

INVITED ARTICLE

Structural, energetic and vibrational properties of some van der Waals complexes of CO₂, OCS and OCSe

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As part of a study of the properties of some chalcogen-bonded complexes with NH_3 , H_2O , PH_3 and H_2S , we have investigated the oxygen-bound species containing CO_2 , OCS and OCSe by means of molecular orbital calculations at the *ab initio* level. The structures of the NH_3 , H_2O and PH_3 complexes are all similar, with a primary C...X interaction (X = N, O, P) and one of the hydrogen atoms approaching an oxygen atom in a weak secondary attraction. The H_2S complexes show a greater variety of alternative structures. The changes in the monomer geometrical parameters, the interaction energies and the harmonic vibrational spectra vary in general in a systematic way as the acid and the base are changed. Deviations from this systematic behaviour have been rationalised.

Keywords: ab initio calculations; molecular complexes; molecular structures; interaction energies; vibrational spectra

1. Introduction

We have previously presented the results of our ab initio calculations of the properties of the van der Waals complexes formed between the related Lewis acids - carbon dioxide, carbonyl sulphide, carbon disulphide and nitrous oxide – and the electron donors – nitrogen [1], ozone [2], carbon monoxide [3] and sulphur dioxide [4]. We found that the structures were, by and large, similar to one another, with a lone pair orbital of the base interacting with the carbon or the central nitrogen atom of the electron acceptor. In the same way, we have reported similar results for the complexes of the series of electron donors, ammonia, water, hydrogen fluoride, phosphine, hydrogen sulphide and hydrogen chloride, with the Lewis acids, boron trifluoride [5–8], sulphur dioxide [9], silicon tetrafluoride [10], fluoroacetylene [11], the halogens and interhalogens, F₂, Cl₂, Br₂, ClF, BrF and BrCl [12], and fluoroform [13,14]. In these cases, the major interaction was the donation of a lone pair of electrons of the base to a vacant orbital located mainly on the B, S or Si atom [5–10], to a σ^* (CH) antibonding orbital [11,13,14] or to a $\sigma^*(XY)$ orbital (X, Y = F, Cl, Br) [12]. The interest in the properties of the complexes with fluoroacetylene and fluoroform [11,13,14] was related to a search for evidence for blue-shifting hydrogen-bonding interactions, and in those with the halogens and interhalogens [12] to detecting halogen-bonding interactions, and to compare the properties of these unusual non-covalent interactions with those of the more conventional hydrogen bonds. A further example of a non-covalent interaction which has generated a good deal of interest recently is the chalcogen bond [15,16]. We are now extending our theoretical studies to the NH₃, H₂O, PH₃ and H₂S family on the one hand, and the CO₂, CS₂, CSe₂, OCS, OCSe and SCSe series on the other, in an attempt to identify the presence of chalcogen-bonded interactions among the various pairs of molecules in these series. In this first paper, as a calibration data-set, we concentrate on the oxygen-containing Lewis acids, CO₂, OCS and OCSe, in which a conventional non-covalent interaction is likely to be observed, before going on to examine the associated species bound through the sulphur and selenium atoms, where the probability of detecting S...X and Se...X interactions (X = N, O, P, S) is higher. Our focus will be mainly on the structures, the interaction energies and the vibrational spectra of the various aggregates, and we shall examine the ways in which these properties vary as the acid and the base are systematically changed, and how they are linked to one another.

Of the possible binary combinations of molecules which may be permuted from these two sets, the $CO_2 \cdot H_2O$ complex has been by far the most thoroughly studied, both experimentally, in the gas phase [17–19] and in cryogenic matrices [20–24], and theoretically [25–41]. Even so, its structure is far from unequivocally settled. In addition, the gas phase experimental studies of $OCS \cdot H_2O$ [42], $CS_2 \cdot H_2O$ [43], $CO_2 \cdot H_2S$ [44], $CO_2 \cdot NH_3$ [45,46] and $OCS \cdot NH_3$ [46], the matrix isolation infrared spectra of $CO_2 \cdot NH_3$ [47,48] and theoretical computations on $OCS \cdot H_2O$ [40,49], $CS_2 \cdot H_2O$ [40], $CO_2 \cdot H_2S$ [41] and $CO_2 \cdot NH_3$ [29,48,50]

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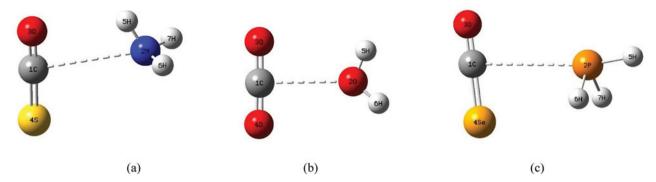


Figure 1. Optimised geometries of the (a) OCS·NH₃, (b) CO₂·H₂O and (c) OCSe·PH₃ complexes.

have appeared. We have found no reports of relevant complexes containing PH₃ or OCSe.

2. Computational details

The calculations were carried out using the Gaussian-09 program [51] at the second-order level of Møller–Plesset perturbation theory (MP2) [52] and with Dunning's augmented correlation-consistent polarised valence triple-zeta basis set (aug-cc-pVTZ) [53–57]. The tight convergence criterion was applied [51], and genuine minima on the potential energy surfaces were confirmed by vibrational analyses. In some cases, a number of possible structures for each complex were examined, but the alternatives were found to be either saddle points or local minima. The interaction energies were computed and corrected for basis set superposition error (BSSE) [58] using the full counterpoise procedure [59], and for vibrational zero-point energy differences.

