

Optimised Cost Considering Huffman Code for Biological Data Compression

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Abstract

Classical Huffman code has widely been used to compress biological datasets. Though a considerable reduction of size of data is obtained by classical Huffman code, yet, more efficient encoding is possible by treating binary bits differently considering requirement of transmission time, energy consumption, and likewise. A number of techniques already modified Huffman code algorithm to obtain optimal prefix-codes for unequal letter costs in order to reduce overall transmission cost (time). In this paper we propose a new approach to improve compression performance of one such extension, cost considering approach (CCA), by applying genetic algorithm for optimal allocation of the codewords to the symbols. The approach start with generating a set of codewords for different input symbols based on their frequencies by considering cost (length) of 0 and 1 as α and β , $\alpha < \beta$. This step ensures optimal cost encoding, however, compression performance is not higher than classical Huffman code. The idea is to sacrifice some cost to minimise total number of bits, hence, the genetic algorithm works by giving penalty on cost. The performance of the approach is evaluated by applying it to compress some standard biological datasets and comparing the result with the results produced by classical Huffman code and cost considering Huffman code.

Keywords: Data Compression, Huffman code, Cost Considering, Genetic

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1. Introduction

In the recent years, application of battery-powered portable devices, e.g. laptop computers and mobile phones has increased significantly. Proper representation of digital data and their transmission efficiency has become a primary concern for digital community because it affects the performance, reliability, and the cost of computation in both portable and non-portable devices. CMOS technologies were developed in order to reduce the power consumption both in data processing and transmission. In order to increase transmission speed and reduce transmission cost, parallel data transmission methods are widely used. However, parallel transmission is limited to short distance communications, e.g. locally connected devices, internal buses. Ruling out the possible availability of parallel transmission links over long distance, we are left with its serial alternative only. If we attempt to transfer big files, e.g. DNA sequences, over a serial transmission link then it would take a significant amount of time. However, we cannot overlook this problem because at present parallel processing is widely used to increase throughput and in parallel processing architecture, processing units are usually distributed in different physical locations and task sharing is a must in such architecture. . Data encoding techniques came into action to improve the data transmission efficiency over serial communication medium by compressing data before transmitting. Efficiency can be measured in terms of incurred cost, required storage space, consumed power, time spent and likewise. Data must be encoded to meet the purposes like: unambiguous retrieval of information, efficient storage, efficient transmission and etc. Let a message consist of sequences of characters taken from an alphabet Σ , where $\delta_1, \delta_2, \delta_3 \dots, \delta_r$ are the elements that represent the characters in the source Σ . The length of δ_i represents its cost or transmission time, i.e., $cost(\delta_i) = length(\delta_i)$. A codeword w_i is a string of characters in Σ , i.e., $w_i \in \Sigma^+$. If a codeword is $w_i = \delta_{i1}, \delta_{i2}, \dots, \delta_{in}$, then the length or cost of the codeword is the sum of the lengths of its constituent elements:

$$cost(w_i) = \sum_{j=1}^n cost(\delta_{ij}) \quad (1)$$

If all the elements of a codeword has unit cost or length then the cost

of the codeword is equivalent to the length of the codeword. However, it is not necessary for the elements in the codeword to have equal length or cost. For example, in Morse Code all the ASCII characters are encoded as sequence of dots (\cdot) and dashes ($-$) where a dash is three times longer than a dot in duration [1]. However, the Morse code scheme suffers from the prefix problem [2]. Ignoring the prefix problem, Morse code results in a tremendous savings of bits over ASCII representation. Using Morse code, we can treat the binary bits differently; 0 as a dot and 1 as a dash. Even if we consider the voltage level to represent the binary digits then they are still different. Table 1 shows the logic level to represent binary digits in CMOS and TTL technologies.

Table 1: Example of binary logic level

Technology	0	1	Notes
CMOS	0 V to $\frac{V_{DD}}{2}$	$\frac{V_{DD}}{2}$ to V_{DD}	V_{DD} = supply voltage
TTL	0 V to 0.8 V	2 V to V_{CC}	V_{CC} is 4.75 V to 5.25 V

As the unequal letter cost problem is not new therefore it has been addressed by different researchers. The more general case where the costs of the letters as well as the probabilities of the words are arbitrarily specified was treated in [3]. A number of other researchers have focused on uniform sources and developed algorithm for the unequal letter costs encoding [4, 5, 6, 7, 8]. Let p_1, p_2, \dots, p_n be the probabilities with which the source symbols occur in a message and the codewords representing the source symbols are w_1, w_2, \dots, w_n then the cost of the code W is:

$$C(W) = \sum_{i=1}^n \text{cost}(w_i) \cdot p_i \quad (2)$$

The aim of producing an optimal code with unequal letter cost is to find a codeword W that consists of n prefix code letters each with minimum cost c_i that produces the overall minimum cost $C(W)$, given that costs $0 < c_1 \leq c_2 \leq c_3 \leq \dots \leq c_n$, and probabilities $p_1 \geq p_2 \geq \dots \geq p_n > 0$.

