



Electronics and Electrical Communications Engineering Department

Faculty of Engineering

Cairo University

Implementation and Comparative Analysis of Huffman and Fano Source Coding Algorithms

ELC4020 "Advanced Communication Systems "

4th Year

1st Semester - Academic Year 2025/2026

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Role of Each Member 3.

ROLE **NAME**

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	Ahmed Wagdy
Report and Hand Analysis	Mohamed Ahmed
Report and Hand Analysis	Abdelrahman Eissa

4. Project Description

Using software (SDR) to transmit randomness bits channel (which small delay) using

هنا ممكن تشرحله انه source code implementqation using matlab radio technique stream of through an ideal performing a Matlab.

Performing measures and analysis to see the performance of the system through three main line codes (unipolar, polar nrz and polar rz).

5. Introduction

Software radio is a revolutionary approach that brings the programming code directly to the antenna, minimizing reliance on traditional radio hardware as shown in figure 1.

By doing so, it transforms challenges associated with radio hardware into software-

where

primarily

هنا ممکن تشرحله انه what's source coding and why it's important related issues. Unlike conventional radios, signal processing relies on analog circuitry

or a combination of analog and digital chips, software radio operates by having software dictate both the transmitted and received waveforms.

This paradigm shift allows for greater flexibility and adaptability in radio systems, as they can be easily reconfigured and optimized through software updates, rather than hardware modifications.

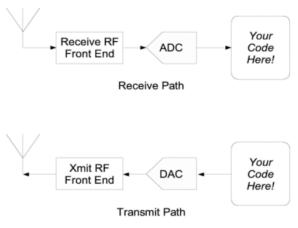


Figure 1 Rx and Tx path

6. Control Flags

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Flag	Value	Description
A	4	Amplitude of line code
N_realizations	500	Number of waveforms (ensemble size)

Communication Project

num_bits	101	Bits per waveform and one extra bit for shifting
bit_duration	70e-3	Duration of each bit
dac_interval	10e-3	DAC update interval

7. Input Data Symbols

Figure 2 Input Symbols

As seen in figure 2, this is the input given

8. Huffman Source Coding

8.1. Algorithm Overview_[2]

Step 1: Sort all the N_s symbols based on their probability in descending order(من الكبير للصغير).

Step 2: Crate a new colume has $(N_s - 1)$ by Sum the two symbols with the smallest probabilities.

Step 3: Repeat step 1 and 2 utill only two symbols remain.

Step 4: Assing codes for: the first as 0 and the second as 1.

Step 5: go step back to Left coalum and copy all non changed proabiltes codes as right colum (exept the lowst two in the left they alrady add in step 3), the chagned ones thier codes will be the same code of their summtion but zero is added in the least significant bit for the first and one for the second .

Figure 3 Huffman Algorithm

8.2. Hand Analysis

Symbol	P0	C0	P1	C1	P2	C2	P3	C3	P4	C4	P5	C5
A	0.35	00	0.35	00	0.35	00	0.35	00	0.35	1	0.65	0
В	0.3	01	0.3	01	0.3	01	0.3	01	0.35	00	0.35	1
C	0.2	10	0.2	10	0.2	10	0.2	10	0.3	01		
D	0.1	110	0.1	110	0.1	110	0.15	11				
E	0.04	1110	0.04	1110	0.05	111						
F	0.005	11110	0.01	1111								
G	0.005	11111										

So here's the output that we are aiming for.

With the Kraft's Sum, entropy, average length and efficiency:

$$H(P(x)) = -\sum_{xi} P(xi) \log_2 P(xi)$$
$$L(C) = -\sum_{xi} P(xi)L(xi)$$

$$\eta = \frac{H(P(x))}{L(C)} * 100\%$$

$$Kraft's Sum = \sum_{Li} 2^{-Li}$$

Kraft's Inequality: Kraft's Sum <= 1

So by calculating them we can find that:

$$\begin{split} H\big(P(x)\big) &= -\left(0.35\log_2 0.35 + 0.3\log_2 0.3 + 0.2\log_2 0.2 + 0.1\log_2 0.1 + 0.04\log_2 0.04 + 0.005\log_2 0.005 + 0.005\log_2 0.005\right) \\ &= 2.11 \ bits/symbol \end{split}$$

And

$$L(C) = 0.35 * 2 + 0.3 * 2 + 0.2 * 2 + 0.1 * 3 + 0.04 * 4 + 0.005 * 5 + 0.005 * 5$$

= 2.21 bits/symbol

So the overall efficiency is
$$\eta = \frac{L(C)}{H(P(x))} * 100\% = \frac{2.11}{2.21} * 100\% = 95.475\%$$

احسب هنا ال kraft اقله_, stratify

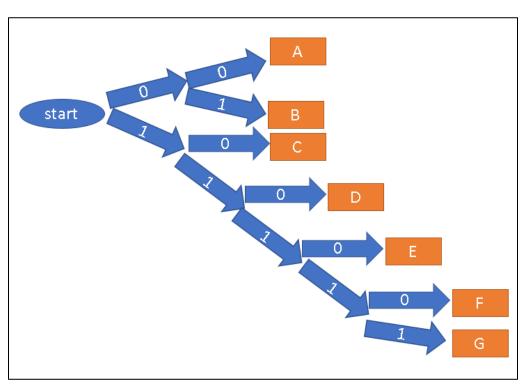


Figure 4 Huffman Output Kraft's Tree

As seen the kraft tree doesn't have a code in the internal not so it's Instantinous code

8.3. MatLab Implementation[3]

8.3.1. Calculations Functions

First we got the calculations Functions:

Figure 5 Entropy Calculation

And

```
Average Length Calculation
Function L = average_length_calc(dict)
$AVERAGE LENGTH CALC Compute average codeword length L(C)
 % L = average_length_calc(dict, P)
    dict: Huffman dictionary cell array {symbol, code}
    P: vector of symbol probabilities (same order as dict)
     If P is empty, it tries to extract from dict(:,2) if present
 % L : average code length
     % --- Compute code lengths ---
     code_lengths = cellfun(@length, codes);
     % --- Normalize probabilities ---
     P = P(:) / sum(P);
     % --- Check dimensions ---
     if length(P) ~= length(code_lengths)
         error('Number of probabilities does not match number of codewords.');
     end
     % --- Compute average code length ---
     L = sum(P .* code_lengths);
 end
```

Figure 6 Average length Calculation

And

```
%%

Efficiency Calculation
%

function eta = efficiency_calc(H, L)

%EFFICIENCY_CALC Compute Huffman coding efficiency n
% eta = efficiency_calc(H, L)
% H : entropy
% L : average code length
% eta : efficiency in percentage (%)

if L <= 0

error('Average length L must be positive.');
end

eta = (H / L) * 100;
end
```

Figure 7 Efficiency Calculation

And

```
Print Kraft Inequality Function
function [kraft_sum, kraft_flag]=kraft_analysis(dict)
□% KRAFT_ANALYSIS Compute Kraft's inequality and visualize Kraft tree
    kraft_analysis(dict)
 옦
     Input:
 용
         dict : cell array \{N \times 3\} \rightarrow \{symbol, P, code\}
 용
 용
    Example:
         dict = {'A','0'; 'B','10'; 'C','110'; 'D','111'};
 용
         kraft analysis(dict);
     % --- 1. Compute Kraft's inequality ---
     code_lengths = cellfun(@length, codes);
     kraft_sum = sum(2.^(-code_lengths));
     fprintf('\n=== Kraft Inequality Check ===\n');
     fprintf('Sum(2^{-1_i}) = %.4f\n', kraft_sum);
```

