

Model-Building

Build a model with correlation analysis:

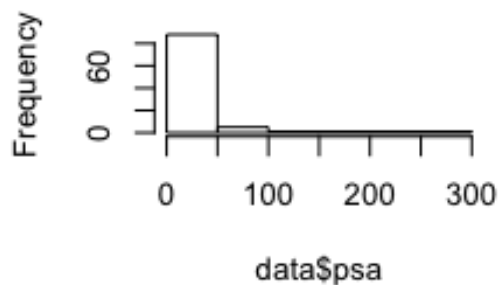
```
file <- "prostate_cancer.csv"
data <- read.csv(file,header = T)

par(mfrow=c(2,2))
#1 explore data and transformation
boxplot(data$psa,main="Box-plot of response variable")
hist(data$psa,main="Histogram of response variable")
data$lnpsa <- log(data$psa)
boxplot(data$lnpsa,main="Box-plot of response variable \nafter
transformation")
hist(data$lnpsa,main="Histogram of response variable \nafter transformation")
```

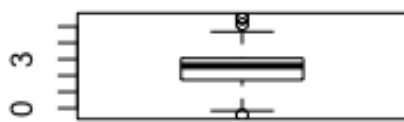
Box-plot of response variable



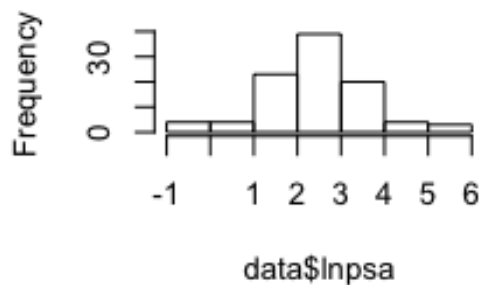
Histogram of response variable



**Box-plot of response variable
after transformation**



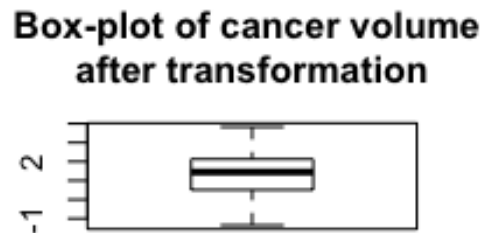
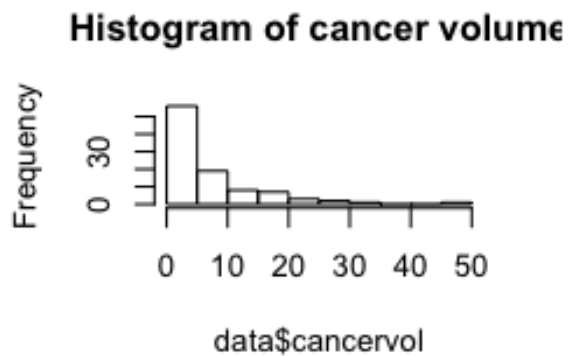
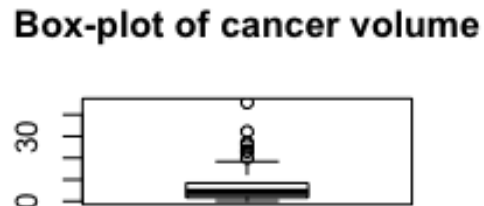
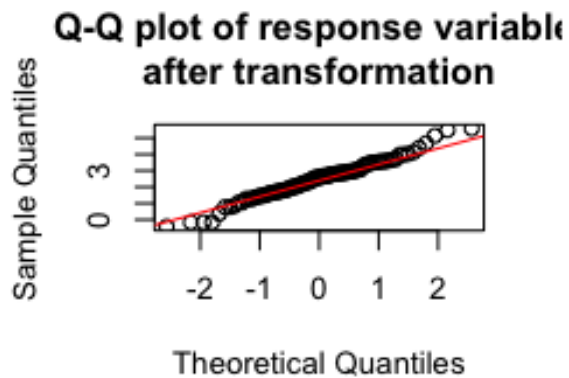
**Histogram of response variable
after transformation**



```
qqnorm(data$lnpsa, main="Q-Q plot of response variable \nafter
transformation")
qqline(data$lnpsa,col="red")