Huffman code[9] is an efficient data compression scheme that takes into account the probabilities at which different quantization levels are likely to occur and results in fewer data bits on the average. It is widely used to

compress biological data, however, all the techniques use the classical form of the Huffman code where bits are treated equally. Out of many variations of the Huffman code where cost of bits are treated unequally, the most recent approach is described in [10]. This approach treated binary bit 0 as a dot (·) and 1 as a dash (—) like Morse code and reduces the transmission cost (time) significantly. Like other variations of the cost considering Huffman code, the compression performance (in terms of number of bits require to encode a message) of this approach is not also better than classical Huffman code. In this paper, we have proposed a new optimised cost considering Huffman code based on the approach shown in [10]. This new approach optimised the number of bits require to encode biological datasets while treating the binary bits unequally. The codewords generated by the approach described in[10] only considers cost reduction but ignores bits reduction therefore number of total bits are considerably high. The proposed approach aims at reducing total number of bits by applying a genetic algorithm. The algorithm works by giving penalty on cost to reduce number of bits, but also ensures that the overall cost is lower than classical Huffman code. The efficiency of the method is evaluated by applying it to compress some standard biological datasets.

The rest of the paper is organised as follows: Section 2 presents the background study of the issues in biological data processing and the Huffman code. The proposed approach is described in Section 3. Experimental results and discussion are presented in Section 4 . Finally, concluding remarks are presented in Section 5.

2. Background

2.1. Issues on Biological Data Transmission

The size of biological data including DNA sequences increase with an ever expanding rate and will be bigger and bigger in the future. These biological data are stored in biology databases. The exponential growth of these databases become a big problem to all biological data processing methods [11]. Different operations are applied to these data such as searching [12], e-mail attachment [13], alignment [14], and transmission on distributed computing platform [15]. Interestingly, biological data compression can play a key role in all sort of biological data processing.

A recent deluge of interest in the development of new tools for biological data processing requires efficient methods for data compression. The

main objective of data compression methods is minimising the number of bits in the data representation. In [16], authors proposed a new general data structure and data encoding approach for the efficient storage of genomic data. This method encodes only the differences between a genome sequence and a reference sequence. For encoding, the method uses different fixed-length encoding schemes such as Golomb[17], Elias codes[18] and variable codes such as Huffman codes. There are other methods based on the same idea of encoding only the difference between reference sequence and the target one. One such approach [13] uses Huffman code for encoding difference between sequences to sent it as an email attachment. The main limitation of this method is that it must send the reference sequence for at least once for each species, and usually this sequence is too big to be sent as an email attachment. Wang and Zhang [19] proposed a new scheme for referential compression of genomes based on the chromosome level. The algorithm searches for longest common subsequence between two sequences and then the differences between them are encoded using Huffman code. All previous studies focus only on the differences and the relation between continuation of the sequence, and use existing encoding approaches to encode biological datasets without considering possible improvement of the encoding schemes.

2.2. *Huffman Codes*

In computer science and information theory, Huffman code is an entropy encoding algorithm used for lossless data compression. It takes into account the probabilities at which different symbols are likely to occur and results into fewer data bits on the average. For any given set of symbols and associated occurrence probabilities, there is an optimal encoding rule that minimises the number of bits needed to represent the source. Encoding symbols in predefined fixed length code, does not attain an optimum performance, because every character consumes equal number of bits irrespective to their degree of contribution to the whole data. Huffman code tackles this by generating variable length codes, given a probability usage frequency for a set of symbols. It generates prefix-code to facilitate unambiguous retrieval of information. A scheme of prefix code assigns codes to letters in Σ to form codeword w_i such that none of them is a prefix to another. For example, the codes $\{1, 01, 001, 0001\}$ and $\{000, 001, 011, 111\}$ are prefix-free, whereas the code $\{1, 01, 100\}$ is not, because 1 is a prefix in 100.

