAP[2–6] and NOAH[7] experiments. Through this, some of the lost ^{1}H^{C} magnetisation is replenished, leading to greater intensity in the HSQC (Figure S4). This mixing period does not need to be inserted prior to either of the ^{15}N or ^{13}C HMBC modules, as they do not use ^{1}H^{C} magnetisation. Figure S4 compares the results obtained with and without this DIPSI block.

The spectral quality in both cases is acceptable. However, the spectrum acquired without DIPSI mixing (Figure S4a) is weaker, which is more clearly shown in the projections onto the F_2 axes (Figure S4c). When DIPSI mixing is added, the average signal enhancement across all peaks in the HSQC is 88% (Figure S4). These observations are consistent with previous studies on NOAH supersequences containing two successive ^{1}H^{C} modules.[7]
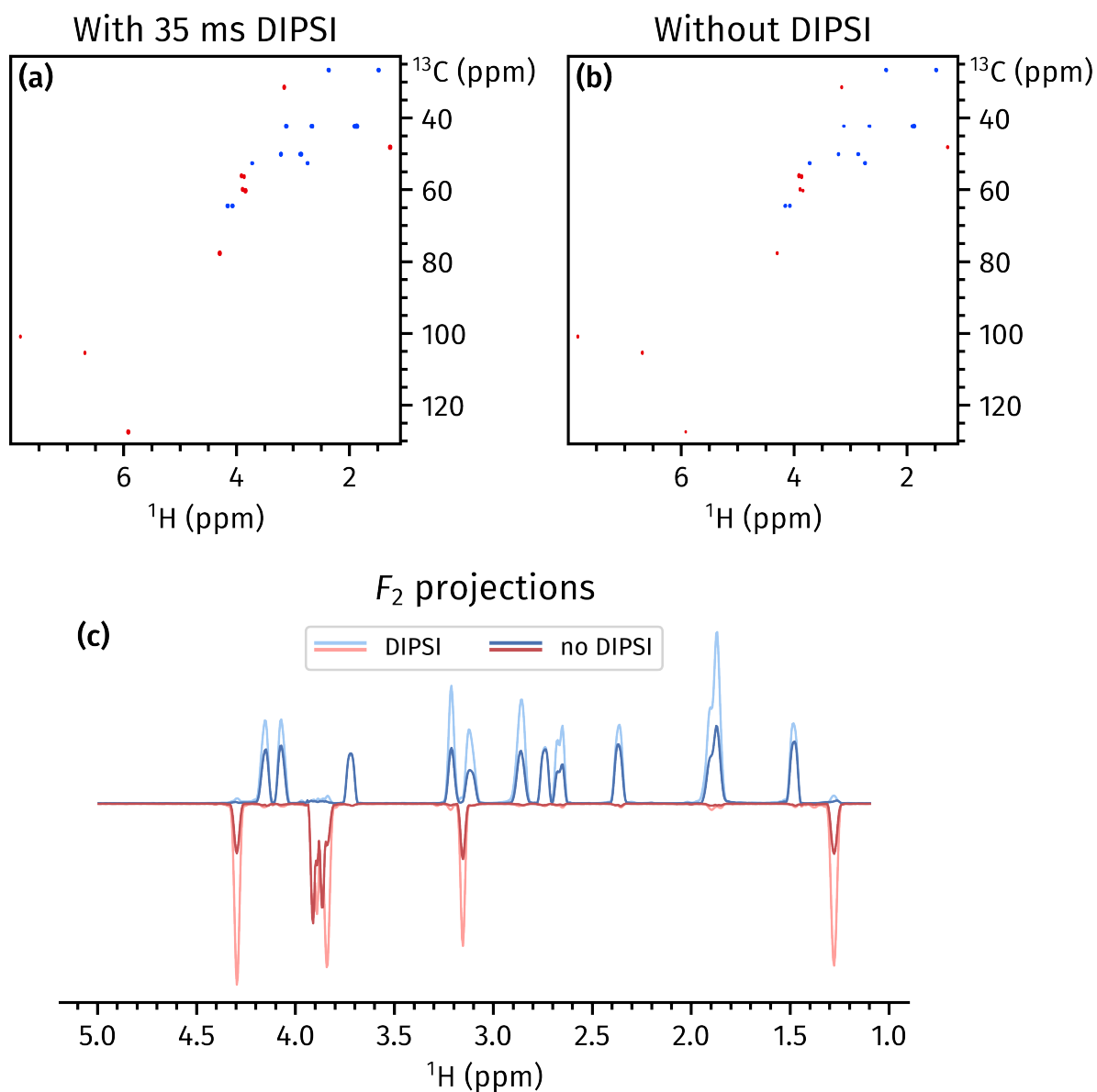
Figure S4: ^{13}C HSQC spectra obtained from the NOAH-4 A(B_N/B/S) experiment (Figure 1d). **(a)** With 35 ms DIPSI mixing between the ADEQUATE and ^{13}C HSQC modules (this spectrum is the same as in Figure 4d). **(b)** Without DIPSI mixing between the ADEQUATE and ^{13}C HSQC modules. **(c)** Projections of the spectra in (a) and (b) onto the F_2 axis. Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM brucine in CDCl$_3$.