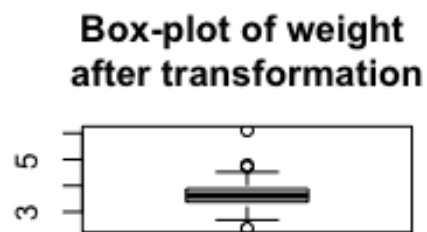
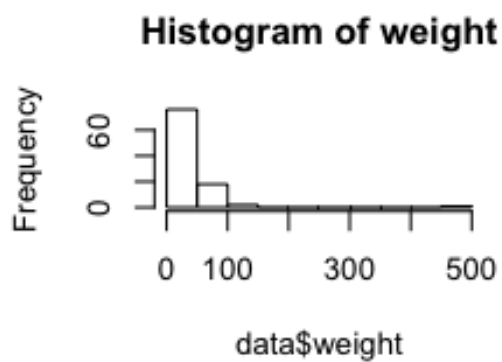
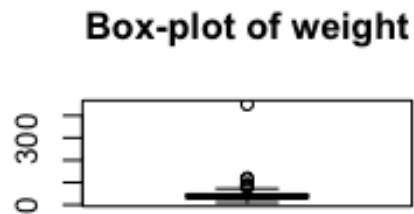
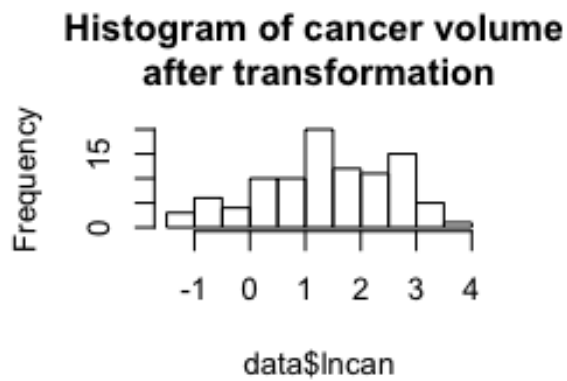
boxplot(data$cancervol,main="Box-plot of cancer volume")
```

```
hist(data$cancervol,main="Histogram of cancer volume")
data$lncan <- log(data$cancervol)
boxplot(data$lncan,main="Box-plot of cancer volume \nafter transformation")
```



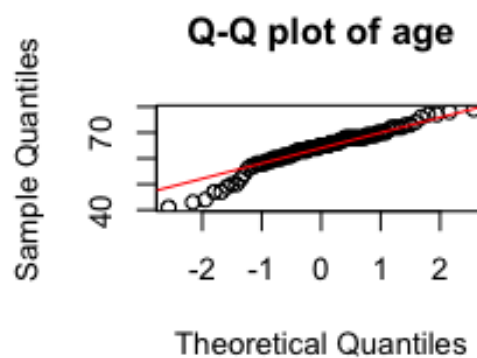
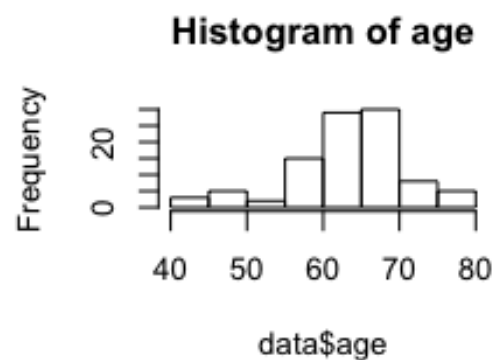
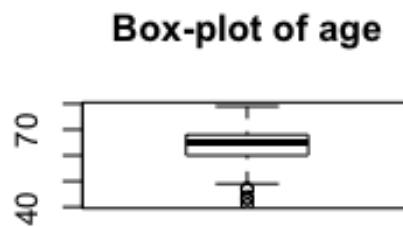
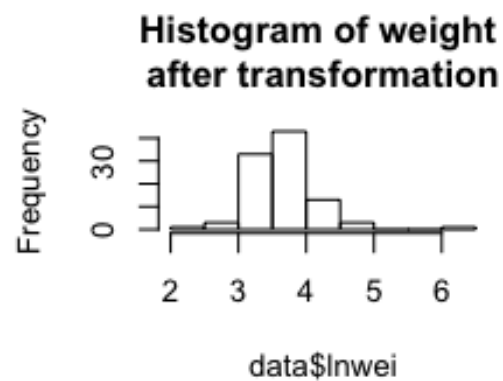
```
hist(data$lncan,main="Histogram of cancer volume \nafter transformation")

boxplot(data$weight,main="Box-plot of weight")
hist(data$weight,main="Histogram of weight")
data$lnwei <- log(data$weight)
boxplot(data$lnwei,main="Box-plot of weight \nafter transformation")
```



```
hist(data$lncan,main="Histogram of cancer volume \nafter transformation")

boxplot(data$weight,main="Box-plot of weight")
hist(data$weight,main="Histogram of weight")
qqnorm(data$weight, main="Q-Q plot of weight")
qqline(data$weight,col="red")
```

