Introduction to Algorithms Science Honors Program (SHP) Session 1

Christian LimSaturday, February 17, 2024

Christian Yongwhan Lim















Part-time Jobs







Full-time Job





Workshops















Coach/Judge





https://www.yongwhan.io

Christian Yongwhan Lim









- Currently:
 - Adjunct, Columbia CS;
 - CEO (Co-Founder), Stealth Mode Startup;
 - Co-Founder, Christian and Grace Consulting;
 - Head Coach, Columbia ICPC;
 - Internship Manager, ICPC Foundation;
 - Leadership Team, ICPC North America (NA);
 - Trainer, ICPC NA Programming Camp;
 - Judge, ICPC NA Qualifiers and Regionals;



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Who are you?

- **School**? (State?)
- Year?
- Programming Experience?
- **USACO level**, if applicable?
- Hobby?

Slide deck in github

- You may find the slide deck from:
 - https://github.com/yongwhan/yongwhan.github.io/blob/master/colu mbia/shp/Spring%202024%20Introduction%20to%20Algorithms %20 Session%201.pdf
- You may get to the link by:
 - https://github.com/yongwhan/
 - => yongwhan.github.io
 - o => columbia
 - \circ => shp
 - => session 1 slide

Spring 2024 Overview - February

February 17, 2024	 Logistics and Introduction Complexity Analysis Sorting Algorithm (bubble sort) Practice Strategies Primitive (Data) Types How to program in C++?
February 24, 2024	 Built-in Data Structures (vector; stack; queue; priority_queue; set; map) Custom Data Structures (disjoint set union; Fenwick/Segment tree; ordered set)

Spring 2024 Overview - March

March 2, 2024	 Complete Search Divide and Conquer (merge sort, quicksort, etc.)
March 9, 2024	 Greedy Dynamic Programming
March 16, 2024	NO CLASSES (SPRING BREAK)
March 23, 2024	 Graphs: Shortest Paths and Minimum Spanning Trees Graphs: Lowest Common Ancestor and Flows
March 30, 2024	NO CLASSES (EASTER WEEKEND)

Spring 2024 Overview - April

April 6, 2024	Ad HocCombinatorics
April 13, 2024	Number TheoryGames
April 20, 2024	NO CLASSES (SPRING BREAK)
April 27, 2024	Strings: FundamentalsStrings: Matchings

Spring 2024 Overview - May

May 4, 2024	Geometry: Fundamentals and Convex HullNext Steps
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Complexity Analysis

Space Complexity

- "the total amount of memory space used by an algorithm"
- typically, it includes the space for inputs too!

Time Complexity

"the total amount of time it takes to run an algorithm"

Analysis Framework: Big O, Big Omega, and Big Theta

- O: We write f(x) = O(g(x)) and read it "f(x) is big O of g(x)" if there exists M>0 and x_0 such that $|f(x)| \le Mg(x)$ for all $x > x_0$
- Ω : We write $f(x) = \Omega(g(x))$ and read it "f(x) is big Omega of g(x)" if there exists M>0 and x_0 such that $|f(x)| \ge Mg(x)$ for all $x > x_0$
- θ : We write $f(x) = \theta(g(x))$ and read it "f(x) is big Theta of g(x)" if f(x) is both O(g(x)) and O(g(x))

Example 1: Big O

- is $n^2 O(n)$?
- is $n^2 O(n^3)$?
- is $n^2 + 1,000,000,000 O(n^3)$?
- is $2^n O(n!)$?
- is log(n) O(n)?
- is $7n^2 O(n^2)$?

Example 2: Big Omega

- is $n^2 \Omega(n)$?
- is $n^2 \Omega(n^3)$?
- is $n^2 + 1,000,000,000 \Omega(n^3)$?
- is $2^n \Omega(n!)$?
- is log(n) Ω(n)?
- is $7n^2 \Omega(n^2)$?

Example 3: Big Theta

- is $n^2 \theta(n)$?
- is $n^2 \theta(n^3)$?
- is $n^2 + 1,000,000,000 \Theta(n^3)$?
- is $2^n \theta(n!)$?
- is $log(n) \theta(n)$?
- is $7n^2 \theta(n^2)$?

```
int ret=0;
for (int i=0; i<n; i++)
  ret++;</pre>
```

- Space Complexity: ?
- Time Complexity: ?

```
int ret=0;
for (int i=0; i<n; i++)
  ret++;</pre>
```

- Space Complexity: $\theta(1)$
- Time Complexity: θ (n)

```
vector<int> a(n);
for (int i=0; i<n; i++)
   cin>>a[i];
int ret=0;
for (int i=0; i<n; i++)
   ret+=a[i];</pre>
```

- Space Complexity: ?
- Time Complexity: ?

```
vector<int> a(n);
for (int i=0; i<n; i++)
   cin>>a[i];
int ret=0;
for (int i=0; i<n; i++)
   ret+=a[i];</pre>
```

- Space Complexity: θ (n)
- Time Complexity: θ (n)

Recurrence Relation

Fibonacci number:

- o f[0]=1;
- o f[1]=1;
- f[n]=f[n-1]+f[n-2] for any $n \ge 2$.

