```
import numpy as np
import pandas as pd
from numpy import linalg as lg
from numpy import cov
```

## 5 Data Sets

```
In [2]: a=pd.read_csv("2015.csv") a
```

| 0 1 | $\Gamma \cap I$ |   |
|-----|-----------------|---|
| Out | 121             | : |
|     |                 |   |

|     | Country     | Region                                   | Happiness<br>Rank | Happiness<br>Score | Standard<br>Error | Economy<br>(GDP per<br>Capita) | Family  | Health (Life<br>Expectancy) | Freedo |
|-----|-------------|--|-------------------|--------------------|-------------------|--------------------------------|---------|-----------------------------|--------|
| 0   | Switzerland | Western<br>Europe                        | 1                 | 7.587              | 0.03411           | 1.39651                        | 1.34951 | 0.94143                     | 0.665! |
| 1   | Iceland     | Western<br>Europe                        | 2                 | 7.561              | 0.04884           | 1.30232                        | 1.40223 | 0.94784                     | 0.6287 |
| 2   | Denmark     | Western<br>Europe                        | 3                 | 7.527              | 0.03328           | 1.32548                        | 1.36058 | 0.87464                     | 0.6493 |
| 3   | Norway      | Western<br>Europe                        | 4                 | 7.522              | 0.03880           | 1.45900                        | 1.33095 | 0.88521                     | 0.6697 |
| 4   | Canada      | North<br>America                         | 5                 | 7.427              | 0.03553           | 1.32629                        | 1.32261 | 0.90563                     | 0.6329 |
| ••• |             |  |                   |                    |                   |                                |         |                             |        |
| 153 | Rwanda      | Sub-<br>Saharan<br>Africa                | 154               | 3.465              | 0.03464           | 0.22208                        | 0.77370 | 0.42864                     | 0.592( |
| 154 | Benin       | Sub-<br>Saharan<br>Africa                | 155               | 3.340              | 0.03656           | 0.28665                        | 0.35386 | 0.31910                     | 0.484! |
| 155 | Syria       | Middle<br>East and<br>Northern<br>Africa | 156               | 3.006              | 0.05015           | 0.66320                        | 0.47489 | 0.72193                     | 0.1568 |
| 156 | Burundi     | Sub-<br>Saharan<br>Africa                | 157               | 2.905              | 0.08658           | 0.01530                        | 0.41587 | 0.22396                     | 0.1185 |
| 157 | Togo        | Sub-<br>Saharan<br>Africa                | 158               | 2.839              | 0.06727           | 0.20868                        | 0.13995 | 0.28443                     | 0.3645 |