Applications of Huffman code are pervasive throughout computer science. The algorithm to completely perform Huffman encoding and decoding is ex-

plained in [20]. It can be used effectively where there is a need for a compact code to represent a long series of a relatively small number of distinct bytes. For example, Table 1 shows 8 different ASCII characters, their frequencies, ASCII codes and the codewords generated for those symbols using Huffman code. It is seen from the table that the codeword to represent each character is compressed and the most frequent character gets the shortest code. In this example, the compression ratio obtained by Huffman code is 64.16%.

Table 2: Example of application of Huffman Code to compress ASCII characters

Symbols	Frequency	ASCII Code	Codewords using Huffman Code
A	50	01000001	00
B	35	01000010	101
C	42	01000011	110
D	22	01000100	1001
E	65	01000101	01
F	25	01000110	1111
G	9	01000111	1000
H	23	01001000	1110

There are many other variants of Huffman codes that compress source data to reduce data size and/or transmission cost. For example, Mannan and Kaykobad[21] introduced block technique in Huffman coding which overcomes the limitation of reading whole message prior to encoding. In the classical Huffman coding scheme, the letter costs are considered as equal. The unequal letter cost versions of Huffman codes scheme are proposed in [22, 23, 24, 25]. In these versions, letters of the alphabet are treated unequally. Recently, in [10] a method is proposed to show the effects of unequal bits cost on classical Huffman code. The idea of this method is to assign the most frequent symbol the minimum cost code and the least frequent symbol the maximum cost code, whereas classical Huffman code assigns most frequent symbol the minimum length code and the least frequent symbol the maximum length code. As a result, the approach in [10] produces an optimal prefix-codes for unequal letter cost, thus reduces the overall (transmission) cost of the encoded data.

3. Approach

3.1. Proposed Scheme

A genome is a stretch of DNA that encodes a polypeptide (protein) which is a set of amino acids bound together in a specific order. Each genomic sequence consists of nucleotides bound together, which are interpreted by the cellular machinery in groups of three, called triplets [26]. This is the main reason to divide the whole sequence in a set of triplet and give a code to each triplet. As each DNA sequence contains a combination of four nucleobases—guanine (G), adenine (A), thymine (T), and cytosine (C), therefore we will have $4^3 = 64$ possible triplets. The first step in the optimised cost considering algorithm is cutting the genome sequence in triplets, then compute the frequency of each triplet in the whole sequence. This table of frequencies are used by the cost considering Huffman code to generate minimal cost code for each triplet (frequency). Finally, these codes with frequencies are used by the optimised cost considering algorithm to generate the optimal allocation with a given penalty on cost. The whole process is shown in Fig.1.

3.2. Cost Considering Huffman code

The classical Huffman algorithm aims at reducing total number of bits and it constructs a tree in a bottom up fashion. It is shown in [27] that if the costs of letters are considered unequal then the straightforward bottom up greedy approach does not work. Authors in [10] uses a top down approach to build a binary tree considering unequal letter cost of bits. They considered cost (length) of 0 and 1 as integer constants α and β , $\alpha < \beta$. Using the analogy of Morse code's '.' and '-', the value of α and β is set as 1 and 3 respectively. The complete algorithm to obtain an optimal prefix-free code for unequal letter cost is shown below. The input to the algorithm are the distinct triplets contained in the genome sequence to be encoded and their frequencies. The process of creating the binary tree starts with a single node (root node) and it is initialised with cost 0. After that, two child (leaf) nodes are created for the root node, i.e., level of the tree is increased by one. Cost of the left child is calculated as the summation of the cost of its parent node and the length of the left arc, and cost of the right child is calculated as the summation of the cost of its parent node and the length of the right arc. Length of left and right arcs are actually the cost (length) of 0 (α) and 1 (β) respectively. The next step is to take a child node with least cost and create two child nodes for it and make it a parent node. In this way, in every