3. Results and discussion

3.1. Molecular structures

The structures of the complexes containing ammonia, water and phosphine were characterised by a formal C...X interaction (X = N, O, P), in an essentially T-shaped

configuration, with one XH bond approaching the oxygen atom of OCY (Y = O, S, Se), tilted to a greater or lesser extent towards the CO bond. Structures of three examples of these complexes are illustrated in Figure 1. The complexes containing hydrogen sulphide yielded a far greater variety of stationary points; Figure 2 shows the optimised structures of the preferred isomers. The gas phase molecular beam electric resonance rotational spectrum of CO₂·NH₃ is interpreted in terms of a T-shaped structure with the N...CO₂ fragment having local $C_{2\nu}$ symmetry, an N...C distance of 298.75 pm and a bending angle of the NH₃ sub-unit of 22.71° relative to the N...C axis [45,46]. This structure is consistent with the conclusions of Reed et al. [29], Jönsson and Nelander [48] and Amos and co-workers [50], based on their ab initio studies, with C...N bond lengths of 291, 286 and 295.0 pm, respectively. Fraser et al., in their microwave and infrared study of OCS·NH₃ [46], concluded that its structure was similar to that of CO₂·NH₃.

A number of rotational gas phase studies of $CO_2 \cdot H_2O$ also proposed a planar T-shaped structure of this adduct, with $C_{2\nu}$ symmetry and C...O distances of 283.6 pm [17] and 279.17 pm [18], although the spectra are complicated by rotation tunnelling splitting and the effect of wide amplitude motions [17–19]. A large number of theoretical studies, at levels ranging from self-consistent field (SCF) [30], Møller-Plesset perturbation theory at second order (MP2)

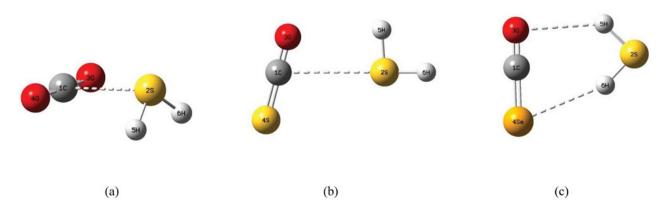


Figure 2. Optimised geometries of the (a) CO₂·H₂S, (b) OCS·H₂S and (c) OCSe·H₂S complexes.

Table 1. Changes in the intramolecular bond lengths and angles of the complexes of NH₃, H₂O, PH₃ and H₂S with CO₂, OCS and OCSe. See Figures 1 and 2 for numbering of the atoms.

eg -2.443		Parameter	Change	Complex	Parameter	Change	Complex	Parameter	Change
0.020	r(C103)/pm r(C104)/pm ∠03C104/deg r(N2H5)/pm r(N2H6), r(N2H7)/pm ∠H5N2H6, ∠H5N2H7/deg ∠H6N2H7/deg	n 7/deg	0.006 -0.023 -2.443 0.048 0.050 0.003	OCS.NH ₃	r(C1O3)/pm r(C1S4)/pm ∠O3C1S4/deg r(N2H5)/pm r(N2H6), r(N2H7)/pm ∠H5N2H6, ∠H5N2H7/deg ∠H6N2H7/deg	0.091 -0.207 -0.870 0.072 0.041 0.016 -0.168	OCSe-NH ₃	r(C1O3)/pm r(C1Se4)/pm ∠O3C1Se4/deg r(N2H5)/pm r(N2H6), r(N2H7)/pm ∠H5N2H6, ∠H5N2H7/deg ∠H6N2H7/deg	-0.321 0.420 -1.359 0.064 0.061 0.185 -0.439
-0.090 OCS-PH ₃ r(C1O3)/pm -0.126 OCSe-PH ₃ r(C1S4)/pm 0.186 0.010 0.010 0.010 0.010 0.010 0.010 0.005 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006 0.006	r(C103)/pm r(C104)/pm ∠03C104/deg r(02H5)/pm r(02H6)/pm ∠H502H6/deg		$\begin{array}{c} 0.020 \\ -0.086 \\ -1.693 \\ 0.036 \\ 0.011 \\ 0.510 \end{array}$	OCS-H ₂ O	r(C103)/pm r(C1S4)/pm ∠03C1S4/deg r(02H5)/pm r(02H6)/pm ∠H502H6/deg	0.204 -0.364 -0.463 0.101 0.007	OCSe·H ₂ O	r(C103)/pm r(C1Se4)/pm ∠03C1Se4/deg r(02HS)/pm r(02H6)/pm ∠H5O2H6/deg	0.207 -0.427 -0.375 0.097 0.013
-0.002 OCS·H₂S r(C1O3)/pm 0.128 OCSe·H₂S -0.919 r(C1S4)/pm -0.194 0.025 ∠O3C1S4/deg -0.188 0.207 r(S2H5)/pm -0.002 r(S2H6)/pm 0.038 ∠H5S2H6/deg 0.442	r(C103)/pm r(C104)/pm 	m 17/deg	-0.090 0.010 -0.572 -0.068 -0.062 0.469	OCS-PH ₃	r(C103)/pm r(C1S4)/pm ∠03C1S4/deg r(P2H5)/pm r(P2H6), r(P2H7)/pm ∠H5P2H6, ∠H5P2H7/deg ∠H6P2H7/deg	-0.126 0.186 -0.332 0.065 -0.006 0.320 0.086	OCSe.PH ₃	r(C103)/pm r(C1Se4)/pm ∠03C1Se4/deg r(P2H5)/pm r(P2H6), r(P2H7)/pm ∠H5P2H6, ∠H5P2H7/deg ∠H6P2H7/deg	-0.139 0.196 -0.313 0.103 -0.014 0.374
	r(C103), r(C104)/pm ∠03C104/deg r(S2H5), r(S2H6)/pm ∠H5S2H6/deg	н н	-0.002 -0.919 0.025 0.207	OCS-H ₂ S	r(C103)/pm r(C1S4)/pm ∠03C1S4/deg r(S2H5)/pm r(S2H6)/pm ∠H5S2H6/deg	0.128 -0.194 -0.188 -0.002 0.038 0.442	OCSe·H ₂ S	r(C1O3)/pm r(C1Se4)/pm ∠03C1Se4/deg r(S2H5)/pm r(S2H6)/pm	0.032 -0.028 -0.659 0.107 0.230 -0.119

