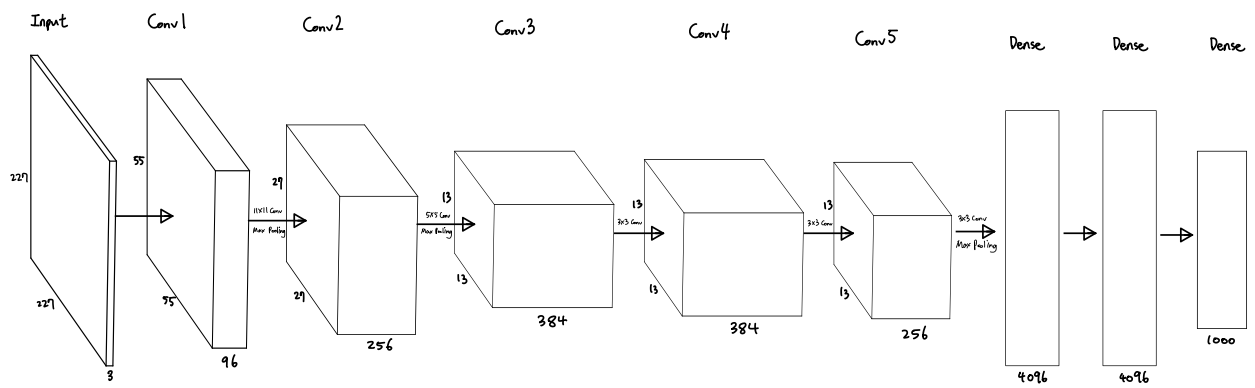


모델 구조



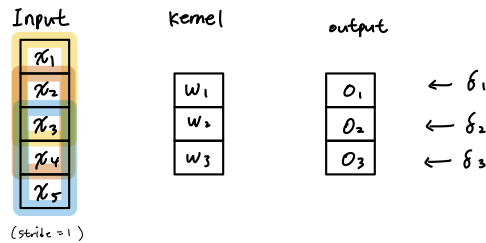
CNN 역전파

∴ 커널이 모든 입력데이터에 적용되므로 역전파 계산에도 Convolution 연산이 사용됨.

* 수식

$$\begin{aligned}\frac{\delta}{\delta x} &= \frac{\delta}{\delta x} \int_{\mathbb{R}^d} f(y)g(x-y) dy \\ &= \int_{\mathbb{R}^d} f(y) \frac{\delta g}{\delta x}(x-y) dy \\ &= [f \cdot g'](x)\end{aligned}$$

* 예시



$$\left. \begin{aligned}o_1 &= w_1 x_1 + w_2 x_2 + w_3 x_3 \\ o_2 &= w_1 x_2 + w_2 x_3 + w_3 x_4 \\ o_3 &= w_1 x_3 + w_2 x_4 + w_3 x_5\end{aligned} \right\} \rightarrow o_i = \sum_{j=1}^3 w_j \cdot x_{i+j-1}$$

- 편미분값: $\delta_1, \delta_2, \delta_3$

- Convolution의 최종 출력값: L

$$\delta_1 = \frac{\partial L}{\partial o_1}, \quad \delta_2 = \frac{\partial L}{\partial o_2}, \quad \delta_3 = \frac{\partial L}{\partial o_3}$$

$$\frac{\partial L}{\partial w_1} = \delta_1 \frac{\partial o_1}{\partial w_1} + \delta_2 \frac{\partial o_1}{\partial w_2} + \delta_3 \frac{\partial o_1}{\partial w_3}$$

$$= \delta_1 x_1 + \delta_2 x_2 + \delta_3 x_3$$

$$\frac{\partial L}{\partial w_2} = \delta_1 x_2 + \delta_2 x_3 + \delta_3 x_4$$

$$\frac{\partial L}{\partial w_3} = \delta_1 x_3 + \delta_2 x_4 + \delta_3 x_5$$

$$\therefore \frac{\partial L}{\partial w_i} = \sum_{j=1}^3 \delta_j x_{i+j-1}$$