Linked Lists

Linked List Class

Linked list class: attributes are passed to __init__

help(isinstance): Return whether an object is an instance of a class or of a subclass thereof.

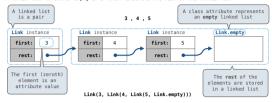
Link(3, Link(4, Link(5)))

(Demo)

Tree Recursion Efficiency

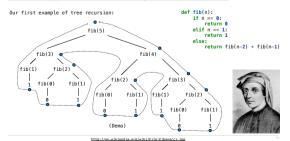
Linked List Structure

A linked list is either empty or a first value and the rest of the linked list



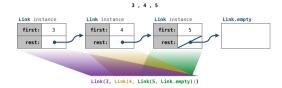
Property Methods

Recursive Computation of the Fibonacci Sequence



Linked List Structure

A linked list is either empty or a first value and the rest of the linked list



Property Methods

In some cases, we want the value of instance attributes to be computed on demand

For example, if we want to access the second element of a linked list



The ${\it @property}$ decorator on a method designates that it will be called whenever it is looked up on an instance

A @<attribute>.setter decorator on a method designates that it will be called whenever that attribute is assigned. <attribute> must be an existing property method.

(Demo)

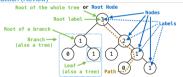
Memoization

Memoization

Idea: Remember the results that have been computed before

(Demo)

Tree Abstraction (Review)



Recursive description (wooden trees):
A tree has a root label and a list of branches

Each branch is a tree

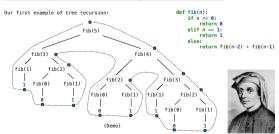
A tree with zero branches is called a leaf
A tree starts at the root

Relative description (family trees):

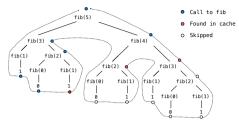
Each location in a tree is called a node
Each node has a label that can be any value
One node can be the parent/child of another
The top node is the root node

People often refer to labels by their locations: "each parent is the sum of its children"

Recursive Computation of the Fibonacci Sequence



Memoized Tree Recursion



Tree Class

```
A Tree has a label and a list of branches; each branch is a Tree

class Tree:
    def_init_[self, label, branches=[]):
        self.label = label
        for branch in branches:
        sasert isistrance(branch, Tree)
        self.branches = list(branches)

def fib_tree(n):
    if n = 0 or n = 1:
        return Tree(n)
else:
        lef = fib_tree(n-2)
        right = fib_tree(n-2)
        right = fib_tree(n-2)
        right = fib_tree(h-1)
        right = fib_tree(h-1)
        return Tree(fib_n, [left, right])

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```

Memoization

Tree Class

Measuring Efficiency

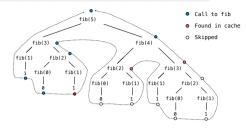
Memoization

Idea: Remember the results that have been computed before

```
def memo(f):
    (cache = {})
    def memoized(n):
    if n not in cache:
        cache[n] = f(n)
    return memoized
        Same behavior as f,
        if f is a pure function
```

(Demo)

Memoized Tree Recursion



Exponentiation

Goal: one more multiplication lets us double the problem size

```
def exp(b, n):
    if n == 0:
        return 1
    ele:
        return b * exp(b, n-1)

    def exp_fast(b, n):
        if n == 0:
        return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    elif n *= 0:
    return 1
    increases the time
    by a constant C
    increases the time
    by a constant C
    increases the time
    by a constant C
    increases the time
    increases the time
    for only 10 times C
```

Linked List Mutation Example

Exponentiation

Mutable Linked Lists

Adding to an Ordered List

add(s, 0)



```
def add(s, v):
    """Add v to an ordered list s with no repeats, returning modified s."""
    (Note: If v is already in s, then don't modify s, but still return it.)
```

Exponentiation

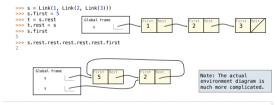
Goal: one more multiplication lets us double the problem size

(Demo)

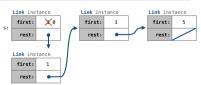
Recursive Lists Can Change

Attribute assignment statements can change first and rest attributes of a Link

The rest of a linked list can contain the linked list as a sub-list



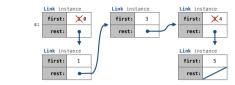
Adding to an Ordered List



```
def add(s, v):
    """Add v to an ordered list s with no repeats, returning modified s."""
    (Note: If v is already in s, then don't modify s, but still return it.)
```

add(s, 0) add(s, 3) add(s, 4)

Adding to an Ordered List

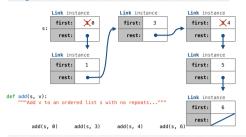


def add(s, v):
 """Add v to an ordered list s with no repeats..."""

add(s, 0) add(s, 3) add(s, 4) add(s, 6)

Tree Mutation

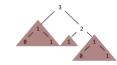
Adding to an Ordered List



Example: Pruning Trees

Removing subtrees from a tree is called *pruning*

Prune branches before recursive processing



def prune(t, n):

"""Prune all sub-trees whose label is n."""

t.branches = [___b ___ for b in t.branches if ____b.label != n ___]
for b in t.branches:

prune(_____, ____n

Adding to a Set Represented as an Ordered List