- Other "named" linear recurrence can be found <u>here</u>.
 - Lucas number, Padovan sequence, Pell number, Pell-Lucas number,
 Perrin sequence, ...
 - No need to memorize these, but knowing these exist is good enough!

- Space: θ (n)
- Time: θ (n)

Recurrence Relation: Iterative Implementation

Writing a code for finding nth Fibonacci number in iterative way is:

```
vector<int> f={1,1};
for (int i=2; i<n; i++)
  f.push_back(f[i-1]+f[i-2]);</pre>
```

- Space: θ (n)
- Time: $\theta(2^n)$

Recurrence Relation: Recursive Implementation

Writing it recursively is:

```
int fib(int n) {
  if(n==0) return 1;
  if(n==1) return 1;
  return fib(n-1)+fib(n-2);
}
```

We will learn how to write it more efficiently using memoization later!

 Given an array of integers (or any other data types that can be pairwise compared in terms of '<'), sorting would reorder the elements in the array from the smallest to the largest (or the largest to the smallest) using a comparing function ("comparer").

 Typically, in C++, you can use sort(v.begin(), v.end()) to sort a container v (e.g., vector).

 Given an array of integers (or any other data types that can be pairwise compared in terms of '<'), sorting would reorder the elements in the array from the smallest to the largest (or the largest to the smallest) using a comparing function ("comparer"). So, after sorting,

5 3 2	7	1	4	6
-------	---	---	---	---

would look like:

 Given an array of integers (or any other data types that can be pairwise compared in terms of '<'), sorting would reorder the elements in the array from the smallest to the largest (or the largest to the smallest) using a comparing function ("comparer"). So,



- There are many sorting algorithms. Some popular ones are:
 - Bubble Sort;
 - Insertion Sort;
 - Selection Sort;
 - Quick Sort;
 - Merge Sort;

- Today, we will cover:
 - Bubble Sort;

Bubble Sort

Repeatedly swaps the adjacent elements if they are in the wrong order.

Bubble Sort

Repeatedly swaps the adjacent elements if they are in the wrong order.

- Specifically, in bubble sort:
 - elements are scanned from left to right,
 - each element is compared to its adjacent element and the higher one is placed at right side by swapping, as necessary.

Bubble Sort: Step 1: the largest element

5	3	2	7	1	4	6
3	5	2	7	1	4	6
3	2	5	7	1	4	6
3	2	5	7	1	4	6
3	2	5	1	7	4	6
3	2	5	1	4	7	6
3	2	5	1	4	6	7

Bubble Sort: Step 2: the 2nd largest element

3	2	5	1	4	6	7
2	3	5	1	4	6	7
2	3	5	1	4	6	7
2	3	1	5	4	6	7
2	3	1	4	5	6	7
2	3	1	4	5	6	7

Bubble Sort: the process will continue until possible!

1	2	2	4	5	6	7	
•	_	J	7	J	0		

• Space: O(n)

Bubble Sort: Code

```
void bubbleSort(vector<int> &a, int n) {
  bool swapped;
  for (int i=0; i<n-1; i++) {
    swapped = false;
    for (j=0; j<n-i-1; j++)
      if (a[j] > a[j+1])
        swap(arr[j], arr[j+1]), swapped = true;
    if (!swapped) break;
```

Remarks

Sorting is guaranteed to be n log n for merge sort.

- In practice, **quicksort** is faster (n log n still on average) but the worst case time complexity is quadratic.
 - Even when the pivot selection is randomized, we can get extremely unlucky and happen to hit the bad pivot each time.

We will look at merge sort and quicksort closely in the future!



CodeForces Zealots Problem Set

Please join the following group:

https://codeforces.com/group/hosRkEuluH

Doing questions in Zealots problem set is COMPLETELY optional!

How to use the Zealots Problem Set?

 Those who are just starting should focus on the first half of problems in Zealots Problem Set. Your main focus should be gaining some experiences with an explicit goal to enjoy the process of solving new problems and potentially making it to USACO Platinum!

 Those who are more serious should focus on the second half of problems in Zealots Problem Set. Your goal would be making into USACO Programming Camp and/or International Olympiad in Informatics!

Practice Strategies

• If your goal is to get to a rating of **X**, you should practice on problems that are **X** + **300** typically, with a spread of 100. So, picking problems within the range of:

$${X + 200, X + 300, X + 400}$$

would be sensible!

- So, if you want to target becoming a red, which has a lower-bound of 2400, you should aim to solving {2600, 2700, 2800}.
- **(Eventual) Target**: You should focus on solving it for 30 minutes or less!

Practice Strategies

You should focus on solving each problem for 30 minutes or less; if you
cannot solve any problem with this range, you should consider solving a
problem with a lower rating.