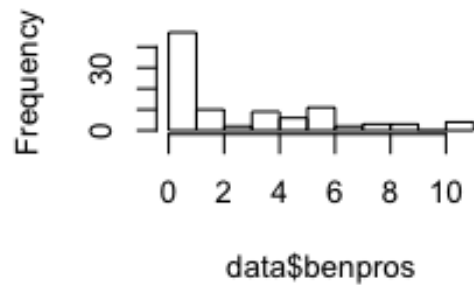


```
boxplot(data$benpros,main="Box-plot of benpros")
hist(data$benpros,main="Histogram of benpros")
data$sqrtben <- sqrt(data$benpros)
boxplot(data$sqrtben,main="Box-plot of benpros \nafter transformation")
hist(data$sqrtben,main="Histogram of benpros \nafter transformation")
```

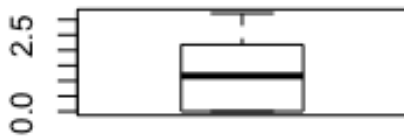
Box-plot of benpros



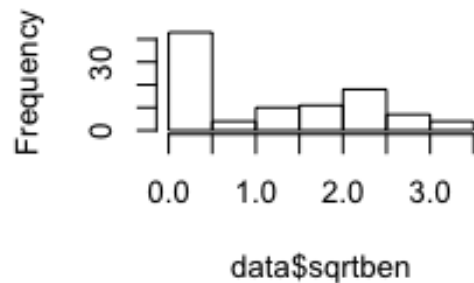
Histogram of benpros



**Box-plot of benpros
after transformation**



**Histogram of benpros
after transformation**

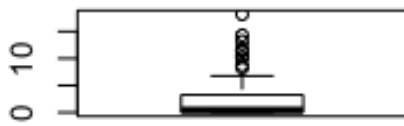


```
data$factves <- factor(data$vesinv)
table(data$vesinv)

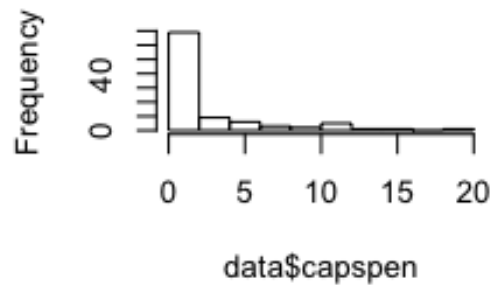
##
##  0  1
## 76 21

boxplot(data$capspen,main="Box-plot of capspen")
hist(data$capspen,main="Histogram of capspen")
data$sqrtcap <- sqrt(data$capspen)
boxplot(data$sqrtcap,main="Box-plot of capspen \nafter transformation")
hist(data$sqrtcap,main="Histogram of capspen \nafter transformation")
```

