## Programming in Haskell – Homework Assignment 2

## UNIZG FER, 2014/2015

Handed out: October 12, 2014. Due: October 17, 2014 at 23:59

Note: Define each function with the exact name specified. You can (and in most cases you should) define each function using a number of simpler functions. Unless said otherwise, a function may not cause runtime errors and must be defined for all of its input values. Use the error function for cases in which a function should terminate with an error message. Problems marked with a star  $(\star)$  are optional.

1. (a) Define a function to Title Case that takes a String and returns a title cased version of it. Articles, conjunctions, and prepositions are to be capitalized as well.

```
toTitleCase "this is an example" \Rightarrow "This Is An Example" toTitleCase "100 bottles of beer on the wall" \Rightarrow "100 Bottles Of Beer On The Wall" toTitleCase "short" \Rightarrow "Short" toTitleCase "" \Rightarrow ""
```

(b) In title case, articles, conjunctions, and prepositions are usually not capitalized, unlike in problem (a). To achieve this, we can define the function toTitleCase' that takes an additional argument: a list of words that will remain in lowercase, unless the word occurs at the beginning of the string, in which case it should be titlecased as well.

```
toTitleCase' "Scientists discover a cure" ["a","the"] \Rightarrow "Scientists Discover a Cure" toTitleCase' "A day in the life" ["a","in","the"] \Rightarrow "A Day in the Life"
```

2. Implement a function trimN that takes a list and a number n. It removes n elements from each side of the list. If the trimming would eliminate more elements than the list contains, the list is returned unchanged.

```
trimN [1,2,3,4,5] 2 \Rightarrow [3]
trimN [] 5 \Rightarrow []
trimN [1,2,3] 2 \Rightarrow [1,2,3]
```

3. Import System.Environment to get access to the getArgs action, which returns a list of command line arguments to the program. Given a single path as an argument, read the file at the given path and print it out with all of its characters capitalized. To read in a file, use the readFile IO action.

```
$ ./ECHOFILE file.txt
THIS IS SOME TEXT IN FILE.TXT
```

Here is an example of using getArgs to print out the first command line argument:

```
import System.Environment
printFirstArg = do
  args <- getArgs
  putStrLn $ head args</pre>
```

4. Define a function onlyDivisible that takes a String and a number n. It should drop all characters located at positions that are not divisible by n. Character positions are 0-indexed.

```
onlyDivisible "example" 1 \Rightarrow "example" onlyDivisible "11+111=122" 2 \Rightarrow "1+1=2" onlyDivisible "This is the third example case" 10 \Rightarrow "Tea" onlyDivisible any 0 \Rightarrow error "n must be positive!"
```

5. You are given a set of points in the Cartesian coordinate system, represented as a list of tuples. Implement a function triangleCounter that returns the number of distinct triangles with endpoints from the given set. Degenerate triangles (formed using three colinear points) should not be included.

```
triangleCounter [] \Rightarrow 0
triangleCounter [(0,0),(1,1),(2,2)] \Rightarrow 0
triangleCounter [(0,0),(1,1),(0,2)] \Rightarrow 1
triangleCounter [(0,0),(0,1),(1,0),(1,1)] \Rightarrow 4
```

6. Implement a function reverseWords that takes a sentence and reverses the order of words. A sentence is represented as a String with words separated by a single whitespace.

```
reverseWords "" \Rightarrow "" reverseWords "human being and fish can coexist peacefully" \Rightarrow "peacefully coexist can fish and being human"
```

7. Let's use lists as sets, even though this isn't recommended for performance reasons. Define intersect' and difference that implement the usual set operators. Assume the list elements don't have an ordering (i.e., don't use operators such as < or > to compare them, and also don't sort them), but do assume we can test them for equality. Both input and output lists may have duplicate elements.

```
intersect' "mio" "mao" \Rightarrow "mo" intersect' [1..3] [1..] \Rightarrow [1..3] intersect' [1..] [1..3] \Rightarrow [1,2,3,\bot] intersect' [] [1..] \Rightarrow [] intersect' [1..] [] \Rightarrow [] difference "mio" "mao" \Rightarrow "i" difference [4,3] [1..] \Rightarrow [] difference [4,3] [5..] \Rightarrow [4] difference [1..] \Rightarrow [3] difference [1..] \Rightarrow [4] difference [1..] \Rightarrow [3] \Rightarrow [4] difference [1..] \Rightarrow [1..]
```