 You should aim to solve 10 ~ 15 problems each day within this range to expect a rank up within a quarter (3 months).

Practice Strategies

- If you cannot solve a problem, here is a sample recipe you can follow:
 - Look at editorial for hints, and try to solve the problem.

Look at editorial for full solutions, and try to solve the problem.

Look at accepted solutions, and try to solve the problem.

Make sure you look back <u>after two weeks</u> and see if you can solve it.

Live Contest Strategies

A Terse Guide to Live Contests

C++ Tips and Tricks: best to learn those through practice!

- C++ Tricks (HosseinYousefi)
- C++ tips and tricks (Golovanov399)
- Some Tips for Coding in C++ in Competitive Programming (Nea1)

Use "#include <bits/stdc++.h>" header to include almost everything.

Standard Input/Output (stdio)

Yet again on C++ input/output (andreyv)

- scanf/printf vs cin/cout
 - Often, use "ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);"

Primitive Type

• int, long long, double, long double, char, float, ...

int

- "int" is short for "integer"
- Used to store whole numbers
- Internally, they are stored using binary numbers: ones and zeros
- Number of bytes used for an int varies by system
- 1 byte = 8 bits

Examples

- 6
- 13
- 1993
- -777
- 10
- 2
- 2021

float

- "float" is short for "floating-point"
- Floats can store numbers with a fractional part (real numbers)

Examples

- -777.77
- 6.131993
- 9.301989
- 10.22021
- -123.765
- 0.0

char

- "char" is short for "character"
- Used to store individual letters, digits, symbols, etc.
- These are the keys you have on your keyboard

- Typically stored using a single byte
- But, with the rise of Unicode, many systems use two bytes now
- In C, chars are delimited by apostrophes (single quotes)

Examples

- 'A'
- '7'
- | | |
- '\$'
- '&'
- ' ^ '
- '_

Numeric Limits (Machine Dependent)

- SIGNED INTEGERS (short, int, long long)
 - \circ short minimum: -32768 = -2¹⁵
 - \circ short maximum: 32767 = 2^{15} 1
 - o int minimum: $-2147483648 = -2^{31}$
 - o int maximum: $2147483647 = 2^{31} 1$
 - o long minimum: $-9223372036854775808 = -2^{63}$
 - o long maximum: $9223372036854775807 = 2^{63} 1$
- UNSIGNED INTEGERS (unsigned short, unsigned int, unsigned long long)
 - o minimum is all zero.
 - o unsigned short maximum: $65535 = 2^{16} 1$
 - o unsigned int maximum: $429467295 = 2^{32} 1$
 - \circ unsigned long maximum: 18446744073709551615 = 2^{64} 1

Numeric Limits (Machine Dependent)

FLOAT PRECISION:

- float precision digits: 6
- float maximum exponent: 38
- o float maximum: 3.402823e+038
- double precision digits: 15
- o double maximum exponent: 308
- o double maximum: 1.797693e+308
- long double precision: 18
- o long double maximum exponent: 4932
- o long double maximum: 1.189731e+4932

Declaring Variables

• All variables **MUST** be declared.

• Examples:

- o int day;
- o int cents;
- o float x;
- o float y1, y2;
- double degrees;
- o double a,b,c;

So, how to program in C++? First, setup your compiler!

https://www.onlinegdb.com/

- If you are serious, you may want to have a local setup.
 - For Windows, I recommend using Visual Studio
 (https://code.visualstudio.com/docs/cpp/config-mingw)
 - For Mac, you should already have a built-in compiler. If you like gcc, you may try: "brew install gcc" in terminal
 (https://osxdaily.com/2023/05/02/how-install-gcc-mac)

So, how to program in C++? First, setup your compiler!

- You may also want to set up "bits/stdc++.h"
 - If you run into issues, please take a look at:
 <u>https://apple.stackexchange.com/questions/148401/file-not-found-er-ror-while-including-bits-stdc-h</u>

So, how to program in C++? Second, try "Hello World!"

Let's try the following hello world program!

```
#include<bits/stdc++.h>
using namespace std;

int main() {
  cout<<"Hello World!"<<endl;
  return 0;
}</pre>
```

So, how to program in C++? Third, learn template code

Typically, you'd like to have the following template as template.cpp:

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;

int main() {
  ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
  return 0;
}
```

(Optional) Try CodeForces Zealots Problem Set

- Next week, we will cover **Data Structures**!
 - Built-in Data Structures: vector; stack; queue; priority_queue; set; map;
 - Custom Data Structures: Disjoint Set Union; Fenwick/Segment Tree;
 Ordered Set;

Next Week!

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 - Built-in Data Structures: vector; stack; queue; priority_queue; set; map;
 - Custom Data Structures: Disjoint Set Union; Fenwick/Segment Tree;
 Ordered Set;

Slide Deck

- You may find the slide decks from:
 - https://github.com/yongwhan/yongwhan.github.io/blob/master/ columbia/shp