S5 Spectra from NOAH-5 A(B_N/B/S_N^+/S)

(1) MeBmt **(2) Abu** **(3) Sar** **(4) N-MeLeu** **(11) N-MeVal** **(10) N-MeLeu** **(9) N-MeLeu** **(8) D-Ala** **(7) Ala** **(6) N-MeLeu** **(5) Val**
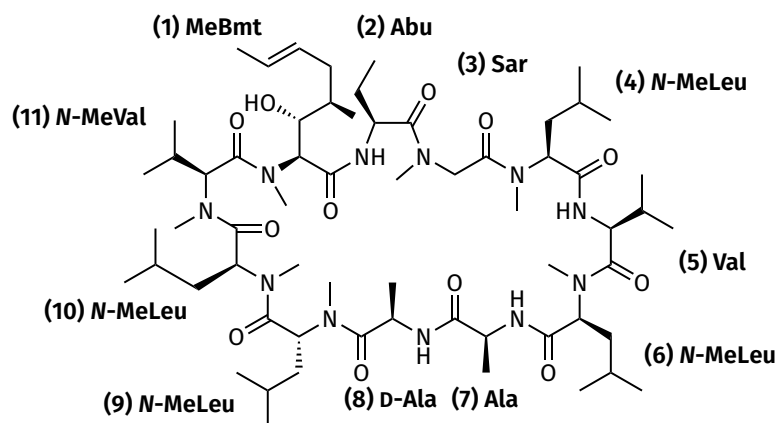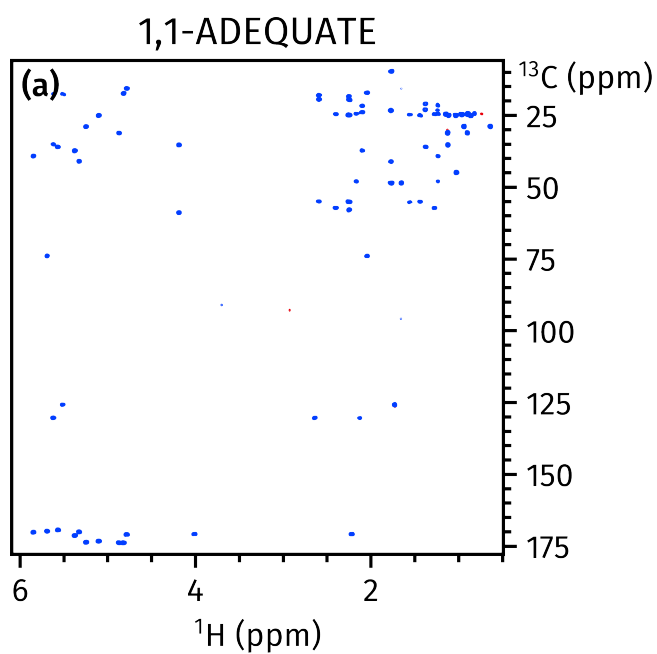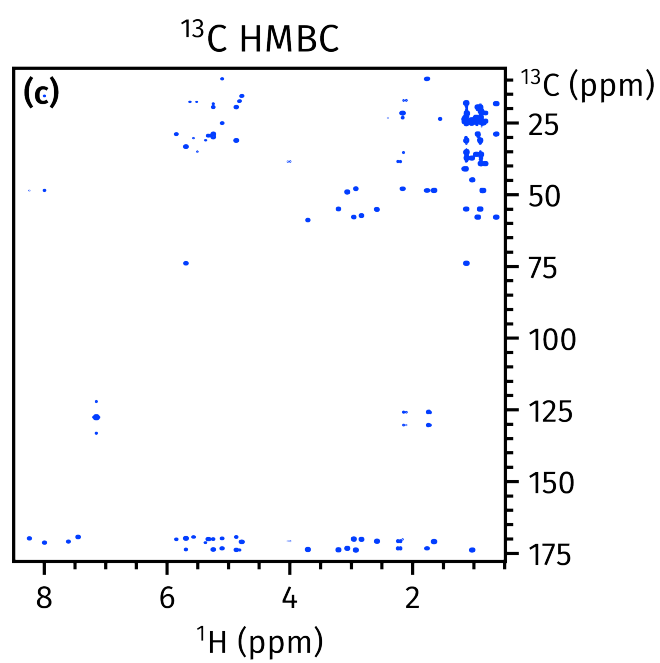
Figure S5: Structure of cyclosporin with residues numbered.