Table 2. Intermolecular geometries of the complexes of NH₃, H₂O, PH₃ and H₂S with CO₂, OCS and OCSe. See Figures 1 and 2 for numbering of the atoms.

Complex	Parameter	Value	Complex	Parameter	Value	Complex	Parameter	Value
CO ₂ ·NH ₃	r(C1N2)/pm ∠03C1N2/deg ∠04C1N2/deg ∠C1N2H5/deg ∠C1N2H5/deg	293.70 90.54 91.90 109.27 113.54	OCS-NH ₃	r(C1N2)/pm LO3C1N2/deg LS4C1N2/deg LC1N2H5/deg LC1N2H6, LC1N2H7/deg	321.46 77.08 103.79 74.32 125.58	OCSe.NH ₃	r(C1N2)/pm ∠03C1N2/deg ∠Se4C1N2/deg ∠C1N2H5/deg ∠C1N2H6, ∠C1N2H7/deg	316.58 93.09 88.27 154.54 87.82
CO ₂ ·H ₂ O	r(C102)/pm ∠03C102/deg ∠04C102/deg ∠C102H5/deg ∠C102H6/deg	277.41 87.97 93.72 115.86 139.52	OCS·H ₂ O	r(C102)/pm ∠03C102/deg ∠S4C102/deg ∠C102H5/deg ∠C102H6/deg	306.52 72.59 107.87 72.00 176.55	$0\mathrm{CSe.H}_2\mathrm{O}$	r(C102)/pm ∠03C102/deg ∠Se4C102/deg ∠C102H5/deg ∠C102H6/deg	308.06 71.92 108.45 72.12 176.63
${ m CO}_2$ ·PH $_3$	r(C1P2)/pm ∠03C1P2/deg ∠04C1P2/deg ∠C1P2H5/deg ∠C1P2H6, ∠C1P2H7/deg	346.88 103.27 77.31 158.43 100.55	$OCS \cdot PH_3$	r(C1P2)/pm ∠03C1P2/deg ∠S4C1P2/deg ∠C1P2H5/deg ∠C1P2H6, ∠C1P2H7/deg	356.65 98.17 82.16 170.70 92.41	$OCSe\cdot PH_3$	r(C1P2)/pm ∠O3C1P2/deg ∠Se4C1P2/deg ∠C1P2H5/deg ∠C1P2H6, ∠C1P2H7/deg	355.72 97.80 82.51 169.54 93.14
CO ₂ ·H ₂ S	r(C1S2)/pm ∠03C1S2/deg ∠04C1S2/deg ∠C1S2H6/deg	339.80 90.46 90.46 95.81 95.81	OCS.H ₂ S	r(C1S2)/pm ∠03C1S2/deg ∠S4C1S2/deg ∠C1S2H6/deg ∠C1S2H6/deg	338.97 73.54 106.28 87.75 179.58	OCSe.H ₂ S	r(C1S2)/pm r(O3H5)/pm r(Se4H6)/pm .S2H5O3/deg .S2H6Se4/deg .S2C1O3/deg .C21S2H5/deg .C11S2H5/deg .C11S2H6/deg .C103H5/deg	371.41 277.22 295.83 130.83 155.61 84.46 94.88 51.56 40.55 93.15 68.97

Table 3. Interaction energies of the complexes of NH₃, H₂O, PH₃ and H₂S with CO₂, OCS and OCSe.

