Exercises for Week 7

The work handed in should be entirely your own. You can consult the textbook and/or the class notes but nothing else. To receive full credit, justify your answer in a clear and logical way. Due Oct. 27th.

Reading. Read Sections 3.2–3.4 of the textbook carefully.

- 1. Section 3.1 Exercise 1, 2, 5
- 2. Section 3.2 Exercise 1, 2 (a) (d) (e), 3, 5 (b), (c), (f), 7, 15, 18, 21.
- 3. Section 3.3 Exercise 1, 2 (a) (c) (e), 5, 6, 8
- 4. Prove the following statement.

In class, we discussed the rank of post-composing with an isomorphism. In this exercise, show that the nullity doesn't change either by precomposing with an isomorphism.

Let $T:U\longrightarrow V$ be a linear map over $\mathbb F$ and $S:U'\longrightarrow U$ be an isomorphism. Show that S restricts to an isomorphism

$$S: \operatorname{Ker}(T \circ S) \longrightarrow \operatorname{Ker}(T).$$

In particular, $n(T) = n(T \circ S)$.

5. Section 3.4 Exercise 1, 2 (a) (d) (h), 3