

Chapter 1

Problem 1.1

A. $25 \div ((1000 \div 100) + (1500 \div 150)) = 1.25 \times$

B. $1500 \div (25 \div 1.67 - 10) = 300(km/h)$

Problem 1.2

$(1 - 0.1) \div (\frac{1}{4} - 0.1) = 6 \times$

Chapter 2

Problem 2.1

A. 0010 0101 1011 1001 1101 0010

B. 0xAE49

C. 1010 1000 1011 0011 1101

D. 0x322D96

Problem 2.2

| n | 2^n (decimal) | 2^n (hexadecimal) |
|-----|-----------------|---------------------|
| 5 | 32 | 0x20 |
| 23 | 8388608 | 0x80000 |
| 15 | 32768 | 0x8000 |
| 13 | 8192 | 0x2000 |
| 12 | 4096 | 0x1000 |
| 6 | 64 | 0x40 |
| 8 | 256 | 0x100 |

Problem 2.3

| Decimal | Binary | Hexadecimal |
|---------|-----------|-------------|
| 0 | 0000 0000 | 0x00 |
| 158 | 1001 1110 | 0x9E |
| 76 | 0100 1100 | 0x7C |
| 145 | 1001 0001 | 0x91 |
| 174 | 1010 1110 | 0xAE |
| 60 | 0011 1100 | 0x3C |
| 241 | 1111 0001 | 0xF1 |
| 116 | 0111 0101 | 0x75 |
| 189 | 1011 1101 | 0xBD |
| 245 | 1111 0101 | 0xF5 |

Problem 2.4

A. $0x605C + 0x5 = 0x6061$

B. $0x605C - 0x20 = 0x603C$

C. $0x605C + 32 = 0x607C$

D. $0x60FA - 0x605C = 0x9e$

Problem 2.5

- A. Little endian: 78 Big endian: 12
- B. Little endian: 78 56 Big endian: 12 34
- C. Little endian: 78 56 34 Big endian: 12 34 56

Problem 2.6

- A. $0x0027C8F8$: 0000 0000 0010 0111 1100 1000 1111 1000
 $0x4A1F23E0$: 0100 1010 0001 1111 0010 0011 1110 0000

Problem 2.7

6d 6e 6f 70 71 72

Problem 2.8

| Operation | Result |
|-----------|----------|
| a | 01001110 |
| b | 11100001 |
| ~a | 10110001 |
| ~b | 00011110 |
| a&b | 01000000 |
| a b | 11101111 |
| a^b | 10101111 |

Problem 2.9

- | | Color | Complement |
|--|-------|------------|
| | White | Black |
- A.

| | |
|-------|---------|
| Blue | Yellow |
| Green | Magenta |
| Cyan | Red |
 - B. $\text{Blue} \mid \text{Green} = \text{Cyan}$
 $\text{Yellow} \& \text{Cyan} = \text{Green}$
 $\text{Red} \wedge \text{Magenta} = \text{Blue}$

Problem 2.10

| Step | *x | *y |
|-----------|----|--------------|
| Initially | a | b |
| Step 1 | a | $a \wedge b$ |
| Step 2 | b | $a \wedge b$ |
| Step 3 | b | a |

Problem 2.11

- A. $\text{first} = \text{last} = k$
- B. The function `implace_swap` was given two identical arguments.
- C. Change line 4 to `"first < last"`.

Problem 2.12

- A. $x \& 0xFF$
- B. $x \wedge \sim 0xFF$
- C. $x \mid 0xFF$

Problem 2.13

```
bis(x, y)
bis(bic(x, y), bitc(y, x))
```

Problem 2.14

| Expression | Value | Expression | Value |
|------------|-------|------------|-------|
| a&b | 0x44 | a&&b | 1 |
| a b | 0x57 | a b | 1 |
| ~a ~b | 0xBB | !a !b | 0 |
| a&!b | 0 | a&&~b | 1 |

Problem 2.15

```
bool equal(int x, int y) {
    return !(x ^ y);
}
```

Problem 2.16

| a | | | a<<2 | | | a>>3 (Logical) | | | a>>3 (Arithmetic) | | |
|------|--------|------|------|--------|------|----------------|--------|------|-------------------|--------|------|
| Hex | Binary | | Hex | Binary | | Hex | Binary | | Hex | Binary | |
| 0xD4 | 1101 | 0100 | 0x50 | 0101 | 0000 | 0x1A | 0001 | 1010 | 0xFA | 1111 | 1010 |
| 0x64 | 0110 | 0100 | 0x90 | 1001 | 0000 | 0x0C | 0000 | 1100 | 0x0C | 0000 | 1100 |
| 0x72 | 0111 | 0010 | 0xC8 | 1100 | 1000 | 0x0E | 0000 | 1110 | 0x0E | 0000 | 1110 |
| 0x44 | 0100 | 0100 | 0x10 | 0001 | 0000 | 0x08 | 0000 | 1000 | 0x08 | 0000 | 1000 |

