

Exercise 1.

$$\begin{aligned}
 c) \quad & p(\text{home}) = 0.7 \\
 & p(\text{uni}) = 0.3 \\
 & p(\text{others}) = 0
 \end{aligned}$$

$$\begin{aligned}
 \text{bel}(x_{t+1}) &= \eta p(z_t | x_t) \underbrace{\sum p(x_{t+1} | x_t, u)}_{\substack{\text{there is no} \\ \text{action}}} \text{bel}(x_t) \\
 &= \eta p(z_t | x_t) \text{bel}(x_t) \Rightarrow
 \end{aligned}$$

$$\text{bel}(\text{home}) = \frac{0.0114 \cdot 0.7}{0.0114 \cdot 0.7 + 0.0978 \cdot 0.3}$$

Exercise 2: Sensor Model

$$z = \begin{pmatrix} z_r \\ z_\theta \end{pmatrix} \sim \mathcal{N} \left(\begin{pmatrix} \sigma_r^2 \\ \sigma_\theta^2 \end{pmatrix} \right)$$

$$p(z_r, z_\theta) = p(z_r) p(z_\theta) \quad \text{independence}$$

$$p(z | x, l) \quad \begin{array}{l} \nearrow \text{pose} \\ \text{sensor model ?} \\ \nwarrow \text{measurement} \quad \searrow \text{landmark} \end{array}$$

sensor model: probability of measurement given the pose of robot for landmark l .

$$\mathcal{N}(\bar{z} = \hat{\bar{z}} | x, l)$$

$$\hat{\bar{z}} = \begin{pmatrix} \hat{z}_r \\ \hat{z}_\theta \end{pmatrix} = \begin{pmatrix} \text{norm}(x - l) \\ \arctan2\left(\frac{ly - x_y}{lx - x_x}\right) \end{pmatrix}$$

$$p(z | x, l) = \underbrace{\text{np.prod}}_{\text{np.prod}} \left(\text{stat. norm}(\text{log-opp scales} \begin{pmatrix} \sigma_r \\ \sigma_\theta \end{pmatrix}) \cdot \text{pdf}(z - \hat{\bar{z}}) \right)$$