	Inte	eraction energy/kJ	mol^{-1}
Complex	Uncorrected	Corrected for BSSE only	Corrected for BSSE and ΔE_o
CO ₂ ·NH ₃	-12.620	-11.545	-9.225
$CO_2 \cdot H_2O$	-12.004	-10.838	-6.847
CO ₂ ·PH ₃	-6.997	-5.702	-4.796
$CO_2 \cdot H_2S$	-7.960	-6.816	-4.980
OCS·NH ₃	-8.283	-7.029	-5.730
OCS-H ₂ O	-9.005	-7.629	-5.658
OCS-PH ₃	-7.980	-6.183	-4.511
OCS·H ₂ S	-7.766	-6.259	-4.582
OCSe·NH ₃	-9.520	-6.445	-4.477
OCSe·H ₂ O	-9.075	-6.994	-4.233
OCSe·PH ₃	-10.000	-6.493	-4.249
OCSe·H ₂ S	-10.036	-6.122	-3.827

[29,32-34,37,38,41] and fourth order (MP4) [39] to coupled cluster with singles, doubles and perturbative triples (CCSD(T)) [40], as well as density functional theory (DFT) [35], and employing a variety of basis sets, are in agreement with these findings, while Nguyen and Ha [26] determined that the planar form was more stable than the corresponding perpendicular $C_{2\nu}$ structure. The computed C...O separations lie in a range from 250.2 pm (DFT/Vosko, Wilk, Nusair (VWN64)) [35] to 290.6 pm (MP4/spd) [39]. Damewood et al. [32], Cox and co-workers [34,36] and Altmann and Ford [41] examined a number of possible configurations and concluded that the potential energy surface was so shallow that facile interconversion among the various competing structures was possible. The present result indicates that the C_s structure is the true global minimum, and that the $C_{2\nu}$ species is simply a vibrationally averaged structure, in agreement with Abashkin et al. [35].

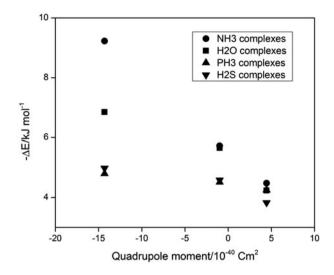


Figure 3. Plots of the interaction energies of the complexes versus the quadrupole moments of the electron acceptors.

The experimental gas phase results of Rice $et\ al.\ [44]$ on ${\rm CO_2\cdot H_2S}$ established that the ${\rm H_2S}$ plane was essentially perpendicular (92°) to the heavy atom plane, and the centre-ofmass separation was 349.8 pm, consistent with our present results and with those of Altmann and Ford [41], using the same computational approach. The microwave rotational spectrum of ${\rm OCS\cdot H_2O}$ [42] represents the first point of departure of our computed structures from those determined experimentally. Tatamitani and Ogata [42] found the structure of this adduct to be planar, of $C_{2\nu}$ symmetry, but with an S...O interaction. This was the structure found theoretically by Garden $et\ al.\ [40]$, although the work of Wojcik and colleagues [49], using a smaller basis set than ours, confirms our findings. In this work, we have examined only those complexes bound through an oxygen atom, so we concede

Table 4. Computed and experimental vibrational spectra of the CO₂·NH₃ complex.

		<u> </u>	<u>-</u>		
Symmetry	Mode	Approximate description	ν(calc.)/cm ⁻¹ (this work)	$v(\text{expt.})/\text{cm}^{-1}[47]$	ν(calc.)/ ν(expt.)
a'	v_1	$\nu_a({\rm NH_3})$	3644.0	_	_
	ν_2	$\nu_s(\mathrm{NH_3})$	3498.0	3326.9	1.05
	ν_3	$\nu_a({\rm CO_2})$	2401.8	2282.8	1.05
	ν_4	$\delta_a(\mathrm{NH_3})$	1668.4	1623.7	1.03
	ν_5	$\nu_s(\mathrm{CO}_2)$	1327.6	_	_
	ν_6	$\delta_s(\mathrm{NH_3})$	1062.5	1001.9	1.06
	ν_7	$\delta(\mathrm{CO_2})$	636.7	662.3	0.96
	ν_8	$\rho(NH_3)$	189.9	_	_
	ν_9	$\nu(CN)$	105.0	_	_
	v_{10}	Antigeared libration	42.4	_	_
a''	v_{11}	$\nu_a({ m NH_3})$	3643.0	_	_
	v_{12}	$\delta_a(\mathrm{NH_3})$	1668.3	1621.7	1.03
	v_{13}	$\gamma(\mathrm{CO_2})$	664.7	662.3	1.00
	v_{14}	$\rho(\mathrm{NH_3})$	135.7	_	_
	v_{15}	$\tau(\mathrm{NH_3})$	7.1	_	_

that the structure determined here may be a local minimum on the potential energy surface, and that the true global minimum is the chalcogen-bonded OCS...OH₂ form. We will be exploring this and similar possible complexes in a future publication.

The changes to the bond lengths and angles of the monomers constituting each of the complexes studied here are collected in Table 1. These changes are minimal, suggesting that the complexes are all weakly bound. The bond lengths of the base fragments tend to increase slightly, except for the PH bond lengths, confirming that PH₃ occupies a unique position among the electron donors considered here, on account of the reversal of the polarity of the PH bond relative to NH, OH and SH, as we have pointed out before [10–14]. The HOH, HPH and HSH angles, as well as the HNH angles involving the in-plane NH bond, increase on complexation accompanied by a contraction in the case of the HNH angles associated with the out-of-plane NH bonds. The bound CO bond lengths of the acids mostly increase, except for the PH3 complexes, as observed above, while the reverse is true for the non-bound CO and the CS and CSe bonds. The changes in the OCY bond angles are generally greater for the complexes with NH₃ and H₂O, and the OCO angle appears to be the most sensitive to complexation, but since these changes are all small some circumspection is required in the interpretation of these numbers.