Box-plot of capspen



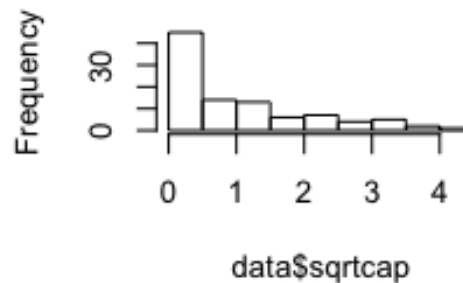
Histogram of capspen



Box-plot of capspen after transformation



Histogram of capspen after transformation



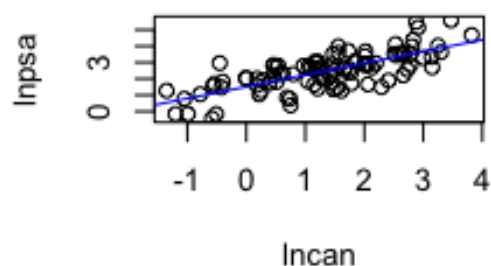
```
table(data$gleason)

##
##  6  7  8
## 33 43 21

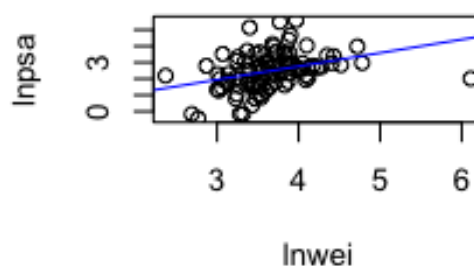
attach(data)

#2 explore relationship between individual columns vs response variable
plot(lncan,lnpsa,main="Cancer volume vs response")
abline(lm(lnpsa~lncan), col="blue")
plot(lnwei,lnpsa,main="Weight vs response")
abline(lm(lnpsa~lnwei), col="blue")
plot(age,lnpsa,main="Age vs response")
abline(lm(lnpsa~age), col="blue")
plot(sqrtben,lnpsa,main="Benpros vs response")
abline(lm(lnpsa~sqrtben), col="blue")
```

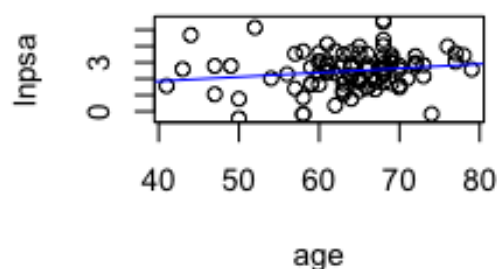
Cancer volume vs response



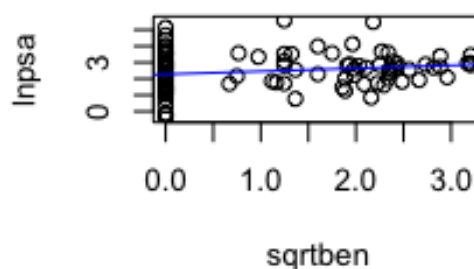
Weight vs response



Age vs response



Benpros vs response



```
plot(vesinv,lnpsa,main="Vesinv vs response")
abline(lm(lnpsa~vesinv), col="blue")
plot(sqrtcap,lnpsa,main="Capspen vs response")
abline(lm(lnpsa~sqrtcap), col="blue")
plot(gleason,lnpsa,main="Gleason vs response")
abline(lm(lnpsa~gleason), col="blue")
```

3 build initial models:

```
fit1 <- lm(lnpsa ~ lncan + lnwei + sqrtcap)
anova(fit1)
```

Analysis of Variance Table

##

Response: lnpsa

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
lncan	1	68.801	68.801	122.897	< 2.2e-16 ***
lnwei	1	5.956	5.956	10.639	0.001549 **
sqrtcap	1	0.948	0.948	1.694	0.196288
Residuals	93	52.064	0.560		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

fit2a <- lm(lnpsa ~ lncan + lnwei + sqrtcap + age)
anova(fit2a)

