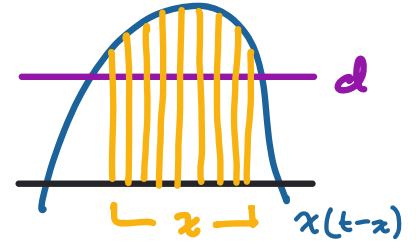


For a time, distance pair  $(t, d)$

We want to find integers  $x$  for which

$$x(t-x) > d. \quad (1)$$



This will be the integers in  $(x_a, x_b)$ ,

where  $x_a$  and  $x_b$  are the solutions of

$$x(t-x) - d = 0$$

$$-x^2 + tx - d = 0$$

$$x_a, x_b = \frac{-t \pm \sqrt{t^2 - 4(-1)(-d)}}{-2} = \frac{t \pm \sqrt{t^2 - 4d}}{2}$$

The minimum integer solution to (1) is:

$$x_{\min} = \left\lfloor \frac{t - \sqrt{t^2 - 4d}}{2} \right\rfloor + 1$$

And the maximum is:

$$x_{\max} = \left\lceil \frac{t + \sqrt{t^2 - 4d}}{2} \right\rceil - 1$$

The number of solutions is:

$$x_{\max} - x_{\min} + 1 = \left\lceil \frac{t + \sqrt{t^2 - 4d}}{2} \right\rceil - \left\lfloor \frac{t - \sqrt{t^2 - 4d}}{2} \right\rfloor - 1$$