Figure 8 Kraft's Inequality

8.3.2. Getting input data

```
% Combine into dictionary-like cell array
dict_input = [symbols(:), num2cell(P(:))];
% Assume not great until great
err flag = 1;
% Validate using the check_symbols() function
[ok, msg] = check_symbols(dict_input);
% Display validation result
if ok
    disp('♥ Dictionary is valid!');
   err_flag =0;
else
    disp(['X Error: ' msg]);
    err_flag = 1;
end
% Compute entropy (only if valid)
H 💆 entropy_calc(P)
```

Figure 9 Input Validation

So the output is:

	Symbol	Probability
1	Α	0.3500
2	В	0.3000
3	С	0.2000
4	D	0.1000
5	E	0.0400
6	F	0.0050
7	G	0.0050

Figure 10 Input Symbols

8.3.3. Huffman Function

First we merged the last 2 probabilities to have in last just 2 probabilities

```
% --- Iteratively merge ---
for step = 2:numCols
    % Sort ascending to pick smallest two
    curP = sort(curP, 'ascend');
    if numel(curP) >= 2
        p1 = curP(1);
        p2 = curP(2);
        mergedP = p1 + p2;
        % Remove two smallest and add merged one
        curP = [mergedP; curP(3:end)];
    end
    % Sort descending for display
    curP = sort(curP, 'descend');
    % Fill current column
    for r = 1: maxRows
        if r <= numel(curP)</pre>
            history\{r, step\} = curP(r);
        else
            history\{r, step\} = NaN;
        end
    end
end
```

Figure 11 Probability Merge

So we got:

Step 1: Huffman Probability Merging Process								
P0	P1	P2	P3	P4	P5			
0.3500	0.3500	0.3500	0.3500	0.3500	0.6500			
0.3000	0.3000	0.3000	0.3000	0.3500	0.3500			
0.2000	0.2000	0.2000	0.2000	0.3000				
0.1000	0.1000	0.1000	0.1500					
0.0400	0.0400	0.0500						
0.0050	0.0100							
0.0050								

Figure 12 Merged Probabilities

s Then we assign the codes from last column to first

```
% === Assign child codes ===
% Last two rows in previous P column are merged into this parent
history_table_full{raw_counter, prevCcol} = [parentCode '0'];
history table full{raw counter+1, prevCcol} = [parentCode '1'];
% For each previous non-merged row (in display order top->bottom)
for ii = 1:(raw_counter-1)
    % Skip the rows that were just merged (raw_counter and raw_counter+1)
    % Get the probability value in the previous column for this row
   valPrev = history_table_full(ii, prevPcol);
    if isnan(valPrev)
        continue; % nothing to copy
    % Find matching value in the current column (exclude merged parent)
   currMatches = find(abs(currPvals - valPrev) < 1e-12);</pre>
    % Remove the matchIdx (the merged parent) if it appears
   currMatches(currMatches == matchIdx) = [];
    if isempty(currMatches)
        continue; % no corresponding match found
    end
    % If there are duplicates (two identical probabilities)
    if numel(currMatches) > 1
        % take both, and copy their codes to the two rows
        history table full(ii, prevCcol) = currCvals(currMatches(1));
        if (ii+1) <= numRows
            history_table_full{ii+1, prevCcol} = currCvals(currMatches(2));
        end
    else
        % single match - copy code directly
        history_table_full{ii, prevCcol} = currCvals{currMatches(1)};
```

Figure 13 Code Assignment

So the output is:

Huffman Encoding: Probability and Code Evolution (P/C Steps)											
P0	CO	P1	C1	P2	C2	P3	C3	P4	C4	P5	C5
0.3500	00	0.3500	00	0.3500	00	0.3500	00	0.3500	1	0.6500	0
0.3000	01	0.3000	01	0.3000	01	0.3000	01	0.3500	00	0.3500	1
0.2000	10	0.2000	10	0.2000	10	0.2000	10	0.3000	01		
0.1000	110	0.1000	110	0.1000	110	0.1500	11				
0.0400	1110	0.0400	1110	0.0500	111						
0.0050	11110	0.0100	1111								
0.0050	11111										

Figure 14 Huffman Steps

8.3.4. Theoretical Vs Practical

The results are:

1	Α		
,	[· ·	0.3500	00
_	В	0.3000	01
3	С	0.2000	10
4	D	0.1000	110
5	Е	0.0400	1110
6	F	0.0050	11110
7	G	0.0050	11111

Figure 15 Huffman Output

As theoretical

9. Fano Source Coding

حط هنا شوية معلومات عنه

9.1. Algorithm Overview[2]

Fano Code

Step 1: Split all proabiltes into Two Groups has nearly equal prabilities.

Step 2: Assign the first one as 0 and the second one as 1.

Step 3: In Each Group Repeat step 1.

Step 4:Repeat step 2 but in Assigning use the code be for last grouping and assign 0 or 1 in the least SB.

Step 5: Repeat 3&4 until each group contain on symbole.

Figure 16 Fano Algorithm

9.2. Hand Analysis

Symbol	P0	C0	P1	C1	P2	C2	Р3	C3	P4	C4	Final Code
В	0.3	0	0.3	01	0.3	01	0.3	01	0.3	01	11
C	0.2	Ü	0.2	00	0.2	00	0.2	00	0.2	00	01
A	0.35	1	0.35	11	0.35	11	0.35	11	0.35	11	00
D	0.1		0.1	10	0.04	101	0.04	101	0.04	101	1000
E	0.04		0.04	10	0.01	100	0.01	1000	0.01	1000	101
\mathbf{F}	0.005		0.005		0.005	100	0.005	1001	0.005	10010	10010
G	0.005		0.005		0.005		0.005	1001	0.005	10011	10011

So here's the output that we are aiming for.

With the Kraft's Sum, entropy, average length and efficiency:

احسب هنا كل الحاجات اللي انا كنت حاسبها عند هافمان زي: length.. kraft ماقله stratify

Kraft's tree:

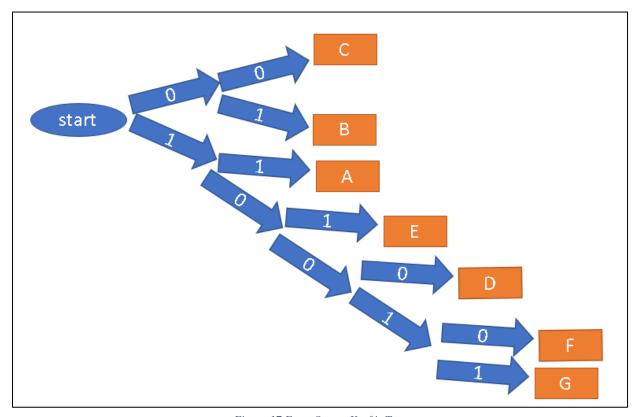


Figure 17 Fano Output Kraft's Tree

9.2.1. Fano Function

First we splitted the probabilities into groups

```
% === STEP 2: ITERATIVE FANO GROUPING ===
while ~isempty(groups)
   new_groups = {};
   for g = 1:length(groups)
        cur = groups(g);
        idxs = cur.idx;
        prefix = cur.prefix;
        % Skip if one symbol only
        if numel(idxs) <= 1</pre>
            continue;
        end
        pvals = probs(idxs);
        % --- Compute reference dynamically ---
        ref = 2^(-iteration);
        % --- Decide split method (COMBINATION-BASED) ---
        best_diff = inf;
        split_idx = [];
        n = length(pvals);
        for mask = 1:(2^n - 1)
            subset = bitget(mask, 1:n);
            subset_sum = sum(pvals(logical(subset)));
            diff = abs(subset sum - ref);
            if diff < best_diff</pre>
                best diff = diff;
                split_idx = find(subset);
            end
        end
```