Table 2 lists the intermolecular geometries of the complexes. Our C...X separations compare reasonably well with those experimental values which are available [17,18,44–46], and with other reported theoretical results, depending on the levels of theory and basis sets used in each case [29,30,32–35,37–41]. The C...X separations roughly follow the generalisations $CO_2 < OCS \approx OCSe$ and $NH_3 \approx H_2O < PH_3 \approx H_2S$. The C...XH angles are a measure of the extent of interaction between the in-plane XH bond and the CO bond. The C...PH angles are substantially larger than the others, as a result of the repulsion between the negatively charged O and H atoms, arising from the reversal of the polarity of the PH bond referred to above. The OCSe·H₂S complex is a unique case, on account of the cyclic doubly hydrogen-bonded structure of this species.

3.2. Interaction energies

The interaction energies of the 12 complexes, corrected for both BSSE and zero-point energy differences, are collected in Table 3. As predicted by the minimal perturbations of the intramolecular bond lengths and angles mentioned above, the magnitudes of these binding energies are also consistent with very weak interactions. Previously reported interaction energies cover a very wide range, indicative of the use of several levels of theory and basis sets (-15.77 [29] to -29.29 kJ mol⁻¹ [48] for CO₂·NH₃, -7.55 [41] to -25.7 kJ mol⁻¹ [25] for CO₂·H₂O, -4.65 kJ mol⁻¹ [41] for CO₂·H₂S and -5.44 [40] to -11.51 kJ mol⁻¹ [49] for

ble 5. Computed and experimental vibrational spectra of the CO₂.H₂O complex.

Iauro J.	Computer	Table 5. Computed and experimental violational specifa of the CO_2 .1120 complex	tional spectia of	uic CO2.112	compies.						
Symmetry Mode	Mode	Approximate description	ν (calc.)/cm ⁻¹ (this work)	$\nu({\rm expt.})/{\rm cm}^{-1}$ [20]	$\nu(\text{calc.})/$ $\nu(\text{expt.})$ [20]	$\nu({\rm expt.})/{\rm cm}^{-1}$ [21,22]	ν(calc.)/ ν(expt.) [21,22]	$\nu({\rm expt.})/{\rm cm}^{-1}$ [23]	$\nu(\text{calc.})/$ $\nu(\text{expt.})$ [23]	$\nu({\rm expt.})/{\rm cm}^{-1}$ [24]	ν(calc.)/ ν(expt.) [24]
a'	ν_1	$\nu_a({ m H_2O})$	3944.6	3724.8	1.06	3731.3	1.06	3725.5	1.06	ı	ı
	-	(H, O)	3818 5	3632 1	1.05	3730.0 3633 5	1.06	3724.1	1.06	3632.0	1 05
	7	V.S(112O)	0.0100	1.700	00:1		60:1	3631.7	1.05	3632.7	1.05
	ν_3	$\nu_{\rm a}({ m CO}_2)$	2404.4	2351	1.02	2344.3	1.03	2351.0	1.02	2351.1	1.02
		ì				2341.9	1.03				
	ν4	$\delta(\mathrm{H}_2\mathrm{O})$	1626.5	1598.1	1.02	1600.7	1.02	1598.4	1.02	ı	ı
	75	$\nu_s(CO_2)$	1328.6	1384.5	96.0	I	I	ı	ı	1384.8	96.0
	ν_6	$\delta(CO_2)$	648.8	656.3	0.99	654.2	0.99	656.3	0.99	656.4	0.99
	77	$\rho(\mathrm{H}_2\mathrm{O})$	166.0	I	I	I	I	I	I	I	I
	ν_8	ν(C0)	110.8	I	I	I	I	ı	I	I	I
	179	Antigeared libration	10.6	Ι	I	I	I	Ι	I	I	I
a''	ν_{10}	$\gamma({ m CO}_2)$	662.6	665.3	1.00	6.999	66.0	665.2	0.97	665.3	1.00
	ν_{11}	$tw(\mathrm{H}_2\mathrm{O})$	156.2	I	I	I		I	I	I	I
	ν_{12}	$\omega({ m H}_2{ m O})$	93.3	I	I	I		I	I	I	I

Table 6. Computed complex-monomer wavenumber shifts of the complexes of NH₃, H₂O, PH₃ and H₂S with CO₂, OCS and OCSe.

