Homework Assignment 4

Functional and Logic Programming, 2025

Due date: Tuesday, June 3rd, 2025 (03/06/2025)

Bureaucracy

- The staff member in charge of this assignment is Shmuel Hanoch(or.tzadik@post.runi.ac.il).
- Submission is in pairs, but solo submission is also allowed. We very much suggest you pair-up, as solving these exercises with another person greatly enhances your learning (as well as being more fun!).
- To submit, create a zip file named HW4_<id1>_<id2>.zip where <id1> and <id2> are the submitters' IDs.
 - Or HW4_<id>.zip if submitting alone.
 - You do not need special permission to submit alone.
- The zip file should contain two (2!), top-level files (no folders!) named HW4.hs and MultiSet.hs!
 - The contents of these files will be explained later.
- Make sure your submission compiles successfully. Submissions which do not compile will not receive a grade!
 - We will be using the following command to compile the file: ghc -Wall -Werror MultiSet.hs HW4.hs.
- You may submit the assignment after the due date even without approval (e.g., excluding reserve duty, serious illness, or other cases covered by the student administration).
 - You will be penalized **5 points for every late day**.
 - The **maximum** extension allowed by this is **3 days**.
- If you don't know how to implement some function, **do not remove it!** Use undefined in the implementation, otherwise your entire submission will fail compilation, which will also result in no grade.
 - This is especially true for the bonus section!

General notes

- The instructions for this exercise are split between this file and HW4.hs. This file offers a more high-level overview of the exercise, as well as offering a few hints and examples. The Haskell file details all the required functionality for this assignment.
- You may **not** modify the **import** statement at the top of the file, nor add new **imports**.

- N.B. HLS has the habit of adding **unnecessary imports** when it doesn't recognize an identifier, **so please double-check this before submitting!**
- If you are unsure what some function does, you can ask HLS or Hoogle.
- Hoogle also supports module lookups, e.g., Prelude.not.
- Do be aware, however, that some functions from the standard library are more general than
 what we have learned so far in class.
 - * And in some cases their definition may not be entirely clear just yet!
- The exercises within each section are defined in a linear fashion. That is, it is a good idea to use previously defined functions (either from the same section or ones before it). It is also a good idea to use functions you saw in class; some of them are already imported, and some of them you would have to define yourself.
 - Do not be alarmed by the large number of functions! Many of them are simple one-liners,
 and were designed to aid you in solving the more complex functions.
 - In general, you may define as many helper functions as you wish.
 - If you're feeling fancy, you might even implement some functions using later ones!
- Try to write elegant code, as taught in class. Use point-free style, η-reductions, and function composition to make your code shorter and more declarative. Although it is not *strictly required* in the homework assignments, elegant code *will* receive a higher grade in the test, so this is a good exercise. HLS and hlint can be very helpful in this.
 - Do note that in some cases, hlint may suggest functions which are not imported!
- If possible, please ask your questions first in Piazza, as this will allow all students to take part in the discussion.
- You can get a grade greater than 100 if you do the bonus!
 - Assuming you have a passing grade in both the homework and the exam, the final grade formula is:

$$0.7 \times \text{ExamGrade} + 0.3 \times \frac{\sum_{i=1}^{6} HW_i}{6} + \text{AttendanceBonus}$$

so a grade greater than 100 can increase your final grade (or help ensure you get a passing grade in the homework).

- Yes, you can also get bonus marks for the exam!
- The final grade is still capped at 100, unfortunately.

A note on testing

- The suggested way of testing yourselves is either via GHCi or using -- >>> comments, as taught
 in the tutorials.
- Although we do not cover unit tests in class, adventurous students can use the internet or even a generative AI to generate a template file for writing Haskell tests.
 - Personally, we recommend looking into <u>HUnit</u> (see the tutorial <u>here</u>), or a wrapper for HUnit called <u>Tasty</u>.
 - N.B. A very important part of programming in general is writing your own unit tests, so try not to offload too much work to your friendly neighborhood chatbot.

Section 1: Foldable Functions

In this section you will implement a few functions we saw for lists for Foldable, plus a few extra ones. Note that functions which can early exit—elem, null, etc.—should support it.