1,1-ADEQUATE

^{15}N HMBC

(b)

^{15}N (ppm)

115

120

125

^{1}H (ppm)

6   4   2

^{13}C HMBC

(c)

^{13}C (ppm)
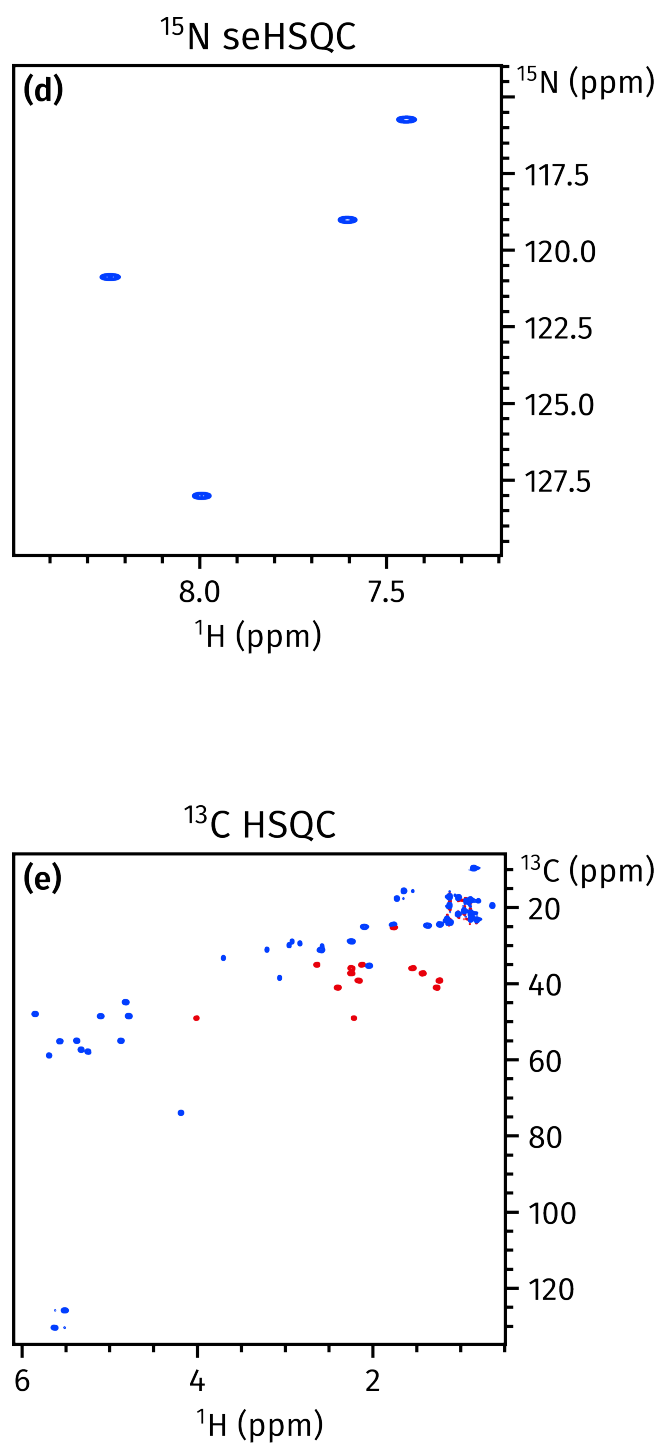
25

50

75

100

125

150

175

^{1}H (ppm)