Complex	Monomer	Mode	Shift/cm ⁻¹	Complex	Monomer	Mode	Shift/cm ⁻¹	Complex	Monomer	Mode	Shift/cm ⁻¹
CO ₂ ·NH ₃	CO ₂	$v_s(CO_2)$ $\delta(CO_2)(a')$ $\delta(CO_2)(a'')$ $v_a(CO_2)$	1.8 -22.3 5.7 0.4	OCS-NH ₃	OCS	ν(CO) δ(OCS)(α') δ(OCS)(α") ν(CS)	-0.3 -8.9 2.4 3.7	OCSe·NH ₃	OCSe	ν(CO) δ(OCSe)(α') ν(CSe)	10.1 -12.1 0.4 -5.8
	NH_3	ν _s (NH ₃) δ _s (NH ₃) ν _a (NH ₃)(α') ν _a (NH ₃)(α') δ _a (NH ₃)(α')	25.1 25.1 -5.9 -6.9 -0.5		NH3	$v_s(NH_3)$ $\delta_s(NH_3)$ $v_a(NH_3)(a')$ $v_a(NH_3)(a')$ $\delta_a(NH_3)(a')$ $\delta_a(NH_3)(a')$	-6.2 12.5 17.7 -7.7 -1.7 -1.3		NH_3	$ u_s(\text{NH}_3) $ $ \delta_s(\text{NH}_3) $ $ u_a(\text{NH}_3)(a') $ $ u_a(\text{NH}_3)(a') $ $ \delta_a(\text{NH}_3)(a'') $ $ \delta_a(\text{NH}_3)(a'') $	-8.3 12.8 -7.4 -8.7 -7.2 -5.3
CO ₂ .H ₂ O	CO_2	$v_s(\text{CO}_2)$ $\delta(\text{CO}_2)(a')$ $\delta(\text{CO}_2)(a'')$ $v_a(\text{CO}_2)$	2.8 -10.2 3.6 3.0	OCS.H ₂ O	OCS	ν(CO) δ(OCS)(a') δ(OCS)(a'') ν(CS)	-1.4 -1.2 1.0 6.2	OCSe.H ₂ O	OCSe	ν(CO) δ(OCSe)(a') ν(CSe)	-2.4 -0.6 1.4 6.8
	H_2O	$ \nu_s(\mathrm{H}_2\mathrm{O}) $ $ \delta(\mathrm{H}_2\mathrm{O}) $ $ \nu_a(\mathrm{H}_2\mathrm{O}) $	-3.4 -1.8 -3.1		H ₂ O	$ u_s(\mathrm{H}_2\mathrm{O}) $ $\delta(\mathrm{H}_2\mathrm{O})$ $ u_a(\mathrm{H}_2\mathrm{O}) $	-9.7 -6.5 -8.5		H ₂ O	$ u_s(\mathrm{H}_2\mathrm{O}) $ $ \delta(\mathrm{H}_2\mathrm{O}) $ $ u_a(\mathrm{H}_2\mathrm{O}) $	-9.7 -6.1 -8.7
CO ₂ .PH ₃	CO_2	$ \nu_s(\text{CO}_2) $ $ \delta(\text{CO}_2)(a') $ $ \delta(\text{CO}_2)(a'') $ $ \nu_a(\text{CO}_2) $	$\begin{array}{c} 0.1 \\ -10.6 \\ -0.2 \\ -1.0 \end{array}$	OCS.PH ₃	OCS	ν(CO) δ(OCS)(a') δ(OCS)(a'') ν(CS)	2.3 -7.0 -0.9 -2.7	$OCSe.PH_3$	OCSe	ν(CO) δ(OCSe)(α') ν(CSe)	3.4 -7.0 -1.1 -2.6
	PH ₃	$ u_s(\text{PH}_3) $ $ \delta_s(\text{PH}_3) $ $ u_a(\text{PH}_3)(a') $ $ u_a(\text{PH}_3)(a'') $ $ \delta_a(\text{PH}_3)(a'') $ $ \delta_a(\text{PH}_3)(a'') $	1.8 5.3 6.3 1.2 1.0		PH_3	$ u_s(\text{PH}_3) $ $ \delta_s(\text{PH}_3) $ $ u_a(\text{PH}_3)(a') $ $ u_a(\text{PH}_3)(a') $ $ \delta_a(\text{PH}_3)(a') $ $ \delta_a(\text{PH}_3)(a') $	- 2.1 - 2.1 - 1.9 - 0.5 - 4.0		PH_3	$ u_s(\text{PH}_3) $ $ \delta_s(\text{PH}_3) $ $ u_a(\text{PH}_3)(a') $ $ u_a(\text{PH}_3)(a'') $ $ \delta_a(\text{PH}_3)(a'') $ $ \delta_a(\text{PH}_3)(a'') $	- 3.8 - 3.1 - 5.2 - 1.4
CO ₂ .H ₂ S	CO_2	$v_s(\text{CO}_2)$ $\delta(\text{CO}_2)(\text{ip})^a$ $\delta(\text{CO}_2)(\text{op})^b$ $v_a(\text{CO}_2)$	$0.7 \\ -13.0 \\ 1.0 \\ 0.1$	OCS.H ₂ S	OCS	ν(CO) δ(OCS)(a') δ(OCS)(a'') ν(CS)	-2.4 -2.2 -1.1 3.1	OCSe.H ₂ S	OCSe	ν(CO) δ(OCSe)(α') δ(OCSe)(α'') ν(CSe)	-1.9 -2.0 0.5 0.8
	$ m H_2S$	$ u_s(\mathrm{H}_2\mathrm{S}) $ $ \delta(\mathrm{H}_2\mathrm{S}) $ $ u_a(\mathrm{H}_2\mathrm{S}) $	-1.9 -0.6 -1.6		$ m H_2S$	$ \nu_s(\mathrm{H}_2\mathrm{S}) $ $ \delta(\mathrm{H}_2\mathrm{S}) $ $ \nu_a(\mathrm{H}_2\mathrm{S}) $	-1.7 -4.3 -0.7		$ m H_2S$	$ \nu_s(\mathrm{H}_2\mathrm{S}) $ $ \delta(\mathrm{H}_2\mathrm{S}) $ $ \nu_a(\mathrm{H}_2\mathrm{S}) $	-19.2 4.7 -14.1

^aBending in the S...CO₂ plane.
^bBending perpendicular to the S...CO₂ plane.