Here are example usages of the new functions:

```
getSum $ fold $ map Sum [1, 2, 3]
6
toList $ Just 4
[4]
toList $ Nothing
[]
-- Not part of HW4.hs.
-- You can take the implementation and instances from the lectures.
single a = Tree Empty a Empty
toList $ Tree (single 1) 2 (single 3)
[1,2,3]
maxBy length [ foo , bar , bazz ]
Just bazz
minBy length [ bar , bazz ]
Just bar
```

Hint: The Arg type from the previous homework can also be useful here (it is already pre-imported from Data.Semigroup).

Tip: Since you already saw how to implement a few of these using foldr, it is a very good exercise to implement them using foldMap!

Section 2: Composing folds

In this section, we'll implement a small utility library to ease the usage of folds. Suppose you want to implement the function average for a list of numbers. We already have implementations of sum and length, so we can define something like

```
average :: Fractional a => [a] -> a
average xs = sum xs / fromIntegral (length xs)
```

This implementation is nice and elegant, but not the most efficient one: since sum and length are both implement using fold, we'll need two folds, which are two different passes on the list. We could solve it by writing a clever implementation which traverse the list only once, but then it would not be as readable and nice. Ideally, we would want folding operations to be more composable, just like regular functions, in a way that is also efficiently implemented.

• To achieve this, we'll define the data type

```
data Fold a b c = Fold (b -> a -> b) b (b -> c )
```

This type represent a left fold operation from a list of a's to some c. It has a step function, an initial b value, and a 'finalize' function that takes the accumulator of type b and create the actual result from it, of type c.

- We'll use *Functor* and *Apply* instances as the way to combine *Folds* into more complex ons. Note that we only have an *Apply*, not the full *Applicative*: we can't have *pure* for this data type (why?).
- We'll also have a *Num* instance, which uses *Apply* to lift mathematical functions to *Folds*. Note: at this stage, we're only *describing* the fold operations, and combining descriptions into a larger fold description. We didn't 'computed' any fold yet.
- Finally we also need to 'execute' the fold operation. runFold will take a Fold, a foldable ta, and runs it as a strict left fold.
- Implement some basic Folds, to be used as building blocks: lengthF, sumF, nullF, toListF, findF and topKF.
- Now implement average F using above building blocks.

Note: This is a particular case of a powerful technique in functional programming, the idea of internal DSL's (domain specific languages). We seaprate the description of computations using a dedicated 'language', and finally 'compile' the language into an actual result.

Section 1: Section 3: Functor functions

In this section you will implement a few functions on Functors. Here are example usages of the new functions:

```
fmapToFst length [ foo , bar ]
  [(3, foo ) ,(3, bar )]
fmapToSnd length $ Just foo
  Just ( foo ,3)

strengthenL 42 $ Right foo
  Right (42, foo )
  strengthenR x [1, 2, 3]
  [(1, x) ,(2, x) ,(3, x)]
  unzip $ Just (1,2)
  (Just1, Just2)
  coUnzip (Right [1,2,3] :: Either String [Int])
  [Right 1,Right 2,Right 3]
  coUnzip (Left foo :: Either String [Int])
  [Left 'f',Left 'o',Left 'o']
```

Section 4: MultiSet Foldable Instances

In this section we'll implement additional instances for MultiSet from exercise 4.

- Implement a Foldable instance. The instance should respect multiplicity: if an element apear n times, it should particiant in the fold operation n times.
- Sometimes, it's also useful to fold over the unique set of the elements in the multiset. Define an additional foldableinstancewhichwillallowtodoso.
 - The instance should be define outside the *MultiSet* module. Use the *FoldOccur* wrapper to avoid an orphan instance.
 - Insances which define outside the module can use only the pubic *MultiSet API*. The API from exercise 4 does not contain an efficient way to traverse each element once, so will add one. Implement the new function *foldOccur*, and also use it in the unique instance of *Foldbale* implementation.

Section 2: Bonus: Ziplists (10 points)

implement a semigroup and monoid instance for ziplist, such that (<>) is applied as a dot product.

```
map getsum $ getziplist $ ziplist (map sum [1, 2, 3]) <> ziplist (map sum [4, 5])
[5,7]
take 5 $ map getproduct $ getziplist $
    ziplist (map product [1..]) <> ziplist (map product [0..])
[0,2,6,12,20]
```

note: remember the monoid laws: mempty <> a == a and a <> mempty == a for all a (including infinite lists)! what would be the correct implementation of mempty for ziplists?