## Analysis of Variance Table
##
## Response: lnpsa
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## lncan      1 68.801   68.801 122.4760 < 2.2e-16 ***
## lnwei      1  5.956    5.956  10.6026  0.001582 **
## sqrtcap    1  0.948    0.948   1.6882  0.197083
## age        1  0.383    0.383   0.6817  0.411143
## Residuals 92 51.681    0.562
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

fit2b <- lm(lnpsa ~ lncan + lnwei + sqrtcap + factves)
anova(fit2b)

## Analysis of Variance Table
##
## Response: lnpsa
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## lncan      1 68.801   68.801 132.5263 < 2.2e-16 ***
## lnwei      1  5.956    5.956  11.4726  0.001041 **
## sqrtcap    1  0.948    0.948   1.8267  0.179826
## factves    1  4.302    4.302   8.2871  0.004965 **
## Residuals 92 47.762    0.519
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

fit2c <- lm(lnpsa ~ lncan + lnwei + sqrtcap + gleason)
anova(fit2c)

## Analysis of Variance Table
##
## Response: lnpsa
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## lncan      1 68.801   68.801 130.1249 < 2e-16 ***
## lnwei      1  5.956    5.956  11.2647  0.00115 **
## sqrtcap    1  0.948    0.948   1.7936  0.18378
## gleason    1  3.421    3.421   6.4699  0.01264 *
## Residuals 92 48.643    0.529
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

fit3a <- lm(lnpsa ~ lncan + lnwei + factves + gleason)
anova(fit3a)

## Analysis of Variance Table
##
## Response: lnpsa

```



```
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## lncan      1 68.801   68.801 139.9962 < 2.2e-16 ***
## lnwei      1  5.956    5.956  12.1193 0.0007652 ***
## factves    1  5.194    5.194  10.5696 0.0016071 **
## gleason    1  2.605    2.605   5.2999 0.0235824 *
## Residuals 92 45.213    0.491
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

fit3b <- lm(lnpsa ~ lncan + lnwei + factves + gleason + sqrtcap + age)
anova(fit3b)

## Analysis of Variance Table
##
## Response: lnpsa
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## lncan      1 68.801   68.801 140.6106 < 2.2e-16 ***
## lnwei      1  5.956    5.956  12.1725 0.0007528 ***
## factves    1  5.194    5.194  10.6160 0.0015824 **
## gleason    1  2.605    2.605   5.3232 0.0233378 *
## sqrtcap    1  0.395    0.395   0.8067 0.3715049
## age        1  0.781    0.781   1.5971 0.2095851
## Residuals 90 44.037    0.489
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

anova(fit3a,fit3b)

## Analysis of Variance Table
##
## Model 1: lnpsa ~ lncan + lnwei + factves + gleason
## Model 2: lnpsa ~ lncan + lnwei + factves + gleason + sqrtcap + age
##   Res.Df  RSS Df Sum of Sq    F Pr(>F)
## 1      92 45.213
## 2      90 44.037  2    1.1761 1.2019 0.3054

# 4 model diagnostics using stepwise model selection
fit.forward <- stepAIC(lm(lnpsa ~ 1, data = data), scope = list(
  upper = ~lncan + lnwei + factves + gleason + sqrtcap + age + sqrtben),
  direction = "forward")

## Start:  AIC=28.72
## lnpsa ~ 1
##
##           Df Sum of Sq    RSS    AIC
## + lncan    1    68.801  58.968 -44.278
## + factves  1    40.984  86.785  -6.794
## + sqrtcap  1    38.679  89.090  -4.251
## + gleason  1    37.122  90.647  -2.571
## + lnwei    1    15.985 111.784 17.760
## + sqrtben  1     4.031 123.738 27.615
```

