

$$\begin{aligned}
&\approx -\frac{L}{2\pi} e^{ik_{0z}r_{ij}} \frac{\omega_0 \mu^2}{\epsilon_0 L S \hbar} 2\pi \frac{\omega_0}{c^2 k_{0z}} \cosh^2 r S_i^+ S_j^- \rho^S(t) \\
&\approx -\left[\frac{\gamma_{1d}}{2} \cos(k_{0z}r_{ij}) + i\frac{\gamma_{1d}}{2} \sin(k_{0z}r_{ij})\right] \cosh^2 r S_i^+ S_j^- \rho^S(t) \\
&\equiv -\left(\frac{\gamma_{ij}}{2} + i\Lambda_{ij}\right) \cosh^2 r S_i^+ S_j^- \rho^S(t)
\end{aligned} \tag{1}$$