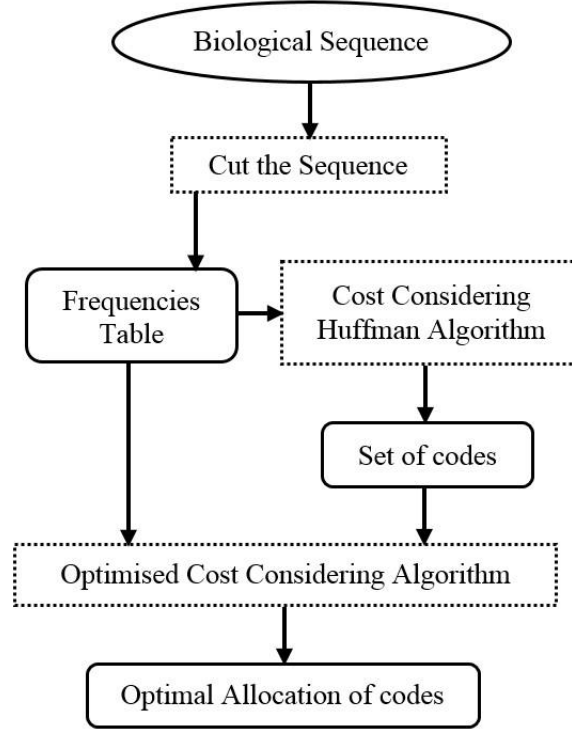


Figure 1: The proposed scheme

iteration the child node with least cost becomes a parent node with two new child nodes. Creation of new child nodes is stopped when total number of child nodes become equal to the number of distinct triplets needed to be encoded.

Now the tree T is constructed and the cost of the tree actually depends on how the frequencies are assigned to the leaf nodes. The overall cost will be minimised if the leaves with highest cost always have smaller or equal weight (frequency). To fulfil this condition the leaves of the T are enumerated in non-decreasing order of their cost, i.e., $cost(l_1) \leq cost(l_2) \leq \dots \leq cost(l_n)$, and that $f_1 \geq f_2 \geq \dots \geq f_n$, where l_i and f_i are leaf nodes and frequencies of distinct triplets respectively for $i = 1, 2, \dots, n$. The frequency or weight of parent nodes are calculated as the sum of the frequencies of its child nodes, and it continues upwards until the root node is reached. After that, the algorithm checks for any possible conflicts between all pair of nodes. Two

nodes are considered as conflicted if the node with a higher cost has higher frequency violating the above condition, i.e., if $cost(l_i) > cost(l_j)$ and $f(l_i) > f(l_j)$, then there remains a conflict. If there remains a conflict between nodes, then it is resolved by swapping the nodes and recalculating the cost of the tree downward and frequency of the nodes upward. When all the conflicts if existed are resolved then the algorithm generates codes for each of the distinct triplets.

3.3. Optimisation of the Codes

3.3.1. Problem formulation

The problem of finding the best allocation of codes to each triplet can be modelled as an assignment problems, the problem is formulated as follows :

Definition: Given a set of codes $C = \{C_1, C_2 \dots C_n\}$, and a set of frequencies $F = \{F_1, F_2 \dots F_n\}$. For each code we have the length of the code $|C_i|$ (number of bits) and the cost of the code S_{C_i} , the objective is to assign to each frequency a code in order to minimise the total number of bits, while respecting the initially assigned total cost S_t with a given penalty $\lambda \rightarrow [0, 1]$. This penalty coefficient represents the allowed amount of cost that can be sacrificed to optimise the total number of bits.

The Objective Function is to:

$$\text{Minimise } \sum (|C_i| \times F_j) \quad (3)$$

while :

$$\sum (|S_{C_i}| \times F_j) \leq (\lambda + 1)S_t \quad (4)$$

3.3.2. Basic Genetic Algorithm

Genetic Algorithm (GA) is a bio-inspired meta-heuristic algorithm developed by [28]. GA is a stochastic optimisation algorithm imitate the natural evolution process of genomes. GA started by generating an initial population of random feasible solutions. The optimisation process of GA takes the initial population and generates a new population based on it. The process can be described as follow:

Firstly, select two or more solutions from the current population by using one of the well-known selection techniques [29]. These selected solutions will be considered as parents. The second operation of the genetic algorithm is

Algorithm 1 Cost-considering / Unequal bit cost Coding

Require: Distinct symbols contained in the message to be encoded and their frequencies

