Problem Set for Week 8

The work handed in should be entirely your own. You can consult Stewart and/or the class notes but nothing else. To receive full credit, justify your answer in a clear and logical way. Due March 25.

Reading. This is the most important part of the homework: Read Sections 16.3–16.4 of the textbook carefully. Since we'll be having the second midterm soon after the Spring break, it is a good idea to start reviewing what we have covered from Chapter 15.

- 1. Section 16.4 Exercises 2, 10, 14, 21, 27.
- 2. Evaluate the integral $\int_C \mathbf{F} \cdot d\mathbf{r}$. Here \mathbf{F} is the field

$$\mathbf{F} = (\sin(x^2) + y)\mathbf{i} + (xy^2 + y^4)\mathbf{j},$$

and the curve C goes from (0,-1) to (0,1) along the parabola $x=1-y^2$.

3. Evaluate the integral $\oint_C \mathbf{F} \cdot d\mathbf{r}$ Here \mathbf{F} is the field

$$\mathbf{F} = \frac{-y}{x^2 + y^2}\mathbf{i} + (\frac{x}{x^2 + y^2} + x)\mathbf{j}.$$

The closed curve C goes from (-4, -12) to (4, -12) on a straight line, then back to (-4, -12) along the parabola $y = 4 - x^2$. Note that \mathbf{F} is not defined at the origin.