8. We can use a list of lists, where all sublists are of equal length, to represent a matrix. Define the following functions over such a matrix:

(a) The function is WellFormed that checks whether the matrix has all rows of equal length.

```
isWellFormed [[1,2,3],[4,5,6],[7,8,9]] \Rightarrow True isWellFormed [[1,2,3],[4,5]] \Rightarrow False isWellFormed [[]] \Rightarrow False
```

(b) The function size that returns the dimensions of a  $n \times m$  matrix as a tuple (n,m).

```
size [[1,2,3],[4,5,6]] \Rightarrow (2,3)
size [[5,0,5],[2]] \Rightarrow error "Matrix is malformed"
size [[]] \Rightarrow error "Matrix is malformed"
```

(c) The function getElement that returns the element at the given position in matrix.

```
getElement [[9,8,7],[6,5,4],[3,2,1]] 0 0 \Rightarrow 9 getElement [[9,8,7],[6,5,4],[3,2,1]] 3 0 \Rightarrow error "Index out of bounds" getElement [[3,2,1],[5,4]] 0 0 \Rightarrow error "Matrix is malformed" getElement [[1],[2,3]] (-1) 0 \Rightarrow either of the errors above
```

(d) The function getRow that returns the i-th row of a matrix.

```
getRow [[1,2],[3,4],[5,6]] 0 \Rightarrow [1,2]
getRow [[1,2,3],[4,5]] 1 \Rightarrow \text{error "Matrix is malformed"}
getRow [[1,2,3]] (-3) \Rightarrow \text{error "Index out of bounds"}
getRow [[1,2],[3,4,5]] 2 \Rightarrow \text{either of the errors above}
```

(e) The function getCol that returns the i-th column of a matrix.

```
getCol [[1,2,3],[4,5,6]] 0 \Rightarrow [1,4]
getCol [[1,2,3],[4,5]] 1 \Rightarrow error "Matrix is malformed"
getCol [[1,2,3]] (-3) \Rightarrow error "Index out of bounds"
getCol [[1,2],[3,4,5]] 2 \Rightarrow either of the errors above
```

(f) The function addMatrices that returns the sum of two given matrices.

```
addMatrices [[1,2,3],[4,5,6]] [[7,8,9],[10,11,12]] 

\Rightarrow [[8,10,12],[14,16,18]] 

addMatrices [[1,2,3],[4,5,6]] [[1]] 

\Rightarrow error "Matrices are not of equal size" 

addMatrix [[1,2],[3,4]] [[5,6],[7]] \Rightarrow error "Matrix is malformed"
```

(g) The function transpose' that returns a transposed version of the given matrix. It may not use the Data.List.transpose function.

```
transpose' [[1,2,3],[4,5,6]] \Rightarrow [[1,4],[2,5],[3,6]] transpose' [[1,2,3],[4,5]] \Rightarrow error "Matrix is malformed"
```

(h)★ The function multMatrices that multiplies two matrices.

```
multMatrices [[1,2],[3,4],[5,6]] [[7,8],[9,10]] 

\Rightarrow [[25,28],[57,64],[89,100]] 

multMatrices [[1,0],[0,1]] [[3,5],[9.2]] \Rightarrow [[3,5],[9,2]] 

multMatrices [[1,2],[3,4]] [[5]] 

\Rightarrow error "Incompatible matrix dimensions" 

multMatrices [[1,2],[3]] [[4]] \Rightarrow error "Matrix is malformed"
```

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## Corrections

v1.1 – Fixed the submission date