Ensure: Non-uniform / variable letter cost i.e, Cost-considering balanced tree

```
1: for each distinct symbol  $i$  do
2:    $Enqueue(max\_Q, frequency [ i ])$ 
3: end for
4: create a root node
5:  $cost [ root ] \leftarrow 0$ 
6:  $Enqueue(min\_Q, cost [ root ])$ 
7: Define costs of the left and right child of the binary tree
8: repeat
9:    $cost\_of\_parent\_node \leftarrow Dequeue(min\_Q)$ 
10:  create  $left$  and  $right$  child for this node
11:   $cost [ left\_child ] \leftarrow cost\_of\_parent\_node + left\_child\_cost$ 
12:   $Enqueue(min\_Q, cost [ left\_child ])$ 
13:   $cost [ right\_child ] \leftarrow cost\_of\_parent\_node + right\_child\_cost$ 
14:   $Enqueue(min\_Q, cost [ right\_child ])$ 
15:  Mark parent node as explored
16: until  $2(n - 1)$  nodes are created
17: while  $min\_Q \neq \emptyset$  do
18:    $leaf\_node \leftarrow Dequeue(min\_Q)$ 
19:    $frequency[leaf\_node] \leftarrow Dequeue(max\_Q)$ 
20: end while
21: for each parent node  $j$  do
22:    $frequency [ j ] \leftarrow frequency [ left\_child ] + frequency [ right\_child ]$ 
23: end for
24: repeat
25:   if conflict between nodes then
26:     resolve conflict by swapping conflicted nodes
27:     calculate and reassign cost of all affected nodes
28:     calculate and reassign frequency of all affected nodes
29:   end if
30: until all conflicts are resolved
```

the crossover, which takes these parents as inputs to generate other new solutions considered as children. The third operation of the genetic algorithm is the mutation which ensures a good diversification in the search process. The new solutions can be mutated according to a given mutation probability. The mutation operation changes the value of one or more positions in the solution. The quality of each solution is verified by the fitness function which controls the evolution of the GA population by deletion of the worst solutions and insertion of the good solutions among parents and sons. This process is repeated until the stopped criteria is reached which can be the number of generation or if the population is stabilised.

3.3.3. GA for Bits minimisation

The main objective of the GA optimisation algorithm for bits minimisation (GaBm) is to assign each frequency a specific code. The encoding of an optimisation problem solution into a chromosome is one of the most important issues to obtaining good optimisation results. The GaBm uses two fixed length arrays of size “64” which is the number of combinations for all nucleotides. The first array contains the frequencies of each triplets and the second array contains the cost of the codewords assigned to each triplets. In this way, our genetic algorithm will work with the two arrays and uses the entry index on the allocation process. The genetic algorithms are stochastic algorithms based on random evolution. Generally the initial population is generated in a random affectation. In the GaBm algorithm, the population contains firstly the affectation given by the cost considering Huffman code algorithm and secondly the rest of the population are randomly generated, but all generated solutions must satisfy the initial cost constraints (step 1). The evolution of the population is the key of the optimisation algorithm. During each generation the process starts with the selection of a proportion of the population to breed a new generation. In the literature many selection methods have been proposed to guide the population evolution [29]. The existent selection methods are varied from a random selection to heuristic based selection. We have chosen to select randomly the part of the population to be processed, as the heuristic methods are very time-consuming (step 3). After that the operations of genetic algorithms are applied on the initial population to generate a new generation of the population (see figure 2). Firstly the crossover operation is applied to these two selected solutions (considered as parents) to generate two new solutions (considered as sons) (step 4). In the literature many crossover techniques have been used in

genetic algorithm [30], such as one-point crossover which divide the chromosome into two fragments and recombine the second fragments with the other chromosome's second fragment, two-point crossover which divide the chromosome into three fragments and recombine the middle fragment with the middle fragments of the other chromosome. There are many other crossover techniques to allow a good convergence of the algorithm. In our case, we have used the two point crossover with two parameters, the first parameter α is a random value in $[0,63]$, which represent the first cut point and β is a random value too in $[0,63]$, which represent the number of position to be crossed. We used two random parameters to ensure a good diversification on the whole search space (step 4). These two new generated children may contain conflict like finding a duplicated code allocated to two different frequencies in the solution, so a regulation step is done to ensure the correctness of the solution (see figure 2). Secondly these two new solutions are mutated according to a predefined probability γ , the best value of mutation rate is very problem specific (step 5). The value of γ is fixed to 0.2 to explorer a few position on the solution. The mutation operator used to maintain genetic diversity from one generation of a population of genetic algorithm chromosomes to the next. In our case, we have used the mutation as a random swap mutation operator (see figure 3). Each newly generated solution must satisfy the cost constraint, these children must be valid with satisfying the cost constraint. The next step is to add these two new solutions (children) to the population (step 7) (see figure 3). Finally the new population are ranked by fitness (step 8), and the worst solutions are deleted until the initial size of the population are achieved (step 9). The whole processes are repeated until the maximum number of operation is achieved (step 10).