158 rows × 12 columns

## a) Find mean, median, mode and describe

```
In [3]:
         print(a.mean)
         print("Median:")
         print(a.median)
         print("Mode:")
         print(a.mode)
         print("Describe")
         print(a.describe())
        <bound method NDFrame. add numeric operations.<locals>.mean of
                                                                                  Country
        Region Happiness Rank \
             Switzerland
                                            Western Europe
        1
                 Iceland
                                            Western Europe
                                                                          2
                 Denmark
                                                                         3
        2
                                            Western Europe
        3
                  Norway
                                            Western Europe
                                                                         5
        4
                  Canada
                                             North America
                     . . .
                                                                        . . .
                                        Sub-Saharan Africa
        153
                  Rwanda
                                                                       154
                                        Sub-Saharan Africa
        154
                   Benin
                                                                       155
                   Syria Middle East and Northern Africa
        155
                                                                       156
        156
                 Burundi
                                        Sub-Saharan Africa
                                                                       157
        157
                    Togo
                                        Sub-Saharan Africa
                                                                       158
             Happiness Score Standard Error Economy (GDP per Capita)
                                                                          Family \
        0
                        7.587
                                     0.03411
                                                                1.39651 1.34951
        1
                       7.561
                                      0.04884
                                                                1.30232 1.40223
        2
                       7.527
                                     0.03328
                                                                1.32548 1.36058
        3
                       7.522
                                     0.03880
                                                                1.45900 1.33095
        4
                       7.427
                                      0.03553
                                                                1.32629
                                                                         1.32261
                         . . .
                                                                     . . .
        153
                       3.465
                                      0.03464
                                                                0.22208 0.77370
        154
                       3.340
                                     0.03656
                                                                0.28665 0.35386
                                                                0.66320 0.47489
        155
                       3.006
                                     0.05015
        156
                       2.905
                                     0.08658
                                                                0.01530 0.41587
        157
                        2.839
                                      0.06727
                                                                0.20868 0.13995
             Health (Life Expectancy) Freedom Trust (Government Corruption)
        0
                               0.94143 0.66557
                                                                        0.41978
        1
                               0.94784 0.62877
                                                                        0.14145
        2
                               0.87464 0.64938
                                                                       0.48357
        3
                               0.88521 0.66973
                                                                       0.36503
        4
                               0.90563 0.63297
                                                                       0.32957
        . .
                                   . . .
        153
                               0.42864 0.59201
                                                                       0.55191
                                                                       0.08010
        154
                               0.31910 0.48450
        155
                               0.72193 0.15684
                                                                       0.18906
        156
                               0.22396 0.11850
                                                                       0.10062
        157
                               0.28443 0.36453
                                                                       0.10731
             Generosity Dystopia Residual
                0.29678
        0
                                    2.51738
        1
                0.43630
                                    2.70201
        2
                0.34139
                                    2.49204
        3
                0.34699
                                    2.46531
        4
                0.45811
                                    2.45176
        153
                0.22628
                                    0.67042
        154
                0.18260
                                    1.63328
        155
                0.47179
                                    0.32858
        156
                0.19727
                                    1.83302
        157
                0.16681
                                    1.56726
        [158 rows x 12 columns]>
        Median:
        <bound method NDFrame._add_numeric_operations.<locals>.median of
                                                                                    Country
