

# DQN: 2constraint Optimal control

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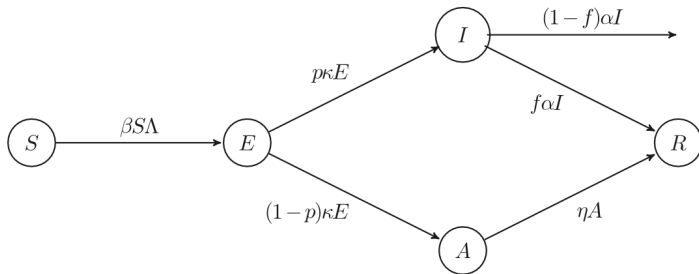
## SLIAR Optimal control

- ▶ GAOL : 2-constraint optimal control
- ▶ Method : DQN

## SLIAR Model

► SLIAR Model Equations and structure.

$$\begin{cases} S' &= -\beta(1-\sigma)S\Lambda - \nu S \\ L' &= \beta(1-\sigma)S\Lambda - \kappa L \\ I' &= p\kappa L - \alpha I - \tau I \\ A' &= (1-p)\kappa L - \eta A \end{cases} \quad \text{with } \Lambda = \epsilon L + (1-q)I + \delta A$$



**Fig. 1.** SEIAR epidemic model.

## SLIAR model parameters

Start: 0

End: 300

S0: 1000000

L0: 0

I0: 1

A0: 0

Reproduction number

: 1.9847

beta: 7.26582E-07

sigma: 0

kappa: 0.526

alpha: 0.244

tau: 0

p: 0.667

eta: 0.244

epsilon: 0

q: 0.5

delta: 1

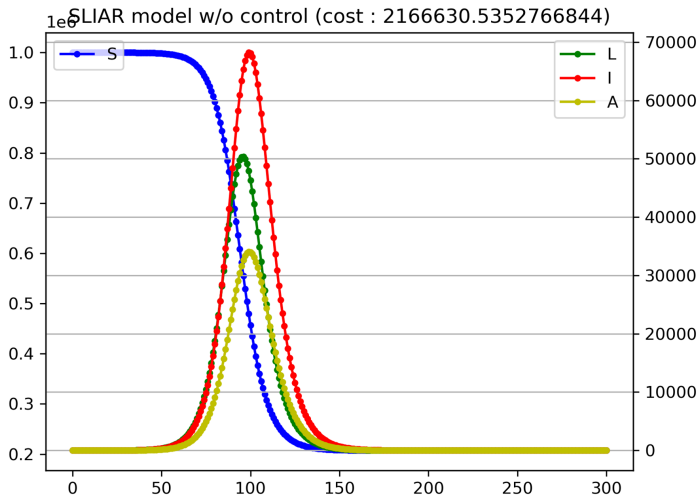
P: 1

Q: 1

R: 0

W: 0

SLIAR w/o control



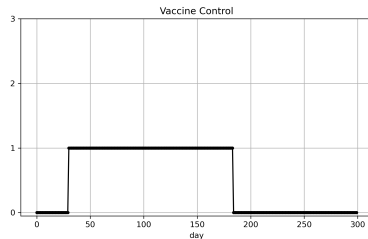
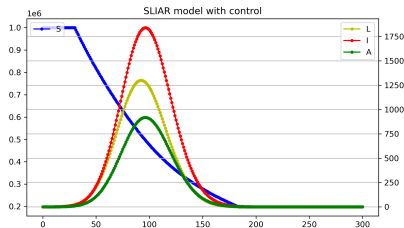
$$\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$$

subject to

$$\begin{cases} S' &= -\beta(1-\sigma)S\Lambda - \nu S \\ L' &= \beta(1-\sigma)S\Lambda - \kappa L \\ I' &= p\kappa L - \alpha I - \tau I \\ A' &= (1-p)\kappa L - \eta A \end{cases} \quad \text{with} \quad \Lambda = \epsilon L + (1-q)I + \delta A$$

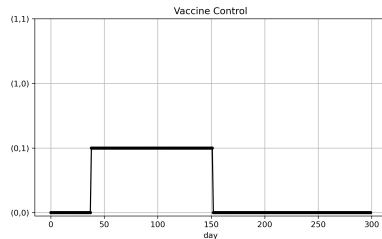
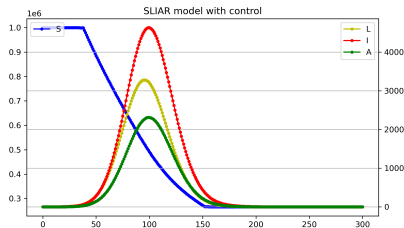
## SLIAR optimal control

- ▶  $\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$
- ▶ Method : DQN
- ▶  $P = 1, Q = 1E6, R = 1E6, \nu_{max} = 0.01, \tau_{max} = 0.05, \text{iteration} : 2000$



## SLIAR optimal control

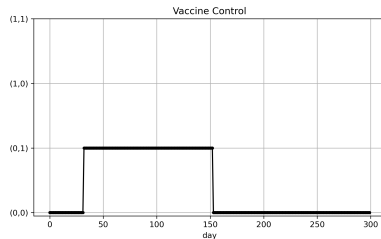
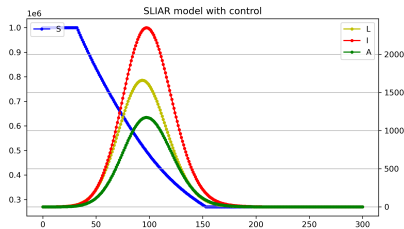
- ▶  $\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$
- ▶ Method : DQN
- ▶  $P = 1, Q = 1E6, R = 1E6, \nu_{max} = 0.01, \tau_{max} = 0.05, \text{iteration} : 5000$





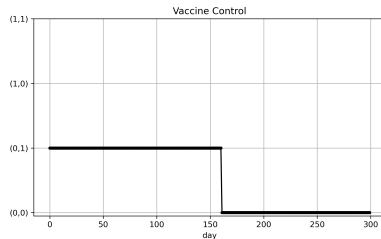
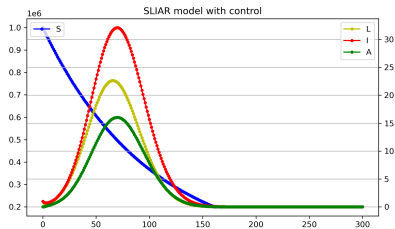
## SLIAR optimal control

- ▶  $\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$
- ▶ Method : DQN
- ▶  $P = 1, Q = 1E6, R = 1E6, \nu_{max} = 0.01, \tau_{max} = 0.05, \text{iteration} : 7000$



## SLIAR optimal control

- ▶  $\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$
- ▶ Method : DQN
- ▶  $P = 1, Q = 1E6, R = 1E6, \nu_{max} = 0.01, \tau_{max} = 0.05, \text{iteration : } 10000$



## Another result of DQN

- ▶  $\min_{u \in \mathcal{U}_{ad}} \int_0^T PI(t) + Q\nu^2(t) + R\tau^2(t) + W\sigma^2(t)dt$
- ▶ Method : DQN
- ▶  $P = 1, Q = 1e6, \nu_{max} = 0.01, \text{iteration} : 10,000$