Figure 18 Group Splitting

Then we assign the codes to each group

```
% --- Create two new groups ---
g1 = idxs(split_idx);
g2 = setdiff(idxs, idxs(split_idx));

% Assign '0' and '1' respectively
for k = g1
        codes(k) = [prefix '0'];
end
for k = g2
        codes(k) = [prefix '1'];
end
```

Figure 19 Group Code Assignment

So each group got a new code

So the output steps is

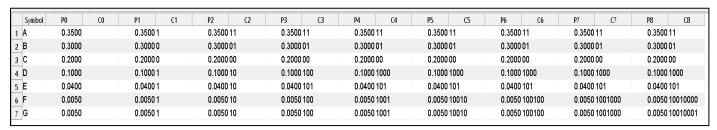


Figure 20 Fano Steps

9.2.2. Theoretical Vs Practical

The results are:

Sy	rmbol	Probability	Code
А		0.3500	11
В		0.3000	01
С		0.2000	00
D		0.1000	1000
E		0.0400	101
F		0.0050	10010000
G G		0.0050	10010001
		0.000	18018001

Figure 21 Fano Output

As theoretical

9.3. Is the Process Stationary

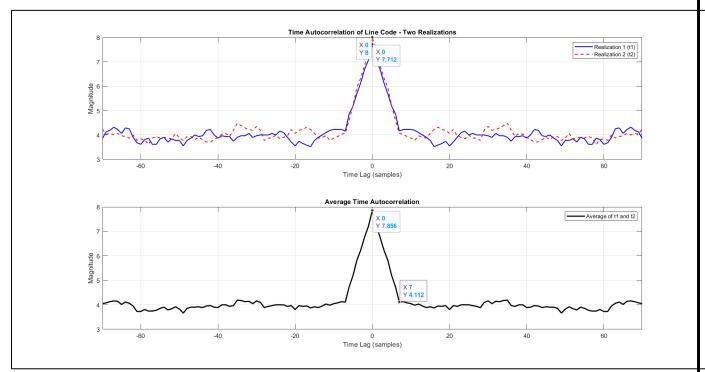


Figure 22 autocorrelation at two different times

- For the **mean**, as shown in section 1 figure 7 the **mean** \approx **constant** with time.
- For the **autocorrelation**, as shown in figure 9 the **autocorrelation** $R(t1=1) \approx R(t2=8)$.

Yes, the process is stationary (WSSP) because the mean is constant function in time as shown in **Error! Reference source not found.** and the autocorrelation depends only on the time difference not the absolute time.

9.4. The time mean and autocorrelation function for one waveform

9.4.1. Time Mean

• We add the values of a realization across time instant then divide by the number of samples (700 sample per realization).

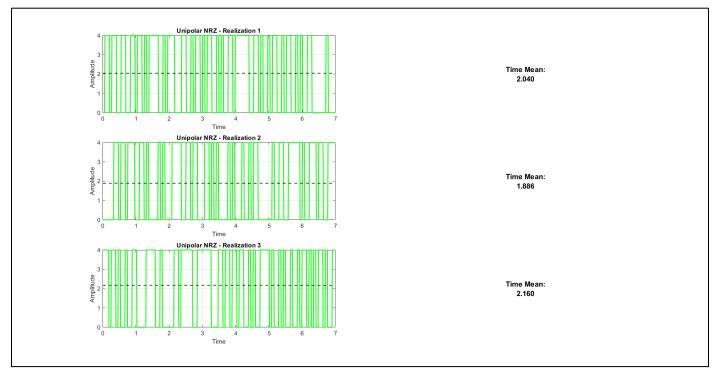


Figure 23 Time Mean for Uni Polar

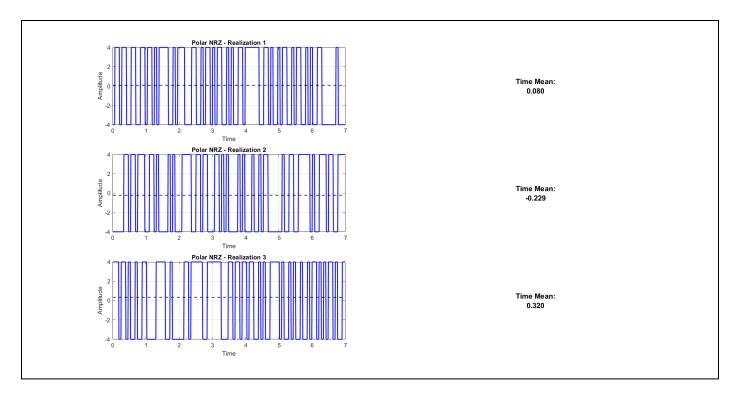


Figure 24 Time Mean for Polar NRZ

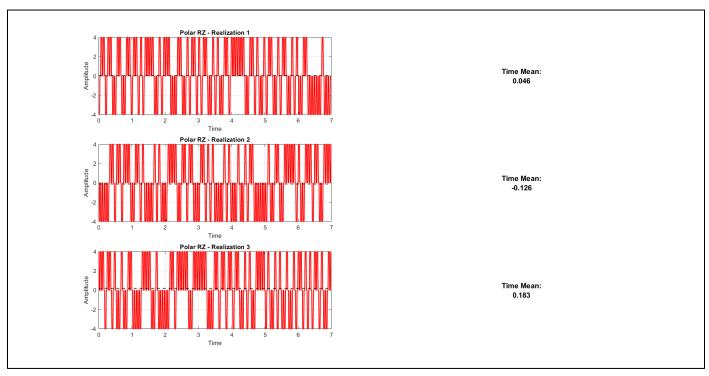


Figure 25 Time Mean for Polar RZ

• As expected, polar RZ & NRZ have almost zero mean and the uni polar has mean around 2 Because its amplitude ranges from 0:4

9.4.2. Time Mean Vs Realization

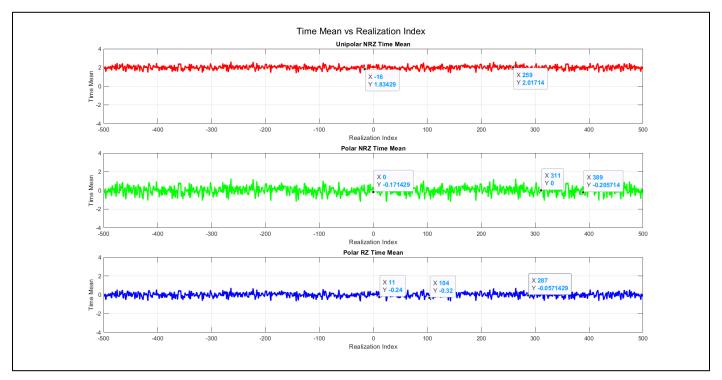


Figure 26 Time Mean Vs Realization

- As expected the time mean is almost equal to the statistical mean.
- Polar RZ & NRZ have almost zero mean and the uni polar has mean around 2.