        Region Happiness Rank \
             Switzerland
                                                                          1
        0
                                            Western Europe
        1
                 Iceland
                                            Western Europe
                                                                          2
```

```
2
        Denmark
                                  Western Europe
                                                               3
3
                                                               4
         Norway
                                  Western Europe
4
         Canada
                                   North America
                                                               5
            . . .
                                                              . . .
                              Sub-Saharan Africa
153
         Rwanda
                                                             154
154
          Benin
                              Sub-Saharan Africa
                                                             155
155
          Syria Middle East and Northern Africa
                                                             156
                              Sub-Saharan Africa
156
         Burundi
                                                             157
                              Sub-Saharan Africa
157
           Togo
                                                             158
     Happiness Score Standard Error Economy (GDP per Capita)
                                                               Family \
              7.587 0.03411
0
                                                       1.39651 1.34951
              7.561
                            0.04884
                                                       1.30232 1.40223
1
              7.527
2
                            0.03328
                                                       1.32548 1.36058
3
              7.522
                            0.03880
                                                       1.45900 1.33095
              7.427
                            0.03553
                                                       1.32629 1.32261
4
                . . .
153
              3.465
                            0.03464
                                                      0.22208 0.77370
              3.340
                            0.03656
                                                      0.28665 0.35386
154
155
                            0.05015
                                                      0.66320 0.47489
              3.006
              2.905
                                                      0.01530 0.41587
156
                            0.08658
                                                      0.20868 0.13995
157
              2.839
                            0.06727
     Health (Life Expectancy) Freedom Trust (Government Corruption)
0
                                                             0.41978
                     0.94143 0.66557
                      0.94784 0.62877
1
                                                             0.14145
2
                      0.87464 0.64938
                                                             0.48357
3
                      0.88521 0.66973
                                                             0.36503
                     0.90563 0.63297
4
                                                             0.32957
                          . . .
153
                     0.42864 0.59201
                                                             0.55191
154
                     0.31910 0.48450
                                                             0.08010
155
                     0.72193 0.15684
                                                             0.18906
                     0.22396 0.11850
                                                             0.10062
156
                     0.28443 0.36453
                                                             0.10731
157
     Generosity Dystopia Residual
       0.29678
0
                          2.51738
       0.43630
                          2.70201
1
       0.34139
                          2.49204
2
3
       0.34699
                          2.46531
4
       0.45811
                          2.45176
153
       0.22628
                          0.67042
154
       0.18260
                          1.63328
155
       0.47179
                          0.32858
156
       0.19727
                          1.83302
157
       0.16681
                          1.56726
[158 rows x 12 columns]>
<bound method DataFrame.mode of</pre>
                                        Country
                                                                           Region H
appiness Rank \
     Switzerland
                                  Western Europe
1
        Iceland
                                   Western Europe
2
         Denmark
                                   Western Europe
3
         Norway
                                  Western Europe
4
                                   North America
                                                               5
         Canada
            . . .
                                                              . . .
153
          Rwanda
                              Sub-Saharan Africa
                                                             154
154
                              Sub-Saharan Africa
          Benin
                                                             155
155
           Syria Middle East and Northern Africa
                                                             156
                               Sub-Saharan Africa
156
         Burundi
                                                             157
                              Sub-Saharan Africa
                                                             158
157
           Togo
     Happiness Score Standard Error Economy (GDP per Capita)
                             0.03411
0
               7.587
                                                       1.39651 1.34951
               7.561
                             0.04884
1
                                                       1.30232 1.40223
2
                             0.03328
                                                       1.32548 1.36058
               7.527
```

```
3
               7.522