4. Results And Discussion

The effectiveness of the approach has been evaluated with different real genomic biological data, these genomes were downloaded from a recent version of The National Center for Biotechnology Information (NCBI) available on ([http : //www.ncbi.nlm.nih.gov](http://www.ncbi.nlm.nih.gov)). We focused on the sequences alone, ignoring any header and any other exogenous information. In table 4 the different data sets are described with the size of each of them and the references on the biological data bank.

Table 4 presents the results obtained by the classical Huffman code, cost considering algorithm (CCA) and optimised cost considering algorithm

Table 3: Dataset description

Data sets	Name	Size (MB)	Reference
Genome 1	Mycobacterium smegmatis	6.66	CP009496
Genome 2	Amycolatopsis benzoatilytica	8.30	NZ_KB912942
Genome 3	Mycobacterium rhodesiae NBB3	6.11	CP003169
Genome 4	Streptomyces bottropensis ATCC 25435	8.54	NZ_KB911581
Genome 5	Mycobacterium smegmatis str. MC2 155	6.66	CP009494
Genome 6	Mycobacterium smegmatis MKD8	6.76	NZ_KI421511
Genome 7	Bradyrhizobium WSM471	7.42	NZ_CM001442
Genome 8	Amycolatopsis thermoflava N1165	8.27	NZ_CM001442
Genome 9	Bacillus thuringiensis Bt407	5.74	NZ_CM000747
Genome 10	Bacillus thuringiensis serovar thuringiensis	6.03	NZ_CM000748
Genome 11	Pseudomonas aeruginosa 9BR	6.48	NZ_AFXI01000001
Genome 12	Bacillus thuringiensis serovar berliner ATCC	5.97	NZ_CM000753
Genome 13	Bacillus thuringiensis serovar pakistani	5.75	NZ_CM000750
Genome 14	Pseudomonas aeruginosa LES400	6.28	CP006982
Genome 15	Mus musculus chromosome 1	25.58	GL456087
Genome 16	Danio rerio chromosome 1	56.14	CM002885
Genome 17	Homo sapiens chromosome 18	76.64	CM000680
Genome 18	Homo sapiens chromosome 22	74.92	CM000684

Algorithm 2 GA for bits minimisation

- 1: Population initialization (P).
 - 2: **repeat**
 - 3: Select two solutions S_1, S_2 form P.
 - 4: Crossover S_1, S_2 to generate S_{11}, S_{21} (Children).
 - 5: Mutate S_{11}, S_{21} .
 - 6: Validate children with cost constraint (equation 4).
 - 7: Add children to population
 - 8: Rank the population by fitness
 - 9: Remove worst candidates until population limit
 - 10: **until** Max number of generation not achieved
 - 11: Display the best solution from the population P;
-

(OCCA) without penalty on cost. The results show that the number of bits required by the classical Huffman algorithm to encode genomic data is the minimum among the other algorithms but the cost is maximum. The cost considering algorithm improve the representation of the generated codes in terms of cost but the number of bits. However, still it compresses the data by X% in the best case, Y% in the worst case, and Z% on an average. In terms of cost, in the best case the CCA improves cost over classical Huffman code by P%, in the worst case by Q%, and on an average by R%. The optimised cost considering algorithm tries to find the best allocation of codes to frequencies by giving penalty on cost. The outcome of this process is a fall in the total number of bits and a rise in the total cost. However, the cost is always lower than the cost incurred by the classical Huffman algorithm. At first, the OCCA optimises number of bits without applying any penalty on cost. Afterwards, it continues giving penalty on cost ranging from 1% to 10% until a balance is found between total cost and bits. For each genome, a maximum amount of effective penalty is identified, after this maximum value, increasing the penalty is not helping any more to reduce number of bits, i.e., number of bits reach to minimum and cost to maximum. The table 5 presents the best founded number of bits for different datasets with different effective penalty.