Problem 2.17

| Hexadecimal | Binary | $B2U_4(\vec{x})$ | $B2T_4(\vec{x})$ |
|-------------|--------|------------------------|-------------------------|
| 0xA | 1010 | $2^3 + 2^1 = 10$ | $-2^3 + 2^1 = -6$ |
| 0x1 | 0001 | $2^0 = 1$ | $2^0 = 1$ |
| 0xB | 1011 | $2^3 + 2^1 + 2^0 = 11$ | $-2^3 + 2^1 + 2^0 = -5$ |
| 0x2 | 0010 | $2^1 = 2$ | $2^1 = 2$ |
| 0x7 | 0111 | $2^2 + 2^1 + 2^0 = 7$ | $2^2 + 2^1 + 2^0 = 7$ |
| 0xC | 1100 | $2^3 + 2^2 = 12$ | $-2^3 + 2^2 = -4$ |

Problem 2.18

- A. 0x2e0=736
- B. -0x58=-88
- C. 0x28=40
- D. -0x30=-48
- E. 0x78=120
- F. 0x88=136
- G. 0x1f8=504
- H. 0xc0=192
- I. -0x48=-72

Problem 2.19

| x | $T2U_4(x)$ |
|----|------------|
| -1 | 15 |
| -5 | 11 |
| -6 | 10 |
| -4 | 12 |
| 1 | 1 |
| 8 | 8 |

Problem 2.20

pass

Problem 2.21

| Expression | Type | Evaluation |
|--------------------------------|----------|------------|
| $-2147483647-1 == 2147483648U$ | Unsigned | 1 |
| $-2147483647-1 < 2147483647$ | Signed | 1 |
| $-2147483647-1U < 2147483647$ | Unsigned | 0 |
| $-2147483647-1 < -2147483647$ | Signed | 1 |
| $-2147483647-1U < -2147483647$ | Unsigned | 1 |

Problem 2.22

- A. $1100_2 = -2^3 + 2^2 = -4$
 B. $11100_2 = -2^4 + 2^3 + 2^2 = -4$
 C. $111100_2 = -2^5 + 2^4 + 2^3 + 2^2 = -4$

Problem 2.23

| | w | fun1(w) | fun2(w) |
|----|------------|------------|------------|
| | 0x00000076 | 0x00000076 | 0x00000076 |
| A. | 0x87654321 | 0x00000021 | 0x00000021 |
| | 0x000000C9 | 0x000000C9 | 0xFFFFF0C9 |
| | 0xEDCBA987 | 0x00000087 | 0xFFFFF087 |

- B. fun1 return the zero extension of the least significant byte of w.
 fun2 return the sign extension of the least significant byte of w.

Problem 2.24

| Hex | | Unsigned | | Signed | |
|----------|-----------|----------|-----------|----------|-----------|
| Original | Truncated | Original | Truncated | Original | Truncated |
| 1 | 1 | 1 | 1 | 1 | 1 |
| 3 | 3 | 3 | 3 | 3 | 3 |
| 5 | 5 | 5 | 5 | 5 | 5 |
| C | 4 | 12 | 4 | -4 | -4 |
| E | 6 | 14 | 6 | -2 | -2 |

Problem 2.25

Reason: When length equals 0, length minus 1 equals $UMax_{32}$, so the expression $i \leq UMax_{32}$ holds for any unsigned i and hence the for loop would never stop.

Correction: Change the expression $i \leq \text{length} - 1$ to $i < \text{length}$.

Problem 2.26

- A. When string s is shorter than string t.
- B. The data type of $\text{strlen}(s) - \text{strlen}(t)$ is unsigned, so it will be greater than 0 for any different $\text{strlen}(s)$ and $\text{strlen}(t)$. So when s is short than t, this function will return a wrong answer.
- C. Change the return value to $\text{strlen}(s) > \text{strlen}(t)$.