9.4.3. Time Auto Correlation

For the time Auto Correlation we're going to use this function

```
function [R_unipolar_nrz_t1, R_polar_nrz_t1, R_polar_rz_t1, tau_vec] = ...
compute_time_autocorr(UnipolarNRZ, PolarNRZ, PolarRZ, t1) ...
```

```
% Preallocate
R_unipolar_nrz_t1 = zeros(1, length(tau_vec));
R polar nrz t1 = zeros(1, length(tau vec));
R_polar_rz_t1 = zeros(1, length(tau_vec));
for idx = 1:length(tau vec)
   tau = tau vec(idx);
   t2 = t1 + tau;
   % Compute element-wise products for all realizations at t1 and t1+tau
   prod_unipolar = UnipolarNRZ(:, t1) .* UnipolarNRZ(:, t2);
   prod_polar = PolarNRZ(:, t1) .* PolarNRZ(:, t2);
   prod_rz
                 = PolarRZ(:, t1)
                                    .* PolarRZ(:, t2);
    % Use custom function to compute mean across realizations
   R unipolar nrz t1(idx) = sum(prod unipolar) / num realizations;
   R_polar_nrz_t1(idx) = sum(prod_polar) / num_realizations;
   R polar rz t1(idx) = sum(prod rz) / num realizations;
end
```

• The time autocorrelation is calculated by $r_{xx} = \frac{1}{N} \sum_{n=0}^{N-1} x(n) x(n-k)$ of the first waveform.

9.4.4. Time Auto Correlation for one wave form:

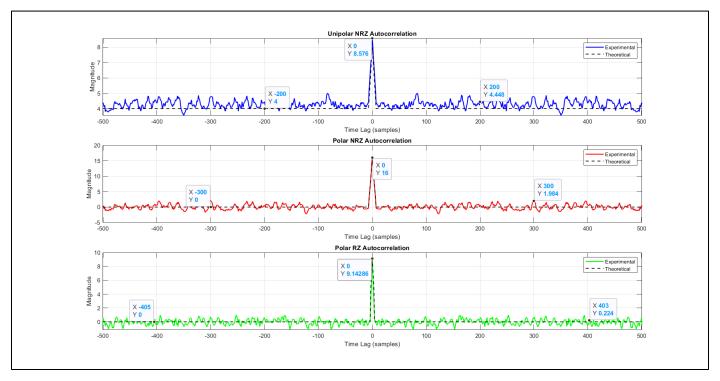


Figure 28 Time Auto Correction plot

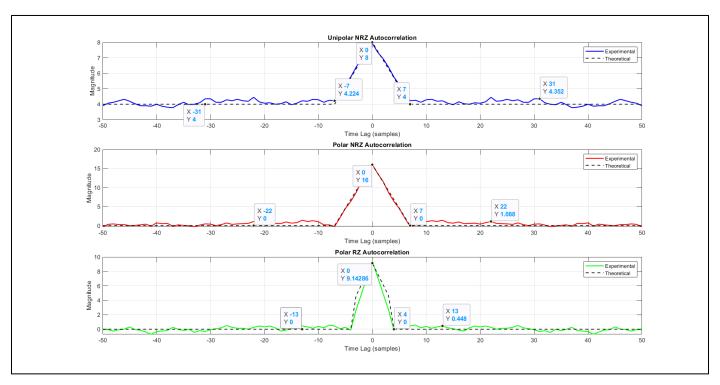


Figure 27 Time Auto Correction plot zoomed

As shown in the graphs:

- The time autocorrelation is closely same as the ensemble autocorrelation.
- The autocorrelation function has maximum at $\tau = 0$ and it is an even function.

9.5. Is The Random Process Ergodic?

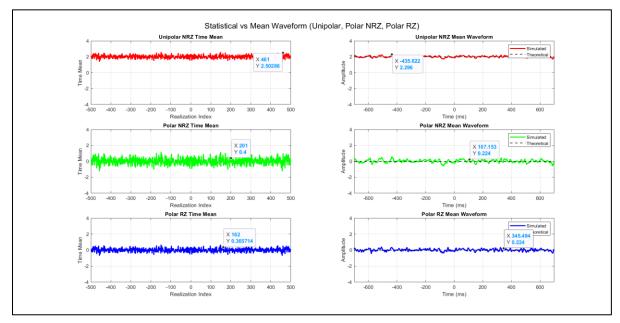


Figure 29 Time Mean vs Statistical

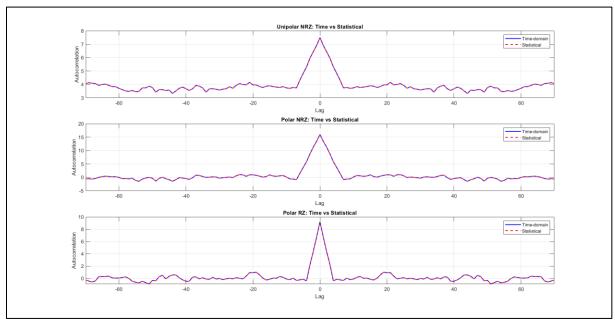


Figure 30 Time Auto Correlation Vs Statistical

- For the **mean**, the Time mean is almost equal to the statistical mean.
- For the **Auto Correlation**, the Time looks almost identical to the statistical. But, There not fully identical as we ran this code snippet

And the result was 0.5760, so they are almost Identical.

- Yes, because the time mean \approx the Statistical mean and the time autocorrelation is \approx the ensemble autocorrelation.
 - Then this process is ergodic

9.6. the PSD & Bandwidth of the Ensemble 9.6.1. PSD using fft:

For the **PSD**, we are going to use this function:

```
function [PSD_unipolar ,PSD_polarNRZ ,PSD_polarRZ] =...
plot_linecode_psd(R_Unipolar, R_PolarNRZ, R_PolarRZ, fs, A, Tb
```

```
% Compute FFTs of autocorrelations
fft_unipolar = fft(R_Unipolar) / n;
fft_polarNRZ = fft(R_PolarNRZ) / n;
fft_polarRZ = fft(R_PolarRZ) / n;

% Compute PSD magnitudes
PSD_unipolar = abs(fft_unipolar);
PSD_polarNRZ = abs(fft_polarNRZ);
PSD_polarRZ = abs(fft_polarRZ);

% Frequency axis centered around 0
freq_axis = (-n/2 : n/2 - 1) * (fs / n);

% Center the FFTs for proper plotting
PSD_unipolar = A*fftshift(PSD_unipolar);
PSD_polarNRZ = A*fftshift(PSD_polarNRZ);
PSD_polarRZ = A*fftshift(PSD_polarRZ);
```

- We take the Fourier transform of the avg time autocorrelation = 0.5*(R(t1)+R(t2)) then centralize the graph around zero.
- since $T_S = \frac{\text{Bit time}}{\text{no of samples per bit}} = \frac{70 \text{ ms}}{7} = 10 \text{ ms} \rightarrow F_S = 100$

For the BW

• the BW is the frequency of the first zero of sinc^2 function (intersection with frequency-axis)

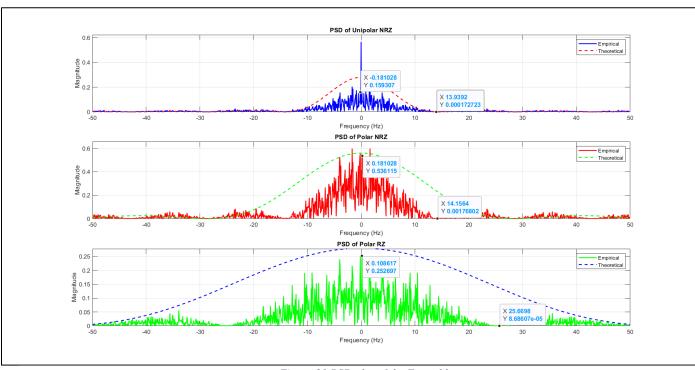


Figure 31 PSD plot of the Ensemble

Annotations

- in polar RZ & NRZ : we have sinc^2 function without delta at zero frequency (NO DC)
- in uni polar NRZ: we have sinc^2 function with delta at zero frequency (there is DC)
- BW of the unipolar NRZ & polar NRZ is the bitrate which approximately equal 14 hz
- BW of the polar RZ is the double of bitrate which approximately equal 25.66 hz