8   6   4   2

(d) ^{15}N seHSQC
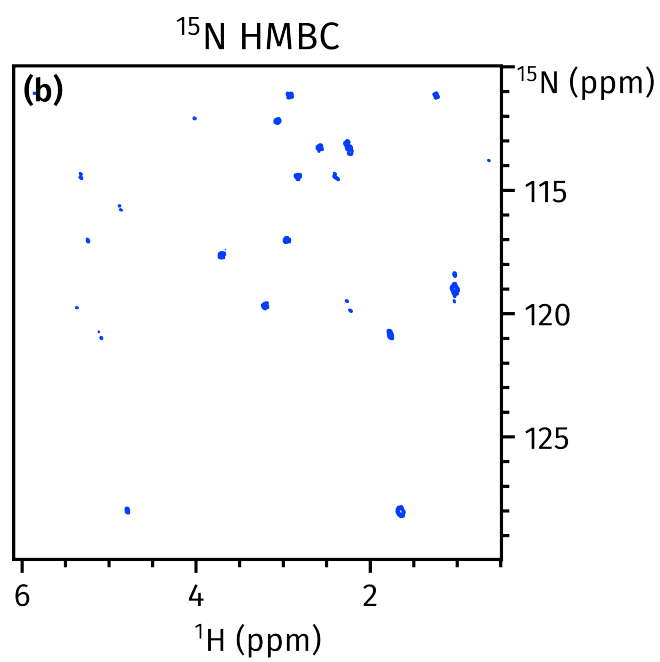
(e) ^{13}C HSQC

Figure S6: Spectra obtained from the NOAH-5 A(B$_N$/B/S$_N^+$/S) supersequence. All modules were recorded with 256 t_1 increments. **(a)** 1,1-ADEQUATE (16 transients). **(b)** ^{15}N HMBC (10 transients). **(c)** ^{13}C HMBC (2 transients). **(d)** ^{15}N sensitivity-enhanced HSQC (2 transients). **(e)** ^{13}C HSQC (2 transients). Spectra were obtained on a 700 MHz Bruker AV III equipped with a TCI H/C/N cryoprobe; the sample used was 50 mM cyclosporin A in C$_6$D$_6$.

S6   Covariance spectra from NOAH-5 A(B_N/B/S_N^+/S)

The heteronuclear spectra obtained from the NOAH-5 A(B_N/B/S_N^+/S) supersequence can be processed using indirect covariance processing[8–10] to yield other forms of correlation spectra. For example, the ^{15}N HMBC and ^{13}C HSQC can be used to generate ^{13}C–^{15}N correlation spectra (Figure S7a).[11–13] Furthermore, the ^{13}C HSQC and ADEQUATE experiments can be used to create ^{13}C–^{13}C one-bond correlation spectra (Figures S7b and S7c).[14,15] It should be further emphasised that all of the 'base' spectra used as the inputs here are obtained *in a single measurement* using either the NOAH-4 or NOAH-5 supersequences discussed above. A notable benefit of this is that t_1 for all modules are incremented simultaneously: this minimises the effects of temporal variations such as temperature drifts, which can lead to inaccurate peaks in covariance spectra.