```

## + age      1      3.688 124.080  27.883
## <none>                127.769  28.725
##
## Step:  AIC=-44.28
## lnpsa ~ lncan
##
##           Df Sum of Sq    RSS      AIC
## + lnwei    1     5.9560 53.012 -52.606
## + factves   1     5.2731 53.695 -51.365
## + gleason   1     4.5889 54.379 -50.137
## + sqrtben   1     3.1654 55.803 -47.630
## <none>                58.968 -44.278
## + sqrtcap   1     0.8366 58.131 -43.664
## + age       1     0.0031 58.965 -42.283
##
## Step:  AIC=-52.61
## lnpsa ~ lncan + lnwei
##
##           Df Sum of Sq    RSS      AIC
## + factves   1     5.1944 47.818 -60.610
## + gleason   1     4.2337 48.778 -58.680
## <none>                53.012 -52.606
## + sqrtcap   1     0.9484 52.064 -52.357
## + sqrtben   1     0.5173 52.495 -51.558
## + age       1     0.4121 52.600 -51.363
##
## Step:  AIC=-60.61
## lnpsa ~ lncan + lnwei + factves
##
##           Df Sum of Sq    RSS      AIC
## + gleason   1     2.60463 45.213 -64.042
## + sqrtben   1     1.15018 46.668 -60.971
## <none>                47.818 -60.610
## + age       1     0.39331 47.424 -59.411
## + sqrtcap   1     0.05616 47.762 -58.724
##
## Step:  AIC=-64.04
## lnpsa ~ lncan + lnwei + factves + gleason
##
##           Df Sum of Sq    RSS      AIC
## + sqrtben   1     1.02520 44.188 -64.267
## <none>                45.213 -64.042
## + age       1     0.71746 44.496 -63.594
## + sqrtcap   1     0.39470 44.818 -62.893
##
## Step:  AIC=-64.27
## lnpsa ~ lncan + lnwei + factves + gleason + sqrtben
##
##           Df Sum of Sq    RSS      AIC
## + age       1     1.39891 42.789 -65.388

```

```

## <none>                44.188 -64.267
## + sqrtcap  1    0.44007 43.748 -63.238
##
## Step:  AIC=-65.39
## lnpsa ~ lncan + lnwei + factves + gleason + sqrtben + age
##
##           Df Sum of Sq    RSS    AIC
## <none>                42.789 -65.388
## + sqrtcap  1    0.55801 42.231 -64.661

fit.backward <- step(lm(lnpsa ~ lncan + lnwei + factves + gleason + sqrtcap +
age + sqrtben,
  data = data), scope = list(lower = ~1), direction = "backward")

## Start:  AIC=-64.66
## lnpsa ~ lncan + lnwei + factves + gleason + sqrtcap + age + sqrtben
##
##           Df Sum of Sq    RSS    AIC
## - sqrtcap  1    0.5580 42.789 -65.388
## <none>                42.231 -64.661
## - age      1    1.5169 43.748 -63.238
## - sqrtben  1    1.8060 44.037 -62.599
## - lnwei    1    2.9027 45.134 -60.213
## - gleason  1    3.3852 45.616 -59.182
## - factves  1    4.5804 46.811 -56.673
## - lncan    1   18.9521 61.183 -30.702
##
## Step:  AIC=-65.39
## lnpsa ~ lncan + lnwei + factves + gleason + age + sqrtben
##
##           Df Sum of Sq    RSS    AIC
## <none>                42.789 -65.388
## - age      1    1.3989 44.188 -64.267
## - sqrtben  1    1.7067 44.496 -63.594
## - gleason  1    2.9291 45.718 -60.965
## - lnwei    1    3.0222 45.811 -60.768
## - factves  1    4.1357 46.925 -58.438
## - lncan    1   19.7174 62.506 -30.626

fit.both <- step(lm(lnpsa ~ 1, data = data), scope = list(
  lower = ~1, upper = ~lncan + lnwei + factves + gleason + sqrtcap + age +
sqrtben),
  direction = "both")