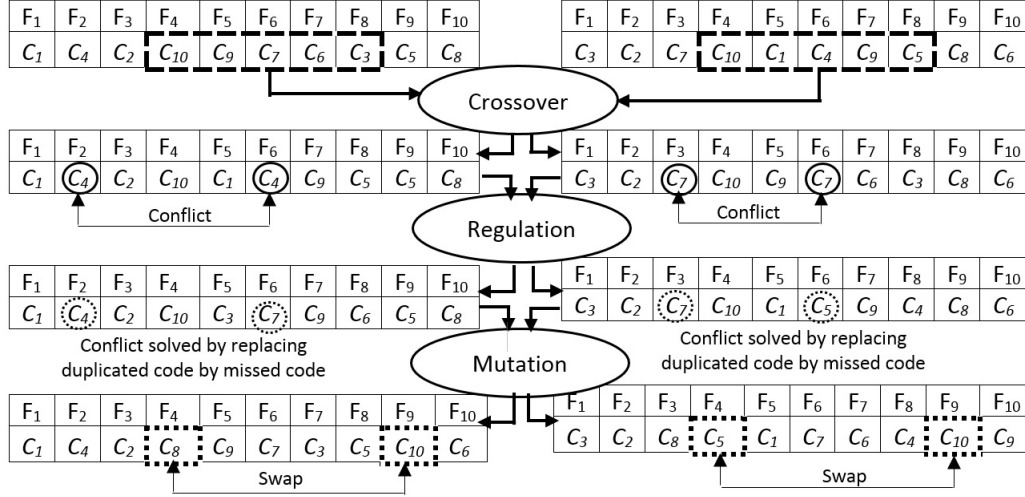


Figure 2: Operations of genetic algorithm

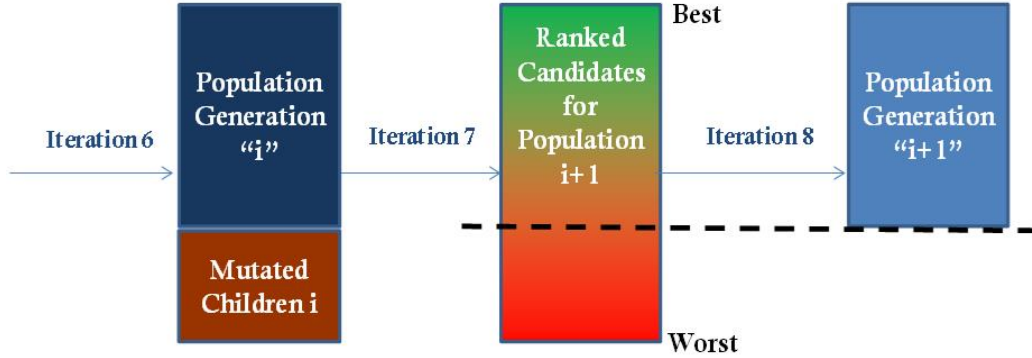


Figure 3: Population Update for genetic algorithm

5. Conclusion

In this paper we have proposed a new approach for efficient data compression using Huffman code and optimised strategy. The new approach is divided into phases, firstly a cost considering Huffman algorithm are proposed which reduce the cost of the generated codes, these codes are secondary passed by the optimisation algorithm to reduce the global number of bits us-

Table 4: GABM for comparison for cost and number of bits of different approaches with different datasets

Data sets	Huffman Algorithm		CCA		OCCA	
	Cost	Bits	Cost	Bits	Cost	Bits
Genome 1	76787151	4.44	67416213	4.92	67416213	4.82
Genome 2	100425402	5.81	88430665	6.51	88430665	6.35
Genome 3	75940155	4.39	66745619	4.87	66745619	4.79
Genome 4	103552729	5.96	90821835	6.69	90821835	6.47
Genome 5	82234926	4.74	71963876	5.27	71963876	5.17
Genome 6	83454842	4.81	73038795	5.34	73038795	5.24
Genome 7	92539488	5.36	81416359	5.93	81416359	5.85
Genome 8	99613856	5.74	87102639	6.41	87102639	6.30
Genome 9	71876739	4.15	62998800	4.58	62998800	5.50
Genome 10	75324432	4.36	66084958	4.81	66084958	4.73
Genome 11	80766360	4.66	70620666	5.41	70620666	5.04
Genome 12	74560825	4.31	65359604	4.75	65359604	4.67
Genome 13	71562941	4.14	62758225	4.56	62758225	4.50
Genome 14	78261299	4.51	68354090	4.8	68354090	4.89
Genome 15	324439242	18.77	286008420	20.66	288866525	19.94
Genome 16	703734840	40.77	618859291	45.08	625042576	43.18
Genome 17	901032667	52.08	791840455	57.36	799757406	55.12
Genome 18	983434816	56.98	867299889	62.42	875969422	60.70

ing a cost penalty.