In Figure S7c, the ^{13}C–^{13}C one-bond covariance spectrum has been subjected to a sign-preserving symmetrisation procedure. This is defined by replacing the intensity at each point $p(\Omega_1, \Omega_2)$ by

$$p(\Omega_1, \Omega_2) \rightarrow \text{sgn}[p(\Omega_1, \Omega_2)] \cdot \min\left\{|p(\Omega_1, \Omega_2)|, |p(\Omega_2, \Omega_1)|\right\}. \tag{1}$$

Here, sgn p refers to the sign of p, or equivalently $p/|p|$ (for $p \neq 0$). The sgn p term ensures that the *sign* of each peak (and hence multiplicity information) is preserved, but the (absolute) intensities are symmetrised about the main diagonal, which suppresses artefactual responses arising from coincidental peak overlap.

It should be noted that such a procedure can only be safely carried out where peaks on both sides of the diagonals are expected. For a *true* ^{13}C–^{13}C correlation spectrum, this would be the case for all pairs of ^{13}C nuclei. However, the covariance spectrum shown in Figures S7b and S7c does not satisfy this: peaks at (Ω_1, Ω_2) are only observed if the carbon at Ω_2 is bonded to at least one proton. Thus, if the symmetrisation procedure is applied across the entire spectrum, correlations between quaternary and non-quaternary carbons (such as those in Figure S7b) will be lost. However, in the case of Figure S7c, the alkyl region of cyclosporin does not contain any quaternary carbons, allowing the symmetrisation to be safely carried out.
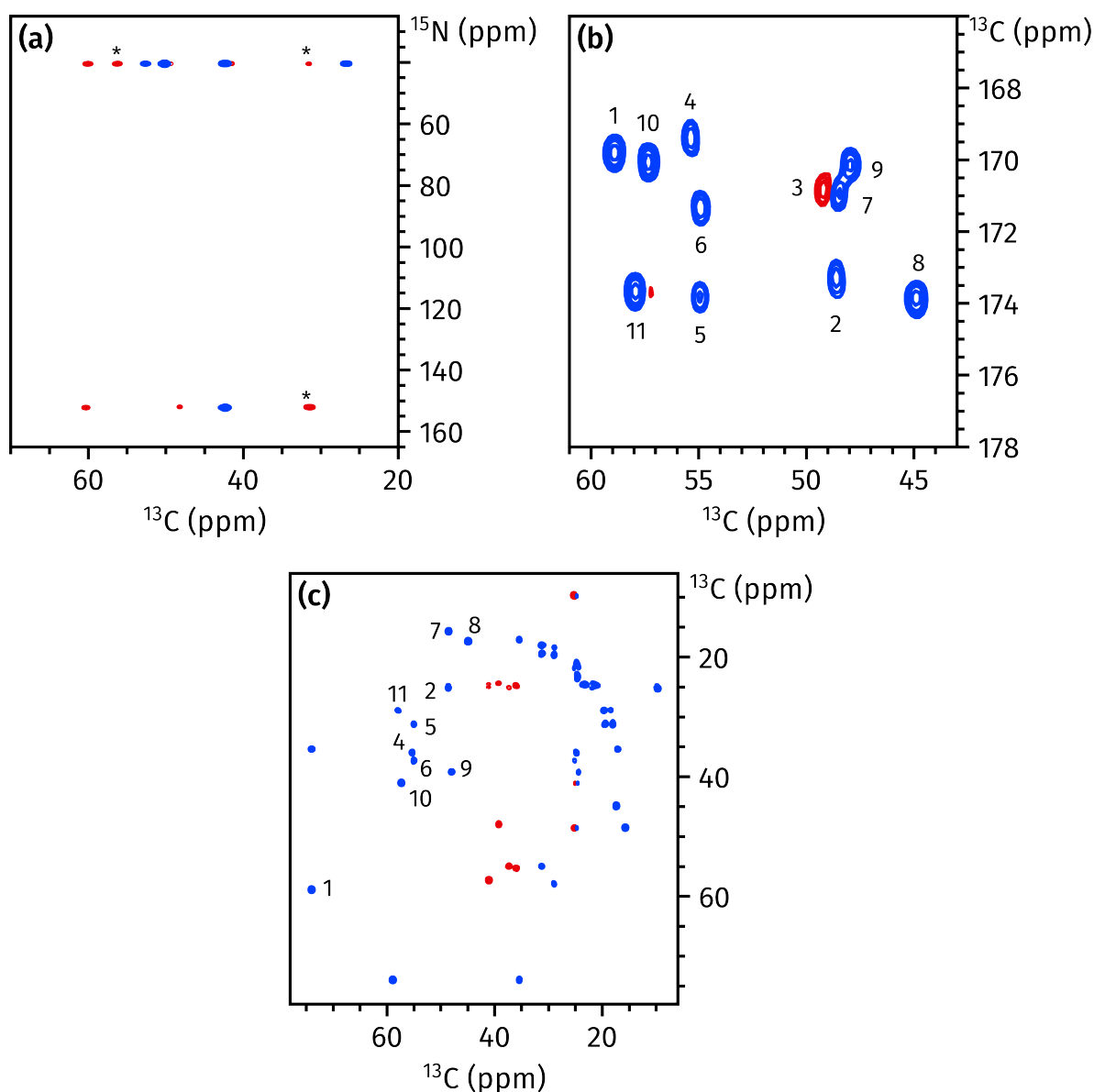
Figure S7: Spectra obtained through indirect covariance processing. In all cases the peak sign indicates carbon multiplicity; this information is contained in the multiplicity-edited ^{13}C HSQC spectrum and arises naturally during covariance processing. **(a)** ^{13}C–^{15}N correlation spectrum (containing both one- and multiple-bond correlations) obtained by processing the brucine ^{15}N HMBC and ^{13}C HSQC spectra (in Figures 4b and 4d) using unsymmetric indirect covariance. Some artefacts (arising from peak overlap in the ^{1}H dimension) are marked with asterisks. **(b–c)** Insets of ^{13}C–^{13}C one-bond correlation spectrum, obtained by processing the cyclosporin ADEQUATE and ^{13}C HSQC spectra (in Figures S6a and S6e) using generalised indirect covariance ($\lambda = 0.5$). The Cα–CO correlations, numbered by residue (see Figure S5), are shown in (b). Sidechain C–C correlations are shown in (c); only peaks corresponding to Cα–Cβ correlations are labelled. The inset in (c) has been further subjected to a sign-preserving symmetrisation procedure, which is described in the text.