                              0.03880
                                                         1.45900 1.33095
4
               7.427
                              0.03553
                                                         1.32629
                                                                  1.32261
                 . . .
                                  . . .
                                                             . . .
               3.465
153
                              0.03464
                                                         0.22208
                                                                  0.77370
               3.340
154
                              0.03656
                                                         0.28665
                                                                  0.35386
               3.006
155
                              0.05015
                                                         0.66320 0.47489
               2.905
156
                              0.08658
                                                         0.01530 0.41587
157
               2.839
                              0.06727
                                                         0.20868 0.13995
     Health (Life Expectancy) Freedom Trust (Government Corruption)
                      0.94143 0.66557
                                                                0.41978
0
                      0.94784 0.62877
1
                                                                0.14145
2
                      0.87464 0.64938
                                                                0.48357
3
                      0.88521 0.66973
                                                                0.36503
4
                      0.90563 0.63297
                                                                0.32957
                           . . .
                                                                0.55191
153
                      0.42864 0.59201
154
                      0.31910 0.48450
                                                                0.08010
155
                      0.72193 0.15684
                                                                0.18906
                      0.22396 0.11850
                                                                0.10062
156
                      0.28443 0.36453
                                                                0.10731
157
     Generosity Dystopia Residual
        0.29678
0
                           2.51738
        0.43630
                           2.70201
1
        0.34139
                           2,49204
2
3
                           2.46531
        0.34699
        0.45811
4
                            2.45176
153
                           0.67042
        0.22628
154
                           1.63328
        0.18260
155
        0.47179
                           0.32858
        0.19727
                           1.83302
156
        0.16681
                           1.56726
157
[158 rows x 12 columns]>
Describe
       Happiness Rank Happiness Score Standard Error
           158.000000
                            158.000000
                                             158.000000
count
            79.493671
                                               0.047885
mean
                               5.375734
std
            45.754363
                              1.145010
                                               0.017146
min
             1.000000
                              2.839000
                                               0.018480
            40.250000
25%
                              4.526000
                                               0.037268
            79.500000
50%
                              5.232500
                                               0.043940
75%
           118.750000
                               6.243750
                                               0.052300
           158.000000
                               7.587000
                                               0.136930
max
       Economy (GDP per Capita)
                                      Family Health (Life Expectancy)
                     158.000000 158.000000
                                                             158.000000
count
mean
                       0.846137
                                    0.991046
                                                               0.630259
std
                       0.403121
                                    0.272369
                                                               0.247078
min
                       0.000000
                                    0.000000
                                                               0.000000
25%
                        0.545808
                                    0.856823
                                                               0.439185
50%
                        0.910245
                                    1.029510
                                                               0.696705
75%
                        1.158448
                                    1.214405
                                                               0.811013
                        1.690420
                                    1.402230
                                                               1.025250
max
          Freedom Trust (Government Corruption)
                                                   Generosity
count 158.000000
                                       158.000000 158.000000
         0.428615
                                         0.143422
                                                      0.237296
mean
         0.150693
                                         0.120034
                                                      0.126685
std
         0.000000
                                         0.000000
                                                      0.000000
min
25%
         0.328330
                                         0.061675
                                                      0.150553
         0.435515
                                         0.107220
50%
                                                      0.216130
         0.549092
                                         0.180255
                                                      0.309883
75%
                                         0.551910
                                                      0.795880
max
         0.669730
```