					Wavenumber sh	nift/cm ⁻¹	
Complex	Monomer	Mode	[47]	[20]	[21,22]	[23]	[24]
CO ₂ ·NH ₃	CO ₂	$v_s(CO_2)$ $\delta(CO_2)(a')$ $\delta(CO_2)(a'')$ $v_a(CO_2)$ $v_s(NH_3)$ $\delta_s(NH_3)$ $v_a(NH_3)(a')$ $\delta_a(NH_3)(a'')$ $\delta_a(NH_3)(a')$ $\delta_a(NH_3)(a')$	-12.7 4.1 -1.0 -3.1 32.7 - -7.0 3.5				
CO ₂ ·H ₂ O	CO_2 H_2O	$ \nu_s(\text{CO}_2) $ $ \delta(\text{CO}_2)(a') $ $ \delta(\text{CO}_2)(a'') $ $ \nu_a(\text{CO}_2) $ $ \nu_s(\text{H}_2\text{O}) $ $ \delta(\text{H}_2\text{O}) $ $ \nu_a(\text{H}_2\text{O}) $		- 3.0 -6.0 2.4 -2.3 0.9 -1.9	- 3.0 -9.8 4.8, 2.4 -3.2 9.1 -1.0, -2.3	- 2.9 -6.0 2.0 -2.5, -3.2 1.4 -1.9, -3.3	- 3.1 -5.8 2.6 -2.7, -2.0

Table 7. Experimental complex-monomer wavenumber shifts of the CO₂·NH₃ and CO₂·H₂O complexes.

OCS·H₂O). The upper bounds of the various ranges can usually be attributed to the neglect of BSSE. The overall trend in the strength of interaction is $NH_3 > H_2O > PH_3$ $\approx H_2S$, for all three electron acceptors. For complexes of the type described here, it may be anticipated that the major source of the interaction energy is the electrostatic component. We have not attempted to dissect the total interaction energies into the attractive electrostatic, charge transfer, polarisation and dispersion contributions, nor the repulsive Pauli exchange constituent. In the absence of a permanent dipole moment in the case of CO₂, the most probable main source of electrostatic attraction which is common to all the complexes is a dipole-quadrupole interaction. Values of the molecular quadrupole moments of CO2, OCS and OCSe are available (-14.31, -0.984 and 4.442 \times 10⁻⁴⁰ C m² for CO₂, OCS [60] and OCSe [61]). As the quadrupole moment changes sign as O is replaced by S and then Se, and the negative poles change from the axial positions in CO₂ and OCS to equatorial in OCSe, the computed interaction energies diminish regularly, as shown in Figure 3. Since all the interaction energies are small, the difference between the PH3 and H2S complex properties barely register, except to distinguish them from those of the NH₃ and H₂O adducts. In any case, it is well known that the properties of complexes of second- and third-row molecules behave differently from those of the first row.

Vibrational spectra

Our computed spectrum of the $CO_2 \cdot NH_3$ complex is presented in Table 4. The matrix isolation infrared data of Fredin and Nelander in nitrogen [47] are consistent with this structure, and their data are also included in this table.

The calculated/experimental wavenumber ratios are well within the normal range for such comparisons at this level. Matrix isolation studies of the $CO_2 \cdot H_2O$ complex [20–24] favour the T-shaped structure over the hydrogen-bonded alternative, although Tso and Lee [21,22] have indicated that a second, hydrogen-bonded isomer may exist in oxygen matrices. While the earlier matrix investigations suggested that the $CO_2 \cdot H_2O$ complex possessed $C_{2\nu}$ symmetry, more recent work, with the benefit of improved cryogenic technology and increased instrumental resolution, admits the possibility of a second C...O bonded species with C_s symmetry [23,24], a result we find to be compatible with

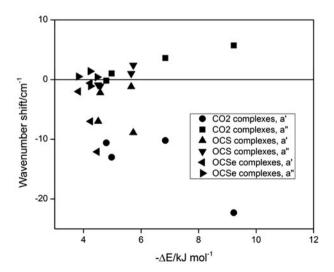


Figure 4. Plots of the OCY bending wavenumber shifts of the electron acceptors versus the complex interaction energies (Y = O, S, Se).

Table 8. Computed intermolecular wavenumbers of the complexes of NH₃, H₂O, PH₃ and H₂S with CO₂, OCS and OCSe.