9.6.2. Theoritical PSD:

From $references_{[1], [2]}$, we found out that the PSDs are:

Line Code	PSD		
Uni Polar	$S(f)=A^2/4*Tb*(sin(\pi f T b)/\pi f T b)^2 + A^2/4*\delta(f)$		
Polar NRZ	$S(f)=A^{2}*Tb*(sin(\pi fTb/2)/\pi fTb/2)^{2}$		
Polar RZ	$S(f)=A^2*Tb*(\sin(\pi f Tb/4)/\pi f Tb/4)^2$		

Note that:

- Uni polar has a DC pulse which is noticeable in figure 19
- Polar don't have the DC pulse
- Polar RZ has double the frequency of Polar NRZ
- A=4, Tb = 70 ms

So by comparing the practical vs theoretical:

Line Code	Theoritcal PSD at f=0	Paractical PSD at f=0
Uni Polar	$A^2/4*Tb = 0.28$	0.159
Polar NRZ	$A^2/2*Tb = 0.56$	0.536
Polar RZ	$A^2/4*Tb = 0.28$	0.252

For **BW**:

Line Code	Theoritcal BW	Paractical BW
Uni Polar	1/Tb = 14.285 Hz	13.972 Hz
Polar NRZ	1/Tb = 14.285 Hz	14.15 Hz
Polar RZ	2/Tb = 28.57 Hz	25.66 Hz

10. References:

- [1] **Dr. Mohammed Nafie,** "Lecture Slides in Advanced Communications," *ELC4020 Advanced Communication Systems*, Cairo University, 2025.
- [2] **Eng. Mohamed Khaled,** "Section Slides in Advanced Communications," *ELC4020 Advanced Communication Systems*, Cairo University, 2025.
- [3] https://github.com/youefkh05/Advanced_Communication_Coding

11. Appendix

```
% Problem 1: Binary Huffman Coding
clc; clear; close all force;
% Given Symbols probabilities
symbols = {'A','B','C','D','E','F','G'};
P = [0.35 \ 0.30 \ 0.20 \ 0.10 \ 0.04 \ 0.005 \ 0.005];
% Create Input Dictionary
[dict input,err flag, H] = create symbols dictionary(symbols, P);
% Check Input
if err flag ==1
   disp('? Stopping execution due to invalid dictionary.');
   return; % exits the current script or function
end
% Print the dictionary neatly
print_symbols_dic(dict_input, H);
% Manual Huffman Coding (with custom output)
§ -----
dict huffman = huffman encoding visual(dict input);
disp('--- Manual Huffman Encoding ---');
disp(dict huffman);
% Print the codded dictionary neatly
print coded dict(dict huffman, H, "Huffman");
% Problem 2: Binary Fano Coding
```

```
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% Manual Fano Coding (with custom output)
§ -----
disp(dict Fano);
```

```
dict Fano = fano encoding visual(dict input)
disp('--- Manual Fano Encoding ---');
% Print the codded dictionary neatly
print coded dict(dict Fano, H, "Fano");
응응
% -----
           Function Definition
           Entropy Calculation
§ -----
function H = entropy_calc(P)
%ENTROPY CALC Compute the source entropy H(P(x))
  H = entropy calc(P)
  P : vector of symbol probabilities
  H : entropy in bits
   % Validate input
   if any (P < 0) \mid | abs(sum(P) - 1) > 1e-6
      warning('Probabilities should sum to 1. Normalizing...');
      P = P / sum(P);
   end
   % Remove zeros (to avoid log2(0))
   P = P(P > 0);
   % Compute entropy
   H = -sum(P .* log2(P));
end
%% -----
           Average Length Calculation
                                 -----
function L = average_length_calc(dict)
%AVERAGE LENGTH CALC Compute average codeword length L(C)
   L = average length calc(dict, P)
   dict : Huffman dictionary cell array {symbol, code}
  P : vector of symbol probabilities (same order as dict)
응
응
  If P is empty, it tries to extract from dict(:,2) if present
  L : average code length
   P = dict(:,2);
   % --- Handle inputs ---
   if nargin < 2 || isempty(P)</pre>
      % Check if dict has a probability column (3 columns)
      if size(dict, 2) >= 3 && isnumeric(dict{1,2})
```

```
P = cell2mat(dict(:,2));
          codes = dict(:,3);
       else
          error('Probability vector P is required or must be in dict(:,2)');
       end
   else
       % Extract codes (assumed in 2nd column)
       codes = dict(:,3);
   end
   % --- Compute code lengths ---
   code lengths = cellfun(@length, codes);
   % --- Normalize probabilities ---
   P = P(:) / sum(P);
   % --- Check dimensions ---
   if length(P) ~= length(code lengths)
       error('Number of probabilities does not match number of codewords.');
   % --- Compute average code length ---
   L = sum(P .* code lengths);
end
88
            Efficiency Calculation
                              function eta = efficiency calc(H, L)
%EFFICIENCY CALC Compute Huffman coding efficiency ?
% eta = efficiency_calc(H, L)
  H : entropy
  L : average code length
  eta : efficiency in percentage (%)
   if L <= 0
       error('Average length L must be positive.');
   end
   eta = (H / L) * 100;
end
             Print Kraft Inequality Function
8 -----
                                        ______
function [kraft sum, kraft flag]=kraft analysis(dict)
% KRAFT ANALYSIS Compute Kraft's inequality and visualize Kraft tree
   kraft analysis(dict)
응
응
   Input:
양
      dict : cell array {N x 3} ? {symbol, P, code}
용
응
   Example:
      dict = {'A','0'; 'B','10'; 'C','110'; 'D','111'};
응
```

```
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```

```
응
       kraft analysis(dict);
   if ~iscell(dict) || size(dict,2) < 2</pre>
       error('Input must be a cell array {symbol, code}');
   end
   % Extract codes
   codes = dict(:,3);
   N = length(codes);
   % --- 1. Compute Kraft's inequality ---
   code lengths = cellfun(@length, codes);
   kraft sum = sum(2.^(-code lengths));
    fprintf('\n=== Kraft Inequality Check ===\n');
    fprintf('Sum(2^{-1} i)) = %.4f\n', kraft sum);
   if abs(kraft sum - 1) < 1e-6
       fprintf('? Code satisfies equality ? Complete Prefix Code.\n');
       kraft flag=2;
   elseif kraft sum < 1</pre>
       fprintf('? Code satisfies inequality (valid but not complete).\n');
       kraft flag=1;
   else
       fprintf('? Invalid prefix code (violates Kraft''s inequality).\n');
       kraft flag=0;
   end
end
88 -----
             Create Dictionary Input Definition
% -----
function [dict input,err flag, H] = create symbols dictionary(symbols, P)
%CREATE DICTIONARY Combines symbols and probabilities into a validated dictionary.
응
   dict input = create dictionary(symbols, P)
응
응
   Inputs:
응
       symbols - cell array of symbols, e.g. {'A', 'B', 'C'}
응
             - corresponding probabilities (row or column vector)
응
응
   Output:
용
       dict input - cell array {symbol, probability}
용
응
   Example:
양
       symbols = {'A','B','C'};
응
       P = [0.5 \ 0.3 \ 0.2];
응
       dict input = create dictionary(symbols, P);
    % Combine into dictionary-like cell array
   dict input = [symbols(:), num2cell(P(:))];
    % Assume not great until great
```

