Arithmetic in Prolog

Exercise 1

How does Prolog respond to the following queries?

1.
$$X = 3 * 4$$
.

$$X = 3*4$$
.

$$X = 12.$$

3. 4 is X.

ERROR: is/2: Arguments are not sufficiently instantiated

4.
$$X = Y$$
.

$$X = Y$$
.

5.
$$3 \text{ is } 1 + 2$$
.

true.

6.
$$3 \text{ is} + (1, 2)$$
.

true.

7. 3 is X + 2.

ERROR: is/2: Arguments are not sufficiently instantiated

$$X = 3$$
.

9.
$$1 + 2$$
 is $1 + 2$.

false.

10.
$$is(X, + (1, 2))$$
.

$$X = 3$$
.

$$11.3 + 2 = + (3, 2).$$

true.

$$12.*(7, 5) = 7 * 5.$$

true.

$$13.*(7, + (3, 2)) = 7 * (3 + 2).$$

true.

```
14.*(7, (3 + 2)) = 7 * (3 + 2). true.
15.7 * 3 + 2 = *(7, + (3, 2)). false.
16.*(7, (3 + 2)) = 7 * ( + (3, 2)). true.
```

Exercise 2

1. Define a 2-place predicate increment that holds only when its second argument is an integer one larger than its first argument. For example, increment(4,5) should hold, but increment(4,6) should not.

$$increment(X,Y) :- Y is X + 1.$$

2. Define a 3-place predicate sum that holds only when its third argument is the sum of the first two arguments. For example, sum(4,5,9) should hold, but sum(4,6,12) should not.

$$sum(X,Y,Z) :- Z is (X + Y).$$

Exercise 3

Write a predicate addone/2 whose first argument is a list of integers, and whose second argument is the list of integers obtained by adding 1 to each integer in the first list. For example, the query

```
?- addone([1,2,7,2],X).
```

should give

$$X = [2,3,8,3].$$

```
addone([], []).
addone([H1 | T1], [H2 | T2]):- is(H2, +(H1, 1)), addone(T1, T2).
```