			Wavenumber/				Wavenumber/				Wavenumber/
Complex	Symmetry	Mode	cm^{-1}	Complex	Symmetry	Mode	cm^{-1}	Complex	Symmetry	Mode	cm^{-1}
CO ₂ ·NH ₃	a'	NH ₃ rock CN stretch Antigeared	189.8 105.0 42.4	OCS.NH ₃	a'	NH ₃ rock CN stretch Antigeared	140.3 99.4 47.1	$OCSe\cdot NH_3$	a'	NH ₃ rock CN stretch Antigeared	156.4 87.6 53.5
	<i>a</i> "	NH ₃ rock NH ₃ torsion	135.7 7.1		<i>a</i> "	NH ₃ rock NH ₃ torsion	73.9 21.3		<i>a</i> "	NH ₃ rock NH ₃ torsion	110.7 49.5
CO ₂ ·H ₂ O	α'	H ₂ O rock CO stretch Antigeared	166.0 110.8 10.6	OCS.H ₂ O	α'	H ₂ O rock CO stretch Antigeared	149.0 112.4 35.2	OCSe.H ₂ O	a'	H ₂ O rock CO stretch Antigeared	141.4 108.0 31.0
	<i>a</i> "	H_2O twist H_2O wag	156.2 93.3		a''	H_2O twist H_2O wag	202.8 99.3		<i>a</i> "	H_2O twist H_2O wag	196.2 105.7
$CO_2 \cdot PH_3$	<i>a</i> ′	PH ₃ rock CP stretch Antigeared	123.7 57.6 25.3	OCS.PH ₃	α'	PH ₃ rock CP stretch Antigeared	126.9 65.7 44.8	OCSe.PH ₃	a'	PH ₃ rock CP stretch Antigeared	140.1 63.9 42.1
	<i>a</i> "	PH ₃ rock PH ₃ torsion	76.2 37.5		α"	PH ₃ rock PH ₃ torsion	117.4		<i>a</i> "	PH ₃ rock PH ₃ torsion	134.1 19.4
$CO_2 \cdot H_2 S$	α'	H_2S wag CS stretch	85.1 67.3	OCS.H ₂ S	α'	CS stretch H ₂ S rock	83.3 68.3	OCSe.H ₂ S	α'	$\mathrm{H}_2\mathrm{S}$ rock Intermonomer stretch	156.3 72.0
	<i>a</i> "	H ₂ S twist H ₂ S rock Antigeared	144.9 43.9 25.6		<i>a</i> "	Antigeared H_2S twist H_2S wag	35.7 142.3 45.5		<i>a</i> "	Antigeared H_2S twist H_2S wag	40.8 133.1 86.1

our present work. Our calculated wavenumbers and those determined experimentally in nitrogen [20,23,24] and oxygen [21,22] are listed in Table 5. Multiple entries for some of the observed bands are attributed to the presence of a second structure. Again, the calculated/experimental ratios are acceptable; only for the CO₂ bending vibrations are the predicted wavenumbers marginally lower than the observed ones. The computed complex-monomer wavenumber shifts for the 12 complexes are collected in Table 6, and their experimental counterparts [20–24,47] in Table 7. In line with the very small perturbations of the intramolecular geometrical parameters (Table 1) and low interaction energies (Table 3), the wavenumber shifts occurring on complexation are also minimal. By far, the most strongly affected modes are the bending vibrations. The symmetric NH₃ bending mode, v_2 , has long been regarded as a sensitive probe of the strength of interaction, particularly in the spectra of inorganic coordination compounds [62]. In this series of complexes, this mode undergoes the largest shift of any of the vibrations, characteristically to the blue. The calculated shift in CO₂·NH₃ of 25.1 cm⁻¹ may be compared with the experimental value of 32.7 cm⁻¹ [47], while those of OCS·NH3 and OCSe·NH3 are also large and to the blue (12.5 and 12.8 cm⁻¹, respectively). The remaining bending mode shifts are almost exclusively to lower wavenumber, but are substantially smaller. The exception is the H₂S bending mode of OCSe·H₂S, v₂, which shifts to the blue $(4.7 \,\mathrm{cm}^{-1})$, as a result of the cyclic doubly hydrogen-bonded structure of this complex. For this complex, too, the H₂S stretching modes suffer uncharacteristically large (-19.2)and -14.1 cm^{-1}) shifts, typical of SH bonds engaged in hydrogen-bonded interactions. In those cases where the degeneracy of a linear bending mode is lifted on complexation, as in the CO₂, OCS and OCSe fragments, the resulting pairs of vibrations are typically perturbed with one large negative shift (the a' mode) and a smaller positive shift (the a" mode). These computed shifts are fairly consistent with their experimental partners, and show a weak correlation with the interaction energies, as indicated in Figure 4.

Table 8 lists the computed wavenumbers of the intermolecular modes of the complexes. These modes fall into fairly well-defined characteristic ranges. For example, the intermolecular stretching vibrations for the NH₃ and H₂O complexes are fairly similar (80–110 cm⁻¹), and are about 50% higher than those for the PH₃ and H₂S adducts (50– 80 cm⁻¹). Likewise, the NH₃ and PH₃ rocking modes are typically in the range 100–160 cm⁻¹, while the corresponding torsional modes are very low ($<50 \text{ cm}^{-1}$). The H₂O vibrations are usually found in the order twisting > rocking > wagging, but apart from the consistently high wavenumbers of the twisting vibrations of the H₂S complexes, no such pattern is observed among the rocking and wagging vibrations of this group, due to the three different types of structure adopted by the H₂S complexes. These regular generalisations serve to confirm the internal consistency of the calculations.

4. Conclusions

The complexes of NH₃, H₂O and PH₃ with CO₂, OCS and OCSe all have qualitatively similar structures, while the H₂S complexes exhibit three different structural models. In those cases where comparison with experimentally determined structures is possible, our predictions are consistent with them. The interaction energies are all small, and the weak interactions are manifested in minimal perturbations of the monomer bond lengths and angles, although a dependence of the strengths of interaction on the quadrupole moments of the electron acceptors is observed. These small perturbations also extend to the vibrational spectra, where the bending wavenumber shifts of the linear electron acceptor molecules show a tentative correlation with the interaction energies. No evidence was found in these calculations for the existence of S or Se chalcogen-bound complexes, but a search for such adducts will be the subject of a forthcoming paper.

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