Dystopia Residual count 158.000000

| mean | 2.098977 |
|------|----------|
| std  | 0.553550 |
| min  | 0.328580 |
| 25%  | 1.759410 |
| 50%  | 2.095415 |
| 75%  | 2.462415 |
| max  | 3.602140 |

## b) Find sum(), cumsum(), count, min and max values

```
In [4]:
         print(a.sum())
                                          SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
        Country
        Region
                                          Western EuropeWestern EuropeWestern EuropeWest...
        Happiness Rank
                                                                                        12560
                                                                                      849.366
        Happiness Score
                                                                                      7.56579
        Standard Error
        Economy (GDP per Capita)
                                                                                    133.68968
                                                                                    156.58526
        Family
                                                                                     99.58098
        Health (Life Expectancy)
                                                                                     67.72116
        Freedom
        Trust (Government Corruption)
                                                                                     22.66065
                                                                                     37,49269
        Generosity
        Dystopia Residual
                                                                                    331.63833
        dtype: object
In [5]:
         print(a.cumsum())
                                                         Country
                                                     Switzerland
                                              SwitzerlandIceland
        1
        2
                                      SwitzerlandIcelandDenmark
        3
                                SwitzerlandIcelandDenmarkNorway
        4
                          SwitzerlandIcelandDenmarkNorwayCanada
             SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
        153
        154
             SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
        155
             SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
             SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
             SwitzerlandIcelandDenmarkNorwayCanadaFinlandNe...
                                                          Region Happiness Rank
        0
                                                  Western Europe
        1
                                   Western EuropeWestern Europe
                                                                               3
        2
                     Western EuropeWestern EuropeWestern Europe
                                                                               6
        3
             Western EuropeWestern EuropeWestern EuropeWest...
                                                                              10
        4
             Western EuropeWestern EuropeWestern EuropeWest...
                                                                              15
                                                                              . . .
             Western EuropeWestern EuropeWestern EuropeWest...
        153
                                                                           11934
             Western EuropeWestern EuropeWestern EuropeWest...
        154
                                                                           12089
             Western EuropeWestern EuropeWestern EuropeWest...
        155
                                                                           12245
             Western EuropeWestern EuropeWestern EuropeWest...
                                                                           12402
        156
             Western EuropeWestern EuropeWestern EuropeWest...
                                                                           12560
             Happiness Score Standard Error Economy (GDP per Capita)
                                                                             Family
        0
                        7.587
                                                                 1.39651
                                      0.03411
                                                                            1.34951
                       15.148
                                      0.08295
                                                                 2.69883
        1
                                                                            2.75174
        2
                                                                 4.02431
                       22.675
                                      0.11623
                                                                            4.11232
        3
                       30.197
                                                                 5.48331
                                      0.15503
                                                                            5.44327
                                                                 6.80960
        4
                       37.624
                                      0.19056
                                                                            6.76588
                          . . .
                                      7.32523
        153
                      837.276
                                                               132.51585
                                                                          155.20069
        154
                      840.616
                                      7.36179
                                                               132.80250
                                                                          155.55455
        155
                      843.622
                                      7.41194
                                                               133.46570
                                                                          156.02944
```

```
156
                                      7.49852
                     846.527
                                                              133.48100 156.44531
        157
                     849.366
                                      7.56579
                                                              133.68968 156.58526
                                         Freedom Trust (Government Corruption)
             Health (Life Expectancy)
        0
                              0.94143
                                                                        0.41978
                                        0.66557
                               1.88927
                                                                        0.56123
        1
                                        1.29434
                                                                        1.04480
        2
                               2.76391 1.94372
        3
                              3.64912 2.61345
                                                                        1.40983
        4
                              4.55475 3.24642
                                                                        1.73940
                                   . . .
                             98.03156 66.59679
        153
                                                                       22.18356
        154
                             98.35066 67.08129
                                                                       22.26366
        155
                             99.07259 67.23813
                                                                       22.45272
                             99.29655 67.35663
                                                                       22.55334
        156
                             99.58098 67.72116
                                                                       22.66065
        157
             Generosity Dystopia Residual
        0
                0.29678
                                   2.51738
                0.73308
                                   5.21939
        1
        2
                1.07447
                                   7.71143
        3
                1.42146
                                  10.17674
                1.87957
        4
                                  12.62850
        153
               36.47422
                                 326.27619
        154
               36.65682
                                 327.90947
        155
               37.12861
                                 328.23805
        156
               37.32588
                                 330.07107
        157
               37.49269
                                 331.63833
        [158 rows x 12 columns]
In [6]:
         print(a.count())
         print(a.min())
         print(a.max())
        Country
                                          158
        Region
                                          158
        Happiness Rank
                                          158
        Happiness Score
                                          158
        Standard Error
                                          158
        Economy (GDP per Capita)
                                          158
        Family
                                          158
        Health (Life Expectancy)
                                          158
        Freedom
                                          158
        Trust (Government Corruption)
                                          158
        Generosity
                                          158
        Dystopia Residual
                                          158
        dtype: int64
        Country
                                                        Afghanistan
        Region
                                          Australia and New Zealand
        Happiness Rank
                                                                  1
        Happiness Score
                                                              2.839
        Standard Error
                                                            0.01848
        Economy (GDP per Capita)
                                                                0.0
                                                                0.0
        Family
        Health (Life Expectancy)
                                                                0.0
        Freedom
                                                                0.0
                                                                0.0
        Trust (Government Corruption)
        Generosity
                                                                0.0
        Dystopia Residual
                                                            0.32858
        dtype: object
        Country
                                                Zimbabwe
        Region
                                          Western Europe
        Happiness Rank
                                                     158
        Happiness Score
                                                   7.587
        Standard Error
                                                 0.13693
        Economy (GDP per Capita)
                                                 1.69042
        Family
                                                 1.40223
```

Health (Life Expectancy) 1.02525
Freedom 0.66973
Trust (Government Corruption) 0.55191
Generosity 0.79588
Dystopia Residual 3.60214
dtype: object