## Start:  AIC=28.72
## lnpsa ~ 1
##
##           Df Sum of Sq    RSS    AIC
## + lncan    1    68.801  58.968 -44.278
## + factves  1    40.984  86.785  -6.794
## + sqrtcap  1    38.679  89.090  -4.251

```

```

## + gleason 1 37.122 90.647 -2.571
## + lnwei 1 15.985 111.784 17.760
## + sqrtben 1 4.031 123.738 27.615
## + age 1 3.688 124.080 27.883
## <none> 127.769 28.725
##
## Step: AIC=-44.28
## lnpsa ~ lncan
##
## Df Sum of Sq RSS AIC
## + lnwei 1 5.956 53.012 -52.606
## + factves 1 5.273 53.695 -51.365
## + gleason 1 4.589 54.379 -50.137
## + sqrtben 1 3.165 55.803 -47.630
## <none> 58.968 -44.278
## + sqrtcap 1 0.837 58.131 -43.664
## + age 1 0.003 58.965 -42.283
## - lncan 1 68.801 127.769 28.725
##
## Step: AIC=-52.61
## lnpsa ~ lncan + lnwei
##
## Df Sum of Sq RSS AIC
## + factves 1 5.194 47.818 -60.610
## + gleason 1 4.234 48.778 -58.680
## <none> 53.012 -52.606
## + sqrtcap 1 0.948 52.064 -52.357
## + sqrtben 1 0.517 52.495 -51.558
## + age 1 0.412 52.600 -51.363
## - lnwei 1 5.956 58.968 -44.278
## - lncan 1 58.772 111.784 17.760
##
## Step: AIC=-60.61
## lnpsa ~ lncan + lnwei + factves
##
## Df Sum of Sq RSS AIC
## + gleason 1 2.6046 45.213 -64.042
## + sqrtben 1 1.1502 46.668 -60.971
## <none> 47.818 -60.610
## + age 1 0.3933 47.424 -59.411
## + sqrtcap 1 0.0562 47.762 -58.724
## - factves 1 5.1944 53.012 -52.606
## - lnwei 1 5.8772 53.695 -51.365
## - lncan 1 27.9829 75.801 -17.921
##
## Step: AIC=-64.04
## lnpsa ~ lncan + lnwei + factves + gleason
##
## Df Sum of Sq RSS AIC
## + sqrtben 1 1.0252 44.188 -64.267

```

