

template - personal notes

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I Stellar evolution remnant

Mass prescriptions	<ul style="list-style-type: none"> • WD : $< 8M_{\odot}$ • NS : $8 - 20M_{\odot}$ • BH : not well constrained?
Natal kicks	<ul style="list-style-type: none"> • BH : not well constrained • NS : Maxwellian, $\sigma \sim 270\text{km s}^{-1}$? (see Hobbs et al. (2005))

II Neutron stars

$M \sim 1.4M_{\odot}$, $R \sim 10\text{km}$.

Highest mass observed : $2.14^{+0.10}_{-0.09}M_{\odot}$ ([Cromartie et al., 2019](#))

In general, softer equation of state yields more compact stars, small radii, relatively small max mass. See [Özel & Freire \(2016\)](#) for a review.

absolute upper limit to the NS spin frequency - mass shedding limit - constraint on the EOS about 1000Hz
the highest observed spin rate : 716Hz ([Hessels et al., 2006](#))

1 FORMATION

Progenitor : Type II SNe ($> 8M_{\odot}$). Neutrinos play a crucial role in the collapse. Interior of proto-NS lose energy rapidly by neutrino emission.

Gravitational binding energy released during collapse is about

$$\frac{3}{5} \frac{GM^2}{R} \sim 0.1Mc^2 \sim 10^{53}\text{erg} \quad (1)$$

Kinetic energy of the expanding SN remnant is about $\sim 10^{51}\text{erg}$; nearly all the energy is carried off by neutrinos and anti-neutrinos.

2 STATE OF MATTER

Typical Fermi energies of a NS are of the order $\text{MeV} \sim 10^{10}\text{K}$, therefore the temperature becomes only important when it is very high; otherwise $T = 0$ (cold matter) is a good approximation.

There is no ‘pure’ neutron stars¹ - an actual NS contains a mixture of n , p , and e .

β -decay and inverse β -decay :

$$n \rightarrow p + e + \bar{\nu}_e \quad (2)$$

$$p + e \rightarrow n + \nu_e \quad (3)$$

Fermi energy level rises more quickly for electrons, so the neutron decay (2) becomes energetically less favorable around a critical density $\sim 10^7\text{g cm}^{-3}$ (Pauli blocking) and as the density more electrons are captured into

¹Free neutron lifetime is about 15 minutes ([Gonzalez et al., 2021](#)).

neutrons: beta equilibrium. This results in the formation of Coulomb crystals of progressively more neutron-rich nuclei ².

At matter densities a few times the n_0 , the nucleon Fermi energies becomes so large that it is energetically favorable to transform into heavier baryons such as hyperons via electroweak interactions.

III Astrophysical black holes

1 HOW TO OBSERVE

- X-ray binaries
LMXB :
HMXB :
- Microlensing e.g. OGLE
- LIGO-VIRGO observations

2 MASS

stellar mass BHs : stellar evolution from massive MS star with $8 - 20M_{\odot}$; IMBH : $10^2 - 10^4M_{\odot}$, extremely rare, GW190521; SMBH : $\sim 10^8M_{\odot}$;

References

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- Hessels J. W. T., Ransom S. M., Stairs I. H., Freire P. C. C., Kaspi V. M., Camilo F., 2006, [Science](#), 311, 1901
- Hobbs G., Lorimer D. R., Lyne A. G., Kramer M., 2005, [Monthly Notices of the Royal Astronomical Society](#), 360, 974
- Özel F., Freire P., 2016, [Annual Review of Astronomy and Astrophysics](#), 54, 401

²Laboratory nuclear matter has nearly equal number of neutrons and protons.