```
err flag = 1;
   % Validate using the check symbols() function
   [ok, msg] = check symbols(dict input);
   % Display validation result
       disp('? Dictionary is valid!');
       err flag =0;
   else
       disp(['? Error: ' msg]);
       err flag = 1;
   end
   8 -----
   % Compute entropy (only if valid)
                               _____
   H = entropy calc(P)
end
%% -----
             Check Input Validation Function
function [isValid, errMsg] = check symbols(dict input)
% CHECK SYMBOLS Validates a symbol-probability dictionary
용
   [isValid, errMsg] = check symbols(dict input)
양
응
   Input:
응
       dict_input : Cell array {N\times2}, where first column = symbols,
양
                  second column = probabilities
응
응
   Output:
용
       isValid: Logical true if valid, false otherwise
양
       errMsq : String describing validation error (if any)
   % Default output
   isValid = false;
   errMsg = '';
   try
       % Extract symbols and probabilities
       symbols = dict input(:, 1);
       P = cell2mat(dict input(:, 2));
       % Check same length
       if numel(symbols) ~= numel(P)
          errMsg = 'Symbols and probabilities must have the same length.';
          return;
       end
       % Check probabilities sum to 1 (within tolerance)
       if abs(sum(P) - 1) > 1e-6
          errMsg = sprintf('Probabilities do not sum to 1 (sum = %.6f).', sum(P));
          return;
```

```
end
       % Check all probabilities are positive
       if any (P <= 0)
          errMsg = 'All probabilities must be positive.';
       end
       % If all checks passed
       isValid = true;
   catch ME
       errMsg = ['Invalid dictionary input: ' ME.message];
   end
end
§§ -----
9
         Print Dictionary Function
% -----
function print symbols dic(dict input, H)
% PRINT SYMBOLS DIC Displays a formatted version of the symbol dictionary in a
     figure,
응
                  and shows the calculated source entropy.
응
응
   print symbols dic(dict input, H)
응
응
   Inputs:
응
       dict input - cell array {symbol, probability}
엉
          source entropy (bits/symbol)
   % Validate input
   if nargin < 1 || isempty(dict input)</pre>
       error('Input dictionary is empty or missing.');
       return;
   end
   % Convert symbols to char (uitable can't handle string objects)
   symbols = cellfun(@char, dict input(:,1), 'UniformOutput', false);
   probs = cell2mat(dict input(:,2));
   % Display result in Command Window
   fprintf('\nInformation Source Entropy: H = %.4f bits/symbol\n', H);
   fprintf('-----\n');
   % Create a responsive UI figure
   f = uifigure('Name', 'Symbol Dictionary', ...
               'NumberTitle', 'off', ...
               'Color', 'w', ...
               'Position', [500 400 350 320]);
   % Format probabilities as strings
   probStr = arrayfun(@(p) sprintf('%.4f', p), probs, 'UniformOutput', false);
   % Combine into table data
   data = [symbols probStr];
```

```
% Create a grid layout (auto-resizes)
   gl = uigridlayout(f, [3,1]);
    gl.RowHeight = {'fit', '1x', 'fit'}; % title, table, entropy
   gl.ColumnWidth = {'1x'};
   gl.Padding = [10 10 10 10];
    % --- Title ---
   uilabel(gl, ...
       'Text', '--- Input Symbol Dictionary ---', ...
       'FontSize', 14, ...
       'FontWeight', 'bold', ...
       'HorizontalAlignment', 'center');
    % --- Table ---
   uitable(gl, ...
       'Data', data, ...
       'ColumnName', {'Symbol', 'Probability'}, ...
       'FontSize', 12, ...
       'ColumnWidth', {'1x', '1x'}, ...
       'RowStriping', 'on');
    % --- Entropy Display ---
   uilabel(gl, ...
       'Text', sprintf('Entropy: H = %.4f bits/symbol', H), ...
       'FontSize', 12, ...
       'FontWeight', 'bold', ...
       'FontColor', [0 0.3 0.7], ...
       'HorizontalAlignment', 'center');
end
Print Coded Dictionary Function (General Purpose)
% -----
function print coded dict(dict, H, title str)
% PRINT CODED DICT Display coding dictionary with entropy, avg length, efficiency,
     and Kraft analysis.
응
   print coded dict(dict, H, title str)
응
응
   Inputs:
응
                - cell array {symbol, probability, code}
       dict
                entropy (bits/symbol)
응
응
       title str - string title for the table window (e.g. 'Fano Coding Results')
응
응
   This function:
응
       • Calculates average codeword length L(C)
양
       • Calculates efficiency ? = (H / L) * 100%
응
       • Checks Kraft's inequality
응
       • Displays results in MATLAB UI + command window
응
응
   Example:
응
       print coded dict(fano dict, H, 'Fano Coding Summary');
    % === Validate input ===
    if nargin < 1 || isempty(dict)</pre>
       disp('Input dictionary is missing or empty.');
       return;
```

```
end
if size(dict, 2) < 3
   disp('Dictionary must have 3 columns: {symbol, probability, code}.');
    return;
end
if nargin < 3 || isempty(title str)</pre>
   title str = 'Coded Dictionary Summary';
end
% === Extract data ===
symbols = cellfun(@char, dict(:,1), 'UniformOutput', false);
P = cell2mat(dict(:,2));
codes = dict(:,3);
% === Compute metrics ===
L = average length calc(dict);
eta = efficiency calc(H, L);
[kraft sum, kraft flag] = kraft analysis(dict);
% === Print to Command Window ===
fprintf('n--- %s --- n', title str);
fprintf('Symbol\tProb.\t\tCode\n');
fprintf('-----
for i = 1:length(symbols)
    fprintf('s\t1, 4f\t\t8s\n', symbols{i}, P(i), codes{i});
end
fprintf('----\n');
fprintf('Entropy (H):
                              %.4f bits/symbol\n', H);
fprintf('Average length (L): %.4f bits/symbol\n', L);
fprintf('Efficiency (?):
                              %.2f %%\n', eta);
                              %.4f\n', kraft sum);
fprintf('Kraft Sum:
if kraft flag == 2
   fprintf('Kraft Result: ? Complete Prefix Code\n');
elseif kraft flag == 1
   fprintf('Kraft Result: ? Valid but Not Complete\n');
else
    fprintf('Kraft Result: ? Invalid Code\n');
end
% === UI Figure ===
f = uifigure('Name', title str, ...
             'NumberTitle', 'off', ...
            'Color', 'w', ...
            'Position', [500 200 480 450]);
gl = uigridlayout(f, [3 1]);
gl.RowHeight = {'fit', '1x', 'fit'};
gl.Padding = [10 10 10 10];
% --- Title ---
uilabel(gl, ...
    'Text', ['--- ' title str ' ---'], ...
    'FontSize', 14, ...
    'FontWeight', 'bold', ...
    'HorizontalAlignment', 'center');
```

