

$$\max z = 8x_1 + x_2$$

$$s.t. \begin{cases} x_1 + x_2 = 5 \\ y_1 = 5 - x_1 - x_2 - z_3 \\ y_2 = 2 - 3x_1 + 2x_2 - 3z_3 \end{cases}$$

(0,0) is réalisable
car $x_3 = 5 = \frac{5}{1}$?

Laure

$$\min w = y_1 + y_2$$

s.c.

m constraints

min

$$w = 7 - 4x_1 - 4x_3$$

s.c.

$$A \begin{cases} y_1 = 5 - x_1 - x_2 - x_3 \\ y_2 = 2 - 3x_1 + 2x_2 - 3x_3 \end{cases}$$

max

$$y_i \geq 0$$

$$-w = -7 + 4x_1 + 4x_3$$

$$s.c. \begin{cases} A \end{cases}$$

$$\begin{aligned} \max z &= \frac{41}{8} - 2x_3 \\ s.c. \begin{cases} x_1 &= \frac{7}{4} - x_3 \\ x_2 &= \frac{13}{8} \end{cases} \end{aligned}$$

méthode des tableaux

		$-x_1$	$-x_2$	$-x_3$
w	-7	-4	0	-4
z	0	-2	-1	0
y ₁	5	1	2	1
y ₂	2	<u>3</u>	-2	3

$$e = \min(1, 3) = 1 \quad x_1$$

$$l = \min(\frac{5}{1}, \frac{2}{3}) = \frac{2}{3} \Rightarrow y_2$$

		$-x_1$	$-x_2$	$-x_3$
w	-13/3	-	-8/3	0
z	-4/3	-	-1/3	0
y ₁	13/3	-	<u>8/3</u>	0
x ₁	2/3	-	-2/3	1

$$e = 2, \quad l = 1 \quad y_1$$

		$-x_1$	$-x_2$	$-x_3$
w	0	-	-	0
z	0	-	-	0
x ₂	13/8	-	-	0
x ₁	7/4	-	-	1

Fin de la phase I

$$w^* = 0$$

La valeur optimale de Laure

max

$$z = 8x_1 + x_2$$

$$= 2 \left(\frac{7}{4} - x_3 \right) + \frac{13}{8}$$

$$z = \left(\frac{11}{2} + \frac{13}{8} \right) - 2x_3$$

$$= \frac{41}{4} + \frac{13}{8} = \frac{83}{8} \quad (2)$$

$$z^* = \frac{83}{8}$$

$$\max z = \frac{41}{8} - 2x_3$$

$$s.c. \begin{cases} x_1 = \frac{7}{4} - x_3 \\ x_2 = \frac{13}{8} \end{cases}$$