The proposed approach is tested with biological genomic sequence and a performance comparison is made with the standard Huffman code and the cost considering without optimisation. Simulation results showed that the proposed approach is more robust and efficient compared to other competing algorithms because its penalty based optimisation strategy to search the best allocation of codes to different frequencies.

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- [2] P. D. Grunwald, P. M. B. Vitany, Kolmogorov complexity and infor-

Table 5: Influence of penalty on bit minimisation

Data sets	Cost	Bits	$\lambda(\%)$	Compression ratio %
Genome 1	70760174	4.50	4	32.72
Genome 2	92010490	5.91	3	28.79
Genome 3	69421783	4.47	3	26.84
Genome 4	96294638	5.99	5	29.85
Genome 5	74855668	4.81	5	27.77
Genome 6	76738330	4.86	4	28.10
Genome 7	84667949	5.47	3	26.28
Genome 8	92416243	5.76	5	30.35
Genome 9	66145783	4.21	4	26.65
Genome 10	68751359	4.44	3	26.63
Genome 11	72737300	4.79	2	26.08
Genome 12	67981988	4.38	3	26.63
Genome 13	65896779	4.18	4	27.30
Genome 14	71762305	4.55	4	27.54
Genome 15	297188002	19.31	3	24.51
Genome 16	643785655	41.68	3	25.75
Genome 17	823506882	53.05	3	30.78
Genome 18	901515198	58.99	3	21.26

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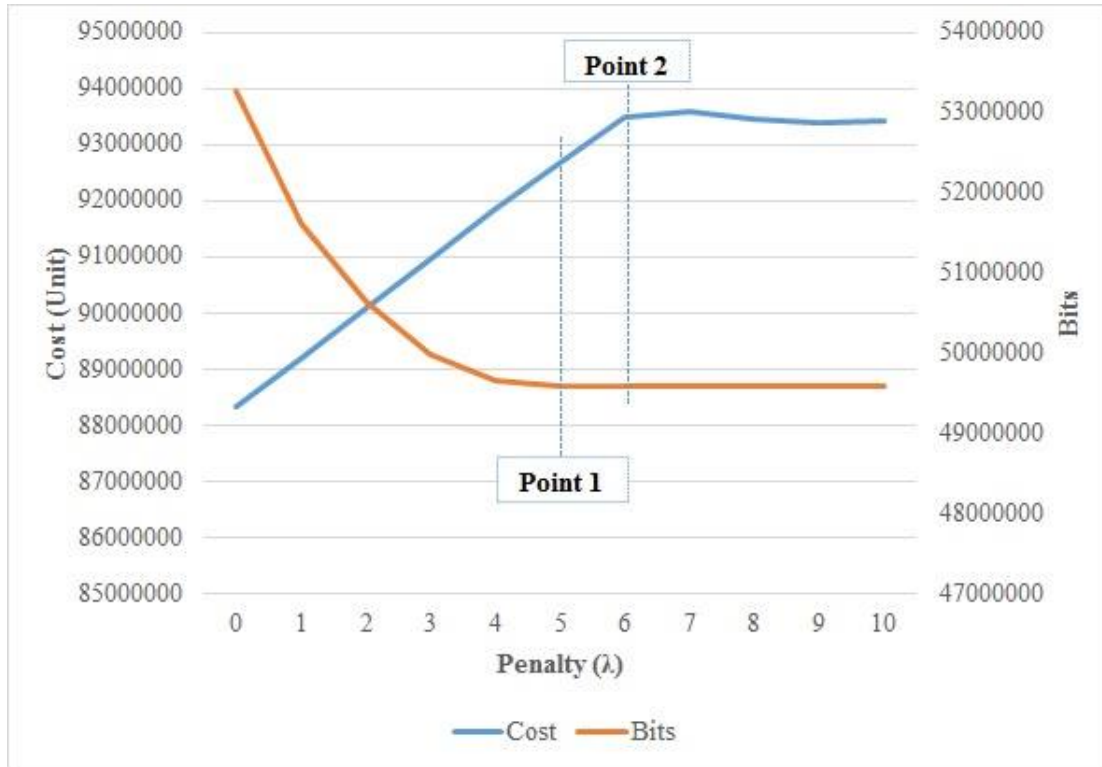


Figure 4: Convergence of Optimised cost considering Huffman algorithm

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