

## Math 185 Quiz 2

Don't forget to write down clearly your **Name**:

and **ID number**:

**1. True or False (10 points).** Mark “T” (True) in front of a correct statement and “F” (False) in front of a wrong one.

\_\_\_\_\_ The complex function  $f(z) = z^3 + 2\bar{z}$  is complex analytic on all  $\mathbb{C}$ .

\_\_\_\_\_ If  $f(z), g(z)$  are complex analytic on a domain  $D$ , so is their product  $f(z)g(z)$ .

\_\_\_\_\_ The function  $f(z) = e^z$  has its real part a two-variable harmonic function.

\_\_\_\_\_ The function  $f(z) = z^3$  is conformal at  $z = 0$ .

\_\_\_\_\_ A harmonic function  $u(x, y)$  on any domain  $D$  has a harmonic conjugate  $v(x, y)$ .

**2. Harmonic functions (5 points).** Prove that  $u(x, y) = x/(x^2 + y^2)$  is harmonic.

**3. Integration of one-forms (5 points).** Integrate the 1-form along the positively oriented unit circle in your favorite way:

$$\oint_{\partial D} x^2 dy,$$

where  $D = \{(x, y) | x^2 + y^2 \leq 1\}$ .