Problem 2.27

```
int uadd_ok(unsigned x, unsigned y) {
    return x + y < x || x + y < y;
}
```

Problem 2.28

| x | | $-\frac{u}{4}x$ | |
|-----|---------|-----------------|-----|
| Hex | Decimal | Decimal | Hex |
| 1 | 1 | 15 | F |
| 4 | 4 | 11 | B |
| 7 | 7 | 9 | 9 |
| A | 10 | 6 | 6 |
| E | 14 | 2 | 2 |

Problem 2.29

| x | y | $x + y$ | $x + \frac{t}{5}y$ | Case |
|-------|-------|---------|--------------------|------|
| -12 | -15 | -27 | 5 | 1 |
| 10100 | 10001 | 100101 | 00101 | 1 |
| -8 | -8 | -16 | -16 | 2 |
| 11000 | 11000 | 110000 | 10000 | 2 |
| -9 | 8 | -1 | -1 | 2 |
| 10111 | 01000 | 11111 | 11111 | 2 |
| 2 | 5 | 7 | 7 | 3 |
| 00010 | 00101 | 00111 | 00111 | 3 |
| 12 | 4 | 16 | -16 | 4 |
| 01100 | 00100 | 10000 | 10000 | 4 |

Problem 2.30

```
int tadd_ok(int x, int y) {
    int z = x + y;
    return !((x > 0 && y > 0 && z <= 0) || (x < 0 && y < 0 && z >= 0));
}
```

Problem 2.31

Signed addition is associative and commutative, so $(x+y)-x = y+(x-x)=y$ and hence whether or not there is an overflow, this function will always return 1.

Problem 2.32

For any x and $y = TMin$, this function will give incorrect results.

Problem 2.33

| x | | $-\frac{t}{4}x$ | |
|-----|---------|-----------------|-----|
| Hex | Decimal | Decimal | Hex |
| 2 | 2 | -2 | E |
| 3 | 3 | -3 | D |
| 9 | 9 | -9 | 7 |
| B | 11 | -11 | 5 |
| C | 12 | -12 | 4 |

The bit patterns generated by two's complement and unsigned negation are identical.

Problem 2.34

| Mode | x | | y | | $x \cdot y$ | | Truncated $x \cdot y$ | |
|------------------|-----|--------|-----|--------|-------------|--------|-----------------------|--------|
| | Hex | Binary | Hex | Binary | Hex | Binary | Hex | Binary |
| Unsigned | 4 | 100 | 5 | 101 | 20 | 010100 | 4 | 100 |
| Two's complement | -4 | 100 | -3 | 101 | 12 | 001100 | -4 | 100 |
| Unsigned | 2 | 010 | 7 | 111 | 14 | 001110 | 6 | 110 |
| Two's complement | 2 | 010 | -1 | 111 | -2 | 111110 | -2 | 110 |
| Unsigned | 6 | 110 | 6 | 110 | 36 | 100100 | 4 | 110 |
| Two's complement | -2 | 110 | -2 | 110 | 4 | 000100 | -4 | 100 |

Problem 2.35

pass

Problem 2.36

```
int tmult_ok(int x, int y) {
    int64_t z1 = (int64_t)x * y;
    int z2 = x * y;
    return (int64_t)z2 == z1;
}
```

Problem 2.37

- No improvement at all. Although variable asize is 64-bit and its value is accurate, when it is passed to malloc as a parameter with type size_t, it will still be truncated to 32 bit as well.
- Since the parameter of malloc is size_t with 32 bit, it's impossible to allocate more than 2^{32} bytes. What we can do is to determine whether there is an overflow before malloc. If there is, do not call malloc and return NULL.

Problem 2.38

A power of $2(2^k, \text{ for any } k > 0)$ or A power of 2 plus 1 ($2^k + 1, \text{ for any } k > 0$).

Problem 2.39

$-(x << m)$

Problem 2.40

| K | Shifts | Add/Subs | Expression |
|----|--------|----------|---|
| 7 | 1 | 1 | $(x << 3) - x$ |
| 30 | 4 | 3 | $(x << 4) + (x << 3) + (x << 2) + (x << 1)$ |
| 28 | 2 | 1 | $(x << 5) - (x << 2)$ |
| 55 | 2 | 2 | $(x << 6) - (x << 3) - x$ |

Problem 2.41

When $m = n$ and $m + 1 = n$, choose form A, otherwise form B.

Problem 2.42

```
int div16(int x) {  
    return (x + ((x >> 31) & 0xF)) >> 4;  
}
```

Problem 2.43

$M = 31, N = 8$.

Problem 2.44

- A. False for $x = -2147483648$.
- B. True. If $(x \& 7) \neq 7$ is false, namely $(x \& 7) == 7$, the least 3 significant bits must be [111]. So the most 3 significant bits of $x \ll 29$ will be 111 and hence $x \ll 29 < 0$.
- C. False for $x = 50000$ where the value of $x * x$ equals $2500000000 > 2147483647$, causes positive overflow and yields a negative value.
- D. True. For any $x \geq 0$, $-x$ must be smaller than or equal to 0. Negation of a nonnegative value will never cause an overflow.
- E. False. This is true for any value of type `int` except -2147483648 . Negation of -2147483648 is still -2147483648 and is smaller than 0.
- F. True. Two's complement addition has the same bit-level representation as unsigned.
- G. True