```

## <none> 45.213 -64.042
## + age 1 0.7175 44.496 -63.594
## + sqrtcap 1 0.3947 44.818 -62.893
## - gleason 1 2.6046 47.818 -60.610
## - factves 1 3.5653 48.778 -58.680
## - lnwei 1 5.6038 50.817 -54.709
## - lncan 1 18.8940 64.107 -32.173
##
## Step: AIC=-64.27
## lnpsa ~ lncan + lnwei + factves + gleason + sqrtben
##
## Df Sum of Sq RSS AIC
## + age 1 1.3989 42.789 -65.388
## <none> 44.188 -64.267
## - sqrtben 1 1.0252 45.213 -64.042
## + sqrtcap 1 0.4401 43.748 -63.238
## - gleason 1 2.4797 46.668 -60.971
## - lnwei 1 2.5838 46.772 -60.755
## - factves 1 4.0873 48.275 -57.686
## - lncan 1 18.8602 63.048 -31.789
##
## Step: AIC=-65.39
## lnpsa ~ lncan + lnwei + factves + gleason + sqrtben + age
##
## Df Sum of Sq RSS AIC
## <none> 42.789 -65.388
## + sqrtcap 1 0.5580 42.231 -64.661
## - age 1 1.3989 44.188 -64.267
## - sqrtben 1 1.7067 44.496 -63.594
## - gleason 1 2.9291 45.718 -60.965
## - lnwei 1 3.0222 45.811 -60.768
## - factves 1 4.1357 46.925 -58.438
## - lncan 1 19.7174 62.506 -30.626

```

5 compare my model against stepwise selection

`anova(fit3a, fit.both)`

Analysis of Variance Table

##

Model 1: lnpsa ~ lncan + lnwei + factves + gleason

Model 2: lnpsa ~ lncan + lnwei + factves + gleason + sqrtben + age

Res.Df RSS Df Sum of Sq F Pr(>F)

1 92 45.213

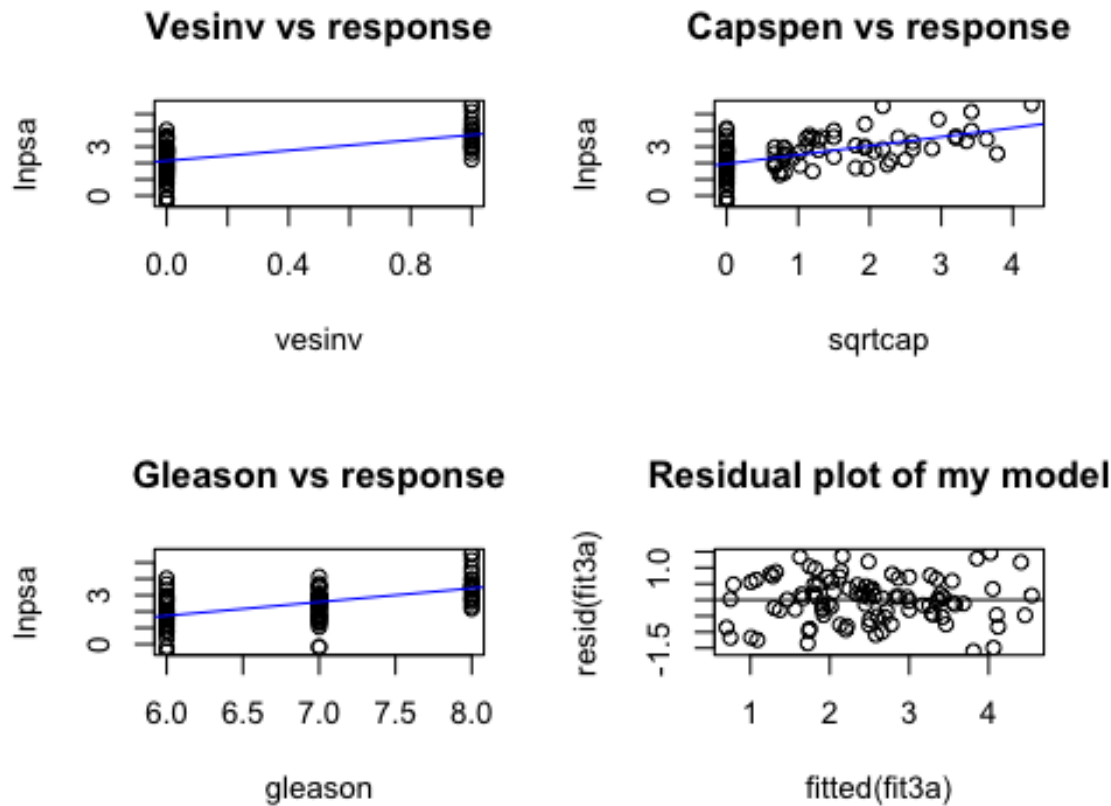
2 90 42.789 2 2.4241 2.5494 0.08376 .

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

6 model evaluation

residual plot

```
plot(fitted(fit3a), resid(fit3a), main="Residual plot of my model")
abline(h = 0)
```



```
# normal QQ plot
qqnorm(resid(fit3a),main="Q-Q Plot of Residual")
qqline(resid(fit3a))

# Time series plot of residuals, ignore because our data is not over time
#plot(resid(fit3a), type="l")
#abline(h=0)

# 7 add new patient data and make prediction
x.new <- data.frame("lncan"=log(mean(cancervol)),
                    "lnwei"=log(mean(weight)),
                    "factves"=factor(names(sort(table(vesinv),decreasing=TRUE)[1])),
                    "gleason"=mean(gleason))

# predict new data
predict(fit3a, newdata=x.new)

##      1
## 2.72739
```