## c) Find covariance and correlation (spearman and pearsons)

In [7]: print(a.cov()) Happiness Rank Happiness Score \ -51.975613 Happiness Rank 2093.461743 -51.975613 Happiness Score 1.311048 0.124358 Standard Error -0.003480 Economy (GDP per Capita) -14.483883 0.360476 -9.142720 0.230969 Family Health (Life Expectancy) -8.316021 0.204881 -3.839647 0.098042 Freedom Trust (Government Corruption) -2.044785 0.054316 Generosity -0.928243 0.026156 Dystopia Residual -13.220847 0.336225 Standard Error Economy (GDP per Capita) Happiness Rank -14.483883 0.124358 Happiness Score -0.003480 0.360476 -0.001504 Standard Error 0.000294 Economy (GDP per Capita) -0.001504 0.162506 Family -0.000564 0.070852 Health (Life Expectancy) -0.001315 0.081323 Freedom -0.000335 0.022495 Trust (Government Corruption) -0.000367 0.014898 Generosity -0.000192 -0.000534 Dystopia Residual 0.000797 0.008939 Family Health (Life Expectancy) Freedom -9.142720 -8.316021 -3.839647 Happiness Rank 0.204881 0.098042 Happiness Score 0.230969 -0.001315 -0.000335 Standard Error -0.000564 Economy (GDP per Capita) 0.070852 0.081323 0.022495 0.035741 0.018122 Family 0.074185 Health (Life Expectancy) 0.035741 0.061047 0.013422 0.018122 0.013422 0.022708 Trust (Government Corruption) 0.006722 0.007365 0.008927 0.003020 0.003391 Generosity 0.007138 Dystopia Residual 0.022332 0.002596 0.005237 Trust (Government Corruption) Generosity \ Happiness Rank -2.044785 -0.928243 Happiness Score 0.054316 0.026156 Standard Error -0.000367 -0.000192 Economy (GDP per Capita) 0.014898 -0.000534 0.006722 0.003020 Family Health (Life Expectancy) 0.007365 0.003391 0.007138 0.008927 0.004199 Trust (Government Corruption) 0.014408 0.004199 Generosity 0.016049 Dystopia Residual -0.002200 -0.007104 Dystopia Residual Happiness Rank -13.220847

0.336225

0.000797

0.008939

Happiness Score

Standard Error

Economy (GDP per Capita)

Family 0.022332
Health (Life Expectancy) 0.002596
Freedom 0.005237
Trust (Government Corruption) -0.002200
Generosity -0.007104
Dystopia Residual 0.306417

In [8]: b=a.dropna(axis=1,how='any')
b

Out[8]:

| : |     | Country     | Region                                   | Happiness<br>Rank | Happiness<br>Score | Standard<br>Error | Economy<br>(GDP per<br>Capita) | Family  | Health (Life<br>Expectancy) | Freedo |
|---|-----|-------------|--|-------------------|--------------------|-------------------|--------------------------------|---------|-----------------------------|--------|
|   | 0   | Switzerland | Western<br>Europe                        | 1                 | 7.587              | 0.03411           | 1.39651                        | 1.34951 | 0.94143                     | 0.665! |
|   | 1   | Iceland     | Western<br>Europe                        | 2                 | 7.561              | 0.04884           | 1.30232                        | 1.40223 | 0.94784                     | 0.6287 |
|   | 2   | Denmark     | Western<br>Europe                        | 3                 | 7.527              | 0.03328           | 1.32548                        | 1.36058 | 0.87464                     | 0.6493 |
|   | 3   | Norway      | Western<br>Europe                        | 4                 | 7.522              | 0.03880           | 1.45900                        | 1.33095 | 0.88521                     | 0.6697 |
|   | 4   | Canada      | North<br>America                         | 5                 | 7.427              | 0.03553           | 1.32629                        | 1.32261 | 0.90563                     | 0.6329 |
|   | ••• |             |  |                   |                    |                   |                                |         |                             |        |
|   | 153 | Rwanda      | Sub-<br>Saharan<br>Africa                | 154               | 3.465              | 0.03464           | 0.22208                        | 0.77370 | 0.42864                     | 0.592( |
|   | 154 | Benin       | Sub-<br>Saharan<br>Africa                | 155               | 3.340              | 0.03656           | 0.28665                        | 0.35386 | 0.31910                     | 0.484  |
|   | 155 | Syria       | Middle<br>East and<br>Northern<br>Africa | 156               | 3.006              | 0.05015           | 0.66320                        | 0.47489 | 0.72193                     | 0.156{ |
|   | 156 | Burundi     | Sub-<br>Saharan<br>Africa                | 157               | 2.905              | 0.08658           | 0.01530                        | 0.41587 | 0.22396                     | 0.1185 |
|   | 157 | Togo        | Sub-<br>Saharan<br>Africa                | 158               | 2.839              | 0.06727           | 0.20868                        | 0.13995 | 0.28443                     | 0.364! |

158 rows × 12 columns

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