```
% --- Table ---
   data = [symbols, arrayfun(@(p) sprintf('%.4f', p), P, 'UniformOutput', false),
     codes];
   uitable(gl, ...
       'Data', data, ...
       'ColumnName', {'Symbol', 'Probability', 'Code'}, ...
       'FontSize', 12, ...
        'RowStriping', 'on', ...
        'ColumnWidth', {'1x', '1x', '1x'});
    % --- Summary Line ---
   uilabel(gl, ...
        'Text', sprintf('H = %.4f | L = %.4f | ? = %.2f %% | Kraft = %.4f', H, L, eta,
     kraft_sum), ...
       'FontSize', 12, ...
        'FontWeight', 'bold', ...
        'FontColor', [0 0.3 0.7], ...
        'HorizontalAlignment', 'center');
end
%% -----
              Huffman Encoding with Visualization Function
function dict = huffman encoding visual(dict input)
%HUFFMAN ENCODING VISUAL Visual Huffman encoding with full table output (UI-based)
응
   dict = huffman encoding visual(symbols, P)
응
    - symbols: cell array of symbol names (e.g. {'A','B','C','D','E','F','G'})
응
   - P: vector of probabilities (same length as symbols)
응
응
   Creates a UI figure showing the probability & code propagation table,
   and prints the final Huffman dictionary.
    % get the info from dictionary
   symbols = dict input(:,1);
   P = cell2mat(dict input(:,2));
    % === Input Validation ===
    if numel(symbols) ~= numel(P)
       error('Symbols and probabilities must have same length.');
   end
    % === Normalize probabilities ===
    P = P(:);
   P = P / sum(P);
    % === Step 1: Generate merging history ===
   history table = merge probabilities(P);
    % === Step 1 Visualization ===
   visualize merging process(P, history table);
    % === Step 2: Assign Huffman codes ===
   history table full = assign coding(history table);
```

```
% === Step 3: Prepare data for visualization ===
% Convert numeric NaNs to empty strings for table display
final visual data = cell(size(history table full));
for r = 1:size(history table full,1)
    for c = 1:size(history table full,2)
        val = history table full{r,c};
        if isnumeric(val)
            if isnan(val)
                final visual data\{r,c\} = '';
                final visual data{r,c} = num2str(val, '%.4f');
            end
        else
            final_visual_data{r,c} = val;
        end
    end
end
% Generate column headers (P1, C1, P2, C2, ...)
numCols = size(history table full, 2);
final visual headers = cell(1, numCols);
for c = 1:numCols
    if \mod(c,2) ==1
        final visual headers{c} = sprintf('P%d', ceil(c/2)-1);
        final visual headers{c} = sprintf('C%d', ceil(c/2)-1);
    end
end
% === Step 4: Build UI Visualization ===
close all;
f = uifigure('Name','Huffman Encoding Visualization', ...
             'Position',[100 100 1000 500]);
gl = uigridlayout(f,[2 1]);
gl.RowHeight = {'fit', '1x'};
uilabel(ql, ...
    'Text', 'Huffman Encoding: Probability and Code Evolution (P/C Steps)', ...
    'FontSize',16, ...
    'FontWeight', 'bold', ...
    'HorizontalAlignment', 'center');
% Column widths (narrow for numeric columns, wider for code columns)
col_widths = repmat({70}, 1, numCols);
col widths(2:2:end) = {100}; % widen code columns
uitable(gl, ...
    'Data', final visual data, ...
    'ColumnName', final visual headers, ...
    'RowName', { }, ...
    'FontSize',12, ...
    'ColumnWidth', col widths, ...
    'RowStriping','on', ...
    'BackgroundColor', [1 1 1; 0.95 0.95 1]);
% === Step 5: Extract Final Huffman Dictionary ===
```

```
% Make a copy
   dict = dict input;
    % Ensure dict has at least 3 columns
    if size(dict, 2) < 3
       dict(:,end+1:3) = {[]};
   dict(:,3)=history table full(:,2);
    % === Step 6: Console Output ===
    firstPcol = 1;
   firstCcol = 2;
   probs = cell2mat(history table full(:, firstPcol));
   codes = history table full(:, firstCcol);
   validIdx = ~isnan(probs);
   symbols = symbols(validIdx);
   codes = codes(validIdx);
   probs = probs(validIdx);
   fprintf('\n--- Final Huffman Codes ---\n');
    for i = 1:length(symbols)
       fprintf('Symbol %s (%.4f): %s\n', symbols{i}, probs(i), codes{i});
    fprintf('========\n\n');
end
% === Probability Merge helper function ===
function history table = merge probabilities(P)
%MERGE PROBABILITIES Builds Huffman probability merging history (descending)
응
   history_table = merge_probabilities(P)
응
응
   Input:
응
       P - vector of symbol probabilities
응
양
   Output:
양
       history table - table of probabilities after each merge
응
                       Columns: P0, P1, P2, ... (N-1 total)
응
응
   Note: Probabilities are shown in descending order.
    % --- Input check ---
   if numel(P) < 2
       error('At least two probabilities are required.');
   end
   % --- Initialization ---
   P = P(:);
   P = sort(P, 'descend'); % sort descending
   N = numel(P);
    % Number of P columns = N - 1
   numCols = N - 1;
   maxRows = N;
```

```
% Initialize history as cell
    history = cell(maxRows, numCols);
    % --- Step 0: Fill P0 (descending order) ---
    for i = 1:maxRows
        history{i,1} = P(i);
    curP = P;
    % --- Iteratively merge ---
    for step = 2:numCols
        % Sort ascending to pick smallest two
        curP = sort(curP, 'ascend');
        if numel(curP) >= 2
            p1 = curP(1);
            p2 = curP(2);
            mergedP = p1 + p2;
            % Remove two smallest and add merged one
            curP = [mergedP; curP(3:end)];
        end
        % Sort descending for display
        curP = sort(curP, 'descend');
        % Fill current column
        for r = 1:maxRows
            if r <= numel(curP)</pre>
                history\{r, step\} = curP(r);
            else
                history\{r, step\} = NaN;
            end
        end
    end
    % --- Column names ---
    colNames = cell(1, numCols);
    for i = 1:numCols
        colNames{i} = sprintf('P%d', i-1);
    end
    % --- Convert to table ---
    history table = cell2table(history, 'VariableNames', colNames);
end
% === Visualization of Probability Merging Process ===
function visualize merging process(P, history table)
% VISUALIZE MERGING PROCESS Display a UI table of Huffman probability merging
양
    visualize merging process(P, history table)
응
응
    Displays the merging steps used in Huffman encoding as a clean table UI.
양
응
    Inputs:
용
                        - Original probability vector (used for scaling)
응
        history table - Table of merging probabilities (output of
      merge probabilities)
```

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```
응
응
    Example:
응
        history table = merge probabilities([0.4 0.2 0.15 0.15 0.1]);
응
        visualize merging process([0.4 0.2 0.15 0.15 0.1], history table);
    % --- Input validation ---
    if nargin < 2
        error('Usage: visualize merging process(P, history table)');
    if ~istable(history table)
        error('history table must be a MATLAB table.');
    end
    % === Step 1: Convert numeric values (NaN ? empty string for display) ===
    merge visual data = cell(size(history table));
    for r = 1:size(history_table,1)
        for c = 1:size(history_table,2)
            val = history table{r,c};
            if isnumeric(val)
                if isnan(val)
                    merge visual data{r,c} = '';
                else
                    merge visual data{r,c} = num2str(val, '%.4f');
                end
            else
                merge visual data\{r,c\} = val;
            end
        end
    end
    % === Step 2: Build UI Table Figure ===
    f merge = uifigure('Name', 'Step 1: Probability Merging History', ...
                 'Position',[150 150 700 400]);
    gl merge = uigridlayout(f merge,[2 1]);
    gl merge.RowHeight = {'fit','1x'};
    uilabel(gl merge, ...
        'Text', 'Step 1: Huffman Probability Merging Process', ...
        'FontSize',16, ...
        'FontWeight', 'bold', ...
        'HorizontalAlignment', 'center');
    uitable(gl merge, ...
        'Data', merge visual data, ...
        'ColumnName', history table. Properties. Variable Names, ...
        'RowName', { }, ...
        'FontSize',12, ...
        'ColumnWidth', repmat({80}, 1, width(history table)), ...
        'RowStriping','on', ...
        'BackgroundColor',[1 1 1; 0.95 0.95 1]);
    % === Step 3: Optional console summary ===
    fprintf('\n--- Probability Merging Steps ---\n');
    disp(history table);
    fprintf('======\n\n');
end
```

```
% === Assign code helper function ===
function history table full = assign coding(history table)
    % assign coding - expands the history table and assigns Huffman codes
    % Input:
       history table : numeric matrix or table (probability merging history)
    % Output:
    % history table full : cell array with 2N columns
           Odd columns: probability values
           Even columns: assigned codes
   % If table, convert to numeric array
   if istable(history_table)
       history_table = table2array(history table);
   end
   % Determine size
    [numRows, numCols] = size(history table);
   newCols = 2 * numCols;
    % Initialize
   history table full = cell(numRows, newCols);
    % === Fill odd columns with probabilities ===
    for col = 1:numCols
       history table full(:, 2 * col - 1) = num2cell(history table(:, col));
   end
   % === Initialize last code column (start with last merge) ===
   lastPcol = 2 * numCols - 1;
   lastCcol = lastPcol + 1;
   history table full{1, lastCcol} = '0';
   history table full{2, lastCcol} = '1';
   raw counter=1; %for parent assignment
    % === Backward propagation of codes ===
    for col = numCols:-1:2 % start from last column going backward
       currPcol = 2 * col - 1;
       currCcol = currPcol + 1;
       prevPcol = 2 * (col - 1) - 1;
       prevCcol = prevPcol + 1;
       raw counter = raw counter+1;
       % Get non-NaN values from P prev column
       prevPvals = cell2mat(history table full(:, prevPcol));
       prevPvals = prevPvals(~isnan(prevPvals));
        % Get non-NaN values from C curr column
       currCvals = history table full(:, currCcol);
        % Identify merged value
        if length(prevPvals) >= 2
           mergedVal = prevPvals(end) + prevPvals(end-1);
```

else

```
continue;
        end
        % Find which row in current P col matches the mergedVal
        currPvals = cell2mat(history table full(:, currPcol));
        matchIdx = find(abs(currPvals - mergedVal) < 1e-12);</pre>
        if numel(matchIdx) > 1
            matchIdx = matchIdx(1); % take top one if duplicate
        end
        % Get parent code
        parentCode = history table full{matchIdx, currCcol};
        if isempty(parentCode)
            parentCode = '';
        end
        % === Assign child codes ===
        % Last two rows in previous P column are merged into this parent
        history table full{raw counter, prevCcol} = [parentCode '0'];
        history table full{raw counter+1, prevCcol} = [parentCode '1'];
        % For each previous non-merged row (in display order top->bottom)
        for ii = 1:(raw counter-1)
            % Skip the rows that were just merged (raw counter and raw counter+1)
            % Get the probability value in the previous column for this row
            valPrev = history table full{ii, prevPcol};
            if isnan(valPrev)
                continue; % nothing to copy
            % Find matching value in the current column (exclude merged parent)
            currMatches = find(abs(currPvals - valPrev) < 1e-12);</pre>
            % Remove the matchIdx (the merged parent) if it appears
            currMatches(currMatches == matchIdx) = [];
            if isempty(currMatches)
                continue; % no corresponding match found
            end
            % If there are duplicates (two identical probabilities)
            if numel(currMatches) > 1
                % take both, and copy their codes to the two rows
                history table full{ii, prevCcol} = currCvals{currMatches(1)};
                if (ii+1) <= numRows</pre>
                    history table full{ii+1, prevCcol} = currCvals{currMatches(2)};
                end
            else
                % single match - copy code directly
                history table full{ii, prevCcol} = currCvals{currMatches(1)};
            end
        end
    end
end
```

```
Fano Encoding with Visualization Function
function table out = fano encoding visual(dict input)
% FANO ENCODING VISUAL
% Fano encoding with dynamic stage-by-stage history table.
% Output table columns:
% Symbol | P0 | C0 | P1 | C1 | ... until convergence
    % === STEP 1: INITIALIZE ===
    symbols = dict input(:,1);
    probs = cell2mat(dict input(:,2));
    % Normalize and sort descending
    probs = probs / sum(probs);
    [probs, idx] = sort(probs, 'descend');
    symbols = symbols(idx);
    % Initialize codes and history
    codes = repmat({''}, size(symbols));
    history = cell(length(symbols), 0);
    % Add first columns PO and CO
    history(:, end+1) = num2cell(probs); % P0
    history(:, end+1) = codes;
    % Start with one full group
    groups = {struct('idx', 1:length(symbols), 'prefix', '')};
    iteration = 1;
    % === STEP 2: ITERATIVE FANO GROUPING ===
    while ~isempty(groups)
        new groups = {};
        for g = 1:length(groups)
           cur = groups{g};
            idxs = cur.idx;
            prefix = cur.prefix;
            % Skip if one symbol only
            if numel(idxs) <= 1</pre>
                continue;
            end
            pvals = probs(idxs);
            % --- Compute reference dynamically ---
            ref = 2^{-iteration};
            % --- Decide split method (COMBINATION-BASED) ---
            best diff = inf;
            split idx = [];
            n = length(pvals);
            for mask = 1: (2^n - 1)
```

```
subset = bitget(mask, 1:n);
            subset sum = sum(pvals(logical(subset)));
            diff = abs(subset sum - ref);
            if diff < best diff</pre>
                best diff = diff;
                split idx = find(subset);
            end
        end
        % --- Create two new groups ---
        g1 = idxs(split idx);
        g2 = setdiff(idxs, idxs(split idx));
        % Assign '0' and '1' respectively
        for k = g1
            codes{k} = [prefix '0'];
        for k = g2
            codes\{k\} = [prefix '1'];
        % Queue for next stage
        if ~isempty(q1)
            new groups{end+1} = struct('idx', g1, 'prefix', [prefix '0']);
        end
        if ~isempty(g2)
            new groups{end+1} = struct('idx', g2, 'prefix', [prefix '1']);
        end
    end
    % Stop if all groups are singletons
    if isempty(new_groups)
        break;
    end
    % Record stage snapshot
    history(:, end+1) = num2cell(probs); % Pi
    history(:, end+1) = codes;
    groups = new groups;
    iteration = iteration + 1;
end
% === STEP 3: COMPILE OUTPUT TABLE ===
cols = {'Symbol'};
for i = 0: (size (history, 2)/2 - 1)
    cols{end+1} = sprintf('P%d', i);
    cols{end+1} = sprintf('C%d', i);
end
table out = [symbols history];
% Display as uitable
figure('Name', 'Fano Encoding Table', 'Position', [300 200 1100 400]);
uitable('Data', table out, 'ColumnName', cols, ...
    'ColumnWidth', num2cell(repmat(80,1,numel(cols))), ...
    'FontSize', 11, 'Units', 'normalized', 'Position', [0 0 1 1]);
```

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```
% === STEP 3: FINAL OUTPUT (Symbol, Prob, Code) ===
  table_out = [symbols num2cell(probs) codes];
  cols = {'Symbol', 'Probability', 'Code'};
end
```