S7 Software and raw data

All processing was carried out using TopSpin 3 or 4. Plots are generated in Python 3, using the `numpy`, `scipy`, and `penguins` libraries. The raw data used for this paper, as well as all scripts required for regenerating the plots, are available on GitHub: https://github.com/yongrenji e/abbs-paper.

S7.1 Covariance

The exact code used for covariance processing can be found in the `figures/covariance.py` script. A short overview is presented here. The following code excerpt calculates the unsymmetric indirect covariance between two spectra. Here, `penguins.read()` returns a `Dataset` object: the `rr` attribute of this is a two-dimensional `numpy` array corresponding to the doubly real part of the spectrum.

```python
# Unsymmetric indirect covariance
import penguins as pg

spec1 = pg.read(path, expno1)
spec2 = pg.read(path, expno2)
cov = spec1.rr @ spec2.rr.T
```

Generalised indirect covariance is slightly more complicated, but follows directly from the procedure given in Snyder and Brüschweiler's work.[9]

```python
# Unsymmetric indirect covariance
import penguins as pg
import numpy as np
from scipy.linalg import fractional_matrix_power   # or just sqrtm

spec1 = pg.read(path, expno1)
spec2 = pg.read(path, expno2)
cov_lambda = 0.5

stacked = np.vstack((spec1.rr, spec2.rr))
cov_full = fractional_matrix_power(stacked @ stacked.T, cov_lambda)
# Figure out number of points in indirect dimensions of both spectra.
si1, si2 = spec1['si'][0], spec2['si'][0]
# `cov` is a block matrix, and we only want an off-diagonal block of it.
cov = np.real(cov_full[0:si1, si1:si1+si2])
```

Finally, this is the symmetrisation process specified in Equation (1). This assumes that the main diagonal of the *spectrum* corresponds to the main diagonal of the *matrix*, i.e. m[i, i] represents a point with the same chemical shift in both dimensions. The matrix cov calculated above satisfies this.

```python
import numpy as np

def symmetrise_preserve_sign(m):
    smallest_amp = np.minimum(np.abs(m), np.abs(m).T)
    sign = np.sign(m)
    